

| | Course Title | Course Instructor | Course Text | Course Description and Main Content | Course Grade |
|----|---|-------------------|--|---|---------------------|
| 1 | Geometry | Xiang Ma | <i>Analytic Geometry</i> by Chengye You | Analytic geometry in \mathbb{R}^3 including quadratic curves and quadratic surfaces, basic projective geometry | 88 |
| 2 | Mathematical Analysis(I) | Jiazhong Yang | <i>Mathematical Analysis (Volume One)</i> by Shengjian Wu | Set of real numbers, sequence and limit, continuity, differential and indefinite integral | 93.5 |
| 3 | Advanced Algebra I (Honor) | Jinpeng An | <i>Linear Algebra (2nd Edition)</i> by K. Hoffman and R. Kunze | Linear space, linear maps, dual space, and determinants of linear maps | 94 |
| 4 | Mathematical Analysis(II) | Jiazhong Yang | <i>Mathematical Analysis (Volume Two)</i> by Shengjian Wu | Riemann integral, improper integral, number series, function sequence and function series, power series, Fourier series | 92 |
| 5 | Advanced Algebra II (Honor) | Jinpeng An | <i>Linear Algebra (2nd Edition)</i> by K. Hoffman and R. Kunze | Characteristic values, invariant subspaces, Jordan forms, inner product spaces and bilinear forms | 93 |
| 6 | Probability Theory | Yanxia Ren | <i>Introduction to Probability Theory</i> by Xianping Li | Event and sample space, probability, random variables and distributions, characteristic functions, and an introduction to law of large numbers and central limit theorem | 91 |
| 7 | Mathematical Analysis(III) | Baoxiang Wang | <i>Mathematical Analysis (Volume Three)</i> by Shengjian Wu | Riemann integral, improper integral, number series, function sequence and function series, power series, Fourier series | 94 |
| 8 | Algebra(I) (Honor) | Liang Xiao | <i>Abstract Algebra</i> by D. Dummit, R. Foote | Definitions and properties of groups, rings, modules, fields, and Galois theory | 96 |
| 9 | Functions of Real Variables | Shiwu Yang | <i>Real Analysis</i> by Stein | Basic set theory, Lebesgue measure, measurable functions, Lebesgue integral, differential and integral revisit, and L^p spaces | 96 |
| 10 | Ordinary Differential Equations | Weigu Li | <i>Ordinary Differential Equations</i> by Bin Liu | Methods to solve ODE and systems of linear ODE, the existence and uniqueness of solution, the influence of initial value and parameters on the solution, topics with respect to boundary values | 97 |
| 11 | Theory of Functions of a Complex Variable (Honor) | Hanlong Fang | <i>Complex Analysis</i> by Stein | Holomorphic functions (Cauchy's integral theorem and related topics, Laurent series, residue), conformal mapping, and proof of prime theorem | 95 |
| 12 | Functional Analysis | Zhifei Zhang | <i>Lecture Notes on Functional Analysis (Volume One)</i> by Gongqing Zhang and Yuanqu Lin | Metric spaces, linear operators and linear forms, compact operators and Fredholm operators (basic category theory, derived functors) | 99 |
| 13 | Algebra II (Honor) | Enlin Yang | <i>Commutative Algebra</i> by M. F. Atiyah, I. G. MacDonald, <i>Introduction to Homological Algebra</i> by Charles A. Weibel | Introduce commutative algebra (covering Atiyah's book), and homological algebra | 94 |
| 14 | Mathematical Modeling | Zhennan Zhou | <i>Methods of Mathematical Modelling --Continuous Systems and Differential Equation</i> by T. Witelski and M. Bowen | An introduction to mathematical modelling using ordinary and partial differential equations. | 89 |
| 15 | Algebraic Geometry I (Graduate) | Zhiyu Tian | <i>Algebraic Geometry</i> by R. Hartshorne | An introduction to the theory of schemes and cohomology, covering part of Chapter 2 and Chapter 3 of GTM52. | 88 |
| 16 | Homology Theory (Graduate) | Houhong Fan | <i>Homology</i> by Boju Jiang, <i>Algebraic Topology</i> by Allen Hatcher | Homology and cohomology theory, covering simplicial homology, CM complexes, and Poincare duality | P (due to COVID-19) |
| 17 | Topology | Wenyuan Yang | <i>Topology</i> by J.R.Munkres, <i>Lecture Notes on Foundations of Topology</i> by Chengye You | Topological space and continuity, topological properties, quotient space and closed surfaces, homotopy and fundamental group, covering space | 94 |
| 18 | Differential Manifolds and Topology (Honor) | Yi Liu | <i>An Introduction to Differential Manifold</i> by Huanwei Chen | Introduction to differential manifolds and vector space, Whitney theorem, Stokes formula, de Rham cohomology and its relationship with singular homology and intersection number. | 93 |
| 19 | Basic Theory of Numbers | Jun Yu | <i>Primes of the Form x^2+ny^2: Fermat, Class Field Theory, and Complex Multiplication</i> by David A. Cox | The work of Lagrange, Legendre and Gauss on quadratic reciprocity and the genus theory of quadratic forms, basic algebraic number theory and class field theory. | 86 |

| | | | | | |
|--|---|--------------|---|--|------|
| 20 | Modular Form and Number Theory (Graduate) | Jun Yu | <i>Introduction to Modular Forms</i> by Wenwei Li | Modular curves with level structures, modular forms, Hecke operators, and L-functions | 95 |
| 21 | Lie Groups and Lie Algebras (Graduate) | Xiaomeng Xu | <i>Lie Groups, Lie Algebras, and Representations, Lie Groups Beyond an Introduction</i> | Introduce the machinery of roots, weights and the Weyl group in the representation of Lie algebra, structure theory of semisimple Lie algebras, and construction of the representations of compact Lie | 90 |
| 22 | Fiber Bundles and Characteristic Classes (Graduate) | Zhiqiang Bao | <i>Characteristic Classes</i> by Milnor | Introduction to characteristic classes, with detailed studies of Stiefel-Whitney classes, Chern classes, Pontrjagin classes, and the Euler class. | 96 |
| 23 | Algebraic Geometry II (Graduate) | Zhiyu Tian | <i>Algebraic Geometry</i> by R. Hartshorne | An introduction to the theory of schemes and cohomology, covering Serre duality, cohomology and base change, theorem on formal functions, basics of algebraic curves and surfaces. | 93.5 |
| 24 | Introduction to Differentiable Manifolds | Bo Dai | <i>Introduction to Manifolds and Geometry</i> by Jiaqiang Mei | Differentiable manifolds, differential forms, and connection | 97 |
| The following are in-progress math courses | | | | | |
| 25 | Number Theory I (Graduate) | Xinyi Yuan | <i>Algebraic Number Theory</i> by J. Neukirch | Number fields, rings of algebraic Integers, local fields and class field theory | |
| 26 | Topics in Number Theory (Graduate) | Enlin Yang | <i>SGA 4 1/2</i> | Etale cohomology, including cohomology of curves, the smooth and proper base change theorems, Poincaré duality, and proof of Weil conjecture | |
| 27 | Topics in Representation Theory (Graduate) | Wenwei Li | <i>Automorphic Forms and Representations</i> by Daniel Bump | Introduction to automorphic forms | |
| 28 | Partial Differential Equations | Zhifei Zhang | <i>Partial Differential Equations: An Introduction</i> by Walter A. Strauss | Laplace equations, heat equations, wave equations | |