

Exam Review

CS 579 Online Social Network Analysis

Dr. Cindy Hood
11/25/25

Remaining Exam and Deliverables

- ▶ HW #5 posted
 - ▶ Problems that will help you prepare for Exam 2
 - ▶ Due 11/24 (~~No late days~~)
 - ▶ Solutions posted soon
 - ▶ HW accepted until solutions posted
- ▶ Exam 2
 - ▶ Cumulative but will focus on material covered after Exam 1
 - ▶ 12/2
- ▶ Final project poster presentation/video (online students)
 - ▶ 12/4
 - ▶ Section 2 students please fill out survey if you haven't done so
- ▶ Final project report
 - ▶ Due by midnight on 12/10

Final Project Presentation

- ▶ Poster session
 - ▶ Outside of SB 104 during class time 11:25am - 12:40pm 12/4
 - ▶ Will start before class and continue after
 - ▶ I will send out an email for you to schedule a timeslot
 - ▶ Plan to be present for the entire class period
 - ▶ For you to complete your reviews
 - ▶ For others to complete their review of your poster
 - ▶ I have mounting putty/tape to stick your posters to the wall there
 - ▶ Pizza will be served
- ▶ Online video
 - ▶ Must be posted to google folder (I will send link) by 11:00am 12/4

Poster/Presentation Requirements

- ▶ Must use printed poster (on campus) or slides (online)
- ▶ Each team member must present and be visible for online presentation
- ▶ No more than 5 minutes
- ▶ Content
 - ▶ Title and names of all team members
 - ▶ Intro - What did you do
 - ▶ Design of project
 - ▶ Execution of project
 - ▶ Data utilized
 - ▶ Results
 - ▶ Discussion of results and conclusion
 - ▶ What worked/what didn't work?
 - ▶ How can you evaluate your project?
 - ▶ What did you do?
 - ▶ What could you do?
 - ▶ What surprised you?
 - ▶ What would you do if you had more time?

Focus on the most
interesting parts of the
project

Poster Creation

- ▶ Your poster should be 24" x 36"
- ▶ Powerpoint
 - ▶ <https://designshack.net/articles/business-articles/how-to-make-a-poster-in-powerpoint/>

Poster Printing

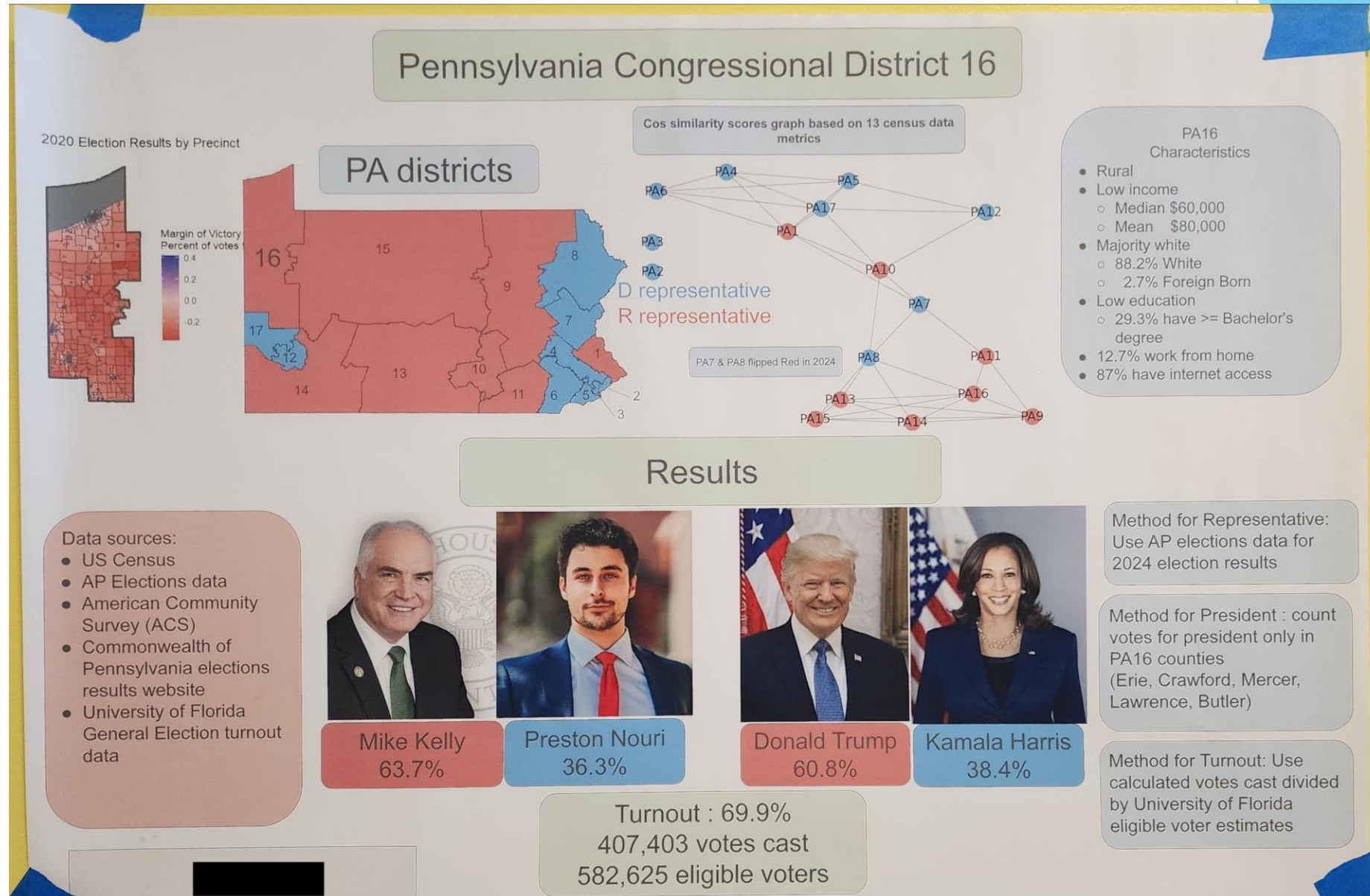
How to Print to a Plotter

Using one of the HP plotters on the Mies Campus (located in Crown and Tech North) takes some additional preparation to get a quality plot and avoid waisting your printing funds. The OTS staff have produced a series of four videos to help you learn how to plot properly. Please review each of these videos before attempting to use a plotter.

1. Plotter Introduction – Preparing Your File [↗](#)
2. Z6200 Plotter Instructional Video [↗](#)

<https://www.iit.edu/ots/services/student-printing>

Example from last fall



Project presentation review assignments

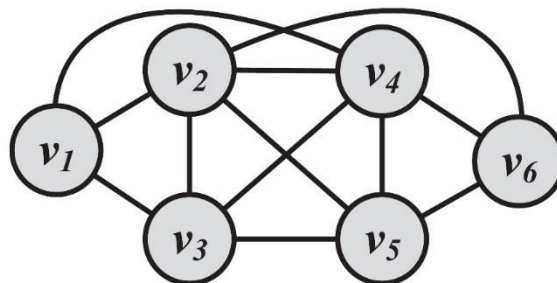
- ▶ All reviews must be completed on 12/4
 - ▶ On campus during class time
 - ▶ Online

II. Relaxing Cliques

- ▶ **k -plex**: a set of vertices V in which we have

$$d_v \geq |V| - k, \forall v \in V$$

- ▶ d_v is the degree of v in the induced subgraph
 - ▶ Number of nodes from V that are connected to v
- ▶ Clique of size k is a 1-plex
- ▶ Finding the maximum k -plex: **NP-hard**
 - ▶ In practice, relatively easier due to smaller search space.



1-plex : $\{v_2, v_3, v_4, v_5\}$

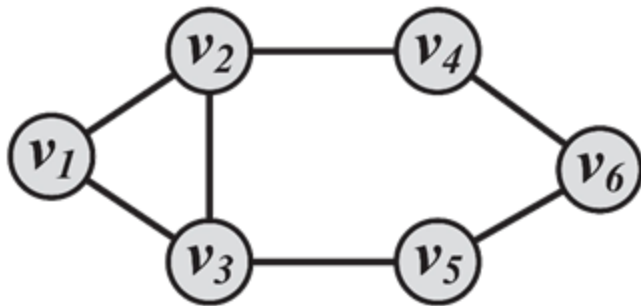
2-plex : $\{v_1, v_2, v_3, v_4, v_5\}, \{v_2, v_3, v_4, v_5, v_6\}$

3-plex : $\{v_1, v_2, v_3, v_4, v_5, v_6\}$

Maximal k -plexes

Special Subgraphs

1. **k -Clique**: a **maximal** subgraph in which the largest shortest path distance between any nodes is less than or equal to k
2. **k -Club**: follows the same definition as a k -clique
 - ▶ **Additional Constraint**: nodes on the shortest paths should be part of the subgraph (i.e., diameter)
3. **k -Clan**: a **k -clique** where for all shortest paths within the subgraph the distance is equal or less than k .
 - ▶ All k -clans are k -cliques, but not vice versa.



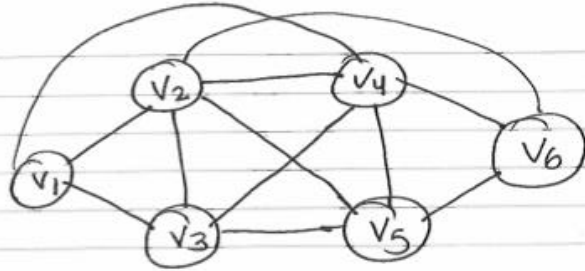
2-cliques : $\{v_1, v_2, v_3, v_4, v_5\}, \{v_2, v_3, v_4, v_5, v_6\}$

2-clubs : $\{v_2, v_3, v_4, v_5, v_6\}, \{v_1, v_2, v_3, v_4\}, \{v_1, v_2, v_3, v_5\}$

2-clans : $\{v_2, v_3, v_4, v_5, v_6\}$

K-Plex

(1)



A node is a member of a k -plex of size n if it has direct ties to $n-k$ members

We know $\{v_2, v_3, v_4, v_5\}$ are a clique since they are fully connected.

We also know that $\{v_2, v_3, v_4, v_5\}$ are members of a 1-plex of size 4. Each node has ties to $n-k = 4-1 = 3$ nodes.

Lets add a node v_1 . Then $n=5$ $\{v_1, v_2, v_3, v_4, v_5\}$
Is this a 1-plex? If it was then each node would need to have direct ties to $n-k = 5-1 = 4$ members. The degree of $v_1 = 3$ so These 5 nodes are not a 1-plex.

How about a 2-plex? Does each node have direct ties to $n-k = 5-2 = 3$ members? Yes so $\{v_1, v_2, v_3, v_4, v_5\}$ is a 2-plex

We can make the same case to say that $\{v_2, v_3, v_4, v_5, v_6\}$ is a 2-plex

(2)

What if we add both v_1 and v_6 to the original clique, do we have a 2-plex with $\{v_1, v_2, v_3, v_4, v_5, v_6\}$

$$n=6 \quad k=2$$

$$n-k=4$$

Since neither v_1 or v_6 has direct ties with 4 other nodes, this set is not a 2-plex.

How about if we try a 3-plex for $\{v_1, v_2, v_3, v_4, v_5, v_6\}$

$$n=6 \quad k=3$$

$$n-k=3$$

Yes, each node has ^{direct} ties to at least 3 nodes in the 3-plex.

N-cliques

- ▶ The strict clique definition (maximal fully-connected sub-graph) may be too strong for many purposes.
 - ▶ It insists that every member or a sub-group have a direct tie with each and every other member.
- ▶ You can probably think of cases of "cliques" where at least some members are not so tightly or closely connected.
- ▶ There are two major ways that the "clique" definition has been "relaxed" to try to make it more helpful and general.
- ▶ One alternative is to define an actor as a member of a clique if they are connected to every other member of the group at a distance greater than one.
- ▶ Usually, the path distance two is used. This corresponds to being "a friend of a friend."
- ▶ This approach to defining sub-structures is called N-clique, where N stands for the length of the path allowed to make a connection to all other members.

https://faculty.ucr.edu/~hanneman/nettext/C11_Cliques.html

N-Clans

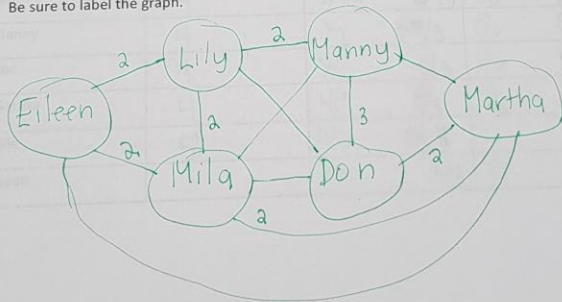
- ▶ The N-clique approach tends to find long and stringy groupings rather than the tight and discrete ones of the maximal approach.
- ▶ In some cases, N-cliques can be found that have a property that is probably undesirable for many purposes: it is possible for members of N-cliques to be connected by actors who are not, themselves, members of the clique.
 - ▶ For most sociological applications, this is quite troublesome.
- ▶ To overcome this problem, some analysts have suggested restricting N-cliques by insisting that the total span or path distance between any two members of an N-clique also satisfy a condition.
- ▶ The additional restriction has the effect of forcing all ties among members of an n-clique to occur by way of other members of the n-clique. This is the n-clan approach.

Problem from previous exam

You are given the following dataset:

Name	Age	Political Affiliation	Causes Interested in	Voted in the last election	Amount donated in the last year
Lily	67	Democrat	Anti-war, civil rights, animal rights, religious liberty	Yes	\$12,000
Manny	53	Republican	Anti-war, environment, religious liberty, freedom	Yes	\$50
Don	28	Libertarian	Environment, anti-tax, religious liberty, freedom	No	\$400
Martha	34	Independent	Environment, anti-tax, food security	No	\$750
Mila	60	Democrat	Anti-war, anti-tax, animal rights, food security	Yes	\$25
Eileen	25	Independent	Civil rights, animal rights, food security	No	0

1. (20 pts) Create a unimodal, connected network graph from this dataset and draw the graph. Be sure to label the graph.



4. (20 pts) K-clique and k-plex structures provide different ways of relaxing the clique structure.
a. (10 pts) Provide the maximal 2-cliques of the network graph in problem 1.

$\{Lily, Manny, Don, Martha, Mila, Eileen\}$

- b. (10 pts) Provide the maximal 2-plexes of the network graph in problem 1.

$\{Lily, Manny, Don, Martha, Mila\}$
 $\{Lily, Don, Martha, Mila, Eileen\}$

5. (10 pts) You are going pay one of the people in the network to be an influencer. For maximum effectiveness, which person would you choose and why?

Mila

Member-Based Community Detection

- ▶ Look at node characteristics; and
- ▶ Identify nodes with similar characteristics and consider them a community

Node Characteristics

A. Degree

- ▶ Nodes with same (or similar) degrees are in one community
- ▶ Example: cliques

B. Reachability

- ▶ Nodes that are close (small shortest paths) are in one community
- ▶ Example: k -cliques, k -clubs, and k -clans

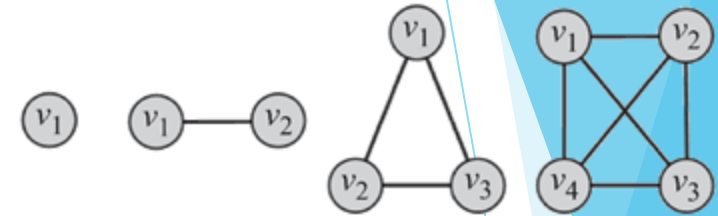
C. Similarity

- ▶ Similar nodes are in the same community

A. Node Degree

Most common subgraph searched for:

- ▶ **Clique:** a maximum complete subgraph in which all nodes inside the subgraph adjacent to each other



Find communities by searching for

- 1. The maximum clique:**
the one with the largest number of vertices, or
- 2. All maximal cliques:**
cliques that are not subgraphs of a larger clique; i.e., cannot be further expanded

To overcome this, we can

- Brute Force
- Relax cliques
- Use cliques as the core for larger communities

Both problems are NP-hard

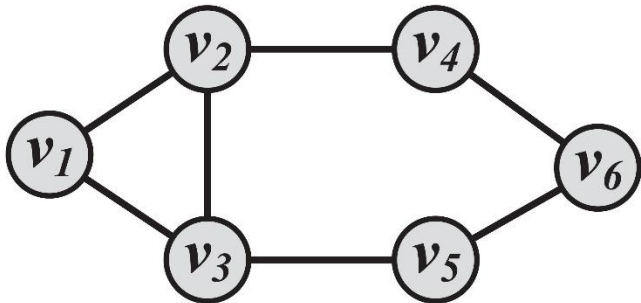
Node Similarity (Structural Equivalence)

Jaccard Similarity

$$\sigma_{\text{Jaccard}}(v_i, v_j) = \frac{|N(v_i) \cap N(v_j)|}{|N(v_i) \cup N(v_j)|}$$

Cosine similarity

$$\sigma_{\text{Cosine}}(v_i, v_j) = \frac{|N(v_i) \cap N(v_j)|}{\sqrt{|N(v_i)| |N(v_j)|}}$$



$$\sigma_{\text{Jaccard}}(v_2, v_5) = \frac{|\{v_1, v_3, v_4\} \cap \{v_3, v_6\}|}{|\{v_1, v_3, v_4, v_6\}|} = 0.25$$

$$\sigma_{\text{Cosine}}(v_2, v_5) = \frac{|\{v_1, v_3, v_4\} \cap \{v_3, v_6\}|}{\sqrt{|\{v_1, v_3, v_4\}| |\{v_3, v_6\}|}} = 0.40$$

Ratio Cut and Normalized Cut

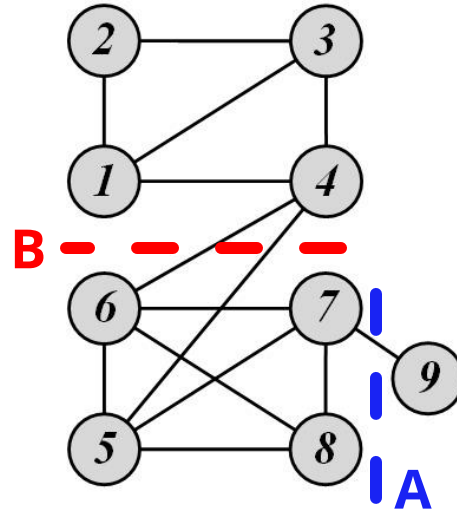
- ▶ To mitigate the min-cut problem we can change the objective function to consider community size

$$\text{Ratio Cut}(P) = \frac{1}{k} \sum_{i=1}^k \frac{\text{cut}(P_i, \bar{P}_i)}{|P_i|}$$

$$\text{Normalized Cut}(P) = \frac{1}{k} \sum_{i=1}^k \frac{\text{cut}(P_i, \bar{P}_i)}{\text{vol}(P_i)}$$

- ▶ $\bar{P}_i = V - P_i$ is the complement cut set
- ▶ $\text{cut}(P_i, \bar{P}_i)$ is the size of the cut
- ▶ $\text{vol}(P_i) = \sum_{v \in P_i} d_v$

Ratio Cut & Normalized Cut: Example



For Cut A

$$\text{Ratio Cut}(\{1, 2, 3, 4, 5, 6, 7, 8\}, \{9\}) = \frac{1}{2} \left(\frac{1}{1} + \frac{1}{8} \right) = 9/16 = 0.56$$

$$\text{Normalized Cut}(\{1, 2, 3, 4, 5, 6, 7, 8\}, \{9\}) = \frac{1}{2} \left(\frac{1}{1} + \frac{1}{27} \right) = 14/27 = 0.52$$

For Cut B

$$\text{Ratio Cut}(\{1, 2, 3, 4\}, \{5, 6, 7, 8, 9\}) = \frac{1}{2} \left(\frac{2}{4} + \frac{2}{5} \right) = 9/20 = 0.45 < 0.56$$

$$\text{Normalized Cut}(\{1, 2, 3, 4\}, \{5, 6, 7, 8, 9\}) = \frac{1}{2} \left(\frac{2}{12} + \frac{2}{16} \right) = 7/48 = 0.15 < 0.52$$

Both ratio cut and normalized cut prefer a balanced partition