

(1) Use Glushkov construction to convert the regular expression $b^* a^* b^? a^*$ (the answer for Part (i) of Exercise 3.3.5 of Lab 2) into an NFA Next, convert the NFA obtained into a DFA using the subset construction.

We add position to the regular expression:

$b^* a^* b^? a^*$

to give

$b_1^* a_2^* b_3^? a_4^*$

NFA for b_1^*

	a	b
$\leftarrow \rightarrow s$	-	q1
$\leftarrow q1$	-	q1

NFA for a_2^*

	a	b
$\leftarrow \rightarrow s$	q2	-
$\leftarrow q2$	q2	-

NFA for $b_1^* a_2^*$

	a	b
$\leftarrow \rightarrow s$	q2	q1
$\leftarrow q1$	q2	q1
$\leftarrow q2$	q2	-

NFA for $b_3^?$

	a	b
$\rightarrow s$	-	q3
$\leftarrow q3$	-	-

NFA for $(b_1^* a_2^* b_3^?)$

	a	b
$\leftarrow \rightarrow s$	q2	q1, q3
$\leftarrow q1$	q2	q1, q3
$\leftarrow q2$	q2	q3

<-- q3	-	-
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NFA for a^4

	a	b
<- -> s	q4	-
<-- q4	q4	-

NFA for $(b^1 a^2 b^3 a^4)^*$

	a	b
<--> s	q2,q4	q1,q3
<-- q1	q2,q4	q1,q3
<-- q2	q2,q4	q3
<-- q3	q4	-
<-- q4	q4	-

Converting the above NFA to DFA gives:

	a	b
<- -> {s}	{q2,q4}	{q1,q3}
<-- {q2,q4}	{q2,q4}	{q3}
<-- {q1,q3}	{q2,q4}	{q1,q3}
<-- {q3}	{q4}	{}
<-- {q4}	{q4}	-

(2) Use Glushkov construction to convert the regular expression $b^* | b^* a^+ (b a^+)^* b^?$ (the answer for Part (i) of Exercise 3.3.5 of Lab 2) into an NFA Next, convert the NFA obtained into a DFA using the subset construction.

We add position to the regular expression:

$b^* | b^* a^+ (b a^+)^* b^?$

to give

$b_1^* | b_2^* a_3^+ (b_4 a_5^+)^* b_6^?$

NFA for b^1 *

	a	b
$\rightarrow s$	-	q1
$\leftarrow q1$	-	q1

NFA for b^2 *

	a	b
$\rightarrow s$	-	q2
$\leftarrow q2$	-	q2

NFA for a^3 +

	a	b
$\rightarrow s$	q3	-
$\leftarrow q3$	q3	-

NFA for $(b^2a^3)^+$

	a	b
$\rightarrow s$	q3	q2
$\leftarrow q2$	q3	q2
$\leftarrow q3$	q3	-

NFA for b^4

	a	b
$\rightarrow s$	-	q4
$\leftarrow q4$	-	-

NFA for a^5 +

	a	b
$\rightarrow s$	q5	-
$\leftarrow q5$	q5	-

NFA for (b4a5+)

	a	b
<--> s	-	q4
q4	q5	-
<-- q5	q5	-

NFA for (b2*a3+(b4a5+)*)

	a	b
<--> s	q3	q2
q2	q3	q2
<-- q3	q3	q4
q4	q5	-
<-- q5	q5	q4

NFA for b6?

	a	b
<--> s	-	q6
<-- q6	-	-

NFA for (b2*a3+(b4a5+)*b6?)

	a	b
<--> s	q3	q2
q2	q3	q2
<-- q3	q3	q4
q4	q5	-
<-- q5	q5	q4,q6
<-- q6	-	-

NFA for $(b^1 \mid (b^2 a^3 + (b^4 a^5)^+ b^6)^?)$

	a	b
$\rightarrow s$	q3	q1,q2
$\rightarrow q1$	-	q1
q2	q3	q2
$\rightarrow q3$	q3	q4,q6
q4	q5	-
$\rightarrow q5$	q5	q4,q6
$\rightarrow q6$	-	-

Converting the above NFA to DFA gives:

	a	b
$\rightarrow \{s\}$	{q3}	{q1,q2}
$\rightarrow \{q3\}$	{q3}	{q4,q6}
$\rightarrow \{q1,q2\}$	{q3}	{q1,q2}
$\rightarrow \{q4,q6\}$	{q5}	\emptyset
$\rightarrow \{q5\}$	{q5}	{q4,q6}

(3) Use Glushkov construction to convert the regular expression $(a \mid bb)^* (ba^*)^?$. Next, convert the NFA obtained into a DFA using the subset construction.

We add position to the regular expression:

$(a \mid bb)^* (ba^*)^?$.

to give

$(a1 \mid b2b3)^* (b4a5^*)^?$.

NFA for a1

	a	b
$\rightarrow s$	q1	-
$\rightarrow q1$	-	-

NFA for b2

	a	b
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--> s	-	q2
<-- q2	-	-

NFA for b3

	a	b
--> s	-	q3
<-- q3	-	-

NFA for b2b3

	a	b
--> s	-	q2
q2	-	q3
<-- q3	-	-

NFA for (a1|b2b3)*

	a	b
<--> s	q1	q2
<-- q1	q1	q2
q2	-	q3
<-- q3	q1	-

NFA for b4

	a	b
--> s	-	q4
<-- q4	-	-

NFA for (a5)*

	a	b
<--> s	q5	-
<-- q5	q5	-

NFA for $(b4a5^*)$?

	a	b
$\langle \rightarrow s$	-	q4
$\langle \rightarrow q4$	q5	-
$\langle \rightarrow q5$	q5	-

NFA for $(a1|b2b3)^*(b4a5^*)$?

	a	b
$\langle \rightarrow s$	q1	q2,q4
$\langle \rightarrow q1$	q1	q2,q4
q2	-	q3
$\langle \rightarrow q3$	q1	q2,q4
$\langle \rightarrow q4$	q5	-
$\langle \rightarrow q5$	q5	-

Converting the above NFA to DFA gives:

	a	b
$\langle \rightarrow \{s\}$	$\{q1\}$	$\{q2,q4\}$
$\langle \rightarrow \{q1\}$	$\{q1\}$	$\{q2,q4\}$
$\langle \rightarrow \{q2,q4\}$	$\{q5\}$	$\{q3\}$
$\langle \rightarrow \{q5\}$	$\{q5\}$	$\{\}$
$\langle \rightarrow \{q3\}$	$\{q1\}$	$\{q2,q4\}$