Assignment 1 – MPI Programming

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1. Distributed Sorting:

1.1 Pseudo-code of algorithm:

The algorithm is used in each process.

For input part, firstly we get array's size from main's argument and generate random numbers with this size. The pseudo-code is as follows.

```
MPI_Init();
Get input;
Set input as array_size;
MPI_Comm_rank(MPI_COMM_WORLD, &rank);
MPI_Comm_size(MPI_COMM_WORLD, &npes);

If(rank==0){
Set sub_array_size to 0;
}else if(rank != npes-1){
Set sub_array_size to array_size/npes;
}else{
Set sub_array_size to array_size - (array_size)/npes*(npes-1);
}

For i = 0: sub_array_size
Generate a random number random;
Set subarray[i] to random;
```

In the next step, we added MPI_IO to get data from specified data file. The related pseudo-code is as below.

```
MPI_Init();
MPI_Comm_rank(MPI_COMM_WORLD, &rank);
MPI_Comm_size(MPI_COMM_WORLD, &npes);
Open file in read only mode with mpi_io;
MPI_File_get_size(file, & filesize);
If(rank == 0){
    Set sub_array_size to 0;
}else if(rank == npes -1){
    Set sub_array_size to filesize-(npes-2)*filesize/(npes-1);
}
Set size_array to filesize/(npes-1);
MPI_File_seek(fh, (rank-1)*size_array*sizeof(int), MPI_SEEK_SET);
```

```
MPI_File_read(fh, subarray, size_array, MPI_INT, &status);
MPI_File_close(&fh);
```

The sorting part is the same in these two situation.

```
If process is not root {
       Osort (subarray):// local sort subarray
       Samples = PickSplitters (subarray);// pick samples from subarray in subprocesses
MPI Gather (sample, sampleNum, MPI INT, rbuf, sampleNum, MPI INT, ROOT,
MPI_COMM_WORLD) // get all samples from sub-process into root
If process is root{
      receive samples;
       qsort(samples);//local sort all samples
       splitters = PickSplitters(allSamples);//pick splitters from sorted samples
       // from root broadcast all splitters into each sub-array
       MPI Bcast(splitters, sampleNum, MPI INT, ROOT, MPI COMM WORLD);
If process is not root{
      // subprocesses receive splitters from root
       MPI_Bcast(splitters, sampleNum, MPI_INT, ROOT, MPI_COMM_WORLD);
      //compute send counts for all to all exchange
       for i = 0: size_array, j = 0: sample number {
              if subarray[i] <= splitters[j]
                     i++:
                     sendcounts[j+1]++;
              else j++;
       sendcounts[last] = size_array - i;
// send send counts to corresponding process's receive counts
MPI_Alltoall(send counts, recieve counts);
based on sendcounts compute sdispels //send displacements array
based on receivecounts compute rdispels //receive displacements array
MPI_Alltoallv(subarray, scount, sdispls, MPI_INT, subarray_sorted, rcount, rdispls,
MPI_INT, MPI_COMM_WORLD); // all to all exchange bins into corresponding subprocess
Qsort(subarray_sorted);
```

For usage of MPI_IO, the algorithm also contains the following part to write result into a file.

Set output_file to result file name;

1.2 Performance:

Our posted task in Kingspeak cluster is in idle status and thus we tested our code locally with partial data from \$SCRATCH/data/sort_data_debug.dat and the result showed its correctness.

2. Graph Coloring:

- 2.1 We chose hash_map to represent the graph with each node as its keys and associated neighbors as values. If notating the number of nodes as n and edges as e, the memory used to store the graph will be (n + 2*e)*sizeof(int). If a matrix used for the same graph instead, its required memory size will be n*n*sizeof(int), which is larger than the one with hash map for all listed graphs.
- 2.2 In the algorithm, it needs to check the neighbors of nodes from other processes. As a result, we use fstream from c++ library to read the whole graph into each process.
- 2.3 We are not able to get the optimal coloring for a representative set of graphs.
- 2.4 Performance:

Our posted tasks have not gotten their slots totally. As a result, we tested our code with different data set locally. The results are as follows:

Data Set	Thread Num / Core Num	Time Consumed Per Thread (s)
le450_5a.col	4/2	2.4
le450_15b.col	4/2	3.6
le450_25a.col	4/2	3.5

Table 2.1 Results of Graph Coloring Test

3. Maximum Sub-array Sum:

3.1 The pseudo-code of a divide & conquer algorithm is as follows:

```
\begin{aligned} & \text{Max\_crossing\_subarray}(a,1,n/2,n) \{ \\ & \text{Set left\_sum to -inf;} \\ & \text{Set sum to 0;} \\ & \text{for } i = n/2:-1:0 \{ \end{aligned}
```

```
Set sum to sum+A[i];
              if sum > left_sum
                     Set left_sum_sum to sum;
       Set right_sum to -inf;
       Set sum to 0;
       for i = n/2+1 : 1: n
              Set sum to sum+A[i];
              if sum > right_sum
                     set right_sum_sum to sum;
      return left_sum + right_sum;
}
Max_subarray(a,low,high){
      if low == high
              return a[low];
       else{
              Set mid to (low + high) / 2;
              Set left_sum to Max_subarray (a,low,mid);
              Set right_sum to Max_subarray(a,mid+1,high);
              Set cross_sum to Max_crossing_subarray(a,low,mid,high);
              return max{left_sum,right_sum,cross_sum};
       }
```

The pseudo-code of linear algorithm is as below:

```
\begin{aligned} & \text{Max\_subarray\_linear}(a,n) \{ \\ & \text{Set sum, current\_max to 0}; \\ & \text{for } k = 1:n \\ & \text{if sum} + a[k] > 0 \\ & \text{Set sum to sum} + a[k]; \\ & \text{if sum} > \text{current\_max} \\ & \text{Set current\_max to sum;} \\ & \text{else} \\ & \text{Set sum to 0}; \\ & \text{return current\_max;} \end{aligned}
```

3.2 The pseudo-code for parallel divide & conquer algorithm is:

```
prefix_sum(array,length,npes,subarray,MIP_COMM_WORLD){
    prefixSum;
    if length == 1
        Set prefixSum to array;
    total_prefix;
```

```
MPI_SCATTER (array,length / npes,MPI_INT,subarray,length /
              neps,MPI_INT,MIP_COMM_WORLD);
       for i = 0: (length / noes-1)
              Set prefix [i] to prefix sum of subarray;
       MPI_SCAN(prefix[length/npes-1],total_prefix,1,datatype,MPI_SUM,comm);
      for m = 0: (length / noes-1){
              Set prefix[m] to total_prefix - prefix[length / noes-1];
      return prefix;
}
suffix sum(array,length,npes,subarray,MIP COMM WORLD){
      suffixSum;
      if length == 1
              Set suffixSum to array;
      total_suffix;
       for i = (npes-1) : 0
              Set sendcounts[i] to length / npes;
              Set displs[i] to (length / npes - 1);
       }
      MPI_SCATTERV (array,sendcounts,displs,MPI_INT,subarray,length /
              npes,MPI_INT,length / neps,MPI_INT,root,MIP_COMM_WORLD);
      for i = (length / noes-1) : 0
              Set suffix [i] to suffix sum of subarray;
      MPI SCAN(suffix[length/npes-1],total suffix,1,datatype,MPI SUM,comm);
      for m = 0: (length / noes-1){
              Set suffix[m] to total_suffix - suffix[0];
       }
      return suffix;
Max\_crossing\_subarray(a,1,n/2,n){
       Set max prefix process to max(prefix sum(a[n/2:n]));
      Set max_suffix_process to max(suffix_sum(a[1:n]));
      scan (max_prefix_process, max_prefix, 1, MPI_INT, MPI_MAX, root,comm);
      scan (max_suffix_process, max_suffix, 1, MPI_INT, MPI_MAX, root,comm);
      return max suffix + max prefix;
Max_subarray(a,low,high){
      if low == high
              return a[low];
       else{
```

```
Set mid to (low + high) / 2;
              Set left_sum to Max_subarray (a,low,mid);
              Set right sum to Max subarray(a,mid+1,high);
              Set cross_sum to Max_crossing_subarray(a,low,mid,high);
              return max{left_sum,right_sum,cross_sum};
       }
}
prefix_sum(array,length,npes,subarray,MIP_COMM_WORLD){
       prefixSum;
      if length == 1
              set prefixSum to array;
       total_prefix;
       MPI_SCATTER (array,length / npes,MPI_INT,subarray,length /
              neps,MPI_INT,MIP_COMM_WORLD);
       for i = 0: (length / noes-1){
              if prefix [i-1] + array[i] > 0
                     set prefix [i] to prefix sum of subarray;
              else set prefix[i] to 0;
       MPI_SCAN(prefix[length/npes-1],total_prefix,1,datatype,MPI_SUM,comm);
       for m = 0: (length / noes-1){
              if prefix + total_prefix - prefix[length / noes-1] > 0
                     set prefix[m] to prefix[m]+ total_prefix - prefix[length / noes-1];
              else
                     set prefix[m] to 0;
       return prefix;
Max_subarray_linear(a,n){
       Set prefix to prefix_sum(a);
       Set max_process to max(prefix);
       scan (max_process, max, 1, MPI_INT, MPI_MAX, root,comm);
       return max;
}
```

3.3 The best algorithm should use n/log(n) processes, where n is the size of array, and size of each subarray in processes is log(n).

It is called EREW PRAM algorithm, which has the following steps:

- A. for all Pi, where i < -1 to $n/\log(n)$ in parallel, do compute prefix sum as sum[1...n], end;
- B. for all Pi, where i <-1 to $n/\log(n)$ in parallel , do compute min[1...n], where $min[i] = MIN\{sum[0],...,sum[i-1]\}$,end;
- C. for all Pi, where i < -1 to n/log(n) in parallel , do compute cand[1...n], where cand[i] = sum[i] min[i],end;

- D. for all Pi, where i <-1 to n/log(n) in parallel , do compute M[1...n], where $M[i] = MAX\{cand[1], ..., cand[i]\}$, end;
- E. output M[n];