

1 Patterns Of Proofs

1.1 Proof by Contradiction

1. A proof by contradiction is essentially proving the contrapositive of $T \implies P$, which is, $\neg P \implies F$, this means if we can prove that $\neg P \implies F$, then P must be true.

1.2 Proofs about Sets

1. Informally, a set is just a collection of objects, which are called elements.
2. A set can contain a set.
3. $\{x, x\} = \{x\}$.

Symbol	Set	Elements
\emptyset	empty set	
\mathbb{N}	non-negative integers	$\{0, 1, 2, \dots\}$
\mathbb{Z}	integers	$\{\dots, -1, 0, 1, \dots\}$
\mathbb{Q}	rational numbers	0.5, -9, 33.33, ect
\mathbb{R}	real numbers	$\pi, \sqrt{2}, 9.9$, ect.
\mathbb{C}	complex numbers	i, 34, ect.

1. \mathbb{R}^+ is only positive real numbers.