1 Putnam

1. Divide and conquer to understand better, i.e. to check if something is divisible, break it up, $\frac{10+5}{2} = \frac{10}{2} \frac{5}{2}$, now check, if one is fraction and other is not, then sum is integer + fraction.

2 Patterns Of Proofs

2.1 Proof by Contradiction

- 1. A proof by contracdiction is essentially proving the contrapositive of T \implies P, which is, $\neg P \implies F$, this means if we can prove that $\neg P \implies F$, then P must be true.
- 2. We have to assume the initial statement is false, and take the negation to be true
- 3. If a sequance of deduction contradicts the hypothesis then we have an inderect proof.
- 4. If it contradicts a fact to be known true we have reductio ad absurdum.

2.2 Proofs about Sets

- 1. Informally, a set is just a collection of objects, which are called elements.
- 2. A set can contain a set.
- 3. $\{x, x\} = \{x\}$.

| Symbol | Set | Elements |
|--------------|-----------------------|------------------------------------|
| Ø | empty set | |
| \mathbb{N} | non-negative integers | $\{0, 1, 2,\}$ |
| $\mathbb Z$ | integers | $\{, -1, 0, 1,\}$ |
| \mathbb{Q} | rational numbers | 0.5, -9, 33.33, ect |
| \mathbb{R} | real numbers | $\pi, \sqrt{2}, 9.9, \text{ ect.}$ |
| \mathbb{C} | complex numbers | i, 34, ect. |

1. \mathbb{R}^+ is only positive real numbers.