

A Learnable Search Result Diversification Method

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Abstract

Search result diversification is to tackle the ambiguous queries and multifaceted information needs. The search result diversification problem can be formalized as a balance between the relevance score and the diversity score. Most previous diversification models utilize a predefined function to calculate the diversity score. The values of parameters need to be tuned by manual experiments. It is time-consuming and hard to reach optimal result in diversity evaluation. Proposing a learnable approach to solve the above problems is a pressing task. Therefore we introduce a Learnable Search Result Diversification model called L-SRD. On this basis, we redefine the diversity function and derive our loss function as the likelihood loss of ground truth generation. Stochastic gradient descent algorithm is employed to optimize the values of parameters. Finally we derive our ranking function to generate the diverse list sequentially. Due to the learning model, the values of parameters are determined automatically and get optimally. The experiments on TREC web tracks show that our approach outperforms several existing diversification models significantly.

Keywords: Explicit Search Result Diversification, Learning Model, Markov Random Fields

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1. Introduction

There are many ambiguous queries in search system. The keyword **apple** may refer to the Apple, one of the most famous companies in the world, or the electronics Apple manufactures. It may be the most familiar fruit also.
5 There are many aspects of information needs underlying a simple query. How to produce a good quality diverse result is our main concern.

The existing diversification approaches have been categorized as either implicit approaches or explicit approaches. The implicit approaches assume each document representing its own aspect and promote diversity by selecting documents for different aspects based on the difference of their vocabulary Carbonell & Goldstein (1998). It is a less effective model for the reason that it cannot express the inherent meaning well Agrawal et al. (2009); Zhai et al. (2003). The explicit approaches are proposed to overcome the weakness. They explicitly formalize the aspects underlying a query and select documents that cover different
15 aspects. The xQuAD and PM2 are classic explicit models Santos et al. (2010a); Dang & Croft (2012). But they just utilize a predefined function to calculate the diversity score based on query aspects. It is subjective and hard to reach optimal result.

In this paper, we treat the Query Aspect Diversification as a learning problem and propose a Learnable Search Result Diversification (L-SRD) method. We incorporate various features into diversity measurement based on the Markov Random Field (MRF), which enables the integration of various types of features. The values of parameters can be determined automatically, which saves the manual labour, and the parameters are more optimal. Firstly we re-
25 fine the diversity function and derive our loss function as the likelihood loss of ground truth generation. Then Stochastic gradient descent algorithm is employed to optimize the values of weights. Finally we derive our ranking function to generate the diverse list sequentially.

We conduct a series of experiments to demonstrate that L-SRD is more effective than other diversification models in terms of the official evaluation metrics
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including α -nDCG, ERR-IA, NRBP and the classical diversification metrics such as Precision-IA and Aspect Recall Clarke et al. (2008); Chapelle et al. (2009); Clarke et al. (2009b). Additionally, we get a remarkable performance in robust evaluation.

35 The main contributions of our work are listed as follows:

1. L-SRD introduces the learning mechanism to the query aspect diversification model. We conduct inference for the loss function based on its sequential selection model, which solves the parameters tuning problem automatically at the same time.
- 40 2. We utilize the Markov Random Field to integrate different types of features to address the diversity measurement problem for query aspect search result diversification.
3. We propose a sequential prediction method, which selects the best document from candidate set by maximizing ranking score.
- 45 4. We conduct extensive experiments to verify L-SRD achieve better performance comparing with the existing diversification methods.

The remainder of this paper is organized as follows. Section 2 introduces the current research situation on the search result diversification. Section 3 describes the definition of the loss function and the estimation of parameters.

50 Sections 4 and 4.3 detail the experiments setup on the TREC web track and their evaluations. In Section 5, we summarize our achievements and give future works.

2. Related Work

Search result diversification has a wide range of applications, such as patent search Kim & Croft (2015), legal information retrieval Koniaris et al. (2017) and so on. The process of diversification can be characterized as a bidirectional optimization problem, in which one seeks to maximize the overall relevance of a document ranking to multiple query aspects, while minimizing its redundancy Santos et al. (2010b). In particular, the existing approaches can be categorized

60 as either implicit or explicit making a difference in how they account for the query aspects Santos et al. (2010c).

The basic assumption of implicit diversification approaches is that dissimilar documents are more likely to satisfy different information needs. The most representative approach in maximal marginal relevance (MMR) method and its probabilistic variants is shown as follows Zhai et al. (2003):

$$S_{MMR}(q, d, c) = (1 - \lambda)S^{rel}(d, q) - \lambda \max_{d_j \in C} S^{div}(d, d_j) \quad (1)$$

where S^{rel} and S^{div} represents document d 's relevance to the query q and its similarity to a selected document d_j respectively. To gain high ranking score, a document should not only be relevant, but also be dissimilar from the selected documents. The special process of MMR proposed by Garbonell & Goldstein is selecting the document iteratively Carbonell & Goldstein (1998), and
65 meanwhile, both content-based relevance and diversity relation between current selected document and the previously selected documents are considered. Yu et al. formulate this as a process of selecting and ranking k exemplar documents and utilize linear programming to solve this problem Yu et al. (2017).
70 In summary, they are all implicit approaches without using aspects to mine the underlying aspects, besides, they are a low effective approaches Santos et al. (2010a); Drosou & Pitoura (2010).

Explicit approaches make use of the aspects underlying the query to select
75 documents that cover different aspects as far as possible. The algorithms such as IA-select Agrawal et al. (2009), xQuAD Santos et al. (2010a) and RxQuAD Vargas et al. (2012) are proposed to reduce redundancy on the aspect levels. These methods select documents that cover more novel aspects. The PM-1 and PM-2 models pay more attention to maintain the proportionality of aspects Dang &
80 Croft (2012). They produce the ranked result according to the proportionality of aspects. Intrinsic diversity products a series of successor queries to figure out the appropriate content to cover Raman et al. (2013). Wang et al. (2016) and Hu & et al. (2015) think the aspects underlying the query should be hierarchical, and propose some hierarchical measures to find the relationships among aspects.

85 Ullah et al. (2016) mine query subtopic by exploiting the word embedding and short-text similarity measure. To conclude, all existing explicit approaches are unsupervised, and the values of parameters need to be tuned by the experiment repeatedly without intention, causing a time-consuming optimizing problem to find the most suitable parameters.

90 Some learning approaches are also proposed for search result diversification. For example, Zhu et al. (2014) use structural SVM to learn to identify a document subset with maximum word coverage, but they just learn the maximum word coverage and do not mine the aspects underlying the query. Xia et al. (2015) utilize both positive and negative ranking documents to train a maximal
95 marginal relevance model for ranking. Xia et al. (2016) propose a neural tensor network to learn a nonlinear novelty function to select document. However, different from the existing approaches, we use a learnable process to identify features from documents using Markov Random Field. Besides, we redefine the diversity function and derive our loss function as the likelihood loss of ground
100 truth generation to resolve this bidirectional optimization problem.

3. Learning Approach for Search Result Diversification

3.1. Mining aspects underlying the query

The key step for Query Aspects Diversification model is mining the aspects underlying the query. With the help of query aspects, we can generate the
105 diverse ranking list by minimizing the redundancy on the basis of the aspects. We mine the query aspects like Santos et al. (2010a), issuing the query to the commercial search engine (we use Yahoo) and get back the query suggestion result list as the aspects. Next, we can use these aspects as a new query to search the candidate document set D and we can get the relevance score between
110 the aspect q_i and each document d in D , which can be formalized as $P(q_i|d)$.

3.2. Topic diversity model

Traditional topic diversity model is a greedy approximation. It sequentially selects the “local-best” document from the candidate document set Santos et al. (2010a). The original function is formalized as follows:

$$f(d, \bar{S}) = (1 - \lambda)P(d|q) + \lambda \sum_{q_i \in Q} P(q_i|q)P(d|q_i)P(\bar{S}|q_i). \quad (2)$$

where d denotes for the current document to be considered in the sequential process, \bar{S} denotes for the unselected document set (equal to the $D \setminus S$ in Fig. (1)), q denotes for the query, λ is a balance parameter for a trade-off between
115 relevance and diversity, q_i denotes for the aspects underlying the query q .

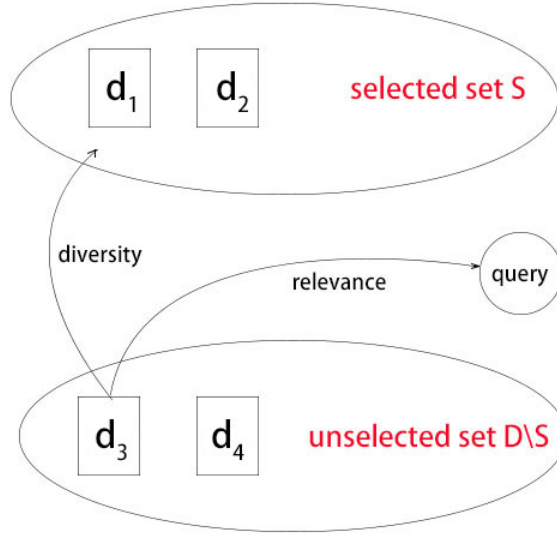


Figure 1: An illustration for sequential selection in topic diversity model

As for Eq. (2), the left part corresponds to the relevance score and the right part corresponds to the diversity score. We look forward to redefine the estimation of diversity score $P(\bar{S}|q_i)$. According to the conditional probabilistic formula, the task can be formalized as follows:

$$P(\bar{S}|q_i) = \frac{P(\bar{S}, q_i)}{P(q_i)} \stackrel{rank}{=} P(\bar{S}, q_i) \quad (3)$$

where $P(q_i)$ denotes the occurrence rate of aspects q_i corresponding to query q , which is usually regard to be normalized as $1/n$ (n denotes the number of

aspects) Santos et al. (2010a). Because the values of $P(q_i)$ are equal and do not impact on the result of ranking, we neglect $P(q_i)$.

120 The main concern is how to define feature function for $P(\bar{S}, q_i)$. There are many ways to integrate different features, just like linear regression, logistic regression and some other ways. Under our situation, we use Markov Random Field (MRF) to model $P(\bar{S}, q_i)$. We benefit from its convenient combination of different types of features and we can get its derivation easily.

125 3.3. Feature extraction via MRF

A MRF is a probabilistic model defined on an undirected graph G . In MRF model, the nodes represent the random variables and the edges represent dependencies between these variables. In our study, the nodes represent the aspect q_i and the unselected set \bar{S} . Consequently, we compute the joint probability defined over the graph G as follows:

$$P(\bar{S}, q_i) = \frac{\prod_{l \in L(G)} \phi_l(l)}{Z}, \quad (4)$$

where $L(G)$ is the cliques over the graph G , $\phi_l(l)$ is a potential function defined over the clique l , and $Z = \sum_{\bar{S}, q_i} \prod_l \phi_l(l)$ is the normalization factor to ensure that $P(\bar{S}, q_i)$ satisfies a probability distribution.

The potential function is usually defined like:

$$\phi_l(l) = \exp(\lambda_l f_l(l)), \quad (5)$$

where $f_l(l)$ is a feature function defined over clique l , and λ_l is the corresponding weightiness factor. By applying log function and neglecting normalization factor, the final feature function is formalized as follows:

$$P(\bar{S}, q_i) \stackrel{rank}{=} \sum_{l \in L(G)} \lambda_l f_l(l). \quad (6)$$

Note that Eq. (6) is derived from Eq. (4) by neglecting the log function because
130 its form is more simple for derivation and the simplifying does not impact the learning and ranking. Nextly, we specify the structure of graph G and its clique set $L(G)$ to derive our final feature functions.

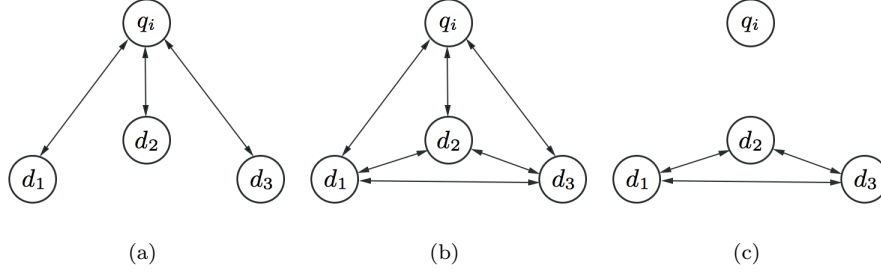


Figure 2: An illustration for three types of cliques. The graph G contains a aspects node q_i and three document nodes (just for example) that correspond to the documents in the unselected set \bar{S} . (a) l_{sd} contains q_i and a single document node; (b) l_{sD} includes q_i and the whole \bar{S} ; (c) l_D only contains \bar{S} .

Fig. (2) shows the three types of cliques in MRF. The formal description about feature extraction based on three cliques is given as follows:

- 135 1. Based on l_{sd} . The high occupancy of aspects q_i reflects the high potential relevance for q_i with respect to \bar{S} .
 - We define $f_{ave-topic} = ave_{d \in \bar{S}} P(q_i|d)$ for feature function on this clique. $P(q_i|d)$ is the aspects distribution measurement which we have mentioned in section 3.1.
- 140 2. Based on l_{sD} . The clique involves the inter-relationships in the candidate set \bar{S} .
 - We use the maximal, minimal, standard deviation of the $P(q_i|d)_{d \in \bar{S}}$ as feature functions defined upon clique l_{sD} .
 - For the sake of minimizing redundancy, we use the $num_{q_i}(\bar{S}) - num_{q_i}(S)$ as a feature function defined on this clique too. $num_{q_i}(x)$ represents the number of documents in set x with respect to aspects q_i .
- 145 3. Based on l_D . Both l_{sd} and l_{sD} consider relations of documents with respect to the above two aspects. The clique l_D only takes into account the relations among documents excluding aspects q_i . Previous research has

shown that the aspect-independent property can indicate the relevance of documents for q_i Kurland & Domshlak (2008).

- We use the entropy of all the documents d in \bar{S} :
 $P_{entropy}(d) \stackrel{def}{=} - \sum_{w \in d} P(w|d) \log p(w|d)$ as feature function, where w is a term and $p(w|d)$ is the probability that w appears in d (given by the language model).
- Spam ratio inspired by the Web Spam Classification is used for feature function, too Fetterly et al. (2004).

To conclude, by replacing the feature function into equation (2) and putting the parameters λ into the learning process, the ranking function is given as follows:

$$f(d, \bar{S}) = \lambda_r P(d|q) + \lambda_n \sum_{q_i \in Q} [P(q_i|q) P(d|q_i) \sum_{l \in L(G(q_i))} \lambda_l f_l(l)] \quad (7)$$

where $L(G(q_i))$ represents the clique set L from the graph G which is built around the aspects q_i , $f_l(l)$ stands for the feature function defined on the clique l . There exists a parameter λ in equation (2), it is a balance parameter between relevance and diversity. In our learning method, we use λ_r and λ_n to replace it and we can infer its value by learning process.

3.4. Loss function

We define the loss function as a likelihood loss of generation probability:

$$L(rank(D, C), Y) = -\log P(Y|D), \quad (8)$$

where $rank$ denotes the ranking function in our model, C is the feature function defined in unselected set \bar{S} , D denotes all the candidate documents, and Y is the final result of search result diversification. Because our L-SRD model is a sequential selection model, it can be viewed as maximizing probability of correctly choosing the top-n document from unselected set:

$$\begin{aligned} P(Y|D) &= P(y_1, y_2, \dots, y_n|D) \\ &= P(y_1|D) P(y_2|D \setminus S_1) \cdots P(y_n|D \setminus S_{n-1}), \end{aligned} \quad (9)$$

165 where y_1, \dots, y_n is the ground truth for search result diversification task with respect to query q , n represents the top n result generated by the sequential selection process, the index i denotes its ranking position, S_{i-1} denotes the selected set after $i - 1$ iterations, the probability $P(y_i|D \setminus S_{i-1})$ represents the probability that select the document y_i under the condition of $D \setminus S_{i-1}$.

On the basis of the Plackett-Luce Model Marden (1996), we derive the steps in our generation process shown as follows:

$$P(Y|D) = \prod_{i=1}^n P(y_i|D \setminus S_{i-1}) = \prod_{i=1}^n \frac{\exp(f(y_i, D \setminus S_{i-1}))}{\sum_{k=i}^n \exp(f(y_k, D \setminus S_{i-1}))}, \quad (10)$$

where S_0 means empty set \emptyset , function f corresponds to Eq. (7). Incorporating Eq.(10) into Eq.(8), we get the definition of the loss function as follows:

$$L(f(D, C), Y) = - \sum_{i=1}^n \log\left(\frac{\exp(f(y_i, D \setminus S_{i-1}))}{\sum_{k=i}^n \exp(f(y_k, D \setminus S_{i-1}))}\right). \quad (11)$$

To get the final loss function, we simplify Eq. (7) by uniting the parameter λ_n and λ_l (because the parameter in our model all can be decided by the learning process):

$$f(d, \bar{S}) = \lambda_r P(d|q) + \vec{\mu}_d \cdot N_{1...L}(d, q_i, \bar{S}) \quad (12)$$

$$N_l(d, q_i, \bar{S}) = \sum_{q_i \in Q} P(q_i|q) P(d|q_i) f_l(l) \quad (l \in L(G(q_i))) \quad (13)$$

170 where $\vec{\mu}_d$ represents a L -dimensional weight vector, L stands for the number of features, $N_{1...L}$ denotes a series of function vectors, l is the cliques defined on \bar{S} and q_i .

The total loss function is formulized as follows:

$$- \sum_{i=1}^{T_r} \sum_{j=1}^n \log\left(\frac{\exp(\lambda_r P(y_j|q) + \vec{\mu}_d \cdot N_{1...L}(y_j, q_i, \bar{S}))}{\sum_{k=j}^n \exp(\lambda_r P(y_k|q) + \vec{\mu}_d \cdot N_{1...L}(y_k, q_i, \bar{S}))}\right) \quad (14)$$

where T_r denotes the number of training examples.

3.5. Learning and prediction

175 Given the precise definition of loss function, the next step is minimizing the loss function to get the best performance. First, we generate the training

data and apply the optimization method. Next, we use our ranking function to predict the final diverse ranking result.

In this study, we use the data in TREC dataset in a format of quadruples: $(q^{(i)}, RD^{(i)}, T_i, J(s_j^{(i)}|t_k))$, where $q^{(i)}$ means the i -th query q , $RD^{(i)}$ is the corresponding related documents set, T_i represent the aspect underlying the query $q^{(i)}$ which are provided by official labeler, and $J(d_j^{(i)}|t_k)$ represents the judgement factor whether the j -th document $d_j^{(i)}$ in $RD^{(i)}$ covers the aspect t_k . Note that the last two elements in quadruples are used to calculate the score of evaluation metrics (e.g. α -nDCG), we cannot make use of it directly in our model.

At first, we should generate a approximate ground truth for training set. So we construct a list y_i which maximize the diversity metrics, such as α -nDCG, ERR-IA, etc. In our study, we use ERR-IA to measure the results which is described as function f_{ERR-IA} . In algorithm 1, at the every i -th step in loop structure, we select the document d from $D \setminus S_{i-1}$ to maximize the function f_{ERR-IA} and update the $S \setminus D_{i-1}$ by adding the document d . By recording the best document in every step, we get our final ideal ranking list as our training data.

ALGORITHM 1: Ideal ranking list construction algorithm

Input: $(q^{(i)}, RD^{(i)}, T_i, J(s_j^{(i)}|t_k)), f_{ERR-IA}$

Output: y_1, y_2, \dots, y_n

1: initialize $S_0 = \emptyset$

2: **for** $k = 1$ to n **do**

3: $bestDoc \leftarrow \arg \max_{d \in RD^{(i)} \setminus S_{k-1}} f_{ERR-IA}(d \cup S_{k-1})$

4: $S_k = S_{k-1} \cup bestDoc$

5: $y_k = bestDoc$

6: **end for**

Nextly, we use the stochastic gradient descent method to optimize the loss function as shown in Algorithm 2. At every step in algorithm 2, we calculate the gradient according to Eq. (15)-(16) and update the value of weight. The

gradient in step i at training set D_{init} is computed as follows:

$$\Delta\lambda_r^{(i)} = \sum_{j=1}^n \left(\frac{\sum_{k=j}^n P(y_j|q) \exp(\lambda_r^{(i-1)} P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S}))}{\sum_{k=j}^n \exp(\lambda_r^{(i-1)} P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S}))} - \frac{P(y_j|q) \exp(\lambda_r^{(i-1)} P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S}))}{\exp(\lambda_r^{(i-1)} P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S}))} \right) \quad (15)$$

$$\Delta\vec{\mu}_d^{(i)} = \sum_{j=1}^n \left(\frac{\sum_{k=j}^n N_l(y_j, q_i, \bar{S}) \exp(\lambda_r^{(i-1)} P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S}))}{\sum_{k=j}^n \exp(\lambda_r^{(i-1)} P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S}))} - \frac{N_l(y_j, q_i, \bar{S}) \exp(\lambda_r^{(i-1)} P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S}))}{\exp(\lambda_r^{(i-1)} P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S}))} \right) \quad (16)$$

ALGORITHM 2: Parameter learning algorithm

Input: training data: $D_{init}^{Tr}, (y_1...y_n)^{Tr}$

parameter: learning rate η , tolerate ϵ

Output: $\lambda_r, \vec{\mu}_d$

1: Initialize $\lambda_r, \vec{\mu}_d$

2: **repeat**

3: $\lambda_r^{(0)} = \lambda_r, \vec{\mu}_d^{(0)} = \vec{\mu}_d$

4: Randomly choose one of the training data

5: **for** $i = 1, \dots, n$ **do**

6: Compute the gradient $\Delta\lambda_r^{(i)}$ and $\Delta\vec{\mu}_d^{(i)}$

7: Update: $\lambda_r^{(i)} = \lambda_r^{(i-1)} - \eta\Delta\lambda_r^{(i)}, \vec{\mu}_d^{(i)} = \vec{\mu}_d^{(i-1)} - \eta\Delta\vec{\mu}_d^{(i)}$

8: **end for**

9: $\lambda_r = \lambda_r^{(n)}, \vec{\mu}_d = \vec{\mu}_d^{(n)}$

10: **until** change for value of loss function below the tolerate ϵ

195 Finally, we propose a sequential prediction method as described in Algorithm

3. At the i -th step in algorithm 3, we select the best document d from $D \setminus S_{i-1}$ to maximize our ranking score and update the candidate set $D \setminus S_{i-1}$ by adding document d . By recording the best document in every step, we predict the final

diverse ranking list as result.

ALGORITHM 3: The prediction process

Input: query q and its retrieval result D_{init} , weight λ_r and λ_{nl}

Output: y_1, y_2, \dots, y_n

1: $S_0 = \emptyset$

200 2: **for** $i = 1, \dots, n$ **do**

3: $best = \arg \max_{d \in D \setminus S_{i-1}} f(d, D \setminus S_{i-1})$

4: $S_i = S_{i-1} \cup best$

5: $y_i = best$

6: **end for**

4. Experiment

4.1. Dataset and evaluation metrics

There are 150 queries in our query set, from TREC web track 2009 (WT2009) Clarke et al. (2009a), WT2010, WT2011(50 for each). Evaluation is done on the
 205 ClueWeb09 Category B retrieval collection¹. The collection consists of nearly 50 millions web pages in English. There is a list of aspects for each query with binary relevance judgements, which are provided by TREC assessors.

There are three mainly evaluation metrics we use to evaluate the performance of our method: α -nDCG Clarke et al. (2008), ERR-IA Chapelle et al.
 210 (2009), NRBP Clarke et al. (2009b). α -nDCG is used to balance both relevance and diversity of candidate documents. ERR-IA measures the expected effort required for a user to satisfy their information needs. And NRBP is a feasible metric to evaluate the balance between the complexity of needs and the query. These metrics penalize redundancy in a different degree for the document at
 215 each sorted position to maximize the aspects coverage. Additionally, we report our result using Precision-IA and Aspect Recall too. To measure the robustness, we use Win/Loss ratio metrics Yue & Joachims (2008); Dang & Croft (2012). The Win/Loss ratio denotes whether the model improve or hurt the result when comparing with the basic relevant baseline QL in terms of evaluation

¹<http://www.lemurproject.org/clueweb09.php/>

220 metrics Dang & Croft (2012). Particularly in our experiment, we use ERR-IA
to calculate the Win/Loss ratio.

The evaluation metrics are reported at different cutoffs. We use {5, 10, 20}
as our cutoffs to set up experiments. These cutoffs focus on the evaluation at
early ranking, which are particularly important in a Web search context Jansen
225 et al. (1998). The α is set to 0.5 in our experiments for the reason it gives equal
weight to both relevance and diversity.

4.2. Baseline methods

We use the Indri² to conduct our retrieval experiments and run with its
default parameters configuration. All of the search result diversification methods
230 are applied based on the top- K retrieved documents. As for the parameter K , we
conduct a series of tests to find the appropriate K maximizing the performance,
which found 50 achieves the best result.

Besides the baseline retrieval models, we compare L-SRD with some ad-
vanced diversification models as follows:

- 235 • **QL**. The Query-likelihood language model is used for indri search engine
as an initial retrieval method. We use it to provide the initial top 1000
documents for our diversification method. We also use it as a baseline
method Dang & Croft (2012).
- **MMR**. A classical implicit diversification model. It is a representation
240 of comparison between implicit and explicit models Carbonell & Goldstein
(1998).
- **xQuAD**. xQuAD is a popular explicit diversification model which focuses
on the redundancy of aspects Santos et al. (2010a).
- **PM2**. PM2 is a popular explicit diversification model. PM2 generates the
245 result set according to the aspects proportionality Dang & Croft (2012).

²<http://www.lemurproject.org/indri.php>

- **SVMDIV**. SVMDIV is also a learning model for search result diversification Yue & Joachims (2008). It uses the structural SVMs to optimize the aspects coverage problem. But it only models the diversity without consideration of relevance. We get the source code from the svmdiv homepage³ provided by the author.
- **HxQuAD** is a hierarchical diversification model based on xQuAD Hu & et al. (2015).
- **SMWE** mines query subtopic by exploiting the word embedding and short-text similarity measure. Ullah et al. (2016)

These baselines 2-4 (corresponding to MMR, xQuAD, PM2) possess a single parameter λ to tune, we perform a 5-fold cross validation to train λ through optimizing ERR-IA. In our model, we use a 5-cross validation with a ratio of 3:1:1 for training, validation and prediction for the test query on each year. The final results are calculated over all the folds.

4.3. Experimental results

In particularly, our experiments aim to answer two main questions:

1. Can we utilize learning mechanism to promote the performance of search result diversification?
2. Does L-SRD achieve better performance in terms of robustness comparing to other search result diversified models?

4.3.1. Diversification analysis

To answer question 1, we compare our L-SRD with other diversification models in terms of diversification metrics. Table 1 shows the result of the evaluation in terms of α -nDCG, ERR-IA, and NRBP. The best result per line is highlighted in bold. The classical MMR method is used as a representative of implicit diversification model Carbonell & Goldstein (1998). As for explicit

³<http://projects.yisongyue.com/svmdiv/>

model, we consider xQuAD and PM2 Santos et al. (2010a); Dang & Croft (2012). SVMDIV is selected for the representative of learning methods, HxQuAD is selected for the hierarchical model.

275 The result shows that L-SRD always performs best in terms of all metrics as shown in Table 1. It consistently improves the initial retrieval ranking method with gains up to 23.19%, 31.17%, 15.11% in terms of α -nDCG on WT2009, WT2010, WT2011 respectively. It indicates that our learning approach tackles the diversity measurement problem more effectively with the consideration of
280 integrate different features. The reason is that features such as query-aspects relevance and information richness conform to the property of diversity. Furthermore, comparing with the explicit diversification models in terms of the evaluation of α -nDCG, the improvement of L-SRD over the xQuAD is up to 28.44%, 16.87%, 14.90% on WT2009, WT2010, WT2011 respectively, and the improve-
285 ment of L-SRD over the PM2 is up to 14.15%, 23.11%, 14.65% on WT2009, WT2010, WT2011 respectively. Previous explicit diversifications use a predefined function to calculate the diversity score, which cannot reach an optimal result from the overall situation. A learnable approach to solve the diversity measurement and parameter tuning problem is significative. In addition, comparing with the hierarchical diversification model in terms of the evaluation of
290 α -nDCG, the improvement of L-SRD over the HxQuAD is up to 3.77%, 9.68%, 5.49% on WT2009, WT2010, WT2011 respectively. HxQuAD only use a predefined function to measure the diversity score, and the parameters may not be optimal because it needs to be tuned manually. Our learning model tackles the
295 parameters tuning problem in an automatic fashion and reaches optimal result. Comparing with SWME in terms of the evaluation of α -nDCG, the improvement of L-SRD over the HxQuAD is up to 3.63%, 5.35%, 3.86% on WT2009, WT2010, WT2011 respectively. SMWE mines enough subtopics, but it cannot learn enough features to represent the document. Besides the non-learning
300 model, the improvement of L-SRD over the SVM DIV is up to 10.18%, 14.70%, 11.09% on WT2009, WT2010, WT2011 respectively. It shows that considering relevance and different types of features in diversity measurement is helpful in

the learning approach. That is the reason why our model wins. Therefore, L-SRD shows better understanding on the diverse ranking and leads to a better result. So we find that utilizing learning mechanism indeed promotes the performance of search result diversification.

We consider not only the advanced diversity metrics, but also traditional diversity metrics, such as Precision-IA and Aspect Recall. The former indicates how many relevant documents for each aspect we have for reranking, the latter indicates how many of the aspects for which we have relevant documents. The result is shown in Fig. 3. MMR still underperforms all of them, as for Precision-IA, xQuAD wins on WT2010 casually, while L-SRD performs more stable, even on WT2010, the gap is small. It proves that L-SRD outperforms others from different perspectives. Our learnable model solves the diverse ranking problem in a global perspective and always reaches prominent results.

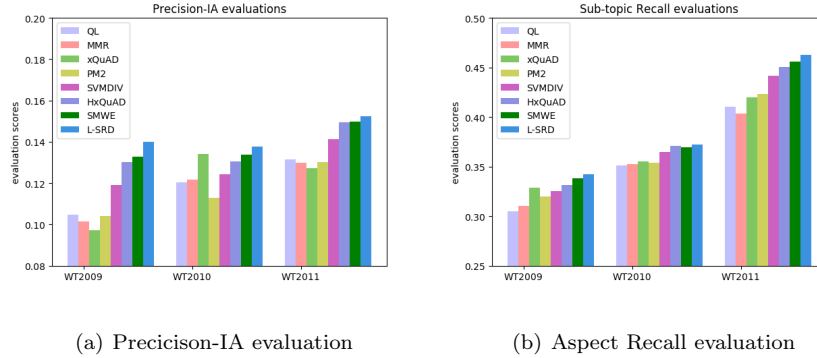


Figure 3: Performance comparison in WT2009, WT2010, WT2011 with Precision-IA and Aspect Recall

4.3.2. Robustness analysis

An effective search result diversification method should not only outperform other models in terms of diversity metrics, but also maintain a high level of robustness, which we have raised the question 2. We set up series of experiments on robustness research to study the Win/Loss behaviour and the usage of different retrieval algorithms respectively.

Year	experiment	ERR-IA@20	α -nDCG@20	NRBP
2009	QL	0.1376	0.2548	0.1008
	MMR	0.1405	0.2526	0.1070
	xQuAD	0.1411	0.2444	0.1113
	PM2	0.1482	0.2750	0.1101
	SVMDIV	0.1531	0.2849	0.1219
	HxQuAD	0.1653	0.3025	0.1372
	SMWE	0.1787	0.3029	0.1482
	L-SRD	0.1862	0.3139	0.1615
2010	QL	0.1484	0.2445	0.1092
	MMR	0.1494	0.2450	0.1129
	xQuAD	0.1732	0.2746	0.1326
	PM2	0.1599	0.2605	0.1175
	SVMDIV	0.1698	0.2796	0.1158
	HxQuAD	0.1807	0.2924	0.1303
	SMWE	0.2038	0.3044	0.1601
	L-SRD	0.2193	0.3207	0.1826
2011	QL	0.3288	0.4454	0.2802
	MMR	0.3253	0.4337	0.2834
	xQuAD	0.3235	0.4462	0.2812
	PM2	0.3316	0.4472	0.2831
	SVMDIV	0.3429	0.4615	0.2923
	HxQuAD	0.3606	0.4860	0.3107
	SMWE	0.3924	0.4936	0.3232
	L-SRD	0.4078	0.5127	0.3374

Table 1: Diversification performance using the official evaluation metrics for WT2009, WT2010, WT2011

From table 2, we find that L-SRD model performs best with its ratio of 2.65. While the Win/Loss ratio of MMR, xQuAD, PM2, SVMDIV, HxQuAD

experiment	WT2009	WT2010	WT2011
MMR	20/18	24/17	23/16
xQuAD	23/18	23/16	24/14
PM2	22/20	26/14	25/14
SVMDIV	24/18	27/13	27/13
HxQuAD	27/15	30/10	31/10
SMWE	27/14	29/11	32/11
L-SRD	28/14	30/10	32/10

Table 2: Win/Loss ratio

and SMWE is 1.31, 1.46, 1.52, 1.77, 2.51, 2.44 respectively. It reflects the remarkable robustness of L-SRD model comparing with other outstanding diversification models. The promotion of robustness over the MMR, xQuAD, PM2, SVMDIV, HxQuAD and SMWE is up to 102.28%, 81.51%, 74.34%, 49.72%, 5.58 %, 8.61% respectively. And it confirms the overall performance of our model is not restricted to a small subset, it still works in the whole dataset for three years data. Our different types of features and learning approach address this problem well.

5. Conclusion and Future Work

In this paper, we propose a Learnable Search Result Diversification model (L-SRD). We pay our attention to the explicit Query Aspect Diversification models and introduce the learning approach to regard the model as a learning problem. Unlike the traditional explicit diversification models utilizing a predefined novelty measure function, we integrate different types of diversity features and estimate the weight with a learning approach. We derive our loss function as the likelihood of ground truth generation. Stochastic gradient descent algorithm is used to estimate the values of parameters. Benefiting from the learning approach, we can optimize the parameters in an automatic method. The prediction of our diversification model is provided by iterative maximizing

the learned ranking function.

We have demonstrated the improvement of L-SRD comparing with other
345 diversification models. We find L-SRD achieve considerable results in terms of
official diversity metrics on three years in TREC web track dataset. To prove its
robustness, we set the experiment about Win/Loss ratio and usage of different
retrieval algorithms. We believe L-SRD will play an important role to improve
the Query Aspect Search Result Diversification by using a learning method.

350 There exist a number of directions to be explored in the future. We look
forward to take some considerable steps to make L-SRD achieve convergency as
quick as possible.

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