

A Learnable Search Result Diversification Method

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Abstract

Search result diversification is to tackle the ambiguous queries and multifaceted information needs. The search result diversification problem can be formalized as a balance between the relevance score and the diversity score. Most previous diversification models utilize a predefined function to calculate the diversity score. The values of parameters need to be tuned by manual experiments. It is time-consuming and hard to reach optimal result in diversity evaluation. Proposing a learnable approach to solve the above problems is a pressing task. Therefore we introduce a Learnable Search Result Diversification model called L-SRD. On this basis, we redefine the diversity function and derive our loss function as the likelihood loss of ground truth generation. Stochastic gradient descent algorithm is employed to optimize the values of parameters. Finally we derive our ranking function to generate the diverse list sequentially. Due to the learning model, the values of parameters are determined automatically and get optimally. The experiments on TREC web tracks show that our approach outperforms several existing diversification models significantly.

Keywords: Explicit Search Result Diversification, Learning Model, Markov Random Fields

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1. Introduction

There are many ambiguous queries in search system. The keyword **apple** may refer to the Apple, one of the most famous companies in the world, or the electronics Apple manufactures. It may be the most familiar fruit also.
5 There are many aspects of information needs underlying a simple query. How to produce a good quality diverse result is our main concern.

The existing diversification approaches have been categorized as either implicit approaches or explicit approaches. The implicit approaches assume each document representing its own aspect and promote diversity by selecting documents for different aspects based on the difference of their vocabulary (Carbonell & Goldstein (1998)). It is a less effective model for the reason that it cannot express the inherent meaning well (Agrawal et al. (2009); Zhai et al. (2003)). The explicit approaches are proposed to overcome the weakness. They explicitly formalize the aspects underlying a query and select documents that cover different aspects. The xQuAD and PM2 are classic explicit models (Santos et al. 15 (2010a); Dang & Croft (2012)). But they just utilize a predefined function to calculate the diversity score based on query aspects. It is subjective and hard to reach optimal result.

In this paper, we treat the Query Aspect Diversification as a learning problem and propose a Learnable Search Result Diversification (L-SRD) method. We incorporate various features into diversity measurement based on the Markov Random Field (MRF), which enables the integration of various types of features. The values of parameters can be determined automatically, which saves the manual labour, and the parameters are more optimal. Firstly we re-define the diversity function and derive our loss function as the likelihood loss of 25 ground truth generation. Then Stochastic gradient descent algorithm is employed to optimize the values of weights. Finally we derive our ranking function to generate the diverse list sequentially.

We conduct a series of experiments to demonstrate that L-SRD is more effective than other diversification models in terms of the official evaluation metrics 30

including α -nDCG, ERR-IA, NRBP and the classical diversification metrics such as Precision-IA and Aspect Recall (Clarke et al. (2008); Chapelle et al. (2009); Clarke et al. (2009b)). Additionally, we get a remarkable performance in robust evaluation.

35 The main contributions of our work are listed as follows:

1. L-SRD introduces the learning mechanism to the Query Aspect Diversification model. We conduct inference for the loss function based on its sequential selection model, which solves the parameters tuning problem automatically at the same time.
- 40 2. We utilize the Markov Random Field to integrate different types of features to address the diversity measurement problem for Query Aspect Search Result Diversification.
3. We conduct extensive experiments to verify L-SRD achieve better performance comparing with the existing diversification models.

45 The remainder of this paper is organized as follows. Section 2 introduces the current research situation on the search result diversification. Section 3 describes the definition of the loss function and the estimation of parameters. Sections 4 and 4.3 detail the experiments setup on the TREC web track and their evaluations. In Section 5, we summarize our achievements and give future
50 works.

2. Related Work

Search result diversification has a wide range of applications, such as patent search (Kim & Croft (2015)), legal information retrieval (Koniaris et al. (2017)) and so on. The process of diversification can be characterized as a bidirectional
55 optimization problem, in which one seeks to maximize the overall relevance of a document ranking to multiple query aspects, while minimizing its redundancy (Santos et al. (2010b)). In particular, the existing approaches can be categorized as either implicit or explicit making a difference in how they account for the query aspects (Santos et al. (2010c)).

The basic assumption of implicit diversification approaches is that dissimilar documents are more likely to satisfy different information needs. The most representative approach in maximal marginal relevance (MMR) method and its probabilistic variants is shown as follows (Zhai et al. (2003)):

$$S_{MMR}(q, d, c) = (1 - \lambda)S^{rel}(d, q) - \lambda \max_{d_j \in C} S^{div}(d, d_j) \quad (1)$$

60 where S^{rel} and S^{div} represents document d 's relevance to the query q and its similarity to a selected document d_j respectively. To gain high ranking score, a document should not only be relevant, but also be dissimilar from the selected documents. The special process of MMR proposed by Garbonell & Goldstein is selecting the document iteratively Carbonell & Goldstein (1998), and mean-
65 while, both content-based relevance and diversity relation between current selected document and the previously selected documents are considered. Yu et al. formulate this as a process of selecting and ranking k exemplar documents and utilize linear programming to solve this problem (Yu et al. (2017)). In summary, they are all implicit approaches without using aspects to mine the
70 underlying aspects, besides, they are a low effective approaches (Santos et al. (2010a); Drosou & Pitoura (2010)).

Explicit approaches make use of the aspects underlying the query to select documents that cover different aspects as far as possible. The algorithms such as IA-select Agrawal et al. (2009), xQuAD Santos et al. (2010a) and RxQuAD
75 Vargas et al. (2012) are proposed to reduce redundancy on the aspect levels. These methods select documents that cover more novel aspects. The PM-1 and PM-2 models pay more attention to maintain the proportionality of aspects Dang & Croft (2012). They produce the ranked result according to the proportionality of aspects. Intrinsic diversity products a series of successor queries to
80 figure out the appropriate content to cover (Raman et al. (2013)). Wang et al. (2016); Hu & et al. (2015) think the aspects underlying the query should be hierarchical, and propose some hierarchical measures to find the relationships among aspects. To conclude, all existing explicit approaches are unsupervised, and the values of parameters need to be tuned by the experiment repeatedly

85 without intention, causing a time-consuming optimizing problem to find the most suitable parameters.

And some learning approaches are proposed. (Zhu et al. (2014)) use structural SVM to learn to identify a document subset with maximum word coverage, but they just learn the maximum word coverage and do not mine the aspects
90 underlying the query. (Xia et al. (2015)) utilize both positive and negative ranking documents to train a maximal marginal relevance model for ranking, (Xia et al. (2016)) propose a neural tensor network to learn a nonlinear novelty function to select document, but they may pay much attention on novelty and less on relevance. Our approach accounts for the aspects of a query in an
95 explicit way. However, differently from the existing approaches, we use a learnable process to identify features from documents, which are all positive differing from (Xia et al. (2015)), using Markov Random Field. Besides, we redefine the diversity function and derive our loss function as the likelihood loss of ground truth generation to resolve this bicriterion optimization problem.

100 **3. Learning Approach for Search Result Diversification**

3.1. Mining aspects underlying the query

The key step for Query Aspects Diversification model is mining the aspects underlying the query. With the help of query aspects, we can generate the diverse ranking list by minimizing the redundancy on the basis of the aspects.
105 We mine the query aspects like (Santos et al. (2010a)), issuing the query to the commercial search engine (we use Yahoo) and get back the query suggestion result list as the aspects. Next, we can use these aspects as a new query to search the candidate document set D and we can get the relevance score between the aspect q_i and each document d in D , which can be formalized as $P(q_i|d)$.

110 *3.2. Topic diversity model*

Traditional topic diversity model is a greedy approximation. It sequentially selects the “local-best” document from the candidate document set (Santos et al.

(2010a)). The original function is formalized as follows:

$$f(d, \bar{S}) = (1 - \lambda)P(d|q) + \lambda \sum_{q_i \in Q} P(q_i|q)P(d|q_i)P(\bar{S}|q_i). \quad (2)$$

where d denotes for the current document to be considered in the sequential process, \bar{S} denotes for the unselected document set (equal to the $D \setminus S$ in Fig. (1)), q denotes for the query, λ is a balance parameter for a trade-off between relevance and diversity, q_i denotes for the aspects underlying the query q .

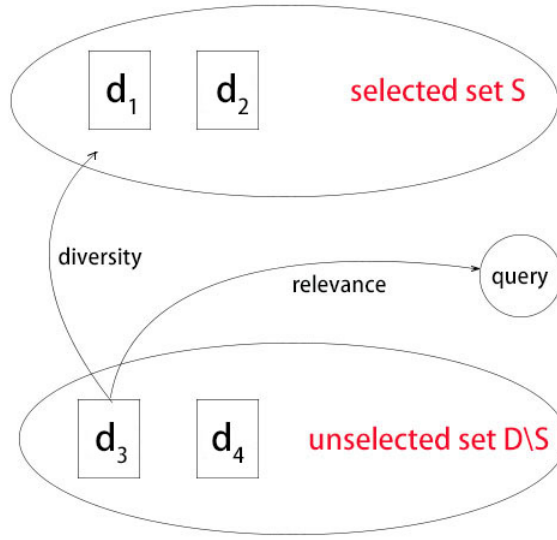


Figure 1: An illustration for sequential selection in topic diversity model

As for Eq. (2), the left part corresponds to the relevance score and the right part corresponds to the diversity score. We look forward to redefine the estimation of diversity score $P(\bar{S}|q_i)$. According to the conditional probabilistic formula, the task can be formalized as follows:

$$P(\bar{S}|q_i) = \frac{P(\bar{S}, q_i)}{P(q_i)} \stackrel{rank}{=} P(\bar{S}, q_i) \quad (3)$$

115 where $P(q_i)$ denotes the occurrence rate of aspects q_i corresponding to query q , which is usually regard to be normalized as $1/n$ (n denotes the number of aspects) (Santos et al. (2010a)). Because the values of $P(q_i)$ are equal and do not impact on the result of ranking, we neglect $P(q_i)$.

The main concern is how to define feature function for $P(\bar{S}, q_i)$. There are
120 many ways to integrate different features, just like linear regression, logistic
regression and some other ways. Under our situation, we use Markov Random
Field (MRF) to model $P(\bar{S}, q_i)$. We benefit from its convenient combination of
different types of features and we can get its derivation easily.

3.3. Feature extraction via MRF

A MRF is a probabilistic model defined on an undirected graph G . In MRF
model, the nodes represent the random variables and the edges represent depen-
dencies between these variables. In our study, the nodes represent the aspect
 q_i and the unselected set \bar{S} . Consequently, we compute the joint probability
defined over the graph G as follows:

$$P(\bar{S}, q_i) = \frac{\prod_{l \in L(G)} \phi_l(l)}{Z}, \quad (4)$$

125 where $L(G)$ is the cliques over the graph G , $\phi_l(l)$ is a potential function defined
over the clique l , and $Z = \sum_{\bar{S}, q_i} \prod_l \phi_l(l)$ is the normalization factor to ensure that
 $P(\bar{S}, q_i)$ satisfies a probability distribution.

The potential function is usually defined like:

$$\phi_l(l) = \exp(\lambda_l f_l(l)), \quad (5)$$

where $f_l(l)$ is a feature function defined over clique l , and λ_l is the correspond-
ing weightiness factor. By applying log function and neglecting normalization
factor, the final feature function is formalized as follows:

$$P(\bar{S}, q_i) \stackrel{rank}{=} \sum_{l \in L(G)} \lambda_l f_l(l). \quad (6)$$

Note that Eq. (6) is derived from Eq. (4) by neglecting the log function because
its form is more simple for derivation and the simplifying does not impact the
130 learning and ranking. Nextly, we specify the structure of graph G and its clique
set $L(G)$ to derive our final feature functions.

Fig. (2) shows the three types of cliques in MRF. The formal description
about feature extraction based on three cliques is given as follows:

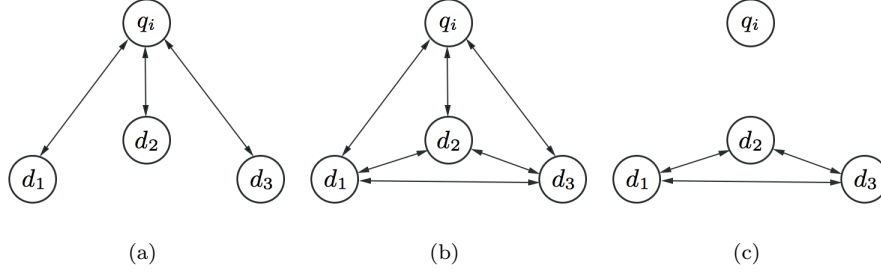


Figure 2: An illustration for three types of cliques. The graph G contains a aspects node q_i and three document nodes (just for example) that correspond to the documents in the unselected set \bar{S} . (a) l_{sd} contains q_i and a single document node; (b) l_{sD} includes q_i and the whole \bar{S} ; (c) l_D only contains \bar{S} .

1. Based on l_{sd} . The high occupancy of aspects q_i reflects the high potential relevance for q_i with respect to \bar{S} .

- We define $f_{ave-topic} = ave_{d \in \bar{S}} P(q_i|d)$ for feature function on this clique. $P(q_i|d)$ is the aspects distribution measurement which we have mentioned in section 3.1.

2. Based on l_{sD} . The clique involves the inter-relationships in the candidate set \bar{S} .

- We use the maximal, minimal, standard deviation of the $P(q_i|d)_{d \in \bar{S}}$ as feature functions defined upon clique l_{sD} .
- For the sake of minimizing redundancy, we use the $num_{q_i}(\bar{S}) - num_{q_i}(S)$ as a feature function defined on this clique too. $num_{q_i}(x)$ represents the number of documents in set x with respect to aspects q_i .

3. Based on l_D . Both l_{sd} and l_{sD} consider relations of documents with respect to the above two aspects. The clique l_D only takes into account the relations among documents excluding aspects q_i . Previous research has shown that the aspect-independent property can indicate the relevance of documents for q_i (Kurland & Domshlak (2008)).

- We use the entropy of all the documents d in \bar{S} :

$P_{entropy}(d) \stackrel{def}{=} -\sum_{w \in d} P(w|d) \log p(w|d)$ as feature function, where w is a term and $p(w|d)$ is the probability that w appears in d (given by the language model).

- Spam ratio inspired by the Web Spam Classification is used for feature function, too (Fetterly et al. (2004)).

To conclude, by replacing the feature function into equation (2) and putting the parameters λ into the learning process, the ranking function is given as follows:

$$f(d, \bar{S}) = \lambda_r P(d|q) + \lambda_n \sum_{q_i \in Q} [P(q_i|q)P(d|q_i) \sum_{l \in L(G(q_i))} \lambda_l f_l(l)] \quad (7)$$

where $L(G(q_i))$ represents the clique set L from the graph G which is built around the aspects q_i , $f_l(l)$ stands for the feature function defined on the clique l . There exists a parameter λ in equation (2), it is a balance parameter between relevance and diversity. In our learning method, we use λ_r and λ_n to replace it and we can infer its value by learning process.

3.4. Loss function

We define the loss function as a likelihood loss of generation probability:

$$L(rank(D, C), Y) = -\log P(Y|D), \quad (8)$$

where $rank$ denotes the ranking function in our model, C is the feature function defined in unselected set \bar{S} , D denotes all the candidate documents, and Y is the final result of search result diversification. Because our L-SRD model is a sequential selection model, it can be viewed as maximizing probability of correctly choosing the top- n document from unselected set:

$$\begin{aligned} P(Y|D) &= P(y_1, y_2, \dots, y_n|D) \\ &= P(y_1|D)P(y_2|D \setminus S_1) \cdots P(y_n|D \setminus S_{n-1}), \end{aligned} \quad (9)$$

where y_1, \dots, y_n is the ground truth for search result diversification task with respect to query q , n represents the top n result generated by the sequential

selection process, the index i denotes its ranking position, S_{i-1} denotes the selected set after $i - 1$ iterations, the probability $P(y_i|D \setminus S_{i-1})$ represents the probability that select the document y_i under the condition of $D \setminus S_{i-1}$.

On the basis of the Plackett-Luce Model Marden (1996), we derive the steps in our generation process shown as follows:

$$P(Y|D) = \prod_{i=1}^n P(y_i|D \setminus S_{i-1}) = \prod_{i=1}^n \frac{\exp(f(y_i, D \setminus S_{i-1}))}{\sum_{k=i}^n \exp(f(y_k, D \setminus S_{i-1}))}, \quad (10)$$

where S_0 means empty set \emptyset , function f corresponds to Eq. (7). Incorporating Eq.(10) into Eq.(8), we get the definition of the loss function as follows:

$$L(f(D, C), Y) = - \sum_{i=1}^n \log\left(\frac{\exp(f(y_i, D \setminus S_{i-1}))}{\sum_{k=i}^n \exp(f(y_k, D \setminus S_{i-1}))}\right). \quad (11)$$

To get the final loss function, we simplify Eq. (7) by uniting the parameter λ_n and λ_l (because the parameter in our model all can be decided by the learning process):

$$f(d, \bar{S}) = \lambda_r P(d|q) + \vec{\mu}_d \cdot N_{1...L}(d, q_i, \bar{S}) \quad (12)$$

$$N_l(d, q_i, \bar{S}) = \sum_{q_i \in Q} P(q_i|q) P(d|q_i) f_l(l) \quad (l \in L(G(q_i))) \quad (13)$$

where $\vec{\mu}_d$ represents a L-dimensional weight vector, L stands for the number of features, $N_{1...L}$ denotes a series of function vectors, l is the cliques defined on \bar{S} and q_i .

The total loss function is formulized as follows:

$$- \sum_{i=1}^{T_r} \sum_{j=1}^n \log\left(\frac{\exp(\lambda_r P(y_j|q) + \vec{\mu}_d \cdot N_{1...L}(y_j, q_i, \bar{S}))}{\sum_{k=j}^n \exp(\lambda_r P(y_k|q) + \vec{\mu}_d \cdot N_{1...L}(y_k, q_i, \bar{S}))}\right) \quad (14)$$

where T_r denotes the number of training examples.

3.5. Learning and prediction

Given the precise definition of loss function, the next step is minimizing the loss function to get the best performance. Firstly, we generate the training data and apply the optimization method. Next, we use our ranking function to predict the final diverse ranking result.

In this study, we use the data in TREC dataset in a format of quadruples: $(q^{(i)}, RD^{(i)}, T_i, J(s_j^{(i)}|t_k))$, where $q^{(i)}$ means the i -th query q , $RD^{(i)}$ is the corresponding related documents set, T_i represent the aspect underlying the query $q^{(i)}$ which are provided by official labeler, and $J(d_j^{(i)}|t_k)$ represents the judgement factor whether the j -th document $d_j^{(i)}$ in $RD^{(i)}$ covers the aspect t_k . Note that the last two elements in quadruples are used to calculate the score of evaluation metrics (e.g. α -nDCG), we cannot make use of it directly in our model.

At first, we should generate a approximate ground truth for training set. So we construct a list y_i which maximize the diversity metrics, such as α -nDCG, ERR-IA, etc. In our study, we use ERR-IA to measure the results which is described as function f_{ERR-IA} . In algorithm 1, at the every i -th step in loop structure, we select the document d from $D \setminus S_{i-1}$ to maximize the function f_{ERR-IA} and update the $S \setminus D_{i-1}$ by adding the document d . By recording the best document in every step, we get our final ideal ranking list as our training data.

ALGORITHM 1: Ideal ranking list construction algorithm

Input: $(q^{(i)}, RD^{(i)}, T_i, J(s_j^{(i)}|t_k)), f_{ERR-IA}$
Output: y_1, y_2, \dots, y_n

- 1: initialize $S_0 = \emptyset$
- 2: **for** $k = 1$ to n **do**
- 3: $bestDoc \leftarrow \arg \max_{d \in RD^{(i)} \setminus S_{k-1}} f_{ERR-IA}(d \cup S_{k-1})$
- 4: $S_k = S_{k-1} \cup bestDoc$
- 5: $y_k = bestDoc$
- 6: **end for**

Nextly, we use the stochastic gradient descent method to optimize the loss function as shown in Algorithm 2. At every step in algorithm 2, we calculate the gradient according to Eq. (15)-(16) and update the value of weight. The

gradient in step i at training set D_{init} is computed as follows:

$$\Delta\lambda_r^{(i)} = \sum_{j=1}^n \left(\frac{\sum_{k=j}^n P(y_j|q) \exp(\lambda_r^{(i-1)}) P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S})}{\sum_{k=j}^n \exp(\lambda_r^{(i-1)}) P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S})} - \frac{P(y_j|q) \exp(\lambda_r^{(i-1)}) P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S})}{\exp(\lambda_r^{(i-1)}) P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S})} \right) \quad (15)$$

$$\Delta\vec{\mu}_d^{(i)} = \sum_{j=1}^n \left(\frac{\sum_{k=j}^n N_l(y_j, q_i, \bar{S}) \exp(\lambda_r^{(i-1)}) P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S})}{\sum_{k=j}^n \exp(\lambda_r^{(i-1)}) P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S})} - \frac{N_l(y_j, q_i, \bar{S}) \exp(\lambda_r^{(i-1)}) P(y_j|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_j, q_i, \bar{S})}{\exp(\lambda_r^{(i-1)}) P(y_k|q) + \vec{\mu}_d^{(i-1)} \cdot N_{1...L}(y_k, q_i, \bar{S})} \right) \quad (16)$$

ALGORITHM 2: Parameter learning algorithm

Input: training data: $D_{init}^{Tr}, (y_1...y_n)^{Tr}$

parameter: learning rate η , tolerate ϵ

Output: $\lambda_r, \vec{\mu}_d$

1: Initialize $\lambda_r, \vec{\mu}_d$

2: **repeat**

3: $\lambda_r^{(0)} = \lambda_r, \vec{\mu}_d^{(0)} = \vec{\mu}_d$

4: Randomly choose one of the training data

5: **for** $i = 1, \dots, n$ **do**

6: Compute the gradient $\Delta\lambda_r^{(i)}$ and $\Delta\vec{\mu}_d^{(i)}$

7: Update: $\lambda_r^{(i)} = \lambda_r^{(i-1)} - \eta\Delta\lambda_r^{(i)}, \vec{\mu}_d^{(i)} = \vec{\mu}_d^{(i-1)} - \eta\Delta\vec{\mu}_d^{(i)}$

8: **end for**

9: $\lambda_r = \lambda_r^{(n)}, \vec{\mu}_d = \vec{\mu}_d^{(n)}$

10: **until** change for value of loss function below the tolerate ϵ

Finally, we propose a sequential prediction method as described in Algorithm

- 195 3. At the i -th step in algorithm 3, we select the best document d from $D \setminus S_{i-1}$ to maximize our ranking score and update the candidate set $D \setminus S_{i-1}$ by adding document d . By recording the best document in every step, we predict the final

diverse ranking list as result.

ALGORITHM 3: The prediction process

Input: query q and its retrieval result D_{init} , weight λ_r and λ_{nl}

Output: y_1, y_2, \dots, y_n

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1:  $S_0 = \emptyset$ 
2: for  $i = 1, \dots, n$  do
3:    $best = \arg \max_{d \in D \setminus S_{i-1}} f(d, D \setminus S_{i-1})$ 
4:    $S_i = S_{i-1} \cup best$ 
5:    $y_i = best$ 
6: end for

```

200 4. Experiment

4.1. Dataset and evaluation metrics

There are 150 queries in our query set, from TREC web track 2009 (WT2009) (Clarke et al. (2009a)), WT2010, WT2011(50 for each). Evaluation is done on the ClueWeb09 Category B retrieval collection¹. The collection consists of
205 nearly 50 millions web pages in English. There is a list of aspects for each query with binary relevance judgements, which are provided by TREC assessors.

There are three mainly evaluation metrics we use to evaluate the performance of our method: α -nDCG (Clarke et al. (2008)), ERR-IA (Chapelle et al. (2009)), NRBP (Clarke et al. (2009b)). α -nDCG is used to balance both relevance
210 and diversity of candidate documents. ERR-IA measures the expected effort required for a user to satisfy their information needs. And NRBP is a feasible metric to evaluate the balance between the complexity of needs and the query. These metrics penalize redundancy in a different degree for the document at each sorted position to maximize the aspects coverage. Additionally, we report
215 our result using Precision-IA and Aspect Recall too. To measure the robustness, we use Win/Loss ratio metrics (Yue & Joachims (2008); Dang & Croft (2012)). The Win/Loss ratio denotes whether the model improve or hurt the result when

¹<http://www.lemurproject.org/clueweb09.php/>

comparing with the basic relevant baseline QL in terms of evaluation metrics (Dang & Croft (2012)). Particularly in our experiment, we use ERR-IA to
220 calculate the Win/Loss ratio.

The evaluation metrics are reported at different cutoffs. We use {5, 10, 20} as our cutoffs to set up experiments. These cutoffs focus on the evaluation at early ranking, which are particularly important in a Web search context (Jansen et al. (1998)). The α is set to 0.5 in our experiments for the reason it gives equal
225 weight to both relevance and diversity.

4.2. Baseline methods

We use the Indri² to conduct our retrieval experiments and run with its default parameters configuration. All of the search result diversification methods are applied based on the top- K retrieved documents. As for the parameter K , we
230 conduct a series of tests to find the appropriate K maximizing the performance, which found 50 achieves the best result.

Besides the baseline retrieval models, we compare L-SRD with some advanced diversification models as follows:

- **QL.** The Query-likelihood language model is used for indri search engine as an initial retrieval method. We use it to provide the initial top 1000
235 documents for our diversification method. We also use it as a baseline method (Dang & Croft (2012)).
- **MMR.** A classical implicit diversification model. It is a representation of comparison between implicit and explicit models (Carbonell & Goldstein
240 (1998)).
- **xQuAD.** xQuAD is a popular explicit diversification model which focuses on the redundancy of aspects (Santos et al. (2010a)).
- **PM2.** PM2 is a popular explicit diversification model. PM2 generates the result set according to the aspects proportionality (Dang & Croft (2012)).

²<http://www.lemurproject.org/indri.php>

- 245 • **SVMDIV**. SVMDIV is also a learning model for search result diversification (Yue & Joachims (2008)). It uses the structural SVMs to optimize the aspects coverage problem. But it only models the diversity without consideration of relevance. We get the source code from the svmdiv homepage³ provided by the author.
- 250 • **HxQuAD** is a hierarchical diversification model based on xQuAD (Hu & et al. (2015)).
- **SMWE** mines query subtopic by exploiting the word embedding and short-text similarity measure. (Ullah et al. (2016))

These baselines 2-4 (corresponding to MMR, xQuAD, PM2) possess a single
 255 parameter λ to tune, we perform a 5-fold cross validation to train λ through optimizing ERR-IA. In our model, we use a 5-cross validation with a ratio of 3:1:1 for training, validation and prediction for the test query on each year. The final results are calculated over all the folds.

4.3. Experimental results

260 In particularly, our experiments aim to answer two main questions:

1. Can we utilize learning mechanism to promote the performance of search result diversification?
2. Does L-SRD achieve better performance in terms of robustness comparing to other search result diversified models?

265 4.3.1. Diversification analysis

To answer question 1, we compare our L-SRD with other diversification models in terms of diversification metrics. Table 1 shows the result of the evaluation in terms of α -nDCG, ERR-IA, and NRBP. The best result per line is highlighted in bold. The classical MMR method is used as a representative of implicit diversification model (Carbonell & Goldstein (1998)). As for explicit model, we
 270

³<http://projects.yisongyue.com/svmdiv/>

consider xQuAD and PM2 (Santos et al. (2010a); Dang & Croft (2012)). SVM-DIV is selected for the representative of learning methods, HxQuAD is selected for the hierarchical model.

The result shows that L-SRD always performs best in terms of all metrics.

275 It consistently improves the initial retrieval ranking method with gains up to 23.19%, 31.17%, 15.11% in terms of α -nDCG on WT2009, WT2010, WT2011 respectively. It indicates that our learning approach tackles the diversity measurement problem more effectively with the consideration of integrate different features. The reason is that features such as query-aspects relevance and information richness conform to the property of diversity. Furthermore, comparing

280 with the explicit diversification models in terms of the evaluation of α -nDCG, the improvement of L-SRD over the xQuAD is up to 28.44%, 16.87%, 14.90% on WT2009, WT2010, WT2011 respectively, and the improvement of L-SRD over the PM2 is up to 14.15%, 23.11%, 14.65% on WT2009, WT2010, WT2011

285 respectively. Previous explicit diversifications use a predefined function to calculate the diversity score, which cannot reach an optimal result from the overall situation. A learnable approach to solve the diversity measurement and parameter tuning problem is significative. In addition, comparing with the hierarchical diversification model in terms of the evaluation of α -nDCG, the improvement of

290 L-SRD over the HxQuAD is up to 3.77%, 9.68%, 5.49% on WT2009, WT2010, WT2011 respectively. HxQuAD only use a predefined function to measure the diversity score, and the parameters may not be optimal because it needs to be tuned manually. Our learning model tackles the parameters tuning problem in an automatic fashion and reaches optimal result. Comparing with SWME

295 in terms of the evaluation of α -nDCG, the improvement of L-SRD over the HxQuAD is up to 3.63%, 5.35%, 3.86% on WT2009, WT2010, WT2011 respectively. SMWE mines enough subtopics, but it cannot learn enough features to represent the document. Besides the non-learning model, the improvement of L-SRD over the SVM-DIV is up to 10.18%, 14.70%, 11.09% on WT2009, WT2010,

300 WT2011 respectively. It shows that considering relevance and different types of features in diversity measurement is helpful in the learning approach. That

is the reason why our model wins. Therefore, L-SRD shows better understanding on the diverse ranking and leads to a better result. So utilizing learning mechanism indeed promotes the performance of search result diversification.

Year	experiment	ERR-IA@20	α -nDCG@20	NRBP
2009	QL	0.1376	0.2548	0.1008
	MMR	0.1405	0.2526	0.1070
	xQuAD	0.1411	0.2444	0.1113
	PM2	0.1482	0.2750	0.1101
	SVMDIV	0.1531	0.2849	0.1219
	HxQuAD	0.1653	0.3025	0.1372
	SMWE	0.1787	0.3029	0.1482
	L-SRD	0.1862	0.3139	0.1615
2010	QL	0.1484	0.2445	0.1092
	MMR	0.1494	0.2450	0.1129
	xQuAD	0.1732	0.2746	0.1326
	PM2	0.1599	0.2605	0.1175
	SVMDIV	0.1698	0.2796	0.1158
	HxQuAD	0.1807	0.2924	0.1303
	SMWE	0.2038	0.3044	0.1601
	L-SRD	0.2193	0.3207	0.1826
2011	QL	0.3288	0.4454	0.2802
	MMR	0.3253	0.4337	0.2834
	xQuAD	0.3235	0.4462	0.2812
	PM2	0.3316	0.4472	0.2831
	SVMDIV	0.3429	0.4615	0.2923
	HxQuAD	0.3606	0.4860	0.3107
	SMWE	0.3924	0.4936	0.3232
	L-SRD	0.4078	0.5127	0.3374

Table 1: Diversification performance using the official evaluation metrics for WT2009, WT2010, WT2011

305 We consider not only the advanced diversity metrics, but also traditional
diversity metrics, such as Precision-IA and Aspect Recall. The former indicates
how many relevant documents for each aspect we have for reranking, the latter
indicates how many of the aspects for which we have relevant documents. The
result is shown in Fig. 3. MMR still underperforms all of them, as for Precision-
310 IA, xQuAD wins on WT2010 casually, while L-SRD performs more stable, even
on WT2010, the gap is small. It proves that L-SRD outperforms others from
different perspectives. Our learnable model solves the diverse ranking problem
in a global perspective and always reaches prominent results.

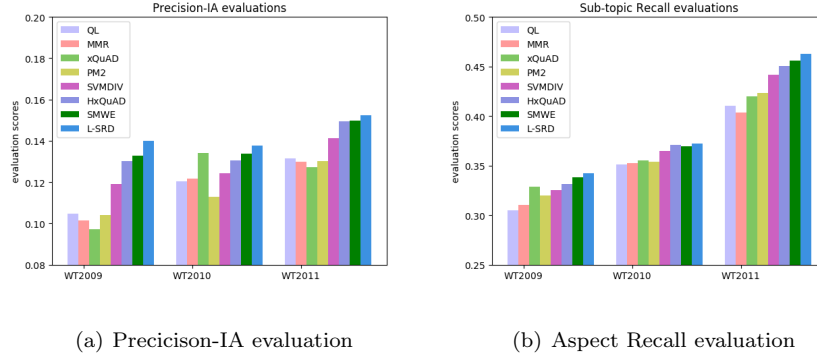


Figure 3: Performance comparison in WT2009, WT2010, WT2011 with Precision-IA and Aspect Recall

4.3.2. Robustness analysis

315 An effective search result diversification method should not only outperform
other models in terms of diversity metrics, but also maintain a high level of
robustness, which we have raised the question 2. We set up series of experi-
ments on robustness research to study the Win/Loss behaviour and the usage
of different retrieval algorithms respectively.

320 From table 2, we find that L-SRD model performs best with its ratio of
2.65. While the Win/Loss ratio of MMR, xQuAD, PM2, SVM DIV, HxQuAD
and SMWE is 1.31, 1.46, 1.52, 1.77, 2.51, 2.51 respectively. It reflects the re-
markable robustness of L-SRD model comparing with other outstanding diver-

experiment	WT2009	WT2010	WT2011
MMR	20/18	24/17	23/16
xQuAD	23/18	23/16	24/14
PM2	22/20	26/14	25/14
SVMDIV	24/18	27/13	27/13
HxQuAD	27/15	30/10	31/10
SMWE	27/14	29/10	32/11
L-SRD	28/14	30/10	32/10

Table 2: Win/Loss ratio

sification models. The promotion of robustness over the MMR, xQuAD, PM2
325 , SVMDIV, HxQuAD and SMWE is up to 102.28%, 81.51%, 74.34%, 49.72%,
5.58 %, 5.58% respectively. And it confirms the overall performance of our
model is not restricted to a small subset, it still works in the whole dataset for
three years data. Our different types of features and learning approach address
this problem well.

330 5. Conclusion and Future Work

In this paper, we propose a Learnable Search Result Diversification model
(L-SRD). We pay our attention to the explicit Query Aspect Diversification
models and introduce the learning approach to regard the model as a learning
problem. Unlike the traditional explicit diversification models utilizing a prede-
335 fined novelty measure function, we integrate different types of diversity features
and estimate the weight with a learning approach. We derive our loss func-
tion as the likelihood of ground truth generation. Stochastic gradient descent
algorithm is used to estimate the values of parameters. Benefiting from the
learning approach, we can optimize the parameters in an automatic method.
340 The prediction of our diversification model is provided by iterative maximizing
the learned ranking function.

We have demonstrated the improvement of L-SRD comparing with other

diversification models. We find L-SRD achieve considerable results in terms of official diversity metrics on three years in TREC web track dataset. To prove its
345 robustness, we set the experiment about Win/Loss ratio and usage of different retrieval algorithms. We believe L-SRD will play an important role to improve the Query Aspect Search Result Diversification by using a learning method.

There exist a number of directions to be explored in the future. We look forward to take some considerable steps to make L-SRD achieve convergency as
350 quick as possible.

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