

CAT-3DGS: A CONTEXT-ADAPTIVE TRIPANE APPROACH TO RATE-DISTORTION-OPTIMIZED 3DGS COMPRESSION

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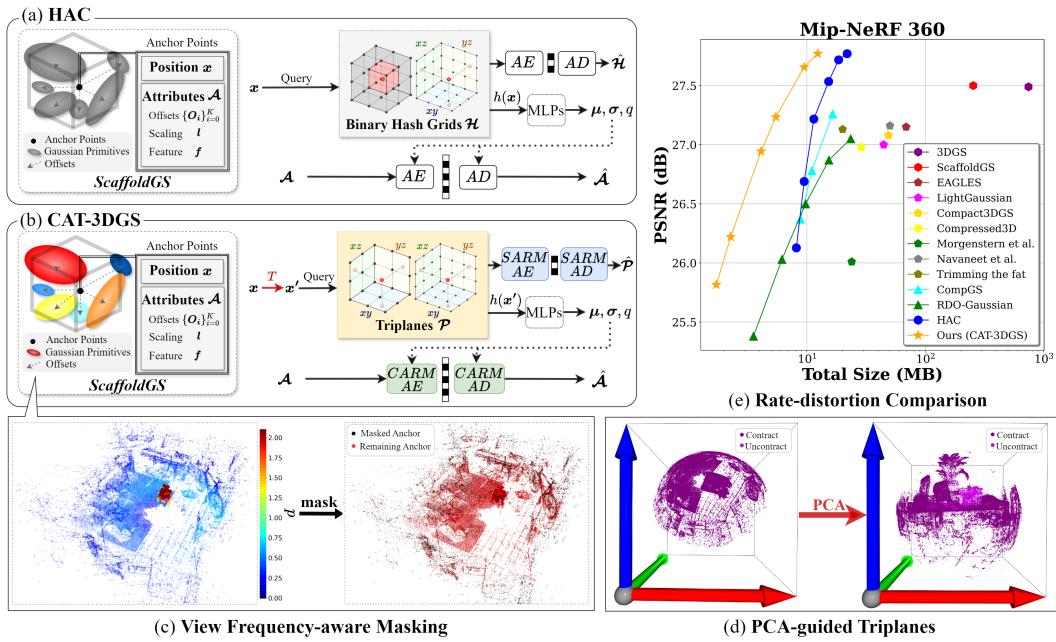


Figure 1: Comparison of the proposed CAT-3DGS and HAC (Chen et al., 2024). CARM: Channel-wise Autoregressive Models. SARM: Spatial Autoregressive Models.

ABSTRACT

3D Gaussian Splatting (3DGS) has recently emerged as a promising 3D representation. Much research has been focused on reducing its storage requirements and memory footprint. However, the needs to compress and transmit the 3DGS representation to the remote side are overlooked. This new application calls for rate-distortion-optimized 3DGS compression. How to quantize and entropy encode sparse Gaussian primitives in the 3D space remains largely unexplored. Few early attempts resort to the hyperprior framework from learned image compression. But, they fail to utilize fully the inter and intra correlation inherent in Gaussian primitives. Built on ScaffoldGS, this work, termed CAT-3DGS, introduces a context-adaptive triplane approach to their rate-distortion-optimized coding. It features multi-scale triplanes, oriented according to the principal axes of Gaussian primitives in the 3D space, to capture their inter correlation (i.e. spatial correlation) for spatial autoregressive coding in the projected 2D planes. With these triplanes serving as the hyperprior, we further perform channel-wise autoregressive coding to leverage the intra correlation within each individual Gaussian primitive. Our CAT-3DGS incorporates a view frequency-aware masking mechanism. It actively skips from coding those Gaussian primitives that potentially have little impact on the rendering quality. When trained end-to-end to strike a good rate-distortion trade-off, our CAT-3DGS achieves the state-of-the-art compression performance on the commonly used real-world datasets.

054 **1 INTRODUCTION**

055

056 3D Gaussian Splatting (3DGS) (Kerbl et al., 2023) has emerged as a promising representation for
 057 3D scenes. It lends itself to novel view synthesis particularly within differentiable rendering frame-
 058 works. Unlike Neural Radiance Fields (NeRF) (Mildenhall et al., 2021), which require many sam-
 059 pling points per pixel for volumetric rendering, 3DGS, as a rasterization-based method, uses 3D
 060 Gaussians as geometric primitives, achieving greater efficiency for real-time rendering and the state-
 061 of-the-art rendering quality.

062 Despite these advantages, the redundancy inherent in the 3DGS representation has prompted new
 063 research directions. Many prior works have been focused on a compact representation of Gaussian
 064 primitives. This category of methods aim at minimizing the parameter count or quantizing param-
 065 eters to save storage space and memory footprint. These techniques include pruning insignificant
 066 Gaussian primitives (Lee et al., 2024; Fan et al., 2023; Girish et al., 2024; Ali et al., 2024; Wang
 067 et al., 2024a), vector quantizing their attributes (Lee et al., 2024; Fan et al., 2023; Navaneet et al.,
 068 2023; Niedermayr et al., 2024; Wang et al., 2024a; Morgenstern et al., 2023), developing compact
 069 latent representations for attributes (Girish et al., 2024), and representing sparse Gaussian primitives
 070 in a more structural way (Lu et al., 2024; Ren et al., 2024; Sun et al., 2024). However, most of them
 071 overlook the needs to transmit the compressed 3DGS representation to the remote side, which calls
 072 for entropy coding and rate-distortion-optimized compression.

073 Recently, the rate-distortion-optimized compression for 3DGS started to attract attention. Unlike the
 074 compact 3DGS representation, this new school of thought (Wang et al., 2024a; Liu et al., 2024; Chen
 075 et al., 2024; Wang et al., 2024b) aims to strike an optimized trade-off between the compressed bit
 076 rate and rendering image quality in an end-to-end manner. Built on the vanilla 3DGS representation,
 077 RDO-Gaussian (Wang et al., 2024a) adopts the entropy-constrained vector quantization to quantize
 078 the attributes (e.g. opacity, scales, rotations and colors) of each Gaussian primitive. Instead of
 079 performing vector quantization, HAC (Chen et al., 2024) and ContextGS (Wang et al., 2024b) turn
 080 to the ScaffoldGS (Lu et al., 2024) representation to perform scalar quantization with respect to the
 081 latent features of these attributes, a technique analogous to the well-established transform coding
 082 plus scalar quantization for image/video compression. To entropy encode the quantized features,
 083 both introduce the hyperprior from learned image compression (Ballé et al., 2018) to model their
 084 coding probabilities. In formulating the hyperprior, HAC (Chen et al., 2024) draws inspiration from
 085 BiRF (Shin & Park, 2024) to create multi-scale binary hash grids (Figure 1 (a)), whereas ContextGS
 086 learns a separate feature as the hyperprior for each individual Gaussian primitive. Both assume the
 087 components of the hyperprior are independent and identically distributed, in coding the hyperprior.
 088 Notably, ContextGS organizes Gaussian primitives in the 3D space in a hierarchical manner in order
 089 to benefit from the contextual coding of the quantized latent features. In this regard, CompGS (Liu
 et al., 2024) shares parallels with ContextGS.

090 This work introduces a novel rate-distortion-optimized compression framework for 3DGS (Figure 1
 091 (b)). First, motivated by the tensor decomposition (Fridovich-Keil et al., 2023), we project the
 092 unorganized Gaussian primitives in the 3D space onto a set of multi-scale triplanes. These triplanes,
 093 oriented according to the principal components of the Gaussian primitives (Figure 1 (d)), serve as
 094 the hyperprior for coding their attributes in the latent space. Because they capture largely the *inter*
 095 *correlation* (i.e. spatial correlation) between the Gaussian primitives in the 3D space, we are able
 096 to encode efficiently the triplane-based hyperprior by spatial autoregressive models. This design
 097 aspect differs significantly from most existing techniques, in which the hyperprior is assumed to be
 098 factorial. Second, given that our triplane-based hyperprior has exploited much of the inter correlation
 099 between the Gaussian primitives, we decouple their coding dependency and encode their latent
 100 features independently by channel-wise autoregressive models. This avoids the challenge of having
 101 to organize sparse Gaussian primitives in the 3D space to leverage their inter correlation. Moreover,
 102 the *intra correlation* within each individual Gaussian primitive is explored for coding. Lastly, we
 103 develop a view frequency-aware masking mechanism, skipping from coding the Gaussian primitives
 that contribute little to the rendering quality (Figure 1 (c)). To sum up, our contributions include:

- A triplane-based hyperprior that leverages the inter correlation (i.e. spatial correlation) between Gaussian primitives in the 3D space for efficient spatial autoregressive coding.
- A channel-wise autoregressive model with uneven slice partition that exploits the intra correlation within each individual Gaussian primitive to further improve coding efficiency.

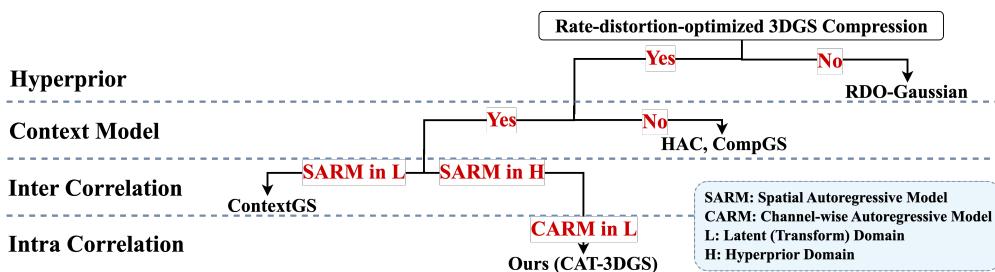


Figure 2: Taxonomy of the rate-distortion-optimized 3DGS compression.

- A view frequency-aware masking mechanism that evaluates the significance of Gaussian primitives based on their impact on the rendering quality to skip less critical ones from coding.

With these novel elements, our scheme, called CAT-3DGS, is able to achieve the state-of-the-art rate-distortion performance on several commonly used real-world datasets (Figure 1 (e)).

2 RELATED WORK

The related work can be divided into two main categories: the compact 3DGS representation and the rate-distortion-optimized 3DGS compression.

Compact 3DGS Representation. This category of methods, being a weak form of compression, aims to make more compact the 3DGS representation by pruning, quantizing, or structuring Gaussian primitives. Typical methods that involve pruning include Compact3DGS (Lee et al., 2024), LightGaussian (Fan et al., 2023), EAGLES (Girish et al., 2024), and Trimming the fat (Ali et al., 2024). Compact3DGS features a learnable binary mask and a mask loss to suppress less critical Gaussian primitives during training. In contrast, LightGaussian and EAGLES adopt a post-processing strategy to remove less significant Gaussians based on score-based criteria. In a similar vein, Trimming the fat (Ali et al., 2024) performs pruning progressively. Other methods that involve structuring sparse Gaussian primitives are ScaffoldGS (Lu et al., 2024), OctreeGS (Ren et al., 2024), and F3DGS (Sun et al., 2024). For instance, ScaffoldGS takes an anchor-based approach, where each anchor represents a group of Gaussian primitives whose attributes are represented collectively by a latent feature vector.

Rate-distortion-optimized 3DGS Compression. This emerging research area targets the generation and coding of Gaussian primitives in an end-to-end and rate-distortion-optimized manner. Figure 2 presents a taxonomy for methods in this category, including RDO-Gaussian (Wang et al., 2024a), CompGS (Liu et al., 2024), ContextGS (Wang et al., 2024b), and HAC (Chen et al., 2024). Unlike the compact 3DGS representation, these compression techniques involve entropy coding the quantized Gaussian primitives. One central theme is how to predict the probability distributions of the coding features and/or attributes. To this end, some (Chen et al., 2024; Liu et al., 2024; Wang et al., 2024b) borrow the idea of hyperprior from learned image compression to model the distributions of the latent features of Gaussian primitives. One exception is RDO-Gaussian (Wang et al., 2024a), which applies entropy-constrained vector quantization to the Gaussian attributes. As opposed to HAC (Chen et al., 2024) and CompGS (Liu et al., 2024), ContextGS (Wang et al., 2024b) additionally introduces contextual coding in the latent space to leverage the inter correlation between Gaussian primitives. In common, all these schemes consider the hyperprior to be factorial. From Figure 2, our CAT-3DGS represents a novel attempt that makes use of both inter and intra correlation for coding Gaussian primitives. In terms of the use of inter correlation, it differs from ContextGS (Wang et al., 2024b) and CompGS (Liu et al., 2024) in performing spatial autoregressive coding in the hyperprior domain, which is made possible with our triplane-based hyperprior. More than that, it makes full use of the intra correlation within each individual Gaussian primitive by performing channel-wise autoregressing coding in the latent domain, which is first proposed for 3DGS compression.

162 **3 PRELIMINARY**
 163

164 ScaffoldGS (Lu et al., 2024) builds upon 3DGS (Kerbl et al., 2023) and introduces a storage-
 165 efficient, anchor-based representation of 3D Gaussian primitives. Instead of directly storing a large
 166 number of Gaussian primitives and their attributes, ScaffoldGS introduces the notion of anchor
 167 points, with each representing a cluster of Gaussian primitives. The attributes of a Gaussian primitive
 168 include its 3D position μ^g , scale s , rotation r , spherical harmonic coefficients c , and opacity
 169 α . Likewise, each anchor is characterized by its position x , latent feature f , scaling factor l , and
 170 K learnable offsets $\{O_i\}_{i=1}^K$. The latent feature f encodes the attributes of the Gaussian primitives
 171 attached to the same anchor, effectively reducing the data redundancy. The learnable offsets indicate
 172 their relative positions with respect to that of the anchor.

173 With ScaffoldGS, rendering a 2D image involves decoding the view-dependent attributes for all the
 174 Gaussians primitives from an anchor representation according to the anchor feature f and camera
 175 position x_c :

$$\{c_i, r_i, s_i, \alpha_i\}_{i=1}^K = F_S(f, \sigma_c, \vec{d}_c), \quad (1)$$

177 where $\sigma_c = \|(x - x_c)\|_2$, $\vec{d}_c = x - x_c / \|x - x_c\|_2$, and F_S is an MLP decoder. The position μ_i^g of
 178 a Gaussian in the cluster is evaluated by adding the anchor position x to the offsets O_i , regularized
 179 by the scaling factor l , as follows:

$$\{\mu_i^g\}_{i=1}^K = x + \{O_i\}_{i=1}^K \cdot l. \quad (2)$$

181 Given these parameters, the rendering process proceeds similarly to 3DGS (Kerbl et al., 2023).
 182

183 **4 PROPOSED METHOD: CAT-3DGS**
 184

187 Based on ScaffoldGS, this work (termed CAT-3DGS) introduces a content-adaptive triplane
 188 approach to coding the anchors' attributes (i.e. the latent feature $f \in \mathbb{R}^{50}$, scaling factor $l \in \mathbb{R}^6$, and
 189 offsets $\{O_i \in \mathbb{R}^3\}_{i=1}^K$) in an end-to-end, rate-distortion-optimized fashion. Our CAT-3DGS adopts
 190 a hyperprior framework to model the probability distributions of the anchors' attributes. Because of
 191 the unordered and sparse nature of the anchor points, which collectively form an unorganized point
 192 cloud in the 3D space, we project them onto the multi-scale, dense triplanes oriented according to
 193 the principal components of the anchor points. As such, our triplane-based hyperprior organizes the
 194 projected anchor points in an ordered way on the 2D triplanes. This enables us to use spatial autore-
 195 gressive models to exploit their *inter correlation* (i.e. spatial correlation) for better entropy coding
 196 the hyperprior itself and thus the anchors' attributes. In comparison, the 3D hash-based grid hy-
 197 perprior (Chen et al., 2024), although compact, is not able to exploit such inherent inter correlation
 198 due to the pseudo random mapping between the dense grid points and their hyperprior representa-
 199 tions in the hash table. In addition, CAT-3DGS features a channel-wise contextual coding scheme
 200 to leverage the *intra correlation* among the components of individual latent features f for their cod-
 201 ing. Lastly, we incorporate a view frequency-aware masking mechanism to skip from coding those
 202 Gaussian primitives that contribute little to the rendering quality in different views.

203 **4.1 SYSTEM OVERVIEW**
 204

205 Figure 3 illustrates our CAT-3DGS framework. The encoding of a 3D scene begins with the gen-
 206 eration of the anchor points characterized by their positions $x \in \mathbb{R}^3$ and attributes, including the
 207 latent feature $f \in \mathbb{R}^{50}$, offsets $\{O_i \in \mathbb{R}^3\}_{i=1}^K$ and scaling $l \in \mathbb{R}^6$. Given the geometry infor-
 208 mation x of the anchor points, we formulate multi-scale, dense triplanes by conducting a principal
 209 component analysis. These triplanes consist of regularly structured grid points, which are quantized
 210 and coded by our lightweight spatial autoregressive models (Sec. 4.2). They serve the purpose of
 211 the hyperprior, and are queried and decoded to arrive at the coding distributions of the learned
 212 attributes associated with an anchor point according to its position x (Sec. 4.2). Considering that the
 213 latent features f collectively constitute a large portion of the compressed bitstream, they each are
 214 encoded recursively by channel-wise autoregressive coding (Sec. 4.4). During the learning process,
 215 our view frequency-aware masking mechanism is incorporated to mask out the Gaussian primitives
 which have a minimal impact on the rendering quality (Sec. 4.5). With CAT-3DGS, the information
 to be compressed in the bitstream include (a) the triplanes, (b) the anchors' attributes and positions,

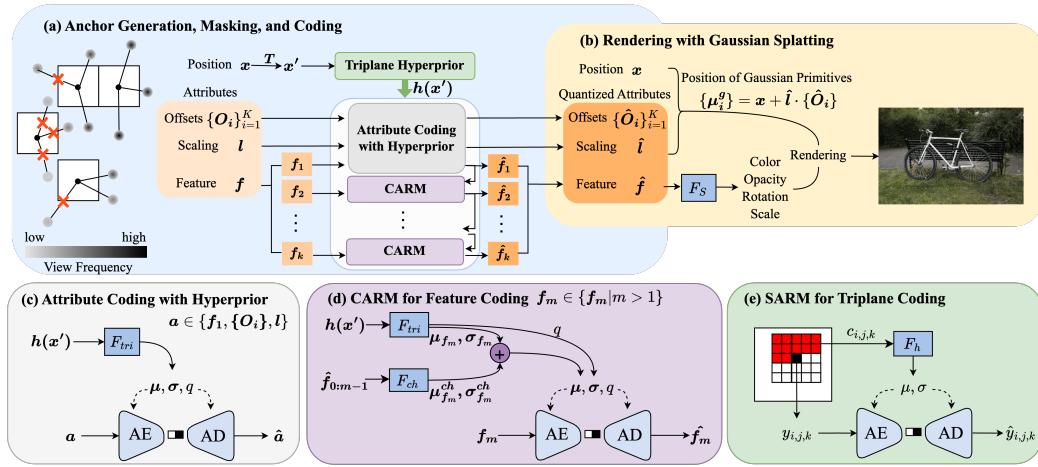


Figure 3: Illustration of our CAT-3DGS framework. CARM: Channel-wise Autoregressive Models. SARM: Spatial Autoregressive Models.

(c) the binary mask, (d) the network weights of the MLP decoder F_s , spatial autoregressive model F_h , hyperprior decoder F_{tri} , and channel-wise autoregressive model F_{ch} . The anchors' positions \mathbf{x} and the network weights are signaled in 16-bit and 32-bit floating-point formats, respectively. The binary mask is entropy encoded.

The rendering of a 2D image proceeds in much the same way as Scaffold-GS (Lu et al., 2024). Specifically, we use an MLP decoder F_S to decode the coded latent feature $\hat{\mathbf{f}}$ of an anchor point to obtain the attributes (i.e. color, opacity, rotation, scale) of all the Gaussian primitives belonging to the same anchor. Accordingly, the coded offsets $\{\hat{O}_i\}_{i=1}^K$ and scaling \hat{l} are combined with the anchor's position \mathbf{x} to reconstruct their positions. The same decoding process is repeated for the remaining anchor points needed to render the 2D image of a specific viewpoint.

4.2 TRIPLANE-BASED HYPERPRIOR

Our triplane-based hyperprior aims to learn the prior distributions on the attributes (the latent features \mathbf{f} , offsets $\{\mathbf{O}_i\}_{i=1}^K$ and scaling \mathbf{l}) of the anchor points. Conceptually, a triplane is composed of three 2D planes, denoted as $\mathcal{P}_c, c \in \{xy, yz, zx\}$, of the same 2D spatial resolution and channel dimension (See Figure 1 (b)). The notion of triplanes originates from decomposing a dense, 3D grid, which is costly to represent, into three 2D planes, which are storage friendly yet with more restricted expressiveness. Each grid point in these 2D planes is a learnable parameter. Our CAT-3DGS learns multiple triplanes of various resolutions to capture both coarse and fine detail. We thus augment \mathcal{P}_c with an upsampling scale r as $\mathcal{P}_{r,c} \in \mathbb{R}^{ch \times rB \times rB}$, where ch denotes the number of channels, r are integers denoting the upsampling scales and B denotes the spatial resolution of the triplane at the lowest scale (i.e. $r = 1$).

To retrieve the hyperprior $h(\mathbf{x})$ for an anchor point \mathbf{x} in the 3D space, we project \mathbf{x} onto each 2D plane $\mathcal{P}_{r,c}$, with the projected 2D coordinates given by $\pi_{r,c}(\mathbf{x})$. When $\pi_{r,c}(\mathbf{x})$ is fractional, we interpolate between the nearest integer grid points with an interpolation kernel ψ to get the triplane feature. In symbols, we have $\psi(\mathcal{P}_{r,c}, \pi_{r,c}(\mathbf{x}))$. The same process is repeated for every combination of permissible r and c , with the resulting triplane features concatenated to formulate the hyperprior $h(\mathbf{x})$:

$$h(\mathbf{x}) = \bigcup_r \bigcup_{c \in \{xy, yz, zx\}} \psi(\mathcal{P}_{r,c}, \pi_{r,c}(\mathbf{x})). \quad (3)$$

In doing so, we notice that \mathbf{x} may potentially be unbounded. However, the spatial resolutions of the triplanes must be bounded, because these triplanes need to be signaled in the bitstream. With their finite spatial resolutions, a contraction function (Barron et al., 2022b) is applied in order to fit the

270 potentially unbounded \mathbf{x} to our bounded triplanes:
 271

$$\text{contract}(\mathbf{x}) = \begin{cases} \mathbf{x} & \text{if } \|\mathbf{x}\| \leq 1 \\ (2 - \frac{1}{\|\mathbf{x}\|})(\frac{\mathbf{x}}{\|\mathbf{x}\|}) & \text{if } \|\mathbf{x}\| > 1. \end{cases} \quad (4)$$

275 Careful examination of Eq. (4) reveals that \mathbf{x} needs to be normalized in order to minimize the
 276 impact of the non-linear scaling applied to \mathbf{x} with $\|\mathbf{x}\| > 1$ while maximizing the usage of the grid
 277 points in each triplane to represent those \mathbf{x} with $\|\mathbf{x}\| \leq 1$. To this end, we conduct a principal
 278 component analysis (PCA) with respect to the positions \mathbf{x} of the anchor points, performing a linear
 279 transformation $T(\mathbf{x})$ of \mathbf{x} before it is contracted with Eq. (4). More specifically, $T(\mathbf{x})$ is given by
 280

$$\mathbf{x}' = T(\mathbf{x}) = \text{contract}\left(\frac{\mathbf{R}^x(\mathbf{x} - \mu^x)}{\sigma^x}\right), \quad (5)$$

282 where $\mu^x \in \mathbb{R}^3$ is the mean vector, $\sigma^x \in \mathbb{R}^3$ are the variances along the three principal axes, and
 283 $\mathbf{R}^x \in \mathbb{R}^{3 \times 3}$ is the PCA rotation matrix. As illustrated in Figure 1 (d), this transformation centers
 284 the point cloud of the anchor points, allowing most of the central anchor points to be linearly scaled.
 285 We finally substitute $T(\mathbf{x})$ into Eq. (3) to evaluate the hyperprior $h(\mathbf{x}')$.
 286

287 To entropy encode (or decode) the quantized attributes $\hat{\mathbf{a}} \in \{\hat{\mathbf{f}}_1, \{\hat{\mathbf{O}}_i\}, \hat{\mathbf{l}}\}$ of an anchor, an MLP
 288 F_{tri} is used to decode $h(\mathbf{x}')$ to predict their means, variances, and quantization step size. That
 289 is, $(\mu, \sigma, q) = F_{tri}(h(\mathbf{x}'))$. Notably, each of these attributes is assumed to follow a Gaussian
 290 distribution, with their coding probabilities given by
 291

$$p(\hat{\mathbf{a}} | h(\mathbf{x}')) = \int_{\hat{\mathbf{a}} - \frac{q}{2}}^{\hat{\mathbf{a}} + \frac{q}{2}} \mathcal{N}(\mu, \sigma) da. \quad (6)$$

294 The acute reader may have observed that only part of the latent feature $\hat{\mathbf{f}}$ is involved in Eq. (6). The
 295 coding of the remaining part (i.e. $\hat{\mathbf{f}}_2, \hat{\mathbf{f}}_3, \dots$) will be elaborated in Sec. 4.4.
 296

297 4.3 SPATIAL AUTOREGRESSIVE MODELS (SARM) FOR TRIPANE CODING

299 The triplane-based hyperprior must be encoded into the bitstream. Observing that the grid points
 300 in each 2D plane capture to a large extent the *inter correlation* (i.e. spatial correlation) between
 301 the anchor points in the 3D space, we introduce spatial autoregressive models for triplane coding.
 302 Currently, a dedicated autoregressive model F_{ARM} is learned and shared for 2D planes $\mathcal{P}_{r,c}$ of the
 303 same orientation $c \in \{xy, yz, zx\}$ without regard to its upsampling scale r . Thus, a total of three
 304 F_{ARM} , one for each orientation, are learned. Moreover, the 2D plane $\mathcal{P}_{r,c}$ has ch channels. These
 305 channels are encoded (and decoded) independently of each other with the same F_{ARM} to strike a
 306 balance between complexity and coding efficiency. In fact, all the channels from these 2D planes
 307 $\mathcal{P}_{r,c}$ can be encoded (and decoded) in parallel.

308 To entropy encode (and decode) a grid point $y_{i,j,k}$ in the channel k of the 2D plane $\mathcal{P}_{r,c}$, F_{ARM}
 309 formulates the context $c_{i,j,k}$ by referring to the previously decoded grid points of the same channel
 310 in the neighborhood specified by $c_{i,j,k} = [\hat{y}_{i-2:i-1,j-2:j+2,k}; \hat{y}_{i,j-2:j-1,k}]$ (Figure 3 (e)). It outputs
 311 the parameters $(\mu_{i,j,k}, \sigma_{i,j,k}) = F_{ARM}(c_{i,j,k})$ of a Laplace distribution that models the distribution
 312 of $y_{i,j,k}$. The coding probability of the quantized grid point $\hat{y}_{i,j,k}$ is then given by
 313

$$p(\hat{y}_{i,j,k} | c_{i,j,k}) = \int_{\hat{y}_{i,j,k} - \frac{Q}{2}}^{\hat{y}_{i,j,k} + \frac{Q}{2}} \text{Laplace}(\mu_{i,j,k}, \sigma_{i,j,k}) dy_{i,j,k}, \quad (7)$$

316 where $Q = 1/16$ is the quantization step size. This small quantization step is chosen to make the
 317 training more stable when the training process transitions from the non-quantization-aware training
 318 to the quantization-aware training.
 319

320 4.4 CHANNEL-WISE AUTOREGRESSIVE MODELS (CARM) FOR FEATURE CODING

321 The coding of the latent features \mathbf{f} deserves additional effort as they normally represent a con-
 322 siderable portion of the compressed bitstream. For efficient feature coding, we leverage the *intra*
 323 *correlation* among the components of a feature \mathbf{f} . We divide every individual feature \mathbf{f} into M

slices along the channel dimension, followed by introducing a channel-wise autoregressive models for coding these slices. The coding of slice \hat{f}_m with $m > 1$ is able to benefit from referring to the previous coded slices, i.e. $\{\hat{f}_i | i < m\}$, and the hyperprior. In symbols, we have the coding probability of the quantized slice \hat{f}_m as

$$p(\hat{f}_m | h(\mathbf{x}'), \hat{f}_{0:m-1}) = \int_{\hat{f}_{m-\frac{q}{2}}}^{\hat{f}_{m+\frac{q}{2}}} N(\boldsymbol{\mu} + \boldsymbol{\mu}_{ch}, \boldsymbol{\sigma} + \boldsymbol{\sigma}_{ch}) d\mathbf{f}, \quad (8)$$

where $(\boldsymbol{\mu}, \boldsymbol{\sigma}, q) = F_{tri}(h(\mathbf{x}'))$ and $(\boldsymbol{\mu}_{ch}, \boldsymbol{\sigma}_{ch}) = F_{ch}(\hat{f}_{0:m-1})$. In our design, the slices are unevenly partitioned, with further details provided in Sec. 5.3.

4.5 VIEW FREQUENCY-AWARE MASKING

Our view frequency-aware masking is designed to distinguish between Gaussian primitives in terms of their potential contribution to the rendering quality. As observed in Compact-3DGS (Lee et al., 2024) and HAC (Chen et al., 2024), using a learnable binary mask $M_{n,k}$ to mask out the k -th Gaussian primitive of the n -th anchor can be effective in reducing the number of Gaussian primitives to be signaled, thereby saving the storage space and transmission bandwidth. This masking mechanism is usually implemented as $M_{n,k} = \mathbb{1}(\text{sigmoid}(m_{n,k}) > \epsilon)$, where $m_{n,k}$ is a learnable parameter and ϵ is a global hyperparameter shared across every Gaussian primitive to determine its existence. Although effective, this blind approach may risk removing some critical Gaussian primitives. A question that arises naturally is whether we could prioritize Gaussian primitives in the masking process according to their potential contribution to the rendering quality. We observe that during training, some Gaussian primitives are more frequently used in rendering the training views. As such, we attach to each Gaussian primitive a weight $p_{n,k}$ that reflects its relative frequency of being used in rendering these training views. We adopt $p_{n,k}$ in our masking function:

$$M_{n,k} = \mathbb{1}(\text{sigmoid}(m_{n,k}) \cdot p_{n,k} > \epsilon). \quad (9)$$

With the same ϵ applied to every Gaussian primitive, a higher $p_{n,k}$ requires $\text{sigmoid}(m_{n,k})$ to approach zero more closely in order to skip the corresponding Gaussian primitive, making the task more difficult. As a result, more Gaussian primitives that are critical to rendering the training views are retained. For this scheme to work well, the basic premise is that the distribution of training views should be similar to that of test views. We argue that this is true to some extent because when their distributions differ significantly, there is little guarantee of the rendering quality in those test views.

4.6 TRAINING OBJECTIVES

The training of CAT-3DGS involves minimizing the rate-distortion cost $L_{\text{Scaffold}} + \lambda_r L_{\text{rate}}$ together with a masking loss $\lambda_m L_m$:

$$L = L_{\text{Scaffold}} + \lambda_r L_{\text{rate}} + \lambda_m L_m, \quad (10)$$

where we follow Scaffold-GS Lu et al. (2024) to evaluate L_{Scaffold} , which includes the distortion between the original and rendered images as well as a regularization term imposed on the scales s of Gaussian primitives. L_{rate} indicates the number of bits needed to signal the hyperprior and the anchors' attributes:

$$L_{\text{rate}} = \frac{1}{N(50 + 6 + 3K)} (L_{\text{rate}}^{\mathcal{A}} + \lambda_{\text{tri}} L_{\text{rate}}^{\mathcal{P}}), \quad (11)$$

where $L_{\text{rate}}^{\mathcal{A}} = -\sum_{\hat{a}} \log_2 p(\hat{a})$ is the estimated bit rate of the anchors' attributes, $L_{\text{rate}}^{\mathcal{P}} = -\sum_{\hat{y}} \log_2 p(\hat{y})$ is the triplanes' bit rate, and $N(50 + 6 + 3K)$ is the total number of parameters of anchors' attributes. In Eq. (10), L_m is the mask loss adopted from Compact3DGS (Lee et al., 2024) to regularize the view frequency-aware masking:

$$L_m = \sum_{n=1}^N \sum_{k=1}^K \text{sigmoid}(m_{n,k}). \quad (12)$$

In particular, $\lambda_m = \max(10^{-3}, 0.3 \cdot \lambda_r)$ changes with the rate parameter λ_r . Further details about this design aspect are provided in Appendix B.

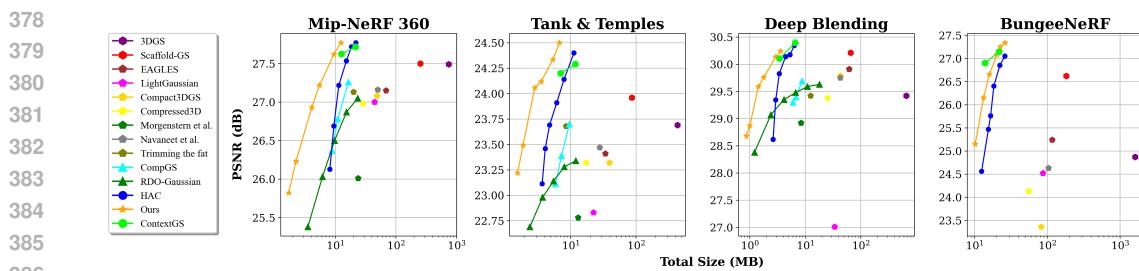


Figure 4: Rate-distortion comparison of our CAT-3DGS, HAC, [ContextGS](#), RDO-Gaussian, CompGS, and several other compact 3DGS representations (normally without entropy coding and visualized as rate-distortion points).

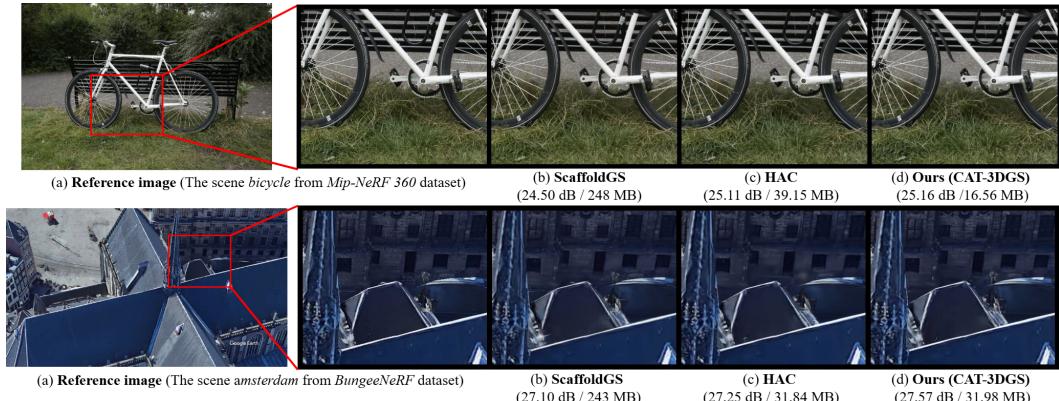


Figure 5: Qualitative results of our CAT-3DGS, HAC and ScaffoldGS.

5 EXPERIMENTAL RESULTS

5.1 IMPLEMENTATION DETAILS

This part summarizes some crucial implementation details for reproducibility. First, the spatial resolution B of the triplane at the lowest scale ($r = 1$) is determined in proportional to the number of anchor points obtained after 10k training iterations. The same anchor points in this stage are also utilized to conduct PCA (Sec. 4.2). The choices of the other hyperparameters include: the channel number $ch = 72$, $\epsilon = 0.01$ (0.0004 for BungeeNeRF) for the view frequency-aware masking, $m = 4$ with uneven slices (5, 10, 15, 25) for the channel-wise autoregressive coding. The rate parameter λ_r ranges from 0.002 to 0.04, and from 0.001 to 0.02 for BungeeNeRF. Lastly, our triplanes have only two scales; that is, $r = 1, 2$. The training details are provided in Appendix A.

5.2 RATE-DISTORTION COMPARISON

Baselines. For comparison, our baseline methods include (1) the vanilla 3DGS, (2) ScaffoldGS (our base model), and (3) four rate-distortion-optimized approaches—namely, HAC (Chen et al., 2024), RDO-Gaussian (Wang et al., 2024a), CompGS (Liu et al., 2024), and [ContextGS](#) (Wang et al., 2024b). Notably, [ContextGS](#) is a concurrent work of our CAT-3DGS. Due to the emerging nature of the rate-distortion-optimized 3DGS compression, there are only few early attempts. We thus also include for comparison several compact 3DGS techniques without joint rate-distortion-optimized training (Lee et al., 2024; Fan et al., 2023; Niedermayr et al., 2024; Navaneet et al., 2023; Morgenstern et al., 2023; Girish et al., 2024; Ali et al., 2024). Generally, these techniques do not consider entropy coding. They are visualized as individual rate-distortion points in our rate-distortion plots.

Datasets. We follow the common test protocol to test our CAT-3DGS on real-world scenes, including Mip-NeRF 360 (Barron et al., 2022a), Tanks & Temples (Knapsch et al., 2017), Deep Blend-

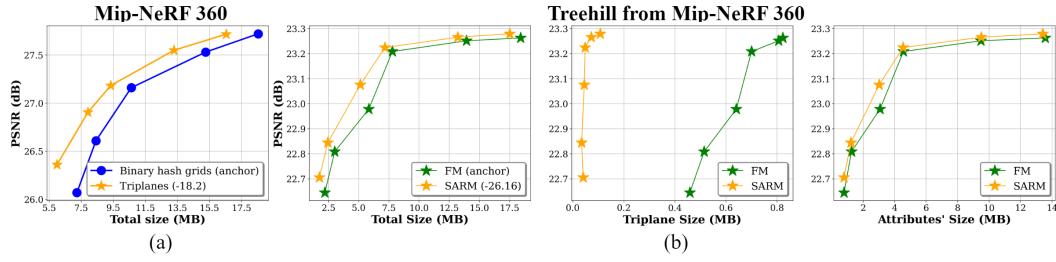


Figure 6: (a) Rate-distortion curves comparing our triplanes and the binary hash grids in HAC. (b) Rate-distortion curves comparing our SARM with the factorized model (FM).

ing (Hedman et al., 2018) and BungeeNeRF (Xiangli et al., 2022). For comparison, we choose the same scenes from each dataset as those used in the prior works (Lu et al., 2024; Chen et al., 2024).

Metrics. We compare the rate-distortion performance of the competing methods by visualizing their rate-distortion plots. The quality metric is PSNR measured in the RGB domain. **The bit rate is the file size of the compressed bitstream obtained by performing entropy encoding. When reporting the rate-distortion results for a dataset, we take the average of the per-sequence PSNRs and file sizes.** In our ablation study, we additionally report the BD-rate saving (Bjontegaard, 2001) to single out the contribution of individual components. In particular, the BD-rate saving is evaluated for each test scene and averaged across all the scenes in the dataset. Negative values suggest rate saving at the same quality level as compared to the anchor (a chosen baseline method) and vice versa. Note that evaluating the BD-rate requires at least 4 rate-distortion points and largely overlapping distortion intervals. We thus use it only in our ablation study.

Compression Results. In Figure 4, our CAT-3DGS outperforms the competing methods (particularly those rate-distortion-optimized ones) across all the datasets, achieving the state-of-the-art rate-distortion performance. On the Mip-NeRF 360 dataset, our CAT-3DGS achieves (at its second highest rate point) 78x and 26x rate reductions than 3DGS and ScaffoldGS, respectively, while achieving slightly higher PSNR by 0.16 dB. Figure 5 offers the subjective quality comparison among ScaffoldGS, HAC, and our CAT-3DGS. On the *bicycle* scene, our CAT-3DGS achieve a 57% size reduction while showing similar visual quality to HAC. Likewise, on the *amsterdam* scene, it achieves 0.32dB higher PSNR and better subjective quality than HAC, but with a similar file size.

5.3 ABLATION EXPERIMENTS

We conduct ablation experiments on the Mip-NeRF360 dataset for its diverse scenes.

Triplanes versus Binary Hash Grids. This study investigates the benefits of our triplane-based hyperprior. Based on the HAC framework, we change its hyperprior from the binary hash grids to our multi-scale triplanes with spatial autoregressive coding. The remaining components and training procedure are the same as HAC. From Figure 6 (a), our triplane-based hyperprior achieves an 18% BD-rate saving. It highlights the advantage of the triplane representations, which are able to capture the spatial correlation of the anchor points and enable more efficient entropy coding with spatial autoregressive models.

Spatial Autoregressive Models (SARM) versus Factorized Models (FM). Based on CAT-3DGS, this ablation study replaces our SARM with FM. The latter assumes that the triplane-based hyperprior has independent and identically distributed components. For fair comparison, 3 FMs (one for each plane orientation) are trained and used for coding the triplanes. The result on Mip-NeRF360 indicates that our SARM achieves 19% BD-rate saving as compared to FM. The result suggests the strong spatial correlation in the triplane-based hyperprior. Figure 6 (b) offers a breakdown analysis, showing that SARM benefits not only the coding of the triplane-based hyperprior, but more importantly that of the anchors' attributes, which constitute the major portion of the compressed bitstream.

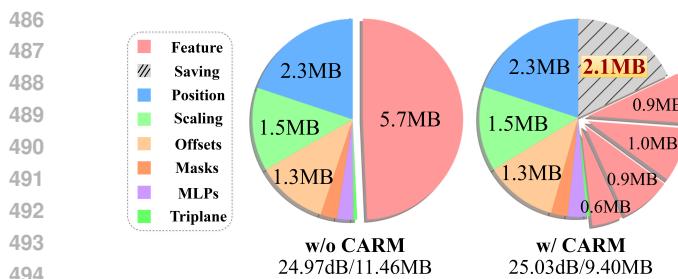


Figure 7: Breakdown analysis of different coding parts w/ and w/o our CARM for the *bicycle* scene.

Table 1: The impact of the slice number and partition in our CARM on compression performance. The results are obtained with Mip-Nerf 360.

M Slices	Channels per Slice	BD-rate
1	50	0
2	25, 25	-6.3
2	15, 35	-8.9
4	12, 12, 13, 13	-8.9
4	5, 10, 15, 20	-11.9

Table 2: Comparison of decoding time and rendering throughput: Ours (CAT-3DGS) vs. HAC.

	Scene	Anchor Count (K)	Base Resolution B	Decoding Time (s) ↓			Rendering Speed (FPS) ↑
				Triplane	Anchor Attributes	Total	
Ours	room amsterdam	109.5 1599.1	64 128	11.4 47.4	2.2 17.0	13.6 64.4	127.0 83.4
HAC	room amsterdam	686.3 1450.6	N/A N/A	N/A N/A	- -	6.6 11.3	103.1 77.9

Channel-wise Autoregressive Models (CARM). Figure 7 presents two pie charts to single out the contribution of our CARM on the *bicycle* scene. As shown, CARM reduces the compressed size of the latent features from 5.7 MB to 3.4 MB, amounting to a 40% rate reduction in this part of the bitstream. We also observe a similar trend in the other scenes. More results are provided in Appendix F. From Table 1, more slices lead to improved coding performance. Unevenly-partitioned slices perform slightly better than evenly-partitioned slices. With uneven slices, we found that more essential information is packed in the first or two slices, an effect that is similar to energy compaction and is much desirable for coding purposes. More discussions are presented in Appendix C.

View Frequency-Aware Masking. We conduct another ablation study that disables the view frequency-aware masking in our CAT-3DGS. In other words, we remove the weight $p_{n,k}$ in the masking function. Doing so results in a 16% BD-rate drop on Mip-NeRF360. The removal of Gaussian primitives less critical to the rendering quality helps reduce the bit rate. More results are provided in Appendix D.

Decoding Time and Rendering Throughput. Table 2 compares the decoding time (seconds) and rendering throughput (frames per second) of our CAT-3DGS and HAC for two scenes, *amsterdam* in BungeeNeRF (Xiangli et al., 2022) and *room* in Mip-NeRF360 (Barron et al., 2022b). This information is collected on one NVIDIA V100. CAT-3DGS has much higher decoding time than HAC due to the use of autoregressive models. However, in terms of rendering throughput, our CAT-3DGS is faster than HAC. This is because our frequency-aware masking effectively reduces the number of anchors. The decoding time of CAT-3DGS can be further improved by making full use of the parallelism in decoding triplanes. Recall that all the 2D planes in our triplane-based hyperprior are independently decodable and so are the channels in each 2D plane (Sec. 4.3). Currently, only the channel parallelism is used in our implementation. The decoding of different anchor attributes is parallelizable to some extent. The coding dependency is in the channel dimension and not between the anchors' attributes. Last but not least, the 3DGS system normally has decoding and rendering as two decoupled processes. The Gaussian primitives are decoded first, followed by rendering images in different views. The decoding is generally less time sensitive and has little impact on the rendering process, which is the same as ScaffoldGS (Lu et al., 2024) with our CAT-3DGS.

6 CONCLUSIONS

This work presents a novel rate-distortion-optimized 3DGS compression framework. In an effort to leverage the inter correlation between Gaussian primitives for coding, it features PCA-guided triplanes as the hyperprior and incorporates a spatial autoregressive model for their coding. Furthermore, a channel-wise autoregressive model is introduced for the first time to explore the intra correlation within each individual Gaussian primitive for coding. When combined with a view frequency-aware masking mechanism, these features lead to the state-of-the-art coding performance.

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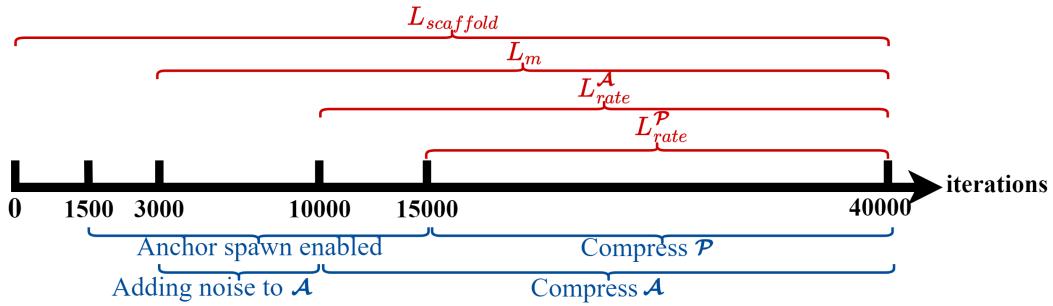
648 A TRAINING PROCESS
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Figure 8: Detailed Training Process of our CAT-3DGS.

Figure 8 depicts our detailed training procedure. It includes the following training stages.

Anchor Spawning In this stage, we adopt ScaffoldGS to ensure a stable start of both anchor attribute training and anchor spawning. However, to simulate the quantization effect, we introduce noise to the attributes of the anchor points starting at iteration 3000. To prevent the generation of an excessive number of anchors, we disable anchor growing during iterations 3000 to 4000.

Triplane-based Hyperprior After adding noise to the attributes of the anchor points during iterations 3000 to 10,000, we begin using the triplane as a hyperprior to learn the distribution of anchors' attributes starting from the 10,000th iteration.

Spatial Autoregressive Models for Triplane Coding We start triplane coding at iteration 15,000. Specifically, we warm up the spatial autoregressive model while freezing the other learnable parameters between iterations 15,000 and 16,000.

B RATE-AWARE MASK TRADE-OFF (RMT)

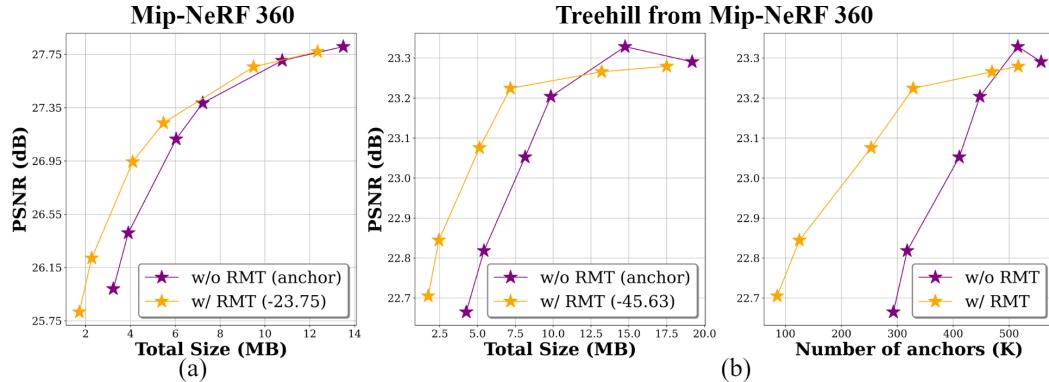


Figure 9: Rate-distortion comparison w/ and w/o our rate-aware mask trade-off. RMT: Rate-aware Mask Trade-off.

Based on the observation that the number of anchors can be further reduced while maintaining similar PSNR, we accordingly relate the mask hyperparameter λ_m to the rate hyperparameter λ_r using the relationship $\lambda_m = \max(10^{-3}, 0.3 \cdot \lambda_r)$. This implies that, at higher bit rates, λ_r decreases and more offsets (i.e. Gaussian primitives) and anchors are kept. Conversely, at lower bit rates, λ_r increases and more offsets and anchors are removed.

In Figure 9 (a), we evaluate the performance with a fixed mask trade-off set to 0.0005 (labeled "w/o RMT") and compare it with the rate-aware mask trade-off approach (labeled "w/ RMT") on Mip-

NeRF 360. The rate-aware mask trade-off has greater coding performance gain, particularly at lower bit rates. For further details regarding this gain, we select the *treehill* scene from Mip-NeRF 360, as shown in Figure 9 (b). Our method with RMT demonstrates that, at the lowest rate point, the number of anchor points is only one-third of that “w/o RMT”, and the total size achieves a 60% reduction, while maintaining similar PSNR.

C THE IMPACT OF SLICE PARTITIONING ON OUR CARM

Table 3: Analysis the number of bits per channel within a slice in different cases.

Method	slices	Channels per slice	Size per channel within one slice (kB)	Size for f (MB)	Total size (MB)	PSNR
w/o CARM	1	(50)	(8.91)	0.44	1.69	30.78
w/ CARM (even)	4	(12, 12, 13, 13)	(22.2, 6.38, 4.65, 3.98)	0.45	1.74	30.85
w/ CARM (uneven)	4	(5, 10, 15, 20)	(17.22, 9.61, 5.35, 3.64)	0.33	1.59	30.89

In this section, we further analyze the number of bits per channel within a slice in the cases of w/o CARM, w/ CARM (even), and w/ CARM (uneven), as shown in Table 3. We observe that when only one slice is used, indicating CARM is disabled, the kilo bytes per channel is 8.91. However, when CARM is enabled, the first slice uses 22.2 kilo bytes per channel for the even partition case and 17.22 kilo bytes per channel for the uneven case. The data suggest that the earlier slices contain more information, resulting in larger sizes. This also indicates that the richer information in the earlier slices can help the coding of the subsequent slices, allowing them to use fewer bits. As for the even and uneven cases, we observe that the uneven partition yields a better result, reducing the size of f by 0.12MB compared to the even case.

D VIEW FREQUENCY-AWARE MASKING

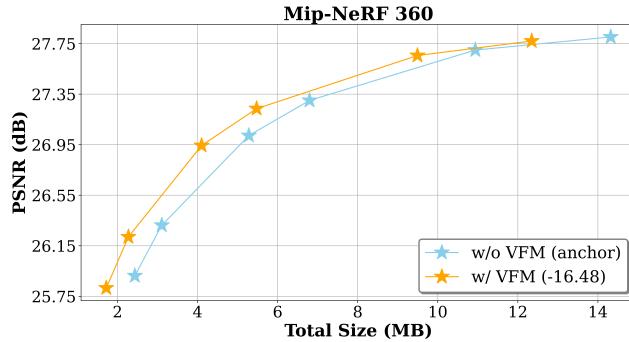


Figure 10: Rate-distortion comparison w/ and w/o our view frequency-aware masking. VFM: View Frequency-aware Masking.

In Figure 10, we compare CAT-3DGS (denoted by “w/ VFM”) with a variant (denoted by “w/o VFM”) that removes the weight $p_{n,k}$ in the masking function. The view frequency-aware masking has a significant effect at low bit rates, reducing the total size by 29% at the lowest rate point while PSNR drops by only 0.1dB. At the highest rate point, it reduces the total size by 14% while still maintaining similar PSNR. This indicates that the view frequency-aware masking can retain more important points while pruning a larger number of relatively less important ones, even when most of the anchors are masked out.

E BITSTREAM OF EACH COMPONENT

Our bit stream consists of seven components: the anchor positions a , three anchor attributes (features f , offsets $\{O_i\}$, and scaling factors l), a set of triplanes \mathcal{P} , binary masks M , and MLPs F_S , F_{tri} , F_{ch} , F_h . After applying our triplane hyperprior and channel-wise autoregressive model, the size of the attributes has been significantly reduced. Additionally, due to the spatial autoregressive model,

the triplane size occupies only a small portion. The rate-aware mask tradeoff further allows us to reduce the number of anchors that need to be compressed at low bit rates, thereby reducing the total size.

Table 4: Bitstream of each component. The result is for the scene *treehill* on Mip-NeRF 360 dataset.

	Number of Anchors (K)	Bitstream of Each Component (MB)						Total size (MB)	Fidelity	
		Position	Feature	Scaling	Offsets	Masks	MLPs		PSNR	SSIM
treehill (high-rate)	516.3	3.10	7.75	2.47	3.19	0.53	0.35	0.11	17.5	23.28 0.646
treehill (low-rate)	85.1	0.51	0.33	0.28	0.18	0.06	0.35	0.04	1.74	22.71 0.558

F ADDITIONAL BREAKDOWN RESULTS FOR CARM

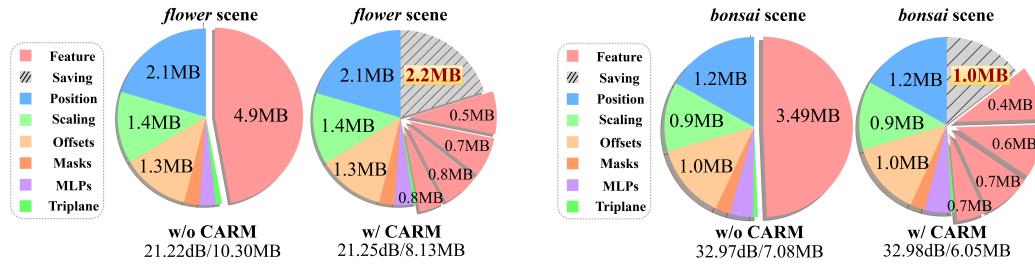
Figure 11: The breakdown analyses of different coding parts w/ and w/o our CARM for the *flower* and *bonsai* scenes, respectively.

Figure 11 provides additional breakdown results for *flower* and *bonsai* scenes. The results confirm again that our CARM effectively reduces the compressed size of the latent features associated with anchors’ attributes.

G THE IMPACT OF CARM ON DECODING TIME

Table 5: Comparison of the decoding time w/ and w/o our CARM.

Scene	Method	Decoding Time (s)		
		Triplane	Anchor Attributes	Total
room	CAT-3DGS (w/ CARM)	11.4	2.2	13.6
	CAT-3DGS w/o CARM	11.3	2.1	13.4
amsterdam	CAT-3DGS (w/ CARM)	47.4	17.0	64.4
	CAT-3DGS w/o CARM	47.2	14.9	62.1

We compare the decoding time of our schemes w/ and w/o CARM in Table 5. The results indicate that CARM has a negligible impact on the decoding time.

H COMPLETE BREAKDOWN OF QUANTITATIVE RESULTS

Quantitative results For a more comprehensive data presentation, we present detailed information on the rate-distortion curves, as shown in Figure 4, and the quantitative results are shown in Table 6.

Per-scene Results of Our CAT-3DGS Framework The detailed results of our approach for Mip-NeRF 360 dataset (Barron et al., 2022a) are presented in Table 7.

810 The detailed results of our approach for BungeeNeRF dataset (Xiangli et al., 2022) are presented in
 811 Table 8.

812 The detailed results of our approach for Tank&Temples dataset (Knapitsch et al., 2017) are presented
 813 in Table 9.

814 The detailed results of our approach for Deep Blending dataset (Hedman et al., 2018) are presented
 815 in Table 10.

816 **Per-scene Results of the Baseline Models** Per-scene results for all datasets from our two baseline
 817 models, ScaffoldGS (Lu et al., 2024) and HAC (Chen et al., 2024) are also provided in Table 15
 818 and Table 11 12 13 14, respectively.

819 Table 6: The Quantitative results of our CAT-3DGS and other approaches. 3DGS (Kerbl et al.,
 820 2023) and ScaffoldGS (Lu et al., 2024) are baseline methods, which are presented in the first sec-
 821 tion. Approaches in the second section are compact representation, while the third section covers
 822 rate-distortion-optimized compression approaches. For comparison, we also provide two results of
 823 different size and fidelity tradeoffs by adjusting λ_r . The size is measured in megabytes (MB).

Methods	Datasets				Mip-NeRF360				Tank&Temples				DeepBlending				BungeeNeRF			
	psnr ↑	ssim ↑	lips ↓	size ↓	psnr ↑	ssim ↑	lips ↓	size ↓	psnr ↑	ssim ↑	lips ↓	size ↓	psnr ↑	ssim ↑	lips ↓	size ↓	psnr ↑	ssim ↑	lips ↓	size ↓
3DGS(SIGGRAPH'23)	27.49	0.813	0.222	744.7	23.69	0.844	0.178	431.0	29.42	0.899	0.247	663.9	24.87	0.841	0.205	1616				
ScaffoldGS (CVPR'24)	27.50	0.806	0.252	253.9	23.96	0.853	0.177	86.50	30.21	0.906	0.254	66.00	26.62	0.865	0.241	183.0				
EAGLES(ECCV'24)	27.15	0.808	0.238	68.89	23.41	0.840	0.200	34.00	29.91	0.910	0.250	62.00	25.24	0.843	0.221	117.1				
LightGaussian	27.00	0.799	0.249	44.54	22.83	0.822	0.242	22.43	27.01	0.872	0.308	33.94	24.52	0.825	0.255	87.28				
Compact3DGS (CVPR'24)	27.08	0.798	0.247	48.80	23.32	0.831	0.201	39.43	29.79	0.901	0.258	43.21	23.36	0.788	0.251	82.60				
Compressed3D (CVPR'24)	26.98	0.801	0.238	28.80	23.32	0.832	0.194	17.28	29.38	0.898	0.253	25.30	24.13	0.802	0.245	55.79				
Morgenstern et al.	26.01	0.772	0.259	23.90	22.78	0.817	0.211	13.05	28.92	0.891	0.276	8.40	-	-	-	-	-	-	-	-
Navaneet et al.	27.16	0.808	0.228	50.30	23.47	0.840	0.188	27.97	29.75	0.903	0.247	42.77	24.63	0.823	0.239	104.3				
Trimming the fat	27.13	0.798	0.248	20.057	23.68	0.831	0.210	8.555	29.42	0.897	0.267	12.49	-	-	-	-	-	-	-	-
CompGS (high-rate)	27.26	0.802	0.239	16.5	23.70	0.835	0.205	9.61	29.33	0.900	0.270	10.4	-	-	-	-	-	-	-	-
CompGS (low-rate)	26.79	0.791	0.258	11.0	23.105	0.815	0.235	5.89	28.99	0.900	0.280	7.00	-	-	-	-	-	-	-	-
RDO-Gaussian (high-rate)	27.05	0.802	0.239	23.46	23.34	0.835	0.195	12.02	29.63	0.902	0.252	18.00	-	-	-	-	-	-	-	-
RDO-Gaussian (low-rate)	24.43	0.683	0.406	1.71	22.09	0.755	0.318	1.32	28.38	0.872	0.331	1.22	-	-	-	-	-	-	-	-
HAC (ECCV'24)(high-rate)	27.77	0.811	0.230	21.87	24.40	0.853	0.177	11.24	30.34	0.906	0.258	6.35	27.05	0.868	0.217	26.16				
HAC (ECCV'24)(low-rate)	26.11	0.759	0.312	5.96	23.11	0.809	0.238	3.68	28.62	0.888	0.302	2.64	24.56	0.768	0.327	9.74				
Ours (high-rate)	27.77	0.809	0.241	12.35	24.41	0.853	0.189	6.93	30.29	0.909	0.269	3.56	27.35	0.886	0.183	26.59				
Ours (low-rate)	25.82	0.730	0.362	1.72	22.97	0.786	0.293	1.42	28.53	0.878	0.336	0.93	25.19	0.808	0.279	10.14				

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Table 7: Results of Our approach for each scene from Mip-NeRF 360 dataset (Barron et al., 2022a).

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λ_r	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.002	bicycle	25.04	0.735	0.280	21.42
	bonsai	32.98	0.947	0.192	6.06
	counter	29.66	0.915	0.197	6.33
	flower	21.41	0.580	0.375	18.92
	garden	27.49	0.847	0.152	18.64
	kitchen	31.34	0.926	0.135	6.92
	room	31.95	0.924	0.212	4.11
	stump	26.79	0.766	0.271	11.23
	treehill	23.28	0.646	0.359	17.50
0.004	AVG	27.77	0.809	0.241	12.35
	bicycle	25.16	0.738	0.280	16.56
	bonsai	32.74	0.944	0.198	4.79
	counter	29.51	0.911	0.203	4.98
	flower	21.37	0.576	0.383	14.28
	garden	27.30	0.840	0.164	14.55
	kitchen	30.97	0.922	0.140	5.36
	room	31.73	0.921	0.221	3.22
	stump	26.87	0.766	0.278	8.50
0.01	treehill	23.27	0.642	0.370	13.20
	AVG	27.66	0.807	0.249	9.49
	bicycle	25.03	0.728	0.302	9.40
	bonsai	31.67	0.932	0.217	2.94
	counter	28.89	0.898	0.225	3.15
	flower	21.25	0.564	0.403	8.13
	garden	26.83	0.816	0.210	8.65
	kitchen	30.37	0.911	0.160	3.32
	room	31.24	0.911	0.243	2.06
0.015	stump	26.62	0.752	0.309	4.45
	treehill	23.22	0.629	0.400	7.17
	AVG	27.24	0.793	0.274	5.47
	bicycle	24.80	0.714	0.323	6.59
	bonsai	31.25	0.927	0.227	2.35
	counter	28.51	0.886	0.244	2.45
	flower	21.12	0.552	0.419	6.13
	garden	26.56	0.803	0.231	6.82
	kitchen	29.90	0.902	0.174	2.59
0.03	room	30.90	0.902	0.262	1.60
	stump	26.38	0.736	0.333	3.25
	treehill	23.08	0.616	0.423	5.13
	AVG	26.94	0.782	0.293	4.10
	bicycle	24.38	0.676	0.368	3.35
	bonsai	29.99	0.905	0.260	1.58
	counter	27.63	0.860	0.285	1.49
	flower	20.74	0.519	0.455	3.32
	garden	25.81	0.755	0.304	3.85
0.04	kitchen	28.76	0.878	0.216	1.53
	room	30.19	0.887	0.292	1.05
	stump	25.64	0.690	0.389	1.83
	treehill	22.84	0.580	0.472	2.44
	AVG	26.22	0.750	0.338	2.27
	bicycle	24.02	0.646	0.399	2.36
	bonsai	29.44	0.892	0.277	1.30
	counter	27.14	0.845	0.306	1.23
	flower	20.44	0.496	0.477	2.42
0.04	garden	25.40	0.727	0.337	3.01
	kitchen	28.16	0.862	0.244	1.20
	room	29.73	0.879	0.307	0.88
	stump	25.30	0.666	0.415	1.35
	treehill	22.71	0.558	0.499	1.74
0.04	AVG	25.82	0.730	0.362	1.72

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Table 8: Results of Our approach for each scene from BungeeNeRF dataset (Xiangli et al., 2022).

λ_r	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.001	amsterdam	27.57	0.908	0.148	31.98
	bilbao	28.25	0.897	0.165	25.38
	hollywood	25.16	0.815	0.254	24.58
	pompidou	25.82	0.864	0.214	28.83
	quebec	30.59	0.943	0.144	21.72
	rome	26.74	0.887	0.178	27.06
	AVG	27.35	0.886	0.184	26.59
0.002	amsterdam	27.52	0.903	0.159	27.33
	bilbao	28.15	0.892	0.176	22.03
	hollywood	25.12	0.808	0.268	20.95
	pompidou	25.70	0.857	0.224	24.26
	quebec	30.23	0.938	0.154	17.84
	rome	26.57	0.881	0.190	23.17
	AVG	27.22	0.880	0.195	22.60
0.003	amsterdam	27.28	0.897	0.169	24.47
	bilbao	28.13	0.888	0.181	19.41
	hollywood	25.05	0.801	0.280	18.72
	pompidou	25.69	0.854	0.232	21.52
	quebec	30.04	0.934	0.163	15.89
	rome	26.42	0.875	0.200	20.81
	AVG	27.10	0.875	0.204	20.14
0.006	amsterdam	26.96	0.882	0.194	19.38
	bilbao	27.72	0.876	0.202	15.63
	hollywood	24.68	0.778	0.307	14.90
	pompidou	25.21	0.839	0.251	17.22
	quebec	29.53	0.925	0.178	13.28
	rome	25.78	0.856	0.223	16.87
	AVG	26.65	0.859	0.226	16.21
0.01	amsterdam	26.32	0.863	0.215	15.96
	bilbao	27.26	0.861	0.222	12.73
	hollywood	24.41	0.757	0.325	12.71
	pompidou	24.86	0.825	0.267	14.33
	quebec	28.84	0.914	0.197	10.68
	rome	25.13	0.834	0.245	13.86
	AVG	26.14	0.842	0.245	13.38
0.02	amsterdam	25.65	0.833	0.253	12.33
	bilbao	26.30	0.829	0.258	9.74
	hollywood	23.80	0.714	0.361	9.12
	pompidou	23.78	0.789	0.298	10.75
	quebec	27.76	0.891	0.225	8.28
	rome	23.85	0.790	0.283	10.63
	AVG	25.19	0.808	0.280	10.14

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977 Table 9: Results of Our approach for each scene from Tank & Temples dataset (Knapitsch et al.,
978 2017).

λ_r	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.002	train	22.68	0.820	0.221	6.28
	truck	26.14	0.885	0.157	7.57
	AVG	24.41	0.853	0.189	6.93
0.004	train	22.45	0.817	0.226	5.06
	truck	25.98	0.882	0.162	5.88
	AVG	24.22	0.850	0.194	5.47
0.01	train	22.31	0.802	0.249	3.43
	truck	25.68	0.871	0.184	3.74
	AVG	23.99	0.837	0.217	3.58
0.015	train	22.23	0.794	0.262	2.71
	truck	25.55	0.866	0.195	3.00
	AVG	23.89	0.830	0.228	2.86
0.03	train	22.01	0.769	0.295	1.80
	truck	24.97	0.842	0.238	1.89
	AVG	23.49	0.806	0.266	1.85
0.04	train	21.42	0.750	0.315	1.47
	truck	24.51	0.822	0.271	1.38
	AVG	22.97	0.786	0.293	1.42

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1001 Table 10: Results of Our approach for each scene from Deep Blending (Hedman et al., 2018).
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λ_r	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.002	drjohnson	29.67	0.906	0.266	4.27
	playroom	30.90	0.911	0.272	2.85
	AVG	30.29	0.909	0.269	3.56
0.004	drjohnson	29.51	0.904	0.272	3.43
	playroom	30.81	0.909	0.279	2.21
	AVG	30.16	0.906	0.275	2.82
0.01	drjohnson	29.23	0.898	0.288	2.12
	playroom	30.23	0.903	0.295	1.46
	AVG	29.73	0.900	0.292	1.79
0.015	drjohnson	29.06	0.892	0.299	1.76
	playroom	29.91	0.897	0.309	1.21
	AVG	29.48	0.894	0.304	1.48
0.03	drjohnson	28.52	0.879	0.323	1.20
	playroom	29.19	0.887	0.331	0.85
	AVG	28.85	0.883	0.327	1.03
0.04	drjohnson	28.31	0.874	0.332	1.09
	playroom	28.74	0.881	0.340	0.76
	AVG	28.53	0.878	0.336	0.93

Table 11: Results of HAC (Chen et al., 2024) for each scene from Mip-NeRF 360 dataset (Barron et al., 2022a).

λ_e	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.001	bicycle	25.11	0.742	0.259	39.15
	bonsai	32.97	0.948	0.180	12.72
	counter	29.74	0.918	0.184	10.44
	flower	21.27	0.575	0.377	27.55
	garden	27.46	0.849	0.139	32.17
	kitchen	31.63	0.930	0.122	12.07
	room	31.90	0.926	0.198	7.85
	stump	26.59	0.763	0.264	25.26
	treehill	23.26	0.648	0.345	29.65
	AVG	27.77	0.811	0.230	21.87
0.002	bicycle	25.10	0.742	0.262	33.14
	bonsai	32.70	0.945	0.184	10.51
	counter	29.65	0.915	0.189	8.88
	flower	21.32	0.576	0.377	23.73
	garden	27.43	0.847	0.143	27.52
	kitchen	31.46	0.928	0.125	10.05
	room	31.87	0.925	0.201	6.47
	stump	26.59	0.761	0.268	21.75
	treehill	23.34	0.647	0.350	24.83
	AVG	27.72	0.809	0.233	18.54
0.004	bicycle	25.05	0.742	0.264	27.54
	bonsai	32.28	0.942	0.189	8.56
	counter	29.35	0.911	0.195	7.26
	flower	21.26	0.572	0.381	19.59
	garden	27.28	0.842	0.151	22.69
	kitchen	31.16	0.923	0.131	8.05
	room	31.55	0.921	0.208	5.53
	stump	26.58	0.762	0.269	18.11
	treehill	23.30	0.645	0.356	20.04
	AVG	27.53	0.807	0.238	15.26
0.01	bicycle	24.79	0.733	0.284	17.80
	bonsai	31.27	0.933	0.208	5.16
	counter	28.68	0.898	0.220	4.54
	flower	21.18	0.561	0.400	12.15
	garden	26.76	0.822	0.188	14.53
	kitchen	30.51	0.914	0.149	4.85
	room	31.20	0.912	0.234	3.27
	stump	26.54	0.752	0.296	11.21
	treehill	23.13	0.628	0.392	12.27
	AVG	27.12	0.795	0.263	9.53
0.02	bicycle	24.60	0.717	0.306	14.97
	bonsai	30.51	0.922	0.225	4.24
	counter	27.78	0.878	0.248	3.30
	flower	20.84	0.537	0.425	8.90
	garden	26.34	0.800	0.222	10.87
	kitchen	29.86	0.902	0.169	3.69
	room	30.51	0.900	0.256	2.56
	stump	26.20	0.730	0.326	8.68
	treehill	23.03	0.610	0.418	9.25
	AVG	26.63	0.777	0.288	7.38
0.035	bicycle	24.16	0.694	0.333	11.59
	bonsai	29.63	0.909	0.242	3.72
	counter	27.19	0.864	0.269	2.68
	flower	20.57	0.513	0.449	7.17
	garden	25.86	0.780	0.252	8.90
	kitchen	29.09	0.886	0.191	3.08
	room	29.94	0.889	0.276	2.15
	stump	25.77	0.707	0.358	7.03
	treehill	22.82	0.591	0.443	7.32
	AVG	26.11	0.759	0.312	5.96

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1088 Table 12: Results of HAC (Chen et al., 2024) for each scene from BungeeNeRF dataset (Xiangli
1089 et al., 2022).

λ_e	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.001	amsterdam	27.25	0.886	0.190	31.84
	bilbao	27.98	0.886	0.190	24.38
	hollywood	24.59	0.772	0.319	23.41
	pompidou	25.58	0.851	0.236	29.19
	quebec	30.30	0.934	0.163	21.23
	rome	26.61	0.876	0.203	26.91
	AVG	27.05	0.868	0.217	26.16
0.002	amsterdam	27.13	0.880	0.202	27.14
	bilbao	28.02	0.880	0.205	20.91
	hollywood	24.43	0.763	0.330	20.09
	pompidou	25.27	0.842	0.249	24.85
	quebec	29.98	0.929	0.175	17.90
	rome	26.28	0.866	0.219	23.07
	AVG	26.85	0.860	0.230	22.33
0.003	amsterdam	26.95	0.873	0.214	24.41
	bilbao	27.82	0.872	0.218	18.76
	hollywood	24.27	0.753	0.342	17.87
	pompidou	25.34	0.837	0.255	22.49
	quebec	29.67	0.924	0.185	16.15
	rome	25.98	0.855	0.231	20.83
	AVG	26.67	0.852	0.241	20.08
0.004	amsterdam	26.80	0.865	0.224	22.49
	bilbao	27.65	0.864	0.231	17.14
	hollywood	24.25	0.748	0.347	16.55
	pompidou	25.16	0.829	0.266	20.40
	quebec	29.33	0.918	0.192	15.06
	rome	25.68	0.845	0.243	19.30
	AVG	26.48	0.845	0.250	18.49
0.008	amsterdam	26.13	0.839	0.258	17.22
	bilbao	26.81	0.842	0.262	14.01
	hollywood	23.83	0.713	0.377	12.90
	pompidou	24.48	0.807	0.289	16.10
	quebec	28.60	0.906	0.216	11.71
	rome	24.71	0.811	0.276	15.34
	AVG	25.76	0.820	0.280	14.55
0.02	amsterdam	25.03	0.788	0.308	11.92
	bilbao	25.84	0.799	0.308	9.08
	hollywood	22.92	0.640	0.425	8.38
	pompidou	23.16	0.759	0.332	10.43
	quebec	27.15	0.872	0.262	8.18
	rome	23.25	0.750	0.327	10.47
	AVG	24.56	0.768	0.327	9.74

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Table 13: Results of HAC (Chen et al., 2024) for each scene from Tank & Temples dataset (Knapitsch et al., 2017).

λ_e	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.001	truck	26.02	0.883	0.147	12.42
	train	22.78	0.823	0.207	10.07
	AVG	24.40	0.853	0.177	11.24
0.004	truck	25.88	0.878	0.158	9.26
	train	22.19	0.815	0.216	6.94
	AVG	24.04	0.846	0.187	8.10
0.01	truck	25.69	0.874	0.172	7.04
	train	22.13	0.807	0.230	5.26
	AVG	23.91	0.841	0.201	6.15
0.02	truck	25.36	0.863	0.189	5.59
	train	22.02	0.795	0.250	3.97
	AVG	23.69	0.829	0.219	4.78
0.035	truck	24.96	0.853	0.208	5.04
	train	21.96	0.783	0.266	3.17
	AVG	23.46	0.818	0.237	4.10
0.045	truck	24.81	0.847	0.216	4.64
	train	21.42	0.771	0.279	2.72
	AVG	23.11	0.809	0.248	3.68

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Table 14: Results of HAC (Chen et al., 2024) for each scene from Deep Blending dataset (Hedman et al., 2018).

λ_e	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
0.001	playroom	30.84	0.906	0.262	5.03
	drjohnson	29.85	0.906	0.255	7.67
	AVG	30.34	0.906	0.258	6.35
0.002	playroom	30.66	0.905	0.265	4.12
	drjohnson	29.69	0.905	0.258	6.51
	AVG	30.17	0.905	0.262	5.32
0.004	playroom	30.44	0.902	0.272	3.15
	drjohnson	29.53	0.903	0.265	5.55
	AVG	29.98	0.902	0.269	4.35
0.01	playroom	30.31	0.906	0.279	2.58
	drjohnson	29.34	0.901	0.275	4.23
	AVG	29.83	0.903	0.277	3.40
0.02	playroom	29.87	0.900	0.292	2.23
	drjohnson	28.81	0.893	0.288	3.65
	AVG	29.34	0.897	0.290	2.94
0.035	playroom	29.26	0.893	0.302	2.01
	drjohnson	27.97	0.883	0.302	3.26
	AVG	28.62	0.888	0.302	2.64

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Table 15: Results of ScaffoldGS (Lu et al., 2024) for all evaluated datasets.

Datasets	Scenes	PSNR↑	SSIM↑	LPIPS↓	SIZE↓
Mip-NeRF360	bicycle	24.50	0.705	0.306	248.00
	bonsai	32.70	0.946	0.185	258.00
	counter	29.34	0.914	0.191	194.00
	flower	21.14	0.566	0.417	253.00
	garden	27.17	0.842	0.146	271.00
	kitchen	31.30	0.928	0.126	173.00
	room	31.93	0.925	0.202	133.00
	stump	26.27	0.784	0.284	493.00
	treehill	23.19	0.642	0.410	262.00
	AVG	27.50	0.806	0.252	253.89
Tank&Temples	truck	25.77	0.883	0.147	107.00
	train	22.15	0.822	0.206	66.00
	AVG	23.96	0.853	0.177	86.50
DeepBlending	playroom	30.62	0.904	0.258	63.00
	drjohnson	29.80	0.907	0.250	69.00
	AVG	30.21	0.906	0.254	66.00
BungeeNeRF	amsterdam	27.16	0.898	0.188	223.00
	bilbao	26.60	0.857	0.257	178.00
	hollywood	24.49	0.787	0.318	155.00
	pompidou	24.94	0.839	0.271	209.00
	quebec	30.28	0.936	0.190	159.00
	rome	26.23	0.873	0.225	174.00
	AVG	26.62	0.865	0.241	183.00

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