

**A Computational Methodology  
for Modelling the Dynamics of  
Statistical Arbitrage**

Andrew Neil Burgess

Decision Technology Centre

Department of Decision Sciences

A thesis submitted to the University of London for  
the degree of Doctor of Philosophy

UNIVERSITY OF LONDON

LONDON BUSINESS SCHOOL

October 1999

To my parents, Arnold and Carol.

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## Acknowledgements

Thanks to my supervisor, Paul Refenes, for bringing me to LBS, keeping me in bread and water, helping me with ideas and even reading the bloody thing!

Thanks to past and present colleagues at the Neuroforecasting Unit/Decision Technology Centre. Especially Yves Bentz, Peter Bolland, Jerry Connor, Stefania Pandelidaki, Neville Towers and Peter Schreiner; for discussions, hard work (not all the time), company and six good years. Also all the ex-CRLers who showed that even a real job can still be fun.

Thanks to the visitors to the LBS group, Fernando and Paul, for good times and hard work in London, Helsinki and Melbourne.

Thanks for the people who helped keep it real, especially to Pratap Sondhi for ideas and support when he was at Citibank at the beginning; the other sponsors of the Neuroforecasting Club and then the Decision Technology Centre; Botha and Derick down in S.A. for trusting me to build a trading system; and David and Andrew for all their efforts on behalf of New Sciences.

Also to whoever first decided to hold NIPS workshops at ski resorts; and to the regulars at NNCM/CF conferences: John Moody, Andreas Weigend, Hal White, Yaser Abu-Mostafa, Andrew Lo and Blake LeBaron in particular for their enthusiasm and inspiration.

Finally, my love and thanks to Deborah, who had to put up with me whilst I was writing up - and whose photographs of chromosomes had to compete for computer time with my equity curves.

## Abstract

Recent years have seen the emergence of a multi-disciplinary research area known as “Computational Finance”. In many cases the data generating processes of financial and other economic time-series are at best imperfectly understood. By allowing restrictive assumptions about price dynamics to be relaxed, recent advances in computational modelling techniques offer the possibility to discover new “patterns” in market activity.

This thesis describes an integrated “statistical arbitrage” framework for identifying, modelling and exploiting small but consistent regularities in asset price dynamics. The methodology developed in the thesis combines the flexibility of emerging techniques such as neural networks and genetic algorithms with the rigour and diagnostic techniques which are provided by established modelling tools from the fields of statistics, econometrics and time-series forecasting.

The modelling methodology which is described in the thesis consists of three main parts. The first part is concerned with constructing combinations of time-series which contain a significant predictable component, and is a generalisation of the econometric concept of cointegration. The second part of the methodology is concerned with building predictive models of the mispricing dynamics and consists of low-bias estimation procedures which combine elements of neural and statistical modelling. The third part of the methodology controls the risks posed by model selection and performance instability through actively encouraging diversification across a "portfolio of models". A novel population-based algorithm for joint optimisation of a set of trading strategies is presented, which is inspired both by genetic and evolutionary algorithms and by modern portfolio theory.

Throughout the thesis the performance and properties of the algorithms are validated by means of experimental evaluation on synthetic data sets with known characteristics. The effectiveness of the methodology is demonstrated by extensive empirical analysis of real data sets, in particular daily closing prices of FTSE 100 stocks and international equity indices.

# Table of Contents

<b>ACKNOWLEDGEMENTS.....</b>	<b>4</b>
<b>ABSTRACT .....</b>	<b>5</b>
<b>TABLE OF CONTENTS .....</b>	<b>6</b>
<b>INTRODUCTION: A METHODOLOGY FOR STATISTICAL ARBITRAGE.....</b>	<b>8</b>
1. INTRODUCTION .....	9
1.1 Scope .....	9
1.2 Motivation.....	10
1.3 Thesis Overview.....	13
1.4 Contributions.....	15
1.5 Organisation.....	17
1.6 Summary.....	20
2. BACKGROUND .....	21
2.1 Statistical Arbitrage .....	21
2.2 Recent Advances in Computational Modelling .....	30
2.3 Applications of Low-bias Modelling in Computational Finance.....	66
2.4 Summary.....	75
3. ASSESSMENT OF EXISTING METHODS.....	76
3.1 Potential for Model-based Statistical Arbitrage .....	76
3.2 Methodological Gaps.....	84
3.3 Summary.....	91
4. OVERVIEW OF PROPOSED METHODOLOGY .....	92
4.1 Overview of Modelling Framework .....	92
4.2 Part I: A Cointegration Framework for Statistical Arbitrage.....	94
4.3 Part II: Forecasting the Mispricing Dynamics using Neural Networks.....	101
4.4 Part III: Diversifying Risk by Combining a Portfolio of Models.....	109
4.5 Summary.....	114
<b>PART I: A COINTEGRATION FRAMEWORK FOR STATISTICAL ARBITRAGE.....</b>	<b>115</b>
5. METHODOLOGY FOR CONSTRUCTING STATISTICAL MISPRICINGS .....	116
5.1 Description of Cointegration Methodology .....	116
5.2 Extension to Time-varying Relationships.....	131
5.3 Extension to High-dimensional Problems.....	137
5.4 Summary.....	143
6. TESTING FOR POTENTIAL PREDICTABILITY .....	145
6.1 Description of Predictability Tests .....	145
6.2 Monte-Carlo Evaluation of Predictability Test Power.....	152
6.3 Bias-Correction of Predictability Tests .....	167
6.4 Evidence for Potential Predictability in Statistical Mispricings.....	173
6.5 Summary.....	176
7. EMPIRICAL EVALUATION OF IMPLICIT STATISTICAL ARBITRAGE MODELS .....	177
7.1 Implicit Statistical Arbitrage Strategies and Trading Rules.....	177

7.2 Empirical Results for FTSE 100 Equity Prices.....	180
7.3 Empirical Results for Equity Market Indices.....	189
7.4 Summary.....	197
<b>PART II: FORECASTING THE MISPRICING DYNAMICS USING NEURAL NETWORKS .....</b>	<b>199</b>
8. LOW-BIAS FORECASTING IN HIGHLY STOCHASTIC ENVIRONMENTS.....	201
8.1 General Formulation of the Model Estimation Problem.....	201
8.2 Estimating Predictive Models in Investment Finance.....	203
8.3 An Equivalent Kernels perspective on Neural Network learning.....	208
8.4 Summary.....	219
9. MODEL-FREE VARIABLE SELECTION.....	221
9.1 Statistical methodology for model-free variable selection .....	221
9.2 Implementation of Variable Selection Methodology .....	227
9.3 Evaluation of Variable Selection Test Power by Monte Carlo Simulation.....	231
9.4 Investigation of Model Bias using Monte Carlo Simulation.....	238
9.5 Summary.....	242
10. STATISTICAL METHODOLOGY FOR NEURAL NETWORK MODEL ESTIMATION .....	244
10.1 Framework for Optimising the Bias-Variance Tradeoff in Neural Networks.....	244
10.2 Algorithms for Neural Network Model Estimation .....	253
10.3 Experimental Validation of Neural Model Estimation Procedures.....	262
10.4 Summary .....	266
11. EMPIRICAL EVALUATION OF CONDITIONAL STATISTICAL ARBITRAGE MODELS.....	268
11.1 Conditional Statistical Arbitrage Models.....	268
11.2 Application of Variable Selection Methodology to FTSE 100 Data.....	273
11.3 Empirical Results of Conditional Statistical Arbitrage Models.....	279
11.4 Summary .....	296
<b>PART III: DIVERSIFYING RISK BY COMBINING A PORTFOLIO OF STATISTICAL ARBITRAGE MODELS .....</b>	<b>297</b>
12. A “PORTFOLIO OF MODELS” APPROACH TO STATISTICAL ARBITRAGE.....	298
12.1 Model Selection in Noisy and Nonstationary Environments.....	298
12.2 Controlling Model Selection Risk by Combining Models.....	304
12.3 Empirical Results for FTSE 100 models .....	309
12.4 Summary .....	315
13. A POPULATION-BASED ALGORITHM FOR JOINT OPTIMISATION OF TRADING MODELS .....	317
13.1 Risk-averse Optimisation .....	317
13.2 Controlled Evaluation of Population-based Algorithm.....	334
13.3 Empirical Evaluation on Equity Index Data.....	341
13.4 Summary .....	347
<b>CONCLUSIONS AND BIBLIOGRAPHY .....</b>	<b>348</b>
14. CONCLUSIONS.....	349
BIBLIOGRAPHY .....	355

## **Introduction: A Methodology for Statistical Arbitrage**

This part of the thesis introduces the concept of statistical arbitrage and examines the issues which will be developed in the rest of the thesis. Chapter 1 consists of a brief introduction which outlines the scope, motivation and organisation of the thesis as well as summarising the major contributions which it makes to the current state of the art. Chapter 2 describes the recent advances in computational modelling and computational finance which provide the background to the thesis. Chapter 3 describes the opportunities for statistical arbitrage which are presented by the advances in modelling methodology, assessing the strengths and weaknesses of existing modelling methods and highlighting the outstanding issues which the methodology presented in the thesis is designed to address. Finally Chapter 4 presents an overview of the methodology and a “route map” to the rest of the thesis.



## **Part I: A Cointegration Framework for Statistical Arbitrage**

In this part of the thesis we describe the first of the three parts of our methodology for statistical arbitrage modelling. This consists of a framework for constructing combinations of time-series which contain a potentially predictable component. An overview of the methodology described in this part of the thesis is presented in Section 4.2.

Chapter 5 describes a framework for modelling combined asset prices, which is inspired by the econometric concept of cointegration. The cointegration framework is used to generate potential statistical mispricings, by performing stochastic detrending of asset prices with respect to other, related, asset prices. The objective of this pre-processing is to generate combinations of time-series which are largely immunised against market-wide uncertainties and which enhance the potentially predictable components of asset price dynamics. The basic methodology is extended to time-varying relationships and also to high-dimensional problems where the number of assets is numbered in the tens or hundreds.

Chapter 6 describes a range of tests which are designed to identify potential predictability in the mispricing time-series. The tests include standard autocorrelation tests, cointegration tests for stationarity, and variance ratio tests for deviations from random walk behaviour as well as novel tests based upon the shape of the variance ratio profile as a whole. The strengths and weaknesses of the various tests are examined under controlled circumstances using Monte-Carlo simulations. Modifications of the predictability tests are presented which correct for the bias induced by the construction procedure. The final section of the chapter contains the results of applying the tests to combinations of FTSE 100 equity prices.

Chapter 7 describes a set of “implicit statistical arbitrage” (ISA) trading strategies which are designed to directly exploit any mean-reverting component in the mispricing dynamics, bypassing the intermediate stage of constructing an explicit forecasting model. The underlying assumption of the ISA strategies is that future price changes will be such as will tend (on average) to reduce the mispricing between a given “target” asset and the associated “synthetic asset”. The ISA rules are used to perform an empirical evaluation of the statistical mispricing methodology. The high-dimensional version of the mispricing construction methodology is evaluated with respect to models of the daily closing prices of FTSE 100 stocks; the adaptive version of the methodology is evaluated on the French CAC 40 and German DAX 30 stock market indices.

## Part II: Forecasting the Mispricing Dynamics using Neural Networks

In this part of the thesis we describe the second of the three parts of our methodology for statistical arbitrage modelling. This consists of algorithms, tools and procedures for supporting the construction of predictive models of the dynamics of statistical mispricing time-series. The methodology is designed to address the particularly hard problems that arise in the context of building predictive models in investment finance. An overview of the methodology described in this part of the thesis is contained in Section 4.3.

Chapter 8 provides the motivation and general framework for our predictive modelling methodology. It firstly presents a general formulation of the model estimation process before moving on to discuss the particularly hard nature of the problems which arise in the case of building predictive models of asset price dynamics. These problems include high noise, low degree of prior knowledge, small sample sizes and potential time-variation (nonstationarity) in the underlying data-generating processes. An “equivalent kernels” perspective is used to highlight the similarities between neural modelling and recent developments in non-parametric statistics. This in turn motivates the use of neural estimation methods in conjunction with statistical testing procedures as a means of achieving both flexibility and parsimony in an attempt to overcome the “bias-variance dilemma”.

Chapter 9 describes our methodology for model-free variable selection, which is based upon methods from non-parametric statistics and is intended to distinguish which variables from the information set should be included in the modelling procedure proper. The purpose of this “pre-selection” stage is to reduce the complexity, and hence **variance**, of the modelling process as a whole. The flexibility of the tests provides an important role in retaining the largest possible amount of *relevant* information upon which to condition the forecasting models. In particular, the tests are capable of identifying both nonlinear dependencies and interaction effects and thus avoid discarding variables which would be passed over by standard linear methods.

Chapter 10 describes our methodology for the actual estimation of low-bias forecasting models. This task is performed through novel algorithms which balance the flexibility of *neural networks* with the noise-tolerance and diagnostic procedures of *statistical regression*. Statistical testing and selection procedures are employed within a rigorous modelling framework which automatically optimises the specification of the neural network. Our

integrated approach to the model estimation problem combines the two aspects of variable selection and architecture selection, within a common framework based upon the statistical significance tests which are developed in Chapter 9. Within this common framework we describe three alternative algorithms which aim to optimise both variable selection and model complexity using the constructive, deconstructive and regularisation-based approaches to model building.

Chapter 11 describes an empirical evaluation of the methodology from Part I and Part II of the thesis used in combination. The model-free variable selection procedures and neural model estimation algorithms are applied to the problem of forecasting the dynamics of the statistical mispricings generated by the first part of our methodology. The objective of this exercise is to generate *conditional statistical arbitrage* (CSA) models in which nonlinearities, interaction effects and time-series effects can all be captured and exploited without being explicitly prespecified by the modeller. An empirical evaluation is presented of a set of CSA models which are based upon statistical mispricings between the constituent stocks of the FTSE 100 index.

### **Part III: Diversifying Risk by Combining a Portfolio of Statistical Arbitrage Models**

In this part of the thesis we describe the third part of our statistical arbitrage methodology. This addresses the implementation issues which arise in the context of applying predictive models to risk-averse decision-making in general and statistical arbitrage in particular. The methodology aims to reduce the risks which are inherent in the modelling process itself, thus increasing the extent to which the predictive information is efficiently exploited and increasing the likelihood of achieving successful statistical arbitrage strategies.

Chapter 12 describes our methodology for diversifying model risk. This is achieved through the use of model combination techniques which take into account the two equally important objectives of maximising return and minimising risk. Furthermore, the methodology emphasises the importance of using selection criteria which are as similar as possible to the ultimate performance measure (i.e. after-costs trading performance) rather than the traditional statistical criteria based upon forecasting accuracy alone. The traditional approach to model combination is used in conjunction with the risk-averse optimisation techniques of modern portfolio theory in order to achieve a “portfolio of models” approach. This approach is evaluated with respect to the conditional statistical arbitrage models described in the previous part of the thesis.

Chapter 13 represents a less developed solution to a much more ambitious task, namely that of integrating all stages of the modelling process in a single optimisation procedure. The objective of this approach is to reduce, and ultimately eliminate, the various inefficiencies which arise through the use of “multi-stage” approaches to modelling; for instance, when pre-processing, predictive modelling, and trading rule implementation are treated as separate rather than inter-dependent tasks. This chapter describes a population-based algorithm in which an entire set of models is generated in the context of a “joint” optimisation procedure. Through the use of optimisation criteria in which individual models are evaluated in terms of the *added-value* they provide to an existing portfolio, the algorithm actively encourages diversification and hence maximises the consequent opportunities for risk-reduction. The approach is evaluated with respect to both artificial and real-world problems.

## **Conclusions and Bibliography**

In this final part of the thesis we present a summary of our main conclusions and a bibliography. Chapter 14 presents the main conclusions of the thesis and discusses directions for further work; it contains an evaluation of the contribution which our current methodology makes to the state of the art, suggestions for future extensions and refinements of the methodology, and a discussion of the scope of possible practical applications of our work both in statistical arbitrage specifically and in the broader context of investment finance in general.

## 14. Conclusions

In this thesis we have proposed and developed an integrated framework which enables the use of recent advances in computational modelling as a means of exploiting small but consistent regularities in asset price dynamics. We adopt a holistic perspective in which our methodology is based on an extensive analysis of the obstacles which arise in financial forecasting and the manner in which they influence the effectiveness of the modelling process as a whole. We have addressed the weaknesses of existing methodology by combining computational modelling techniques from a number of different fields. Within our methodological framework we apply the different techniques only to the parts of the modelling process for which they are inherently suitable, thus maximising the strengths of the various techniques whilst minimising the effect of their weaknesses.

Within our integrated modelling framework, we have developed specific tools and techniques which represent significant advances upon the existing state of the art. We have consistently exploited the *flexibility* which is offered by emerging modelling techniques such as neural networks and genetic algorithms whilst ensuring that this flexibility is employed in an *appropriate* manner. This has been achieved by placing the emerging modelling techniques in the context of, and in partnership with, the methodological rigour and diagnostic techniques which are provided by established modelling tools from the fields of statistics, econometrics and time-series forecasting.

In particular, we have developed extensions of the econometric methodology of cointegration which are suitable for use in cases where the parameters of the underlying relationship are time-varying and for cases where the number of time-series involved in the analysis is numbered in tens or hundreds rather than units. We have developed novel tests for identifying deterministic components in time-series behaviour which are based upon the joint distribution of a set of variance ratio statistics. We have demonstrated, through controlled simulations, that our new tests are sensitive to a *wider range* of deviations from random behaviour than are standard predictability tests. By means of a computationally intensive approach based upon Monte-Carlo simulation, we have generalised the applicability of both our new tests and existing predictability tests to the case where the time-series under analysis represents the result of a cointegration-based pre-processing procedure. The advantage of the simulation-based approach is that the actual empirical distribution of the test statistics can be determined under equivalent experimental parameters to those which are present in a given analysis, thus

accounting for any artefacts which are induced by the pre-processing stage, automatically adjusting for sample size effects and avoiding any inefficiencies which would be incurred through the use of incorrect theoretical assumptions.

Through the use of an “equivalent kernels” perspective taken from nonparametric statistics, we have achieved a synthesis which includes both traditional parametric regression modelling and neural network learning. In particular, this approach allows us to compute the “degrees of freedom” which are contained in a neural network model and use this as the basis of a variety of statistical significance tests for neural network models and components within such models. We have developed three variant algorithms for neural model estimation which combine the low-bias of neural modelling techniques with the low-variance of statistical modelling procedures. Through controlled simulations, we have verified the properties of the algorithms and demonstrated that such a combined approach is vital in the case of modelling highly noisy time-series in which few *a priori* assumptions can be made about the nature of the underlying data-generating process.

We have generalised the model combination approaches of statistical forecasting in order to achieve diversification, and hence reduction, of the model risk which applies in the case of trading model-based strategies. Our “portfolio of models” approach extends the ensemble approach to forecasting with ideas from portfolio theory in order to provide a means of maximising the expected returns whilst simultaneously minimising the level of risk of a combined set of trading strategies as a whole. We have built upon this approach in order to develop a population-based algorithm, which exploits the particular strengths of genetic (and evolutionary optimisation) algorithms as a means of jointly optimising the whole set of models within a population. We have demonstrated, through the use of controlled simulations, that this approach can overcome the *criterion* risk which arises in cases where complex models are optimised in multiple stages and on an *individual* rather than *collective* basis. In particular, the population-based algorithm can be used to generate a portfolio of complementary models by actively encouraging diversification within the population and thus maximising the benefits which can be achieved through the portfolio approach.

We have applied these various methodological developments from a particular perspective which we refer to as “statistical arbitrage”. We consider statistical arbitrage as a generalisation of traditional “riskless” arbitrage strategies which are based on predefined relationships between financial assets, typically between derivative instruments such as options

and futures contracts and the “underlying” assets upon which the derivatives are based. From our statistical arbitrage perspective, we apply our extended cointegration methodology to identify statistical “fair price” relationships between sets of related asset prices. Just as deviations from theoretical no-arbitrage relationships are considered “mispricings” which represent potential opportunities for riskless arbitrage, we likewise consider deviations from the analogous statistical fair-price relationships as potential opportunities for statistical arbitrage, and refer to them as “statistical mispricings”.

We have demonstrated that our methodology is applicable to real-world problems by performing extensive experimental evaluations from the statistical arbitrage perspective. This approach can, perhaps, be considered the purest method of evaluating the added-value which is provided by a computational modelling approach to investment finance. This is because the profits and losses of the resulting models are almost entirely independent of the underlying movements in the market as a whole and instead reflect only the informational advantage, if any, which is provided by the models themselves. Furthermore, the significance of the resulting performance can be evaluated not only from a statistical perspective but also from a practical perspective in which the economic advantages of the models can be assessed after factors such as transaction costs have been taken into account. In principle, the risk and return of our strategies can either be multiplied through leverage (up or down) and/or overlaid as a market-timing component on top of a more traditional trading strategy. Thus the benefits of our approach are potentially of value to active fund managers in general, as well as arbitrageurs and hedge funds in particular.

From this perspective, the results of our empirical evaluations can be taken as being highly promising whilst at the same time not conclusive. The results are highly promising because they indicate that significant levels of profitability can be achieved, at acceptable levels of risk, even after transaction costs have been taken into account. At the same time we believe that the results are not conclusive because the true tests of a trading methodology cannot be evaluated in a research environment using historical data but must ultimately be performed in a true trading environment using real prices, real trading costs and real trading infrastructure. Having made this caveat, we do believe that our experimental results demonstrate significant potential. Our first set of extensive experiments were based upon an implicit assumption of mean-reverting behaviour in the time-series dynamics of statistical mispricings between daily closing prices of FTSE 100 constituents. During a 200 day out-of-sample period, a set of these “implicit statistical arbitrage” strategies produced a backtested performance of between 7 and



10%, assuming typical institutional levels of transaction costs, with the corresponding Sharpe Ratios of between 2 and 3 demonstrating a high degree of consistency within this performance. More advanced “conditional statistical arbitrage” strategies based upon low-bias neural models of the mispricing dynamics achieved a collective annualised out-of-sample performance of 21% return and 2.45 Sharpe Ratio even at a moderately high level of transaction costs (0.5%). This annualised out-of-sample performance was further improved to 26.6% return and 3.40 Sharpe Ratio by means of the “portfolio of models” approach. Additional experimental results of statistical arbitrage models between international equity market indices indicate that the methodology has real potential in these cases also.

Whilst beyond the scope of this thesis itself, certain additional evaluations and developments of the methodology have been made in the commercial world itself. The original inspiration for our methodology arose from collaborative projects between the Computational Finance Group of the Decision Technology Centre (formerly Neuroforecasting Unit) at London Business School and a number of financial institutions. An earlier version of the methodology formed the basis of the modelling work conducted in the ESPRIT research project “High frequency Arbitrage Trading” (HAT), with favourable live performance evaluations carried out by the two banks in the consortium, one bank evaluating models within the equity and equity derivatives markets and the other evaluating models within the fixed-income (and derivatives) markets. Additional developments of the methodology currently form the basis of commercial negotiations between an LBS spin-off company and a major financial information services company and data vendor.

In terms of further methodological developments we believe that our work raises many avenues for future research. In particular we have highlighted the important role played by the different sources of potential error during the modelling process, especially in the context of the high noise content and temporal instability (nonstationarity) of predictive relationships between asset prices. We believe that further analysis of the issues raised in the thesis will lead to developments concerning the identification of appropriate modelling biases for financial markets, and methods for controlling the sources of model error which are represented by model variance, data snooping, performance nonstationarity and criterion risk.

We believe that there is significant potential to develop the specific methodology described in this thesis, both in the context of statistical arbitrage modelling and also extensions to other modelling domains. Furthermore, our modelling framework as a whole should be considered as

inclusive rather than exclusive. We have referred within the body of the thesis to the fact that our cointegration based approach for constructing statistical mispricings could be replaced or combined with other multivariate approaches such as principal components analysis, factor analysis and independent components analysis. Furthermore the linear fair price relationships, to which we restrict ourselves for reasons of implementational convenience, could nevertheless be extended to the nonlinear cases enabled by recent advances in these modelling techniques.

Similarly, the low-bias neural modelling methodology in the second stage of our framework could be either extended to include, or indeed be replaced by, related low-bias approaches from nonparametric statistics or machine learning. It is our belief that given appropriate underlying modelling assumptions the achievable level of performance will be limited more by the informational content of the data itself than by the differences between alternative modelling techniques. However, it would certainly be interesting to quantify the extent to which this is true, and also the circumstances under which techniques such as projection pursuit, smoothing splines and support vector machines will indeed achieve similar results to our synthesis of neural and statistical techniques.

It is at the final stage of our methodology that perhaps the largest questions remain, and the greatest potential for future development. Assuming that cases exist where financial asset price data *can* be preprocessed into a form which contains significant deterministic components, and predictive models *can* be estimated of the resulting time-series dynamics, then the most interesting and important question arises in the form of “how can this advantage best be exploited ?” We believe that we have made important first steps in this direction, in particular through our recognition of the inter-related nature of the various stages of the modelling process and our integration of these stages in the joint optimisation procedure of our population-based algorithm.

Perhaps a productive route towards future advances may be to adopt a similar philosophy to that which underlies this thesis, namely to identify the important problems which established techniques have been developed to solve, and then also to identify the manner in which overly restrictive assumptions of these techniques can be relaxed, through the appropriate application of the continual developments in computational hardware, software, data availability and modelling methodology. Another fruitful route may be to identify the important but previously unanswerable (and hence generally unasked) *questions* which these developments now make

it possible to answer. If the financial markets can be thought of as an artificial ecology, then we believe that computational analogies with natural evolution, neural recognition and reinforcement learning, which have achieved such amazing results in the natural ecology, have an equivalent potential in finance which we are only just beginning to realise.

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