

1) When $s_A = 0.9 \text{ m}$

$$s_B = \frac{0.18}{0.12} s_A$$

$$= 1.35 \text{ m}$$

$$\theta = \frac{s_A}{0.12}$$

$$= 7.5 \text{ rad}$$

$$I_G = mk^2$$

$$= 6 \times 0.14^2$$

$$= 0.1176 \text{ kgm}^2$$

$$U_{1 \rightarrow 2} = -3g(0.9) + 3g(1.35) - 0.5(7.5)$$

$$= 9.4935$$

$$U_{1 \rightarrow 2} = E_{k2} - E_{k1}$$

$$= \frac{1}{2} I_G \omega^2 + \frac{1}{2} m_A v_A^2 + \frac{1}{2} m_B v_B^2$$

$$= 0.5(0.1176) \omega^2 + 0.5(3)(0.12^2) \omega^2$$

$$+ 0.5(3)(0.18^2) \omega^2$$

$$= 0.129 \omega^2$$

$$9.4935 = 0.129 \omega^2$$

$$\omega = 8.578637611 \text{ rad s}^{-1}$$

$$v_A = 0.12(8.578637611) \\ \approx 1.029 \text{ ms}^{-1}$$

2) Assuming cylinder C has speed v and acceleration a

$$\omega_A = \frac{v}{r_1} = \frac{v}{0.1} = 10v$$

$$\omega_A(0.15) = \omega_B(0.1)$$

$$\omega_B = 15v$$

$$\alpha_A = \frac{a}{r_1} = \frac{a}{0.1} = 10a$$

$$\alpha_A(0.15) = \alpha_B(0.1)$$

$$\alpha_B = 15a$$

$$a) mgs = \frac{1}{2}mv^2 + \frac{1}{2}I_G\omega_A^2 + \frac{1}{2}I_G\omega_B^2$$

$$10gs = \frac{1}{2}(10)v^2 + \frac{1}{2}(6.25)(10v)^2 + \frac{1}{2}(0.25)(15v)^2$$

$$10gs = 45.625v^2$$

$$\frac{16g}{73}s = v^2$$

$$2\left(\frac{8g}{73}\right)s = v^2$$

$$\therefore a = \frac{8 \times 9.81}{73}$$

$$= 1.075068493 \text{ ms}^{-2}$$

$$v = at = 1.075(3)$$

$$= 3.225205479 \approx 3.225 \text{ ms}^{-1}$$

$$2b) T_B(0.1) = I_G \alpha_B$$

$$T_B = 10(0.25)(15)(1.075) \\ = 40.31506849 \text{ N}$$

$$c) T_A(0.1) - T_B(0.15) = \hat{I}_G \alpha_B$$

$$T_A(0.1) - \frac{8829}{1460} = 0.25(10)(1.075)$$

$$T_A = 87.34931507 \text{ N}$$

3) Making use of instantaneous centre C,

$$v_G = \frac{L}{2} \dot{\theta} = \frac{L}{2} \omega$$

So E_K of AB can be expressed as:

$$\begin{aligned} E_K &= \frac{1}{2} m v_G^2 + \frac{1}{2} I_G \omega^2 \\ &= \frac{1}{2} m L^2 \omega^2 \end{aligned}$$

The E_P of the system can be expressed as:

$$\begin{aligned} E_P &= E_g + E_e \\ &= mgy + \frac{1}{2} k \delta^2 \\ &= mg(-0.5L \sin \theta) + \frac{1}{2} k (L \sin \theta)^2 \end{aligned}$$

$$E_K + E_P = 0$$

$$\frac{1}{6} m L^2 \omega^2 - \frac{1}{2} m g L \sin \theta + \frac{1}{2} k L^2 \sin^2 \theta = 0$$

$$\omega^2 = \frac{3}{m L^2} (m g L \sin \theta - k L^2 \sin^2 \theta)$$

$$\omega = \pm \sqrt{3 \left(\frac{g}{L} \sin \theta - \frac{k}{m} \sin^2 \theta \right)}$$

3) For point A, using instant centre C,

$$v_A = L \cos \theta \omega$$

$$= \pm L \cos \theta \sqrt{3 \left(\frac{g}{L} \sin \theta - \frac{k}{m} \sin^2 \theta \right)}$$

$$= \pm 0.75 \cos \theta \sqrt{39.24 \sin \theta - 30 \sin^2 \theta}$$

4) Using instant centre for rolling without slipping

$$v_A = v_B = 0.5 v_c$$

$$= 0.5 v$$

$$\omega_A = \omega_B = \omega$$

$$= \frac{0.5 v}{r}$$

$$U = 10 \text{ s}$$

$$U = \frac{1}{2} (6) v^2 + 2 \left[\frac{1}{2} (4) (0.5 v)^2 + \frac{1}{2} I_c \omega^2 \right]$$

$$= 3v^2 + 2 \left[\frac{2}{4} v^2 + \frac{1}{2} \left(\frac{1}{2} \right) (4) (\cancel{0.015^2}) \left(\frac{0.5}{\cancel{0.075}} \right)^2 \right]$$

$$= 3v^2 + v^2 + \frac{1}{2} v^2$$

$$= 4.5 v^2$$

$$\therefore 10 \text{ s} = 4.5 v^2$$

$$\frac{20}{9} \text{ s} = v^2$$

$$2 \left(\frac{10}{9} \right) \text{ s} = v^2$$

$$\therefore a = \frac{10}{9} \text{ ms}^{-2}$$

$$v = at$$

$$= \frac{10}{9} (2.5)$$

$$= \frac{25}{9} \text{ ms}^{-1}$$

5) Let D be a point on the belt,

$$2s_A - s_D = \text{constant}$$

$$v_D = 2v_A = 2v$$

$$a_D = 2a = 2a$$

$$\omega_B = \frac{v_D}{r} = \frac{2v}{r}$$

$$\omega_A = \frac{v_A}{r} = \frac{v}{r}$$

$$\alpha_B = \frac{a_D}{r} = \frac{2a}{r}$$

$$\alpha_A = \frac{a_A}{r} = \frac{a}{r}$$

$$a) mgs = \frac{1}{2} m v_A^2 + \frac{1}{2} I_G \omega_A^2 + \frac{1}{2} I_G \omega_B^2$$

$$10gs = \frac{1}{2}(10)v^2 + \frac{1}{4}(10)(\cancel{0.125})^2 \left(\frac{v}{\cancel{0.125}}\right)^2 \\ + \frac{1}{4}(10)(\cancel{0.125})^2 \left(\frac{2v}{\cancel{0.125}}\right)^2$$

$$10gs = 17.5v^2$$

$$gs = \frac{7}{4}v^2$$

$$2\left(\frac{2}{7}g\right)s = v^2$$

$$5a) \therefore a = \frac{2}{7}g$$

$$= \frac{981}{350} \approx 2.803 \text{ms}^{-2}$$

$$v = at$$

$$= 2.5 \times \frac{981}{350}$$

$$= \frac{981}{140} \approx 7.01 \text{ms}^{-1}$$

b) Considering disk B,

$$M_B = Tr$$

$$= I_G \alpha_B$$

$$= \frac{1}{2}mr^2 \left(\frac{2a}{r} \right)$$

$$T = \frac{1}{2}mr^2 \left(\frac{2a}{r} \right)$$

$$T = ma$$

$$= 10 \left(\frac{981}{350} \right)$$

$$= \frac{981}{35}$$

$$\approx 28.03 \text{N}$$