

$$2.1a) E = 70 \times 10^9 \text{ Pa}$$

$$F_P = 4 \times 10^3 \text{ N}$$

$$\delta_{AB} = \frac{F_P L_{AB}}{A_{AB} E}$$

$$= \frac{4 \times 10^3 \times 0.4}{\left(\frac{20}{2} \times 10^{-3}\right)^2 \pi \times 70 \times 10^9}$$

$$= 0.07275654541 \text{ mm}$$

$$\approx 0.0728 \text{ mm}$$

For the deflection at A to be 0,

$$\delta_{BC} = \frac{F_{P-Q} L_{BC}}{A_{BC} E}$$

$$0.07275654541 \times 10^{-3} = \frac{\frac{1}{2} F_{P-Q}}{\left(\frac{60}{2} \times 10^{-3}\right)^2 \times \pi \times 70 \times 10^9}$$

$$F_{P-Q} = 28800 \text{ N}$$

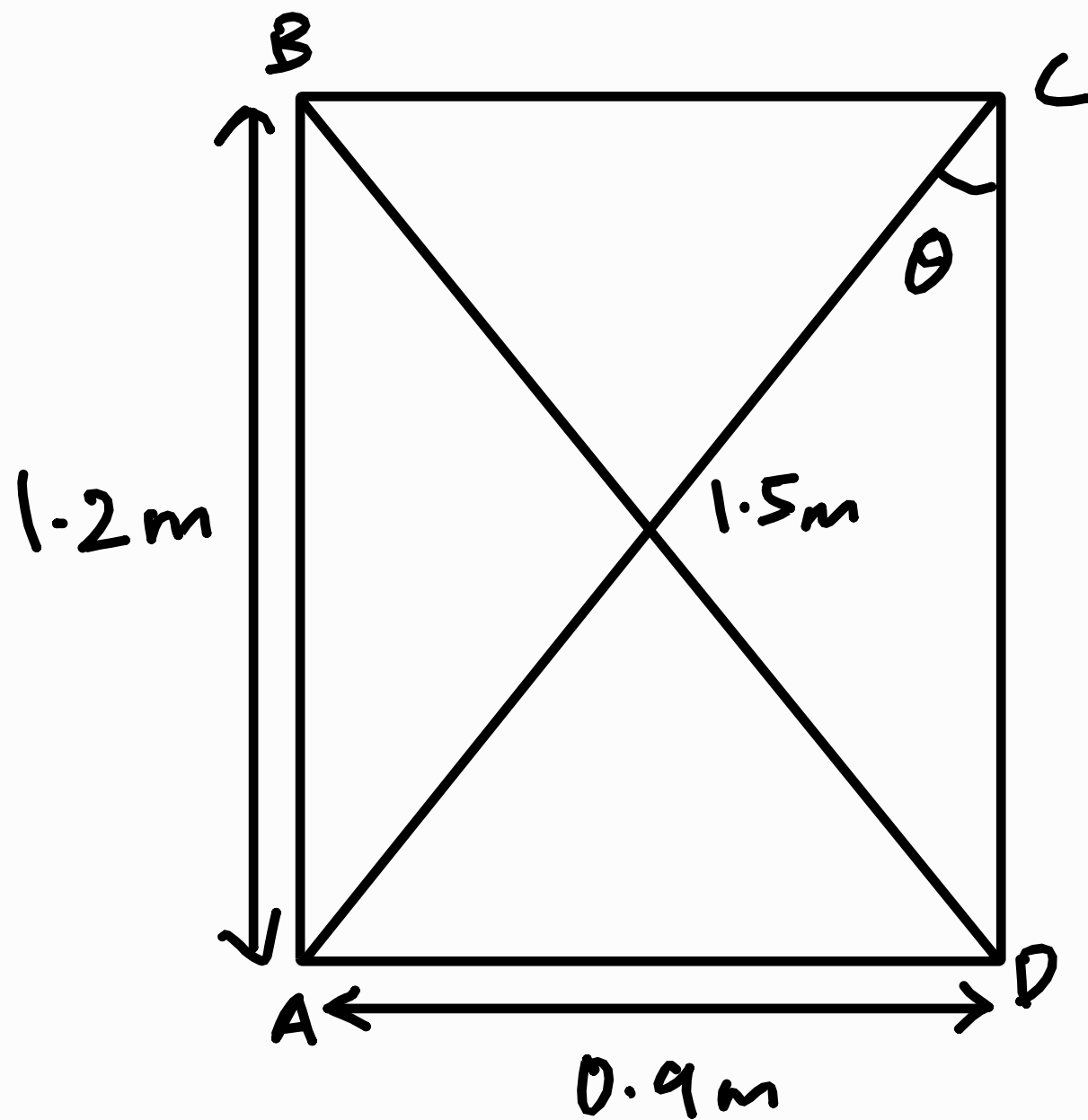
$$F_Q = F_{P-Q} + F_P$$

$$= 32.8 \text{ kN}$$

$$\therefore Q_{\sim} \text{ is } 32.8 \text{ kN.}$$

The corresponding deflection of B is 0.0728 mm.

2.23)



$$\text{length of AC} = \sqrt{1.2^2 + 0.9^2} \\ = 1.5 \text{ m}$$

$$\delta_{CD} = \frac{F_{AC} L_{CD}}{A_{CD} E}$$

$$1 \times 10^{-3} = \frac{F_{AC} \cos \theta (1.2)}{\left(\frac{30}{2} \times 10^{-3}\right)^2 \pi (200 \times 10^9)}$$

$$37500\pi = F_{AC} \left(\frac{1.2}{1.5}\right)$$

$$F_{AC} = 147262.1556 \\ \approx 147.3 \text{ kN}$$

$$2.69) E = 87 \times 10^9 \text{ Pa}$$

$$\nu = 0.34$$

$$\epsilon_x = \frac{\sigma_x}{E} - \frac{\nu \sigma_y}{E} - \frac{\nu \sigma_z}{E}$$

$$= \frac{1}{E} (\sigma_x - \nu(\sigma_y + \sigma_z))$$

$$= \frac{1}{87 \times 10^9} (120 \times 10^6 - 0.34(0 + 160 \times 10^6))$$

$$= \frac{41}{54375}$$

$$\epsilon_x = \frac{\delta_x}{L}$$

$$\delta_x = \epsilon_x L_x$$

$$= \frac{41}{54375} (100 \times 10^{-3})$$

$$= 0.075400229885 \text{ mm}$$

$$\approx 0.0754 \text{ mm}$$

$$\epsilon_z = \frac{1}{E} (\sigma_z - \nu(\sigma_x + \sigma_y))$$

$$= \frac{1}{87 \times 10^9} (160 \times 10^6 - 0.34(120 \times 10^6 + 0))$$

$$= \frac{149}{108750}$$

$$\delta_z = \epsilon_z L_z$$

$$= \frac{149}{108750} (75 \times 10^{-3})$$

$$= 0.01027586207 \text{ mm} \approx 0.028 \text{ mm}$$

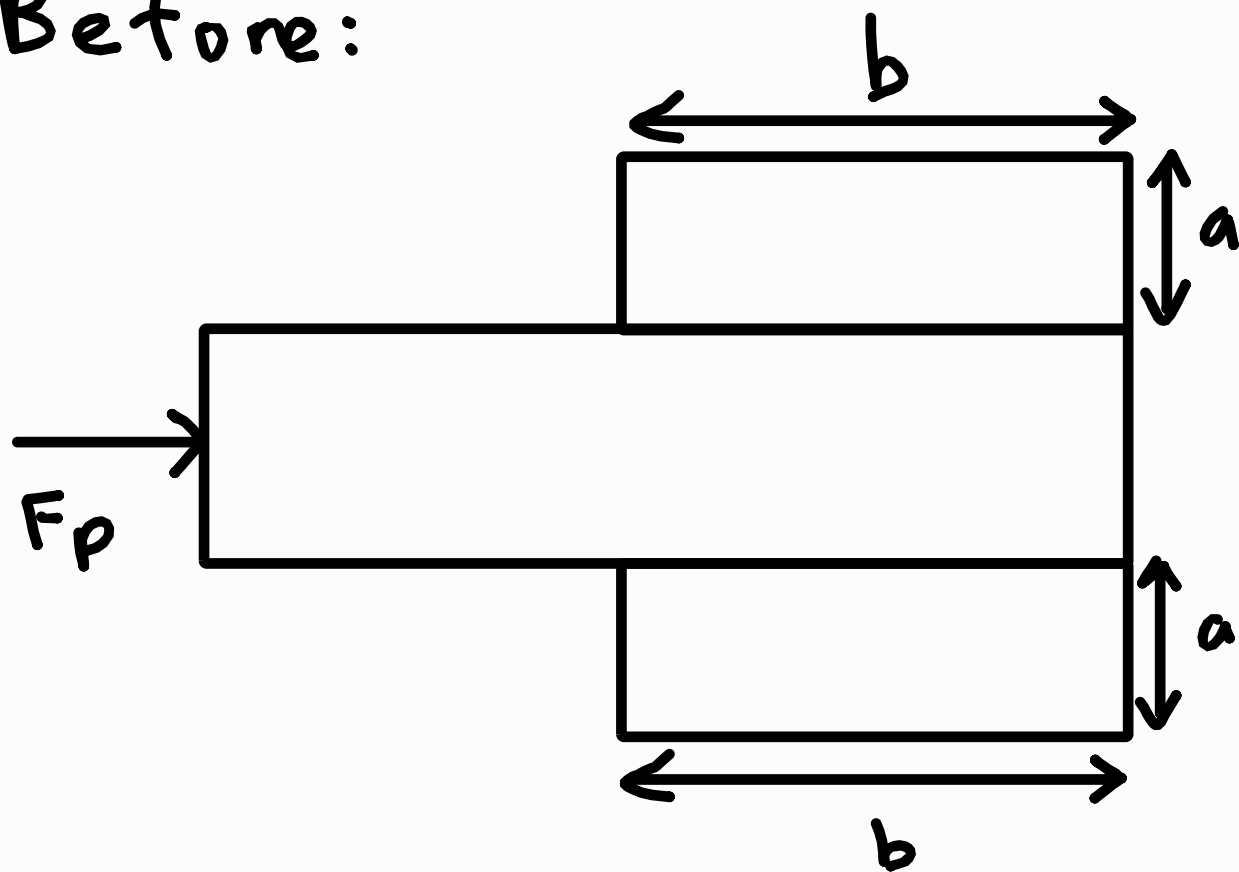
$$\begin{aligned} 2.6a) \quad \delta_{Ac} &= \sqrt{(100+0.0754)^2 + (75+0.1028)^2} - \sqrt{75^2 + 100^2} \\ &= 0.121982472 \text{ mm} \\ &\approx 0.122 \text{ mm} \end{aligned}$$

$$2.7a) G = 12 \times 10^6 \text{ Pa}$$

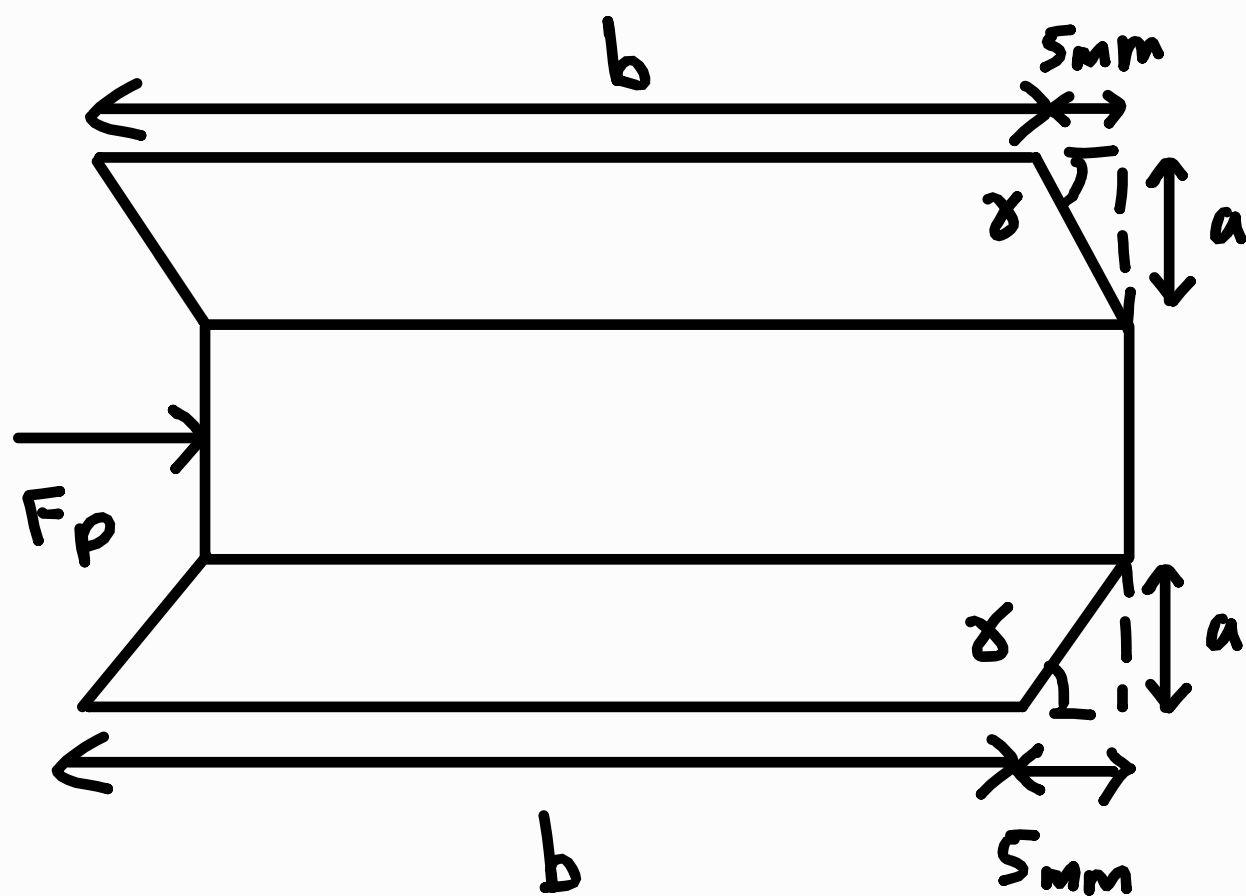
$$F_p = 40 \times 10^3 \text{ N}$$

$$c = 100 \times 10^{-3} \text{ m}$$

Before:



After:



$$\tau = G \gamma$$

Since γ is small,

$$\tau = G \tan \gamma$$

$$1.4 \times 10^6 = 12 \times 10^6 \left(\frac{5}{a} \right)$$

$$a = 42.85714286 \text{ mm}$$

$$\approx 43 \text{ mm}$$

2.79) Since the above is a double shear (after diagram),

$$\tau = \frac{\frac{1}{2} F_p}{b_c}$$

$$1.4 \times 10^6 = \frac{\frac{1}{2} (40 \times 10^3)}{100 \times 10^{-3} b}$$

$$b = 142.8571429 \text{ mm}$$

$$\approx 143 \text{ mm}$$