

1) Wave frequency,  $f_{\max} = \frac{1}{T}$   
 $= \frac{1}{2} \text{ Hz}$

a) Sampling rate,  $f_s = 1 \text{ Hz}$

$$\therefore f_s = 2 f_{\max}$$

b)  $f_s = \frac{1}{1.5} \text{ Hz}$

$$= \frac{2}{3} \text{ Hz}$$

$$\therefore f_s = \frac{4}{3} f_{\max}$$

c)  $8\Delta s = 3T$

$$\Delta s = \frac{3T}{8}$$

$$= \frac{6}{8}$$

$$f_s = \frac{1}{\Delta s}$$

$$= \frac{8}{6} \text{ Hz}$$

$$\therefore f_s = \frac{16}{6} f_{\max}$$

$$1d) f_s = \frac{1}{0.5}$$

$$= 2 \text{ Hz}$$

$$\therefore f_s = 4 f_{\max}$$

$$e) f_s = 4 \text{ Hz}$$

$$\therefore f_s = 8 f_{\max}$$

$$2) \sum_{n=1}^{\infty} \frac{4}{(2n-1)\pi} \sin \left[ \frac{2\pi(2n-1)t}{10} \right]$$

$$f_{\max} = 2 \text{ Hz}$$

$$f_s > 2 f_{\max}$$

$$f_s > 4 \text{ Hz}$$

An appropriate sampling rate would be 5 Hz.

$$\therefore f_s = 5 \text{ Hz}$$

2) Frequencies = 0.1, 0.3, 0.5, 0.7, 0.9, 1.1, 1.3, 1.5, 1.7, 1.9

Alias frequency,  $f_a = |f_{s \cdot i} - f_n|$

$f_s$	$f_a$
0.1	$ 5(1) - 0.1  = 4.9$
0.3	$ 5(1) - 0.3  = 4.7$
0.5	$ 5(1) - 0.5  = 4.5$
0.7	$ 5(1) - 0.7  = 4.3$
0.9	$ 5(1) - 0.9  = 4.1$
1.1	$ 5(1) - 1.1  = 3.9$
1.3	$ 5(1) - 1.3  = 3.7$
1.5	$ 5(1) - 1.5  = 3.5$
1.7	$ 5(1) - 1.7  = 3.3$
1.9	$ 5(1) - 1.9  = 3.1$

$$3a) \log_2 756 = \frac{\ln 756}{\ln 2}$$

$$= 9.562242424$$

$$\approx 10$$

$\therefore$  10 bits are required to represent 756.

b)

	Remainder
2   756	0
2   378	0
2   189	1
2   94	0
2   47	1
2   23	1
2   11	1
2   5	1
2   2	0
2   1	1
0	

$$756 = (1011110100)_2$$

$$3b) \text{ Resolution} = \frac{5-0}{2^8}$$
$$= \frac{5}{256}$$

$$\approx 0.0195V$$

$$\text{Voltage value} = 32 \left( \frac{5}{256} \right)$$
$$= 0.625V$$