

5.9) Taking moments about A:

$$45 \times 1.8 \times \frac{1}{2} \times 1.8 + (1.8 + 0.9)(120) = R_c(1.8)$$

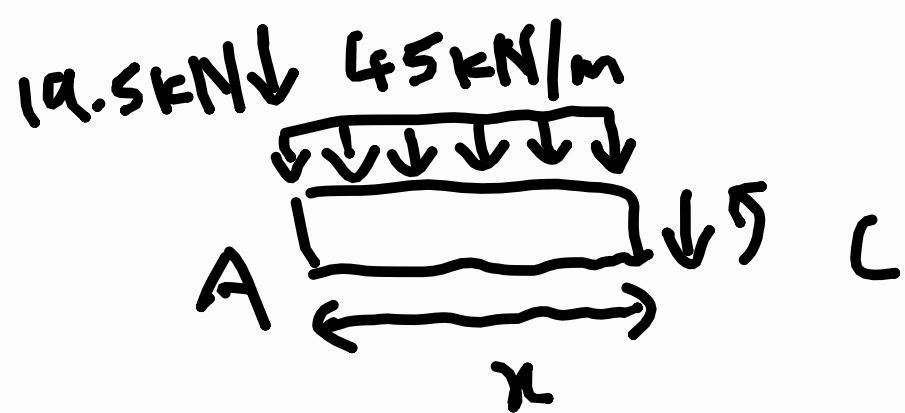
$$R_c = 220.5 \text{ kN}$$

Taking moments about B:

$$0.9(220.5) + R_A(1.8 + 0.9) = (45 \times 1.8)(0.9 + \frac{1}{2}(1.8))$$

$$R_A = -19.5 \text{ kN}$$

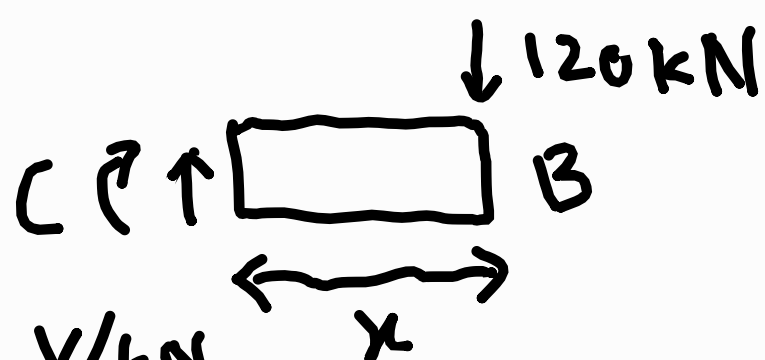
From A to C:



$$V = -19.5 - 45x \text{ kN}$$

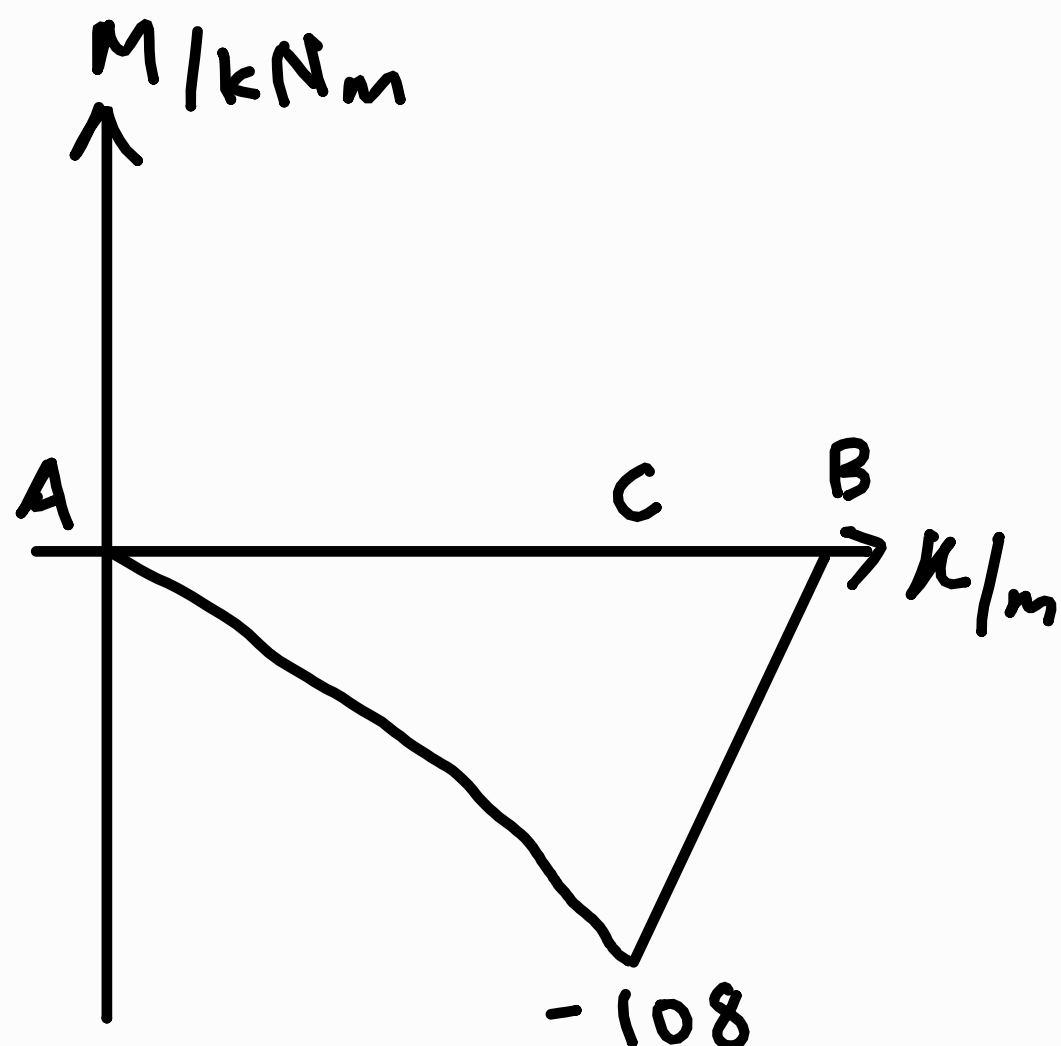
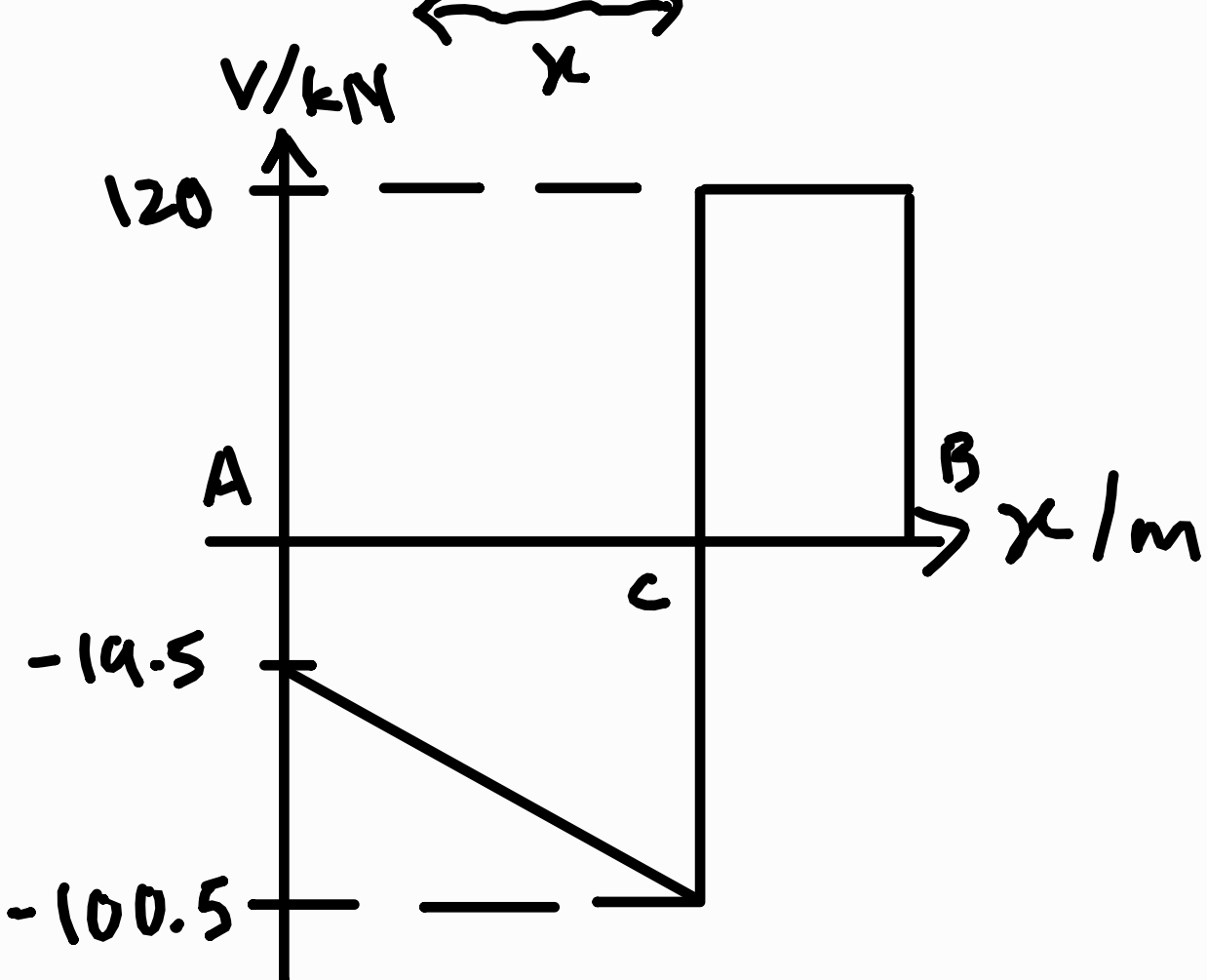
$$M = -19.5x - 22.5x^2 \text{ kNm}$$

From B to C:



$$V = 120 \text{ kN}$$

$$M = -120x \text{ kNm}$$



5.11) Taking moments about A:

$$F_B = 3 \times 300 + 450 + 3 \times (300 + 400)$$

$$= 3450 \text{ N}$$

$$= 3.45 \text{ kN}$$

Taking moments about B:

$$F_A(300 \times 2 + 400) + 450 = 3(300 + 400) + 3(300)$$

$$F_A = 2.55 \text{ kN}$$

From A to C:

$$V = 2.55 \text{ kN}$$

$$M = 2.55x \text{ Nm}$$

From A to D:

$$V = 2.55 - 3 = -0.45 \text{ kN}$$

$$M = 2.55x - 3(x - 300)$$

$$= -0.45x + 900 \text{ Nm}$$

5.11) From A to E:

$$V = -0.45 \text{ kN}$$

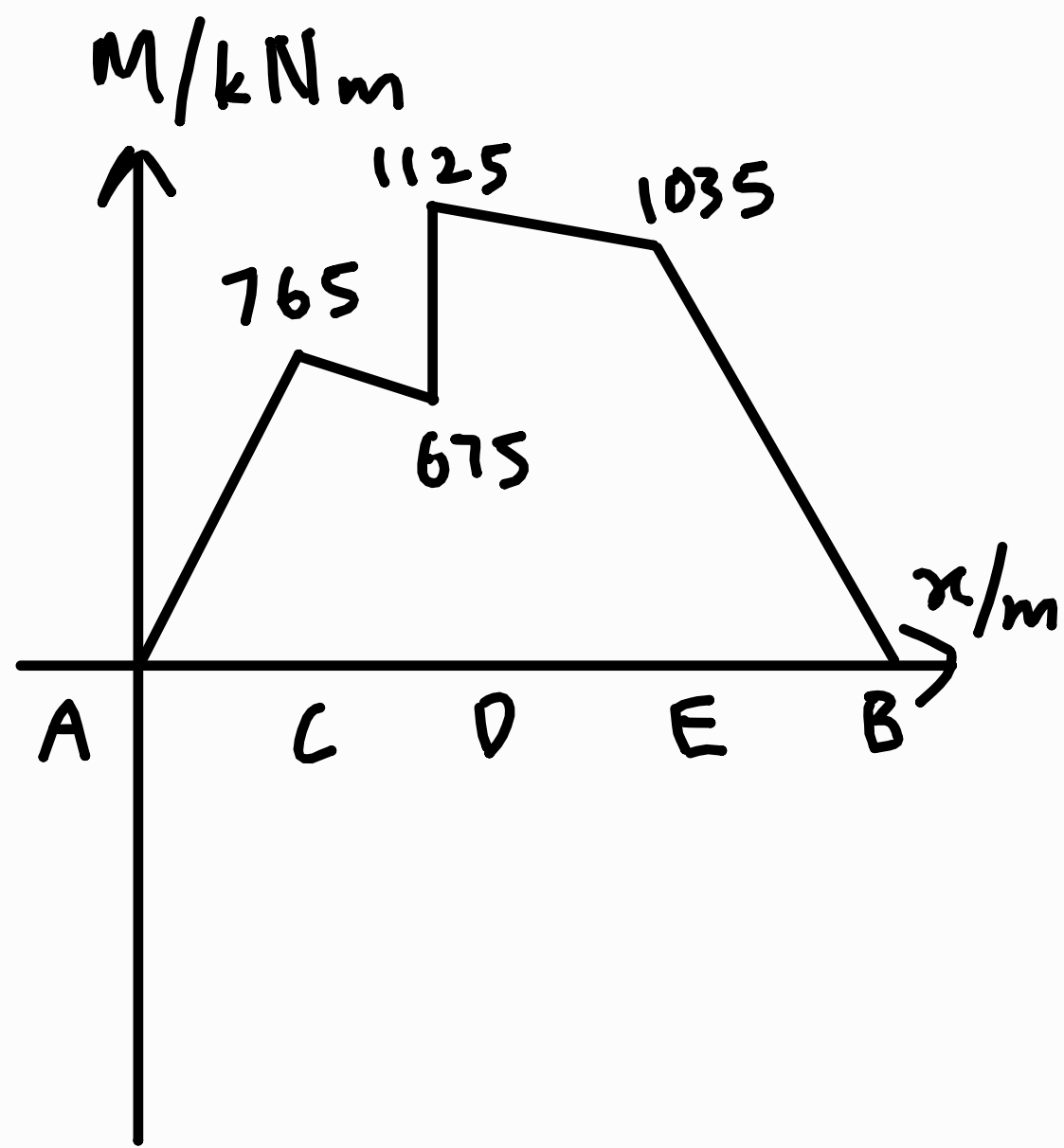
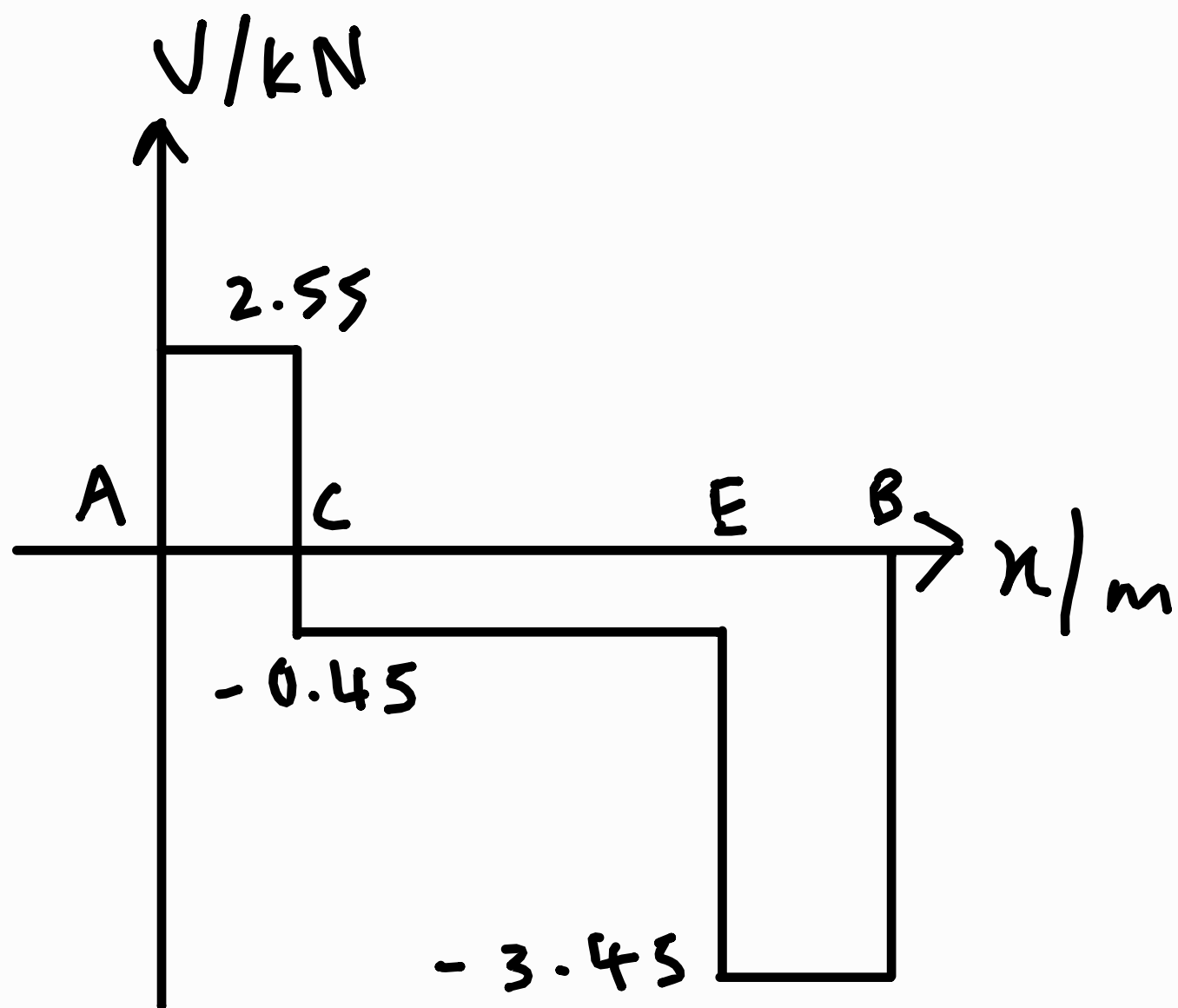
$$M = 2.55x - 3(x - 300) + 450$$

$$= -0.45x + 1350 \text{ Nm}$$

From B to E:

$$V = -3.45 \text{ kN}$$

$$M = 3.45x \text{ Nm}$$



5.33) Let $w = 7860b^2g$, and $L = 3.6m$

Taking moments about C:

$$F_D(1.2) = 7860b^2g(1.8-1.2)$$

$$F_D = 3930b^2g = \frac{w}{2}$$

Taking moments about D:

$$F_C(1.2) = 7860b^2g(1.8-1.2)$$

$$F_C = 3930b^2g = \frac{w}{2}$$

Let X be the midpoint of the bar

From A to C:

$$\begin{aligned} M &= -w\left(\frac{L}{3}\right)\left(\frac{L}{3} \times \frac{1}{2}\right) \\ &= -\frac{wL^2}{18} \end{aligned}$$

From A to X:

$$\begin{aligned} M &= -w\left(\frac{L}{2}\right)\left(\frac{L}{2} \times \frac{1}{2}\right) + \frac{w}{2}\left(\frac{L}{3}\right) \\ &= -\frac{wL^2}{24} \end{aligned}$$

$$\begin{aligned} \therefore \sigma_{\max} &= \frac{\frac{wL^2}{18} \times \frac{1}{2}b}{\frac{1}{12}b^4} \\ &= \frac{wL^2}{3b^3} \end{aligned}$$

5.33a) When $\sigma_{\max} = 10 \text{ MPa}$,

$$10 \times 10^6 = \frac{wL^2}{3b^3}$$

$$10 \times 10^6 = \frac{7860 \cancel{\text{kg}} \text{g} (3.6)^2}{3b^3}$$

$$b = 33.3100512 \text{ mm}$$

$$\approx 33.3 \text{ mm}$$

b) When $\sigma_{\max} = 50 \text{ MPa}$,

$$50 \times 10^6 = \frac{wL^2}{3b^3}$$

$$50 \times 10^6 = \frac{7860 \cancel{\text{kg}} \text{g} (3.6)^2}{3b^3}$$

$$b = 6.66201024 \text{ mm}$$

$$\approx 6.66 \text{ mm}$$

5.65) Let $L = 2.4 \text{ m}$

Taking moments about A:

$$F_D L = 1.8\left(\frac{L}{3}\right) + 3.6\left(\frac{2L}{3}\right)$$

$$F_D = 3 \text{ kN}$$

Taking moments about D:

$$F_A L = 1.8\left(\frac{2L}{3}\right) + 3.6\left(\frac{L}{3}\right)$$

$$F_A = 2.4 \text{ kN}$$

From A to B:

$$\begin{aligned} M &= 2.4\left(\frac{L}{3}\right) \\ &= 0.8L \text{ kNm} \end{aligned}$$

From A to C:

$$\begin{aligned} M &= 2.4\left(\frac{2L}{3}\right) - 1.8\left(\frac{L}{3}\right) \\ &= L \text{ kNm} \end{aligned}$$

$$5.65) \quad \sigma_{\max} = \frac{M_y}{I}$$

$$12 \times 10^6 = \frac{L \left(\frac{h}{2} \right) \times 10^3}{\frac{1}{12} (40 \times 10^{-3}) h^3}$$

$$12 \times 10^6 h^2 = 150 L \times 10^3$$

$$h = \sqrt{\frac{150 \times 2.4 \times 10^3}{12 \times 10^6}}$$

$$h = 0.1732050808 \text{ m}$$

$$\approx 173.2 \text{ mm}$$