

Sem 2 AY 17/18

2a) Longitudinal stress required = 1.0 MPa

$$\sigma_2 = 1.0 \text{ MPa} + \frac{mg}{\pi(401^2 - 400^2) \times 10^{-6}}$$
$$\approx 1.0 \times 10^6 + \frac{30 \times 9.81}{\pi(401^2 - 400^2) \times 10^{-6}}$$

$$= 1116952.059 \text{ Pa}$$

$$\sigma_2 = \frac{pr}{2t}$$

$$1116952.059 = \frac{p(400 \times 10^{-3})}{2(1 \times 10^{-3})}$$

$$p = 5584.760297 \text{ Pa}$$

$$\approx 5.585 \text{ kPa}$$

Sem 1 AY13/14

(a) At section H,

$$\text{Axial force} = 400\text{N}$$

$$\text{Shear force} = 300\text{N}$$

$$\text{Torque} = R_b = 30\text{Nm}$$

$$\begin{aligned} \text{Moment about the vertical axis} \\ = S_b = 40\text{Nm} \end{aligned}$$

(b) Axial force = 400N

$$\text{Shear force} = 300\text{N}$$

$$\text{Torque} = R_b = 30\text{Nm}$$

$$\begin{aligned} \text{Moment about the vertical axis} \\ = S_b = 40\text{Nm} \end{aligned}$$

Sem 1 AY 13/14

$$\text{1c) Area of the circular cross-section} = \pi \left( \frac{20 \times 10^{-3}}{2} \right)^2 \\ = \pi \times 10^{-4} \text{ m}^2$$

For the top element,

$$\sigma_a = \frac{400}{\pi \times 10^{-4}}$$

$$= \frac{4}{\pi} \text{ MPa}$$

$$\sigma_b = \frac{My}{I}$$

$$= \frac{R(c-a) \times 10 \times 10^{-3}}{\frac{1}{4} \pi (10 \times 10^{-3})^4}$$

$$= \frac{300(25) \times 10 \times 10^{-6}}{\frac{1}{4} \pi (10)^4 \times 10^{-12}}$$

$$= \frac{30}{\pi} \text{ MPa}$$

$$\sigma_{\text{total}} = \sigma_a + \sigma_b$$

$$= \frac{4}{\pi} + \frac{30}{\pi}$$

$$= \frac{34}{\pi}$$

$$= 10.8225361 \text{ MPa}$$

$$\approx 10.8 \text{ MPa}$$

Sem 1 AY 13/14

$$1c) \tau_e = \frac{\tau_c}{j}$$

$$= \frac{30 \times 10 \times 10^{-3}}{\frac{1}{2} \pi (10^4) \times 10^{-12}}$$

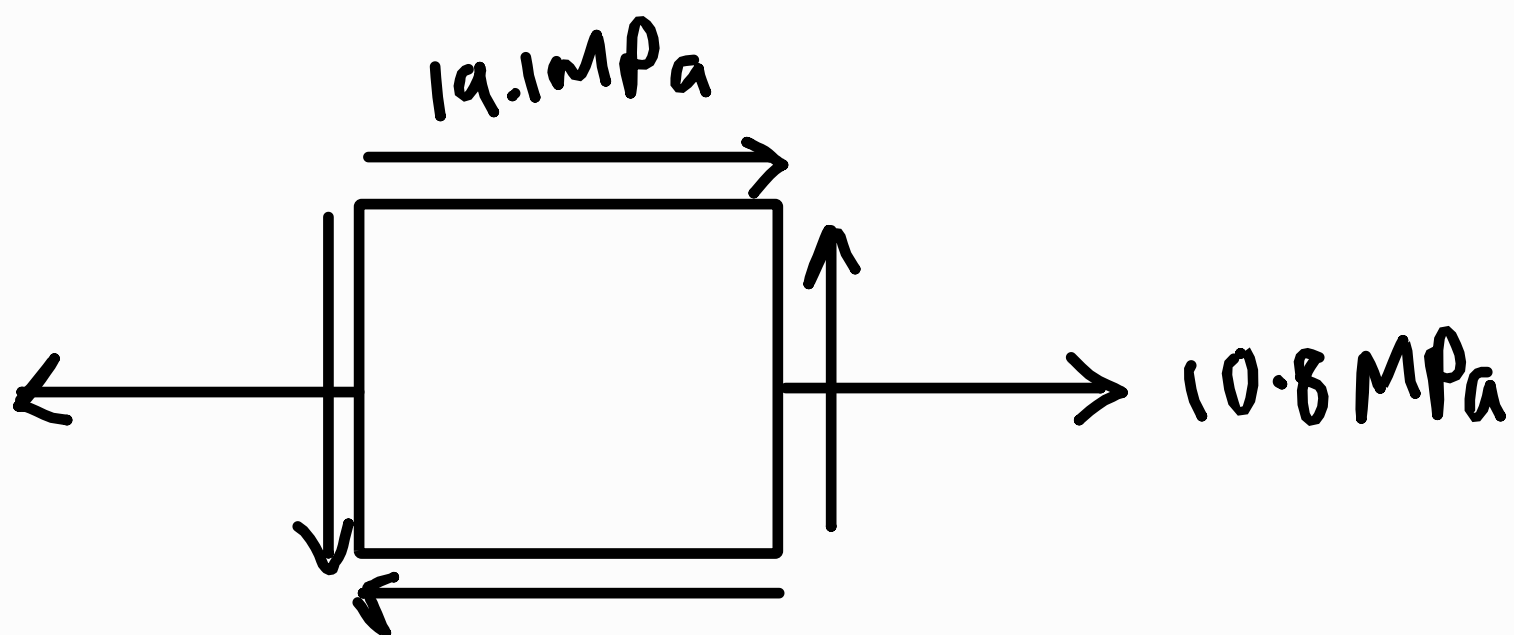
$$= \frac{60}{\pi} \text{ MPa}$$

$$\tau_b = 0$$

$$\tau_{\text{total}} = \tau_e + \tau_b$$
$$= \frac{60}{\pi} + 0$$

$$= 19.09859317 \text{ MPa}$$

$$\approx 19.1 \text{ MPa}$$



Sem 1 AY13/14

(c) For the side element,

$$\sigma_a = \frac{400}{\pi \times 10^{-4}}$$
$$= \frac{4}{\pi} \text{ MPa}$$

$$\sigma_b = \frac{My}{I}$$

$$= \frac{56 \times 10 \times 10^{-3}}{I}$$

$$= \frac{400 \times 100 \times 10^{-3} \times 10 \times 10^{-3}}{\frac{1}{4} \pi (10^4) \times 10^{-12}}$$

$$= \frac{160}{\pi}$$

$$\sigma_{\text{total}} = \sigma_a - \sigma_b$$

$$= \frac{4}{\pi} - \frac{160}{\pi}$$

$$= -\frac{156}{\pi} \text{ MPa}$$

$$= -49.65634224 \text{ MPa}$$

$$\approx -49.7 \text{ MPa}$$

Sem 1 AY13/14

$$\begin{aligned} 1c) \tau_t &= \tau_t \text{ of the top element} \\ &= \frac{60}{\pi} \text{ MPa} \end{aligned}$$

$$\tau_b = \frac{VQ}{It}$$

$$= \frac{300 \times \frac{2(10 \times 10^{-3})^3}{3}}{\frac{1}{4} \pi (10^4) \times 10^{-12} \times 20 \times 10^{-3}}$$

$$= \frac{4}{\pi} \text{ MPa}$$

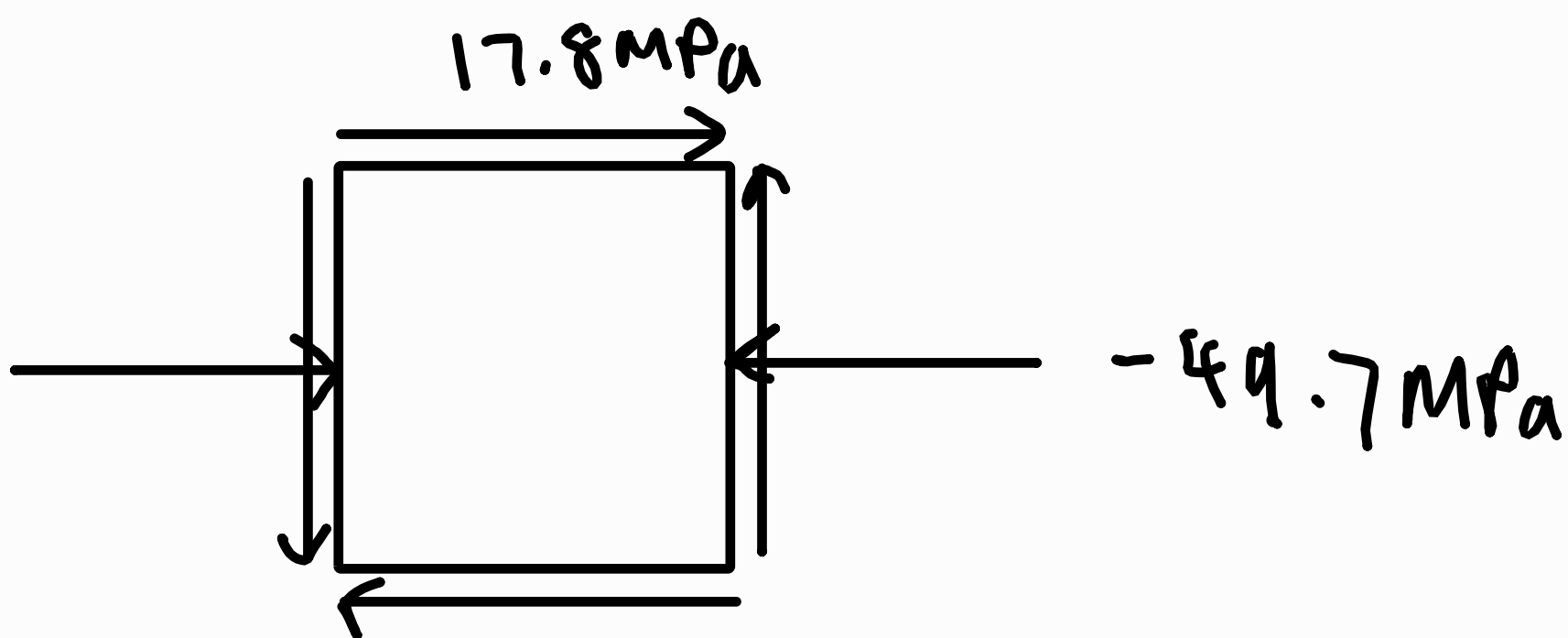
$$\tau_{\text{total}} = \tau_t - \tau_b$$

$$= \frac{60}{\pi} - \frac{4}{\pi}$$

$$= \frac{56}{\pi}$$

$$= 17.82535363 \text{ MPa}$$

$$\approx 17.8 \text{ MPa}$$



Sem 1 AY 15/16

$$\begin{aligned} 3a) P_x &= 1.0 \cos 30^\circ \\ &= \frac{\sqrt{3}}{2} \text{ kN} \end{aligned}$$

$$\begin{aligned} P_y &= 1.0 \sin 30^\circ \\ &= \frac{1}{2} \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Anti-clockwise moment due to } P_x, M_p &= P_x r_o \\ &= \frac{\sqrt{3}}{2} \times 100 \\ &= 50\sqrt{3} \text{ Nm} \end{aligned}$$

At  $0.8L$ :

$$\text{Axial load} = -\frac{\sqrt{3}}{2} \text{ kN}$$

$$\text{Shear force} = \frac{1}{2} \text{ kN}$$

$$\text{Torque} = 200 \text{ Nm}$$

$$\begin{aligned} M_{0.8L} &= M - M_p - P_y(0.8) \\ &= 500 - 50\sqrt{3} - \frac{1}{2} \times 0.8 \times 10^3 \\ &= 13.39745962 \text{ Nm} \\ &\approx 13.40 \text{ Nm.} \end{aligned}$$

MP2001 Exam Sem 1 04/05

$$\begin{aligned} \text{1a) } F_G &= -12 \times 10^6 \times 4500 \times 10^{-6} \\ &= -54 \text{ kN} \end{aligned}$$

$$\begin{aligned} \sigma_F &= 300 \times 10^{-6} \times 200 \times 10^9 \\ &= 60 \text{ MPa} \end{aligned}$$

$$\begin{aligned} F_F &= 60000 \times 500 \times 10^{-6} \\ &= 30 \text{ kN} \end{aligned}$$

$$P(300) = 54(150) + 450(30)$$

$$P = \frac{21600}{300}$$

$$= 72 \text{ kN}$$

$$\text{1b) } \tau_{ult} = 700 \text{ MPa}$$

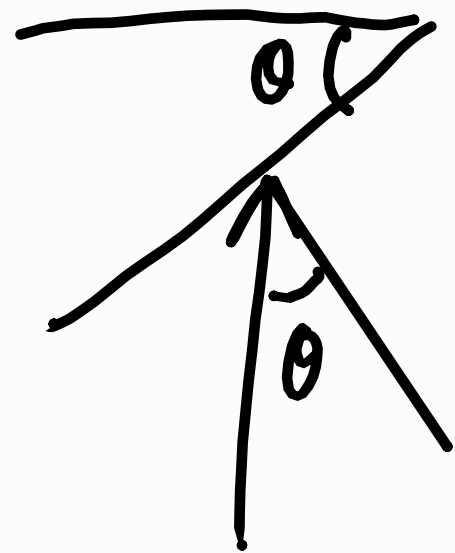
$$\frac{700 \times 10^6}{2.5} = \frac{30 \times 10^3 \times \frac{c}{2}}{\pi \left(\frac{d}{2}\right)^2}$$

$$\begin{aligned} d &= 8.258889836 \times 10^{-3} \text{ m} \\ &\approx 8.26 \text{ mm} \end{aligned}$$



MP2001 exam sem 1 04/05

$$\begin{aligned} (c) F_{\text{shear}} &= F \sin \theta \\ &= 30 \sin \theta \end{aligned}$$



$$F_{\text{normal}} = 30 \cos \theta$$

$$\begin{aligned} \sigma &= \frac{30 \cos \theta}{\pi \left( \frac{15}{2} \times 10^{-3} \right)^2} \\ &= \frac{1.6 \times 10^6 \cos \theta}{3\pi} \text{ kPa} \end{aligned}$$

$$\begin{aligned} \tau &= \frac{30 \sin \theta}{\pi \left( \frac{15}{2} \times 10^{-3} \right)^2} \\ &= \frac{1.6 \times 10^6 \sin \theta}{3\pi} \text{ kPa} \end{aligned}$$

When  $\theta = 50^\circ$ ,

$$\sigma_{50^\circ} = \frac{1.6 \times 10^6 \cos 50^\circ}{3\pi}$$

$$= 109123.0138 \text{ kPa}$$

$$\approx 109.1 \text{ MPa}$$

$$\tau_{50^\circ} = \frac{1.6 \times 10^6 \sin 50^\circ}{3\pi}$$

$$= 130047.7437 \text{ kPa}$$

$$\approx 130.0 \text{ MPa}$$

M201 99/00 sem 2

$$\begin{aligned} (b) \quad \sigma_b &= \frac{M_y}{I} \\ &= \frac{F\left(\frac{1}{2}L\right)\left(\frac{1}{2}h\right)}{\frac{1}{12}bh^3} \\ &= \frac{3FL}{bh^2} \end{aligned}$$

$$\sigma_p = \sigma_b$$

$$\frac{2P}{\cancel{bh}} = \frac{3FL}{\cancel{bh^2}}$$

$$2Ph = 3FL$$

$$F = \frac{2}{3} \left( \frac{Ph}{L} \right)$$

G262 03/04 Sem 2

$$\sigma_{ult} = -5 \text{ MPa}$$

$$\frac{Pr}{2t} - \sigma_{max} = \sigma_{ult}$$

$$\sigma_{max} = \frac{Pr}{2t} - \sigma_{ult}$$

$$= \frac{200 \times 10^3 \times 31.9 \times 10^{-3}}{2(0.1 \times 10^{-3})} - (-5) \times 10^6$$

$$= 36.9 \text{ MPa}$$

$$F_{max} = 36.9 \times 10^6 \times \pi(32^2 - 31.9^2) \times 10^{-6}$$
$$= 740.7592734 \text{ N}$$

$$N_{max} = \frac{F_{max}}{400 \times 10^{-3} \times 9.81}$$

$$= 188.7765732$$

$$\approx 188$$

M201 Exam 99/00 Sem 2

$$\sigma_z = \frac{pr}{2t}$$

$$\sigma_{\text{axial due to load}} = \frac{200}{\pi(125^2 - 124^2) \times 10^{-6}}$$
$$= 0.2556705913 \text{ MPa}$$

$$\sigma_b = \frac{My}{I}$$

$$= \frac{200(500 \times 10^{-3}) \times 125 \times 10^{-3}}{\frac{1}{4} \pi (125^4 - 124^4) \times 10^{-12}}$$

$$= 2.061793098 \text{ MPa}$$

$$\sigma_z = \sigma_{\text{axial}} + \sigma_b$$

$$\frac{pr}{2t} = (0.2556705913 + 2.061793098) \times 10^6$$

$$\frac{p(248 \times 10^{-3})}{2(2 \times 10^{-3})} = 2317463.689$$

$$p = 37378.4466 \text{ Pa}$$
$$\approx 0.03738 \text{ MPa}$$

# M201 Exam 99/00 Sem 2

For element A,

$$\sigma_{vert} = 0$$

$$\sigma_{horiz} = \frac{p_r}{t}$$

$$= \frac{0.0373784466 \times 10^6 \times 248 \times 10^{-3}}{2 \times 10^{-3}}$$

$$= 4.634927378 \text{ MPa}$$

$$\approx 4.635 \text{ MPa}$$

For element B,

$$\sigma_{horiz} = \sigma_{horiz} \text{ of element A}$$

$$\approx 4.635 \text{ MPa}$$

$$\sigma_{vert} = \frac{p_r}{2t} + \sigma_b - \sigma_{axial}$$

$$= \frac{0.0373784466 \times 10^6 \times 248 \times 10^{-3}}{2(2 \times 10^{-3})}$$

$$+ 2.061793098 \times 10^6 - 0.2556705913 \times 10^6$$

$$= 4.123586196 \text{ MPa}$$

$$\approx 4.124 \text{ MPa}$$

MP2001 Sem 1 05/06

$$2a) \epsilon_x = \frac{\sigma_x}{E} - \nu \frac{\sigma_y}{E}$$

$$3 \times 10^{-5} = \frac{\sigma_x}{200 \times 10^9} - 0.3 \frac{\frac{1 \times 10^6 \times 200 \times 10^{-3}}{2 \times 10^{-3}}}{200 \times 10^9}$$

$$\sigma_x = 36 \text{ MPa}$$

$$b) \sigma_x = \sigma_2 - \sigma_F$$

$$\sigma_x = \sigma_2 - \sigma_F$$

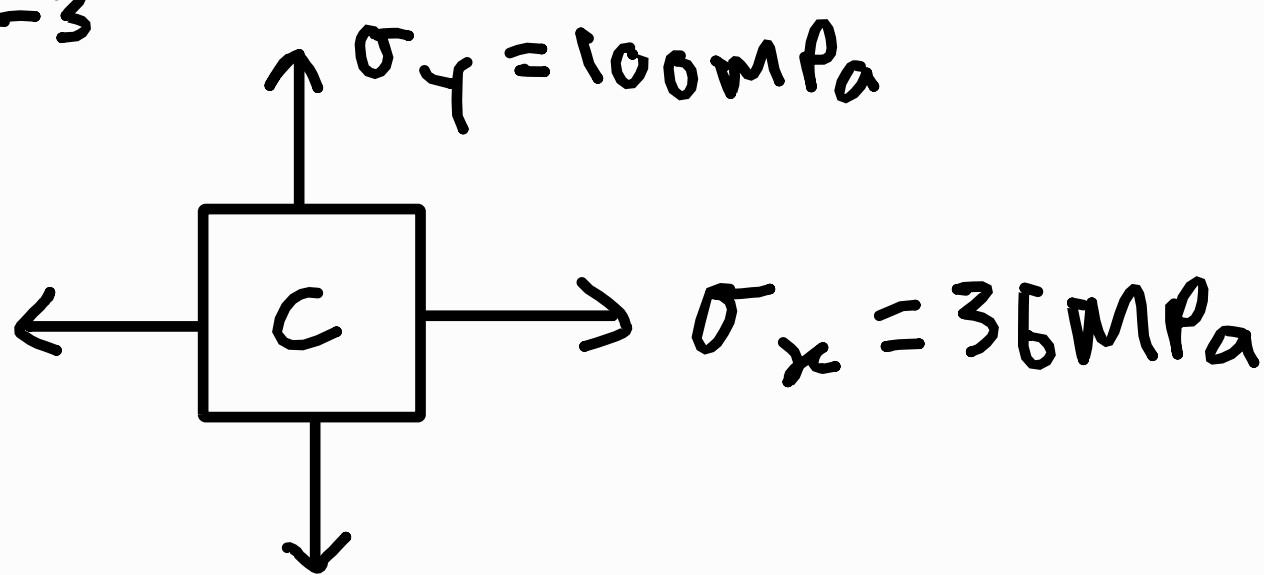
$$36 \times 10^6 = \frac{1 \times 10^6 \times 200 \times 10^{-3}}{2 \times 2 \times 10^{-3}} - \frac{F}{\pi (202^2 - 200^2) \times 10^{-6}}$$

$$14 \times 10^6 = \frac{F}{804\pi \times 10^{-6}}$$

$$F = 35361.7669 \text{ N}$$

$$\approx 35361.8 \text{ N}$$

$$c) \sigma_y = \frac{1 \times 10^6 \times 200 \times 10^{-3}}{2 \times 10^{-3}} = 100 \text{ MPa}$$



MP 2001 Sem 1 05/06

$$2d) \sigma_{\min} = \frac{\sigma_x + \sigma_y}{2} - \sqrt{\left(\frac{\sigma_x - \sigma_y}{2}\right)^2 + \tau_{xy}^2}$$

$$0 = \frac{36 + 100}{2} - \sqrt{\left(\frac{36 - 100}{2}\right)^2 + \tau_{xy}^2}$$

$$68^2 = 1024 + \tau_{xy}^2$$

$$\tau_{xy} = 60 \text{ MPa}$$

$$\tau_{xy} = \frac{T_c}{J}$$

$$60 \times 10^6 = \frac{T(202 \times 10^{-3})}{\frac{1}{2} \pi (202^4 - 200^4) \times 10^{-12}}$$

$$T = 30311.58642 \text{ N}$$

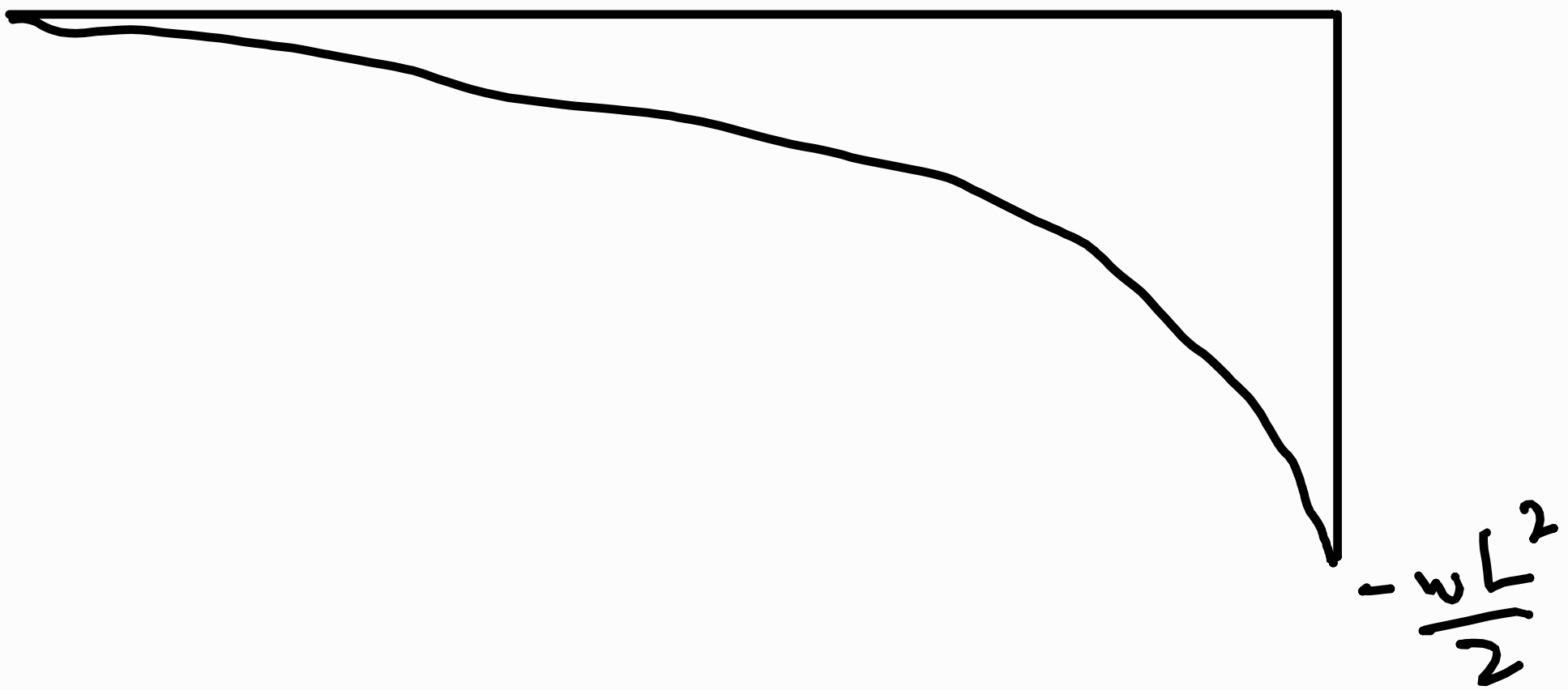
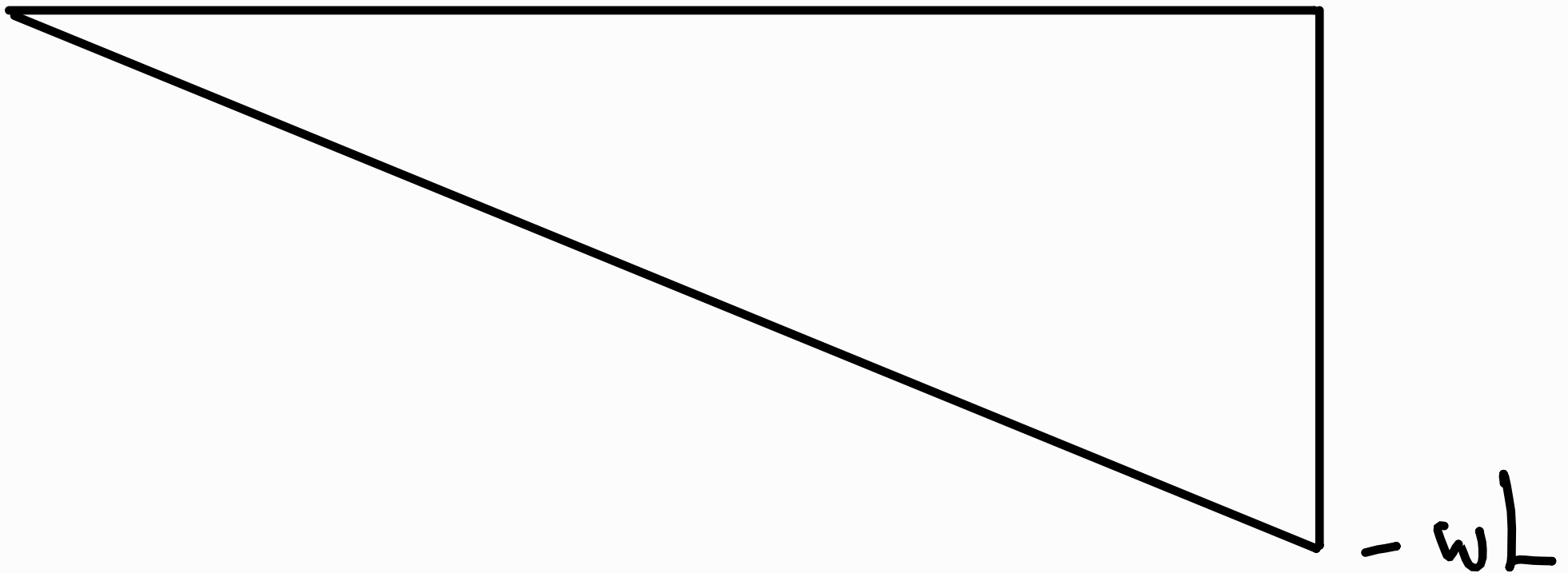
$$e) \tan^{-1} 2\theta_p = \frac{2\tau_{xy}}{\sigma_x - \sigma_y}$$

$$\tan^{-1} 2\theta_p = \frac{2(60)}{36 - 100}$$

$$\theta_p = -30.96375653^\circ, 59.03624347^\circ$$
$$\approx -30.96^\circ, 59.03^\circ$$

G 262 Sem 2 02/03

2a)



$$b) \sigma_b = \frac{-M_y}{I}$$

$$= \frac{-0.3 \times 0.8 \times 1000 \times 0.4 \times 50 \times 10^{-3}}{2 \times 10^5 \times 10^{-12}}$$

$$= -24 \text{ MPa}$$



G262 Sem 2 02/03

$$2c) I = \frac{1}{4} \pi \left[ \left( \frac{d_o}{2} \right)^4 - \left( \frac{d_i}{2} \right)^4 \right]$$

$$2 \times 10^5 \times 10^{-12} = \frac{\pi}{64} (d_o^4 - d_i^4)$$

$$2 \times 10^{-7} = \frac{\pi}{64} (100^4 - d_i^4) \times 10^{-12}$$

$$\frac{12.8 \times 10^6}{\pi} = 100^4 - d_i^4$$

$$d_i = 98.96546486$$
$$\approx 98.97 \text{ mm}$$

$$2d) \sigma_1 = 24 \text{ MPa}$$

$$\frac{p r}{2 t} = 24 \times 10^6$$

$$\frac{p (98.97 \times 10^{-3})}{2 (100 - 98.97) \times 10^{-3}} = 24 \times 10^6$$

$$p = 0.5017678338 \text{ MPa}$$
$$\approx 0.5 \text{ MPa}$$

G262 Sem 2 02/03

$$2e) \sigma_8 = \sigma_1 + \sigma_2$$

$$= 24 \times 10^6 + 24 \times 10^6$$

$$= 48 \text{ MPa}$$