

$$1) F_R = \rho g h_c A$$

$$= \rho g \frac{L \sin \theta}{2} L w$$

$$= 1000 \times 9.81 \left( \frac{3^2 \sin 30^\circ}{2} \right) (2)$$

$$= 44145 \text{ N}$$

$$Y_R = \frac{I_{xc}}{Y_c A} + y_c$$

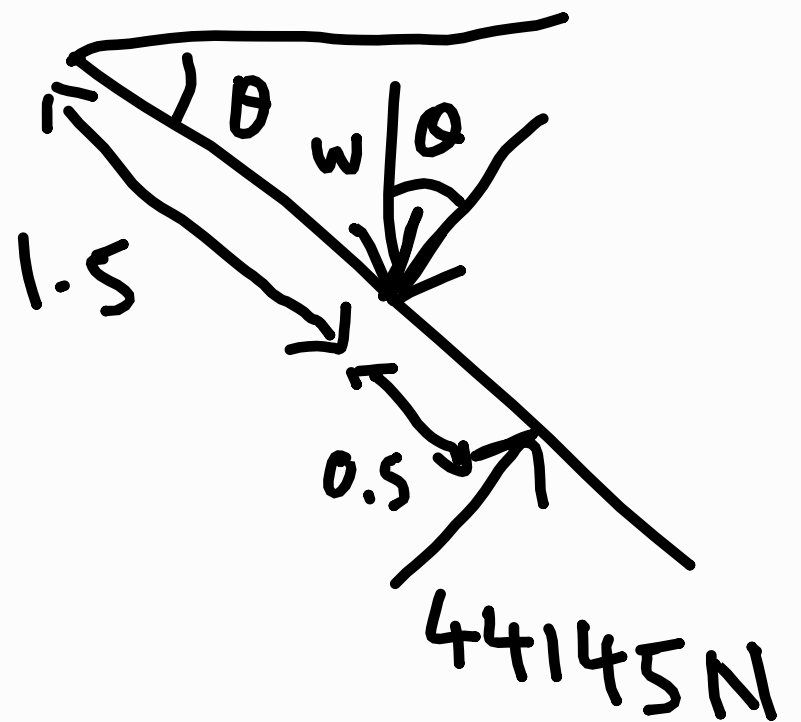
$$= \frac{\frac{1}{12} (2) (3)^3}{1.5 (3) (2)} + 1.5$$

$$= 2 \text{ m}$$

$$W \cos 30^\circ (1.5) = 2 \times 44145$$

$$W = 67965.67369 \text{ N}$$

$$\approx 68 \text{ kN}$$



2) For the square part:

$$h_c = \frac{6}{2} = 3 \text{ m}$$

$$F_R = \rho g h_c A$$

$$= 1000 \times 9.81 (3) (6^2)$$

$$= 1059480 \text{ N}$$

$$\bar{y}_R = \frac{I_{xc}}{y_c A} + y_c$$

$$= \frac{\frac{1}{12} (6)^4}{3 (6)^2} + 3 = 4 \text{ m}$$

For the semicircular part:

$$\bar{y} = \frac{4r}{3\pi} = \frac{4 \times 3}{3\pi} = \frac{4}{\pi}$$

$$h_c = 6 + \frac{4}{\pi}$$

$$F_R = \rho g h_c A$$

$$= 1000 \times 9.81 \times \left(6 + \frac{4}{\pi}\right) \times \frac{1}{2} \pi (3^2)$$

$$= 1008693.646 \text{ N}$$

$$y_R = \frac{I_{xc}}{y_c A} + y_c$$

$$= \frac{0.1098 \times 3^4}{\left(6 + \frac{4}{\pi}\right) \frac{1}{2} \pi (3)^2} + 6 + \frac{4}{\pi}$$

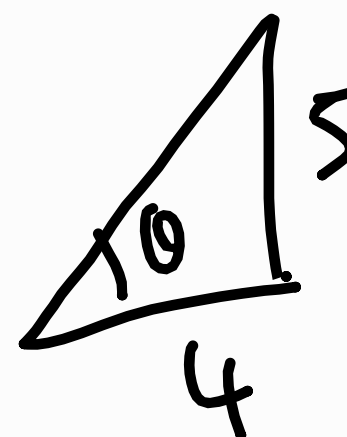
$$= 7.359735755 \text{ m}$$

$$\begin{aligned} \text{Net moment} &= 1059480(6-4) - \\ &\quad (7.359735755 - 6) \times 1008693.646 \\ &= 747403.1832 \\ &\approx 750 \text{ kNm} \end{aligned}$$

3) Calculating the force on a unit width:

$$F_R = \rho g h_c A$$
$$= 1000 \times 9.81 \times \frac{4}{2}$$
$$\times \frac{4}{\sin(\tan^{-1}(\frac{5}{4}))}$$

$$= 100503.438 \text{ N}$$


$$\theta = \tan^{-1}\left(\frac{5}{4}\right)$$
$$= 51.34019175^\circ$$

$$F_{R_n} = 100503.438 \cos(90 - \tan^{-1}(\frac{5}{4}))$$

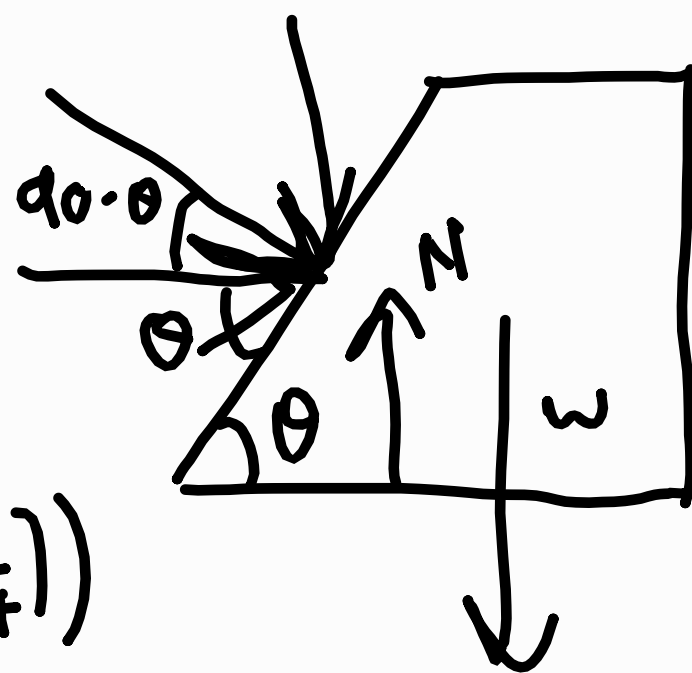
$$= 78480 \text{ N}$$

$$\approx 78.5 \text{ kN}$$

$$F_{R_y} = 100503.438 \sin(90 - \tan^{-1}(\frac{5}{4}))$$

$$= 62784 \text{ N}$$

$$\approx 62.8 \text{ kN}$$



$$N = F_{R_y} + W$$

$$= 62784 + 23.6 \times 10^3 (1) \left( \left( \frac{6+2}{2} \right) (5) \right)$$

$$= 534784 \text{ N}$$

$$3) \mu_s N = F_{Rx}$$

$$\mu_s (534784) = 78480$$

$$\mu_s = 0.1467508377$$

$$\approx 0.147$$