

i) Yes, 100% duty cycle can be achieved.

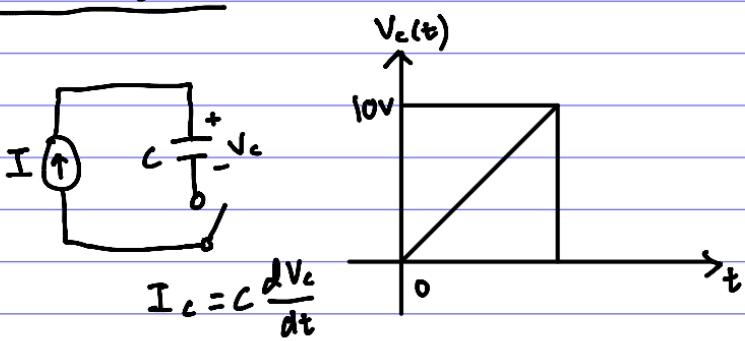
$$\text{ii) } P_{\max} = \frac{V_{\max}^2}{R_{LD}}$$
$$= \frac{100^2}{10}$$
$$= 1000\text{W}$$
$$= 1\text{kW}$$

$$\text{iii) } \frac{V_C}{V_{\max}} = \frac{4}{10} = 0.4$$

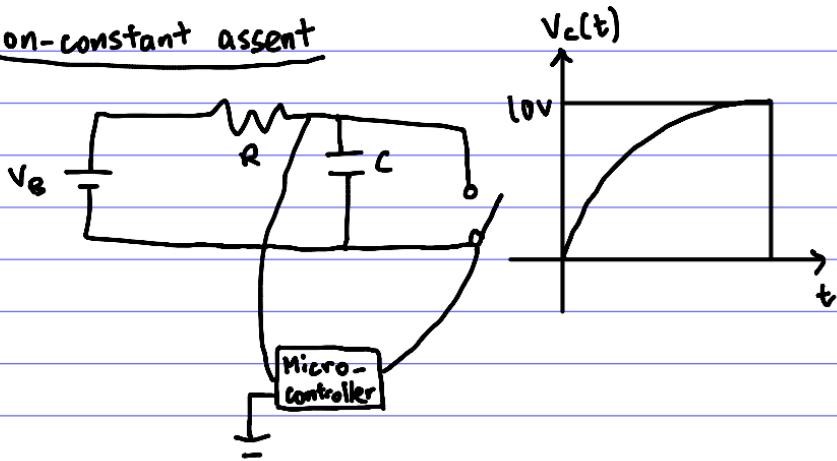
$$P_{40\%} = 40\% P_{\max}$$
$$= 0.4 (1 \times 10^3)$$
$$= 400\text{W}$$

iv) The control voltage should be doubled to double the power into the load.

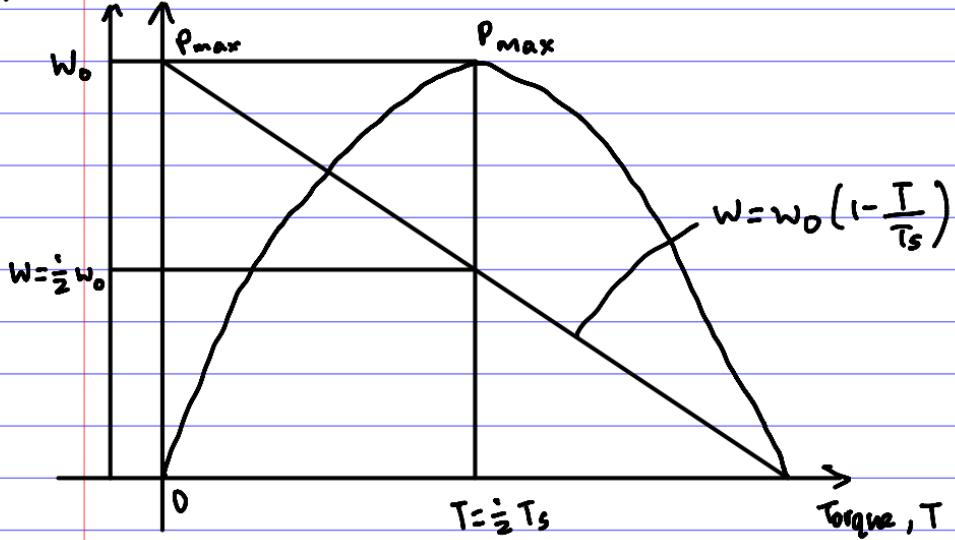
### 1v) Constant ascent



### Non-constant ascent



2) Speed, w Power, P



$T=0$

No load condition

$$P_{out} = w T$$

When  $T=0, w=w_0$

When  $T=T_s, w=0$

$$i) P_{out} = w_0 \left(1 - \frac{T}{T_s}\right) T$$

$$P_{max} = \frac{1}{2} w_0 \left(1 - \frac{\frac{1}{2}T_s}{T_s}\right) T_s$$

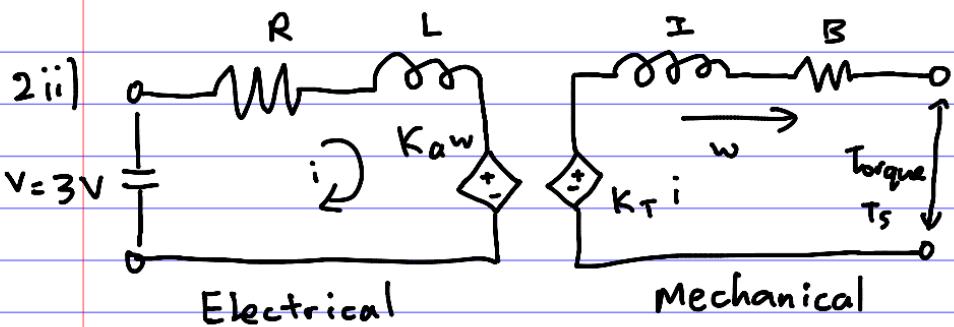
$$= \frac{1}{2} w_0 \left(\frac{1}{2}\right) T_s$$

$$= \frac{1}{4} w_0 T_s$$

$$= \frac{1}{4} \left(2\pi \left(\frac{18108}{60}\right)\right) (0.7)$$

$$= 331.846432 \text{ mW}$$

$$\approx 332 \text{ mW}$$



Assuming the stall condition,  $\omega=0$ ,

$$R = \frac{V_0}{i}$$

$$= \frac{3V}{4.22mA}$$

$$= 7.109004739\Omega$$

$$\approx 7.11\Omega$$

iii) Assuming the stall condition,  $\omega=0$ ,

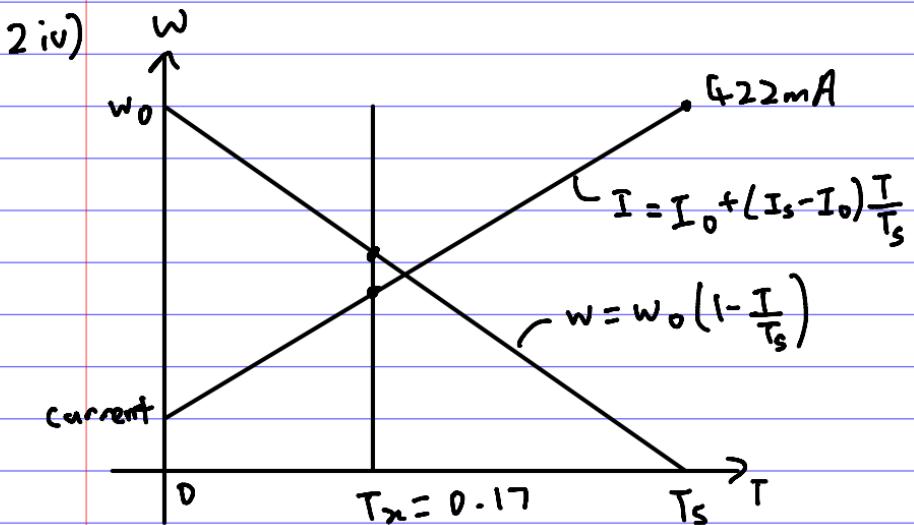
$$K_T i = T_S$$

$$K_T = \frac{T_S}{I_S}$$

$$= \frac{0.7}{4.22}$$

$$= \frac{7}{42.2}$$

$$\approx 1.66 \text{ mNm/A}$$



$$\text{Efficiency} = \frac{P_{\text{out}}}{P_{\text{in}}} \\ = \frac{w^T}{VI}$$

When  $T_x = 0.17$

$$w = \frac{2\pi}{60} (18108) \left(1 - \frac{0.17}{0.7}\right)$$

$$= 1435.743747$$

$$\approx 1436$$

$$I = 46 + (422 - 46) \left(\frac{0.17}{0.7}\right)$$

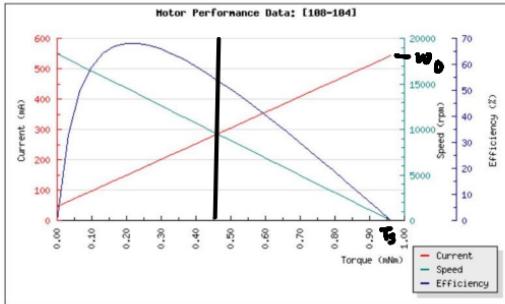
$$= \frac{4806}{35}$$

$$\therefore \text{Efficiency} = \frac{1436(0.17)}{3 \left(\frac{4806}{35}\right)}$$

$$= 0.5925007139$$

$$\approx 59\%$$

3)



$$T = \frac{1}{2} T_s$$

$$F = mg$$

$$= \frac{1}{2} mg \text{ per wheel}$$

$$T = r F$$

$$= r \left( \frac{1}{2} mg \right) \sin\theta$$

~~$$\frac{1}{2} T_s = \frac{1}{2} mg r \sin\theta$$~~

$$T_s = mgr \sin\theta$$

$$0.92 = 20(9.81) r \sin 30^\circ$$

$$r = 9.378185525 \times 10^{-3} \text{ m}$$

$$\approx 9.4 \text{ mm}$$

$$v = wr$$

$$= \frac{1}{2} \omega_0 r$$

$$= \frac{1}{2} \left( \frac{2\pi}{60} \times 18000 \right) (9.4)$$

$$= 8.859291283 \text{ ms}^{-1}$$

$$\approx 8.86 \text{ ms}^{-1}$$