Stat 134 18631

Gamma and Beth densities

For 170, we define the gamma function

For ros integer $\Gamma(\iota) = (\iota - \iota) \iota$

This fundion allows us

to generalize the gamma darkty for

r>o (not necessarily integers)

 $\times \sim gamma(r, \lambda)$ r>0, λ >0

$$f^{(k)} = \frac{L(i)}{\gamma_{i}} \times_{i-1} \epsilon_{jk}$$

lets check this integrates to 1.

$$\int_{\infty}^{0} t^{K}(x) = \frac{L(i)}{i} \int_{\infty}^{0} \int_{\infty}^{1} \frac{1}{(1-i)^{-1}} \int_{x}^{0} \frac{1}{(1-i)^{-1}} \int_{x}^{x} \frac{1}{(1-i)^{-1}} \int_{x$$

set t=>x = ====

Recall beta (1,5) has variable part $X^{r-1}(1-X)^{s-1}$ ocx 1 w constant (r+s-1)! (5-1)1 (5-1)1 Mese are we can generalité beta(rs) so rs >0 (not nec integers) For 1>0, 570 (not nec Integers) ar detilne X ~ beta (r.s) to have density \[
\begin{align*}

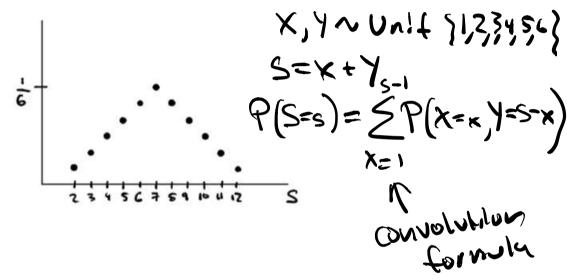
 $\int_{\Gamma} f(x) f'(s)$ We need $\int_{\Gamma} f(x) dx = \int_{\Gamma} f(x) f'(s)$ $\int_{\Gamma} f(x) dx = \int_{\Gamma} f(x) f'(s)$

in sec 5.4 that seems completely unrelated,

Sec 5.4 Sums of independent random variables.

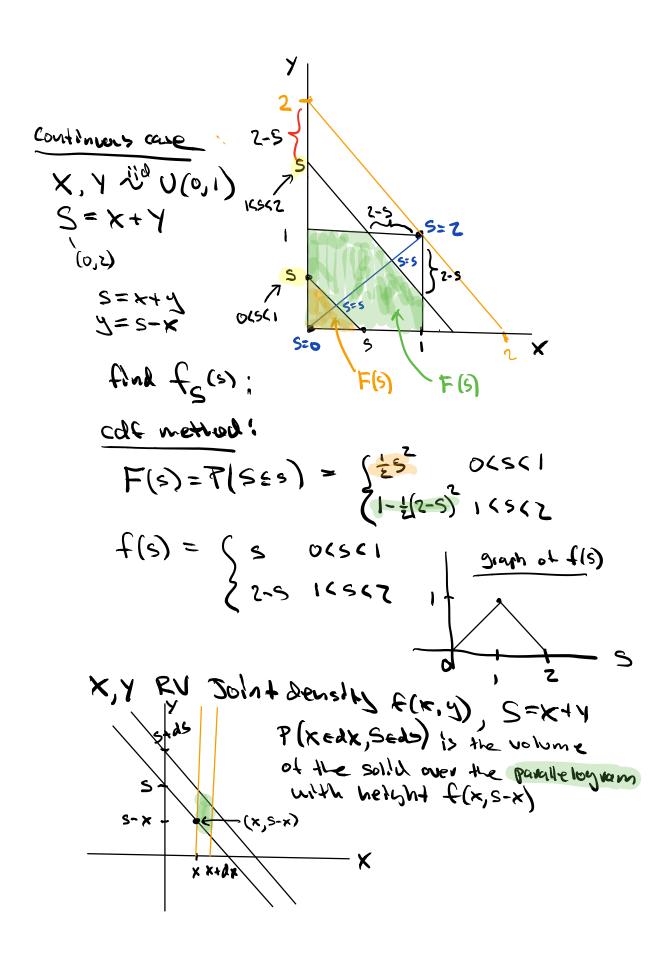
Stat 134 Friday April 6 2018

1. Let S be the sum of the roll of two fair die. The distribution of S is given below:



atrue **b** false

$$P(S=3) = \sum_{x=1}^{2} P(x=x, y=3-x)$$
 $= P(x=1, y=2) + P(x=2) + P($



SO P(KEdn, SEds) = f(x, s-x)dxds

to find the marginal density we integrate cut x:

$$f(s) = \begin{cases} f(x,s+x) = x \\ f(x) = x \\ f(x) = x \end{cases}$$

indep

Convolution

$$f_{S}(s) = \int_{0}^{s} f_{x}(x) f_{y}(s-x)dx$$

$$= \int_{0}^{s} \frac{1}{\lambda} e^{-\lambda x} dx = \int_{0}^{s} \frac{1}{\lambda} e^{-\lambda x} dx$$

$$= \int_{0}^{s} \frac{1}{\lambda} e^{-\lambda x} dx = \int_{0}^{s} \frac$$

vartable Port ot gamma (2,1)

 \Rightarrow S \wedge gamma (z, λ),

Next thre we will probe that \(\frac{1}{\times \frac{1}{\times}} \frac{1}{\times \frac{1}{\times \frac{1}{\times}}} = \frac{\frac{1}{\times \frac{1}{\times}}}{\triangle \frac{1}{\times}}.