

Chapter 4 Review Session

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Some Things to Remember

Given a Poisson Process with rate λ :

- a. $P(\text{arrival in interval } \delta t) =$
- b. The distribution of the waiting time between any 2 consecutive arrivals is:
- c. The distribution of T_r , the waiting time until the r th arrival is:
- d. The number of arrivals in an interval of length t is:
- e. The CDF of the waiting time until the r th arrival is:

Problem 1

Consider two independent Poisson processes with rates λ_1 and λ_2 . Those processes measure the number of customers arriving in store 1 and 2.

- a. What is the probability that a customer arrives in store 1 before any arrives in store 2?
- b. What is the probability that in the first hour exactly 6 customers arrive at the two stores?
- c. Given exactly 6 have arrived at the two stores, what is the probability all 6 went to store 1?

Problem 2

Let $T \sim \exp(\lambda)$, $Y = \sqrt{T}$

- a. Find the density of Y , using the CDF of Y .
- b. Identify the distribution Y for $\lambda=1/2$

Problem 3

We will show that the minimum of exponentials is exponentially distributed, using multiple approaches. Let $Z = \min(X, Y)$, where $X, Y \sim \exp(\lambda)$

- a. Find the density of Z , using the CDF of Z
- b. Find the density of Z directly from $P(Z \in dz)$
- c. Generalize to find the distribution of the minimum of n exponentials