2/16/18 5tat 134 le 14. last time E(XY) = E(X)E(Y) it X, 1 Indep. Next, Var(x+y) = Var(x) + Var(y) if x, y indep Recall, $Var(x) = E((x-E(x))^2) = E((x-M_x)^2)$ $Va_1(x+y) = E(((x+y)-E(x+y))^2)$ $= F\left(\left(\left(x+y\right) - \left(M_x - M_v\right)\right)^2\right)$ $= E\left(\left(\left(x - w^{x}\right) - \left(\lambda - w^{\lambda}\right)\right)\right)$ FOIL $= E((x-n_x)^2 - 2(x-n_x)(y-n_y) + (y-n_y))$ $= E((x-M_*)) - 2E((x-M_*)(Y-M_Y)) + E((Y-M_Y)^2)$ /ar (y) Var (x) 2E(x-1/x)E(Y-1/y) Note $E(x-M_X) = E(x)-M_X = M_X-M_X = 0$

So [var (x+y) = var(x) + var (y) wan x, y Indep.

$$X = I_1 + \cdots + I_n$$
 som at indep Bernoull |m + n: |q| s,
 $E(X) = E(I_1) + \cdots + E(I_n) = np$

$$SD(x) = \sqrt{npq}$$

Expertation, and SD of Sample sum and average

$$X_{1}, X_{2}, \dots, X_{n}$$
 iid $E(x) = M, SD(x_{i}) = \sigma$

$$E(An) = E(\frac{Sn}{n}) = E(\frac{Sn}{n}) = In$$

$$SD(A_n) = SD(S_n) = \frac{1}{n}SD(S_n) = \frac{1}{n}TnT = \frac{\pi}{n}$$

Central Limit Theorem (CLT)

X1,..., Xn iid mean= M, SD= 0

 $S_n = \chi_1 + \dots + \chi_n$, $A_n = \frac{S_n}{n}$

Then for "large" n, the distribution of Sn and An are normal.

Plature

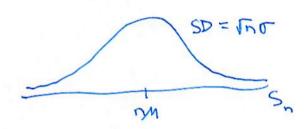
distribution

dran

n u) replacement

X1, X2, ..., Xn

Sn= X1+ xc+ ·· + Xn



SD= Th An

For CLT app: 600yle Brown CLT Seeing Theory

€ (3,3,17)

Let X be a RV VI P(x=-100)=P(x=0)=1/4, P(x=100)=1/2 Let S be sum of 25 Index RV each with.

the same dist as X.

Fund P[S=0)

values

100

- 2500 to 2500

increment of

R burs

100.

$$E(x) = -100 \cdot \frac{1}{4} + 0 \cdot \frac{1}{4} + 100 \cdot \frac{1}{2}$$

$$= 25$$

$$SD(x) = \sqrt{E(x^2) - E(x)}$$

$$E(x^2) = (-100)^2 \cdot \frac{1}{4} + 0^2 \cdot \frac{1}{4} + (100)^2 \cdot \frac{1}{2}$$

$$E(x)^2 = 25^2$$

$$E(S) = 25^{2}$$

 $SP(S) = 100 \sqrt{11}.5$

$$\frac{1}{200 \times 10^{11}} - \frac{1}{200 \times 10^{11}} = \frac{200 \times 10^{11}}{200 \times 10^{11}} = \frac{200 \times 10^{11}}{200 \times 10^{11}}$$

Finished with section 3.3.

Next Sec 3.6. See Realing Guide what to read in this section.

Understand how to find variance of a sum of non independent indicators as in next example,

Stat 134 Friday February 16 2018

1. A building has 10 floors above the basement. If 12 people get into an elevator at the basement, and each chooses a floor at random to get out, independently of the others, at how many floors do you expect the elevator to make a stop to let out one or more of these 12 people?

$$a 12(1 - (9/10)^{10})$$

b
$$10(1-(9/10)^{12})$$

c none of the above

$$E(t_i) = 1 - \left(\frac{1}{10}\right)\left(\frac{9}{10}\right)^2$$

$$X = I_1 + \cdots + I_0$$

$$E(x) = 10 \left(1 - \left(\frac{9}{10}\right)^{12}\right)$$

$$X = I_1 + \cdots + I_0$$

$$= \lim_{n \to \infty} |I_n| = \lim_{n \to$$



Find Var (x).

Var(x) + Var(II) + ... Var (II) since I; not indep.

 $E(X^{7}) = E\left(\left(\sum_{i=1}^{10} I_{i}\right)^{2}\right)$

(芝红潭)

= \(\frac{1}{5} \); \(\frac{1}{

I II = indicator stop at 1st I and 2nd flow

In = at least one person gets
of at 1st and 2nd floor

The E(IIS) = brop (no one det off 12 floor)

Prob (no one off 1st (100)) + (9)2

Prob ("" 2nd floor) + (9)2

Prob ("" 15t and 2nd floor)

(9)2

(9)2

(9)2

(10). (8)12

$$\frac{E(x^{2})}{E(x^{2})} = E\left(\underbrace{\xi}_{j=1}^{10}\right) + E\left(\underbrace{\xi}_{1\xi j + 3 \le 10}^{1\xi j}\right)$$

$$= NE(I) + 10.9E\left(I, I_{2}\right)$$

$$Vac(x) = E(x^{2}) - E(x) = 1.34$$

Next understand devivation of vaviance of hypergeonotic distribution. I normal out to details for you on the next page,