# Stat 134: Section 4

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Note: You may leave your answers in terms of  $\Phi$  or  $\Phi^{-1}$  as necessary, where  $\Phi(x)=\int_{-\infty}^x \frac{1}{\sqrt{2\pi}}e^{-z^2/2}dz$ , and  $\Phi^{-1}$  is the inverse of  $\Phi$ .

### Problem 1

Let H be the number of heads in 400 tosses of a fair coin. Find normal approximations to

- a.  $P(190 \le H \le 210)$
- b.  $P(210 \le H \le 220)$
- c. P(H = 200)
- d. P(H = 210)

Ex 2.2.1 in Pitman's Probability

#### Problem 2

A fair coin is tossed repeatedly. Consider the following two possible outcomes: (i) 55 or more heads in the first 100 tosses, or (ii) 220 or more heads in the first 400 tosses.

- a. Without calculation, say which of these outcomes is more likely. Why?
- b. Confirm your answer to (a) by calculation.

Ex 2.2.3 in Pitman's Probability

## *Problem 3: Confidence Intervals*

A pollster wishes to know the percentage p of people in a population who intend to vote for a particular candidate. How large must a random sample with replacement be in order to be at least 95% sure that the sample percentage is within one percentage point of p? Ex 2.2.13 in Pitman's Probability

How does the term  $\sqrt{p(1-p)}$  vary with *p*? When is it maximized?

## Problem 4

An airline knows that over the long run, 90% of passengers who reserve seats show up for their flight. On a particular flight with 300 seats, the airline accepts 324 reservations.

- a. Assuming that passengers show up independently of each other, what is the chance that the flight will be overbooked?
- b. Suppose that people tend to travel in groups. Would that increase or decrease the probability of overbooking? Explain your answer.
- c. Redo the calculations in part (a), assuming now that passengers always travel in pairs. Is this consistent with your answer to part (b)?

Ex 2.2.9 in Pitman's Probability