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1. Index to determine fit

The residual sum of squares (RSS) is used to determine the fit the the equation. The formula of RSS is $RSS = \sum_{i=1}^n (y_i - f(x_i))^2$, where y_i is the i^{th} value of the variable to be predicted, x_i is the i^{th} value of the explanatory variable, and $f(x_i)$ is the predicted value of y_i .¹For the same data, the smaller RSS the regression equation has , the better fit it gets.

2. Regression results

Input 1

Through my regressions I found the following equations:

- **Linear:** $2454529.3x + -62434056.7$ **RSS:** $1.653780779657326e+17$
- **Polynomial:** $3.0x^4 + 0.0x^3 + 2.9x^2 + -3.0x + 12.4$ **RSS:** 0.0
- **Exponential:** $20949.08 * e^{0.11x}$ **RSS:** $3.706194116603769e+18$
- **Logarithmic:** $55750333.26 * \ln(x) + -141266241.14$ **RSS:** $4.023690804595027e+17$

As a result, I conclude this data set is best modelled by a polynomial equation of $3.0x^4 + 0.0x^3 + 2.9x^2 + -3.0x + 12.4$

Input 2

Through my regressions I found the following equations:

- **Linear:** $1.0x + -120.14$ **RSS:** 50.66
- **Polynomial:** $0.0x^2 + 1.0x + -120.15$ **RSS:** 50.55
- **Exponential:** Cannot perform exponential regression on this data **RSS:** nil
- **Logarithmic:** $27.95 * \ln(x) + -171.36$ **RSS:** 16570.29

As a result, I conclude this data set is best modelled by a polynomial equation of $0.0x^2 + 1.0x + -120.15$

Input 3

Through my regressions I found the following equations:

- **Linear:** $2.4261830428093766e+127x + -8.163822007981575e+128$ **RSS:** $1.4471952060402615e+261$
- **Polynomial:** $8.788049620169372e+114x^{10} + -4.2052422358538933e+117x^9 + 8.569451830202117e+119x^8 + -9.701541183315148e+121x^7 + 6.675513074042082e+123x^6 + -2.8702874772585813e+125x^5 + 7.637493778397592e+126x^4 + -1.2023377497393e+128x^3 + 1.0195784688450535e+129x^2 + -3.865067625141235e+129x + 4.216998277378988e+129$ **RSS:** $3.935311600371197e+260$
- **Exponential:** $2.0 * e^{3.0x}$ **RSS:** $3.7998257678036214e+233$

¹ http://en.wikipedia.org/wiki/Residual_sum_of_squares

- **Logarithmic:** $4.63779174480991e+128 \ln(x) + -1.2781072373933265e+129$ **RSS:** $1.4779031630466608e+261$

As a result, I conclude this data set is best modelled by a exponential equation of $2.0 * e^{3.0x}$

Input 4

Through my regressions I found the following equations:

- **Linear:** $2.57x + -19.3$ **RSS:** 5.42
- **Polynomial:** $0.0x^2 + 2.57x + -19.3$ **RSS:** 5.42
- **Exponential:** Cannot perform exponential regression on this data **RSS:** nil
- **Logarithmic:** $72.09 \ln(x) + -151.51$ **RSS:** 109000.03

As a result, I conclude this data set is best modelled by a linear equation of $2.57x + -19.3$

Input 5

Through my regressions I found the following equations:

- **Linear:** $109527.14x + -2485136.33$ **RSS:** 189404567266571.53
- **Polynomial:** $12.1x^3 + -11.9x^2 + 9.2x + -19.21$ **RSS:** 0.0
- **Exponential:** Cannot perform exponential regression on this data **RSS:** nil
- **Logarithmic:** $2585634.24 \ln(x) + -6358985.6$ **RSS:** 618934634431085.4

As a result, I conclude this data set is best modelled by a polynomial equation of $12.1x^3 + -11.9x^2 + 9.2x + -19.21$

Input 6

Through my regressions I found the following equations:

- **Linear:** $0.54x + 50.63$ **RSS:** 6021.8
- **Polynomial:** $-0.01x^2 + 1.4x + 36.1$ **RSS:** 6631.39
- **Exponential:** $48.48 * e^{0.01x}$ **RSS:** 20515.6
- **Logarithmic:** $18.91 \ln(x) + 9.21$ **RSS:** 0.0

As a result, I conclude this data set is best modelled by a logarithmic equation of $18.91 \ln(x) + 9.21$

3. Problems in this project

In this projects, I met with many questions. Many of them are solved, but there are still three questions that need to be shared and to be further studied ,

- 1) When using the command line as input, I naturally remember that Java has the same function as ruby. Java takes in the "String[] args" in the "main" method. The "main" method is the function that is "executed" when run this class. But ruby does not have a "main" method in one class. How should I do if I want a ruby class is automatically run. Is there a similar "main" method in the ruby?

- 2) In my project, even though I accomplish the final results as required, I believe my quality of code needs to be improved. "Ruby" is famous for its simplicity. But some of my codes seems a little bit complicated. I think some of codes can be simplified using some good methods or some functions in ruby. As I am getting more familiar with ruby, I think this problem should and would be settled.
- 3) In the polynomial regression, the performance or to be more specific, the running speed of the polynomial regression is slow but the result is correct. I think there are 2 reasons. First is the matrix calculation is complicated for my computer. Second is that the "opt_poly_degree" and "put_opt_poly" methods call too many times the "co_poly" and "var_poly" methods. So maybe the structure and design of my code is not very perfect. I hope if any of the tutor would see this report and my code, you could give some improvement suggestions. Thank you very much!