

CHAPTER 4 HW

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4.2) Rec 709 matrix:

$$\begin{bmatrix} Y \\ C_b \\ C_r \end{bmatrix} = \begin{bmatrix} .213 & .715 & .072 \\ -.117 & -.394 & .511 \\ .511 & -.464 & .047 \end{bmatrix} \begin{bmatrix} R' \\ G' \\ B' \end{bmatrix} + \begin{bmatrix} 16 \\ 128 \\ 128 \end{bmatrix}$$

Plug & Chug for $[128 \ 128 \ 128]$, $[255 \ 255 \ 255]$, $[000 \ 000]$:
to get (using matrix calculator function in graphing calculator)

$$(RGB)_1 = [144 \ 128 \ 128]$$

$$(RGB)_2 = [271 \ 128 \ 128]$$

$$(RGB)_3 = [37 \ 116 \ 179]$$

4.4) For 4:4:4, there are 3 bytes per pixel

For 4:2:0, there are $1 + \frac{1}{2} = 1.5$ bytes per pixel

For 4:2:2, there are $1 + \frac{1}{2} + \frac{1}{2} = 2$ bytes per pixel

$$4:4:4 \text{ Total} = 1920 \times 1080 \times 60 \times 10 \times 3 \\ = 3.7325 \times 10^9 \text{ bits/sec}$$

$$4:2:0 \text{ Total} = 1920 \times 1080 \times 60 \times 10 \times 1.5 \\ = 1.8662 \times 10^9 \text{ bits/sec}$$

$$4:2:2 \text{ Total} = 1920 \times 1080 \times 60 \times 10 \times 2 \\ = 2.4883 \times 10^9 \text{ bits/sec}$$

$$4.5) \underbrace{1.3 \times 1920 \times 1080}_{\text{Luminance Section}} + \underbrace{2 \times 0.6 \times \overbrace{960 \times 540}^{\substack{\text{for } C_b, C_r \\ \frac{1}{2}(1920 \times 1080)}}}_{\text{Chrominance Section}} \\ = 3317760 \text{ bits}$$

$$4.6) \text{MAD} = \frac{1}{A} \sum_{i=0}^{N-1} \sum_{j=0}^{Y-1} |S_1[x,y] - S_2[x,y]|$$

Means do row by row subtraction

$$= \frac{1}{16} (1+1+1+1+2+2+1+2+1) = \frac{12}{16} = 0.75$$

$$4.8) \text{PSNR} = 10 \log_{10} \left(\frac{A^2 S_{\max}^2}{\sum_{x=0}^{N-1} \sum_{y=0}^{Y-1} (e[x,y]^2)} \right) = 10 \log_{10} \left(\frac{255^2}{1} \right) = 48.13 \text{ dB}$$

for x, y

$$= 10 \log_{10} \left(\frac{255^2}{9} \right) = 38.59 \text{ dB for } x_1, y_2$$