



ITP30011

Modeling Languages (PLAI Chapter 1)

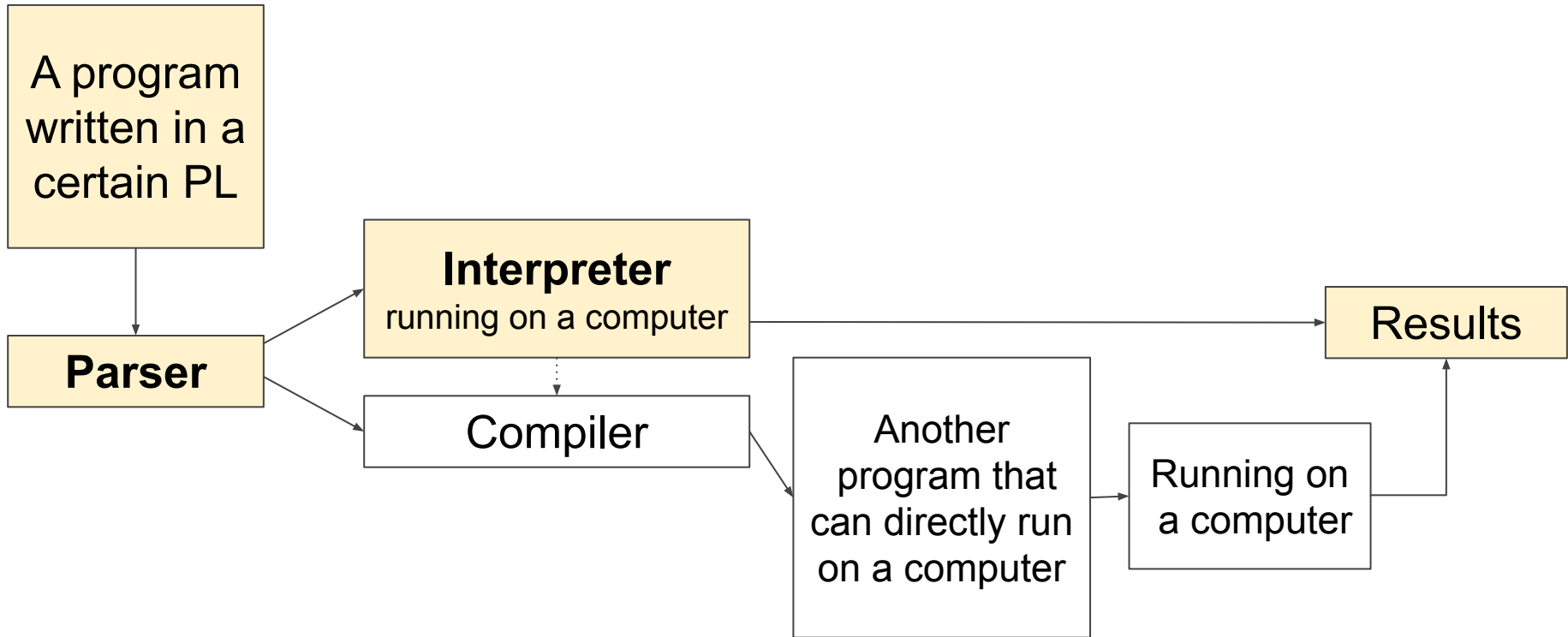
Lecture04

JC

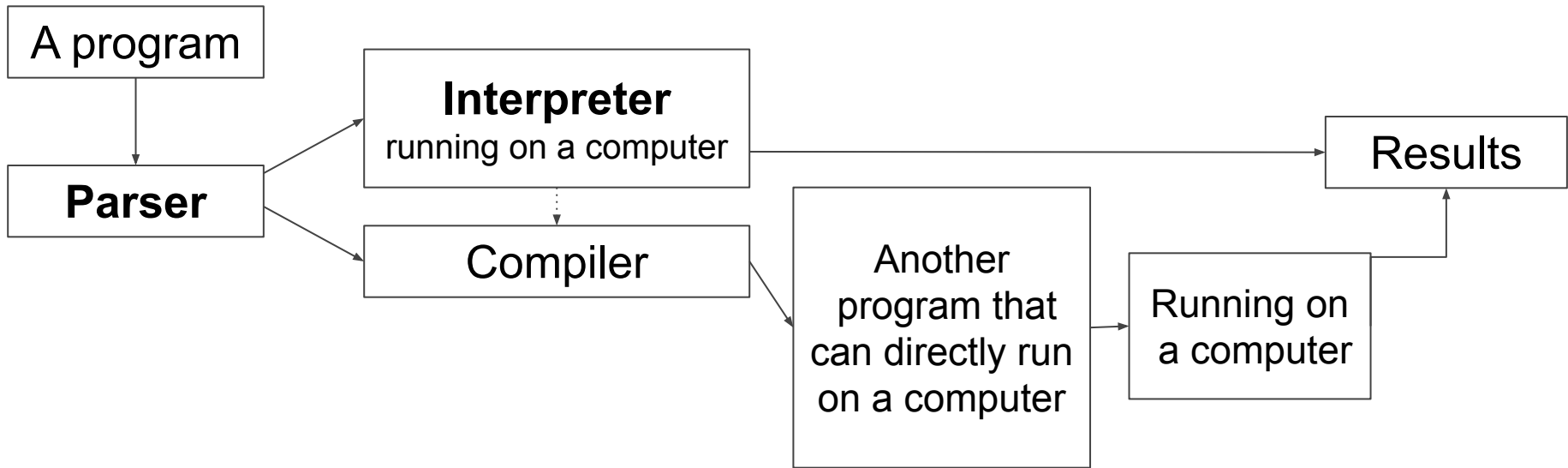


Are we learning Raket or PLT???

Big Picture



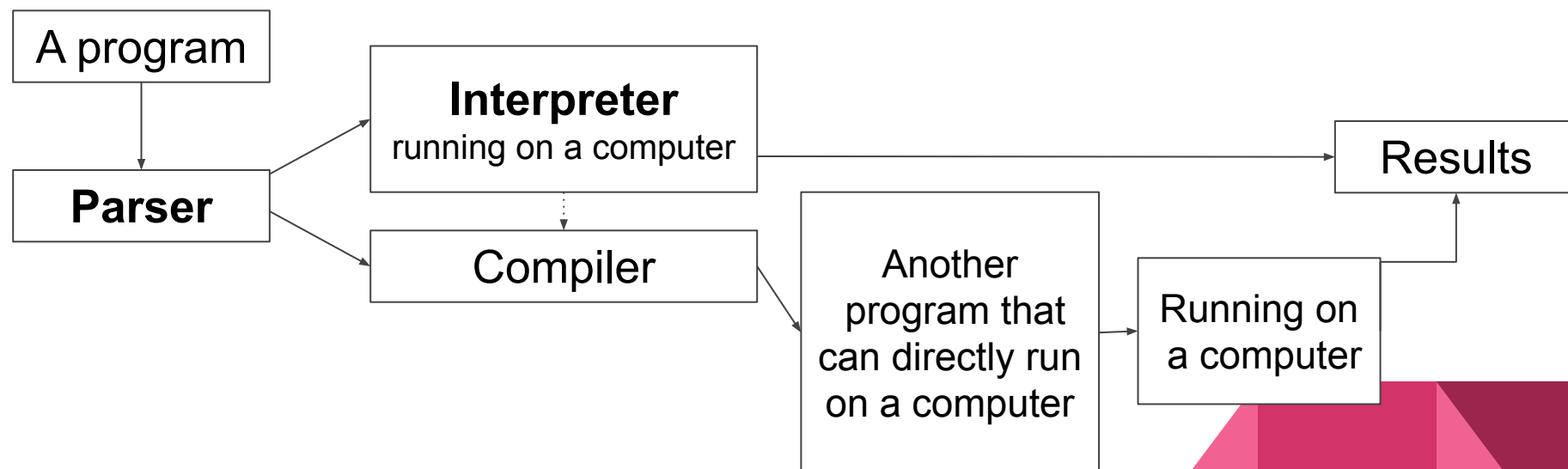
Big Picture (with a natural language example)



- An article (a set of sentences): I love you. [...]
- Parser to generate the abstract form of a sentence.
 - I (subject) love (verb) you (object).
- Interpreter (English → Korean)
 - 나는(subject) 여러분을 (object) 사랑합니다 (verb).
 - Love is (has been) growing in the writer's mind.
 - Feeling or actual behaviors from a writer.

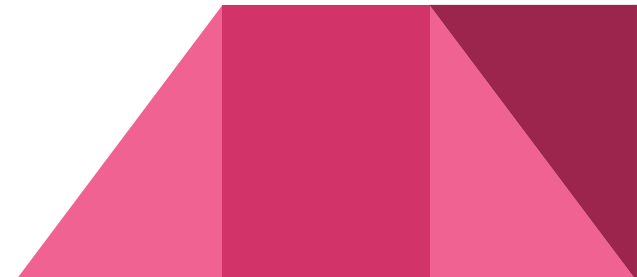
Big Picture (modeling languages)

- Just write an interpreter to explain a language.
- By writing an interpreter, we can understand the language!
- Interpreter can be converted into a compiler!!!

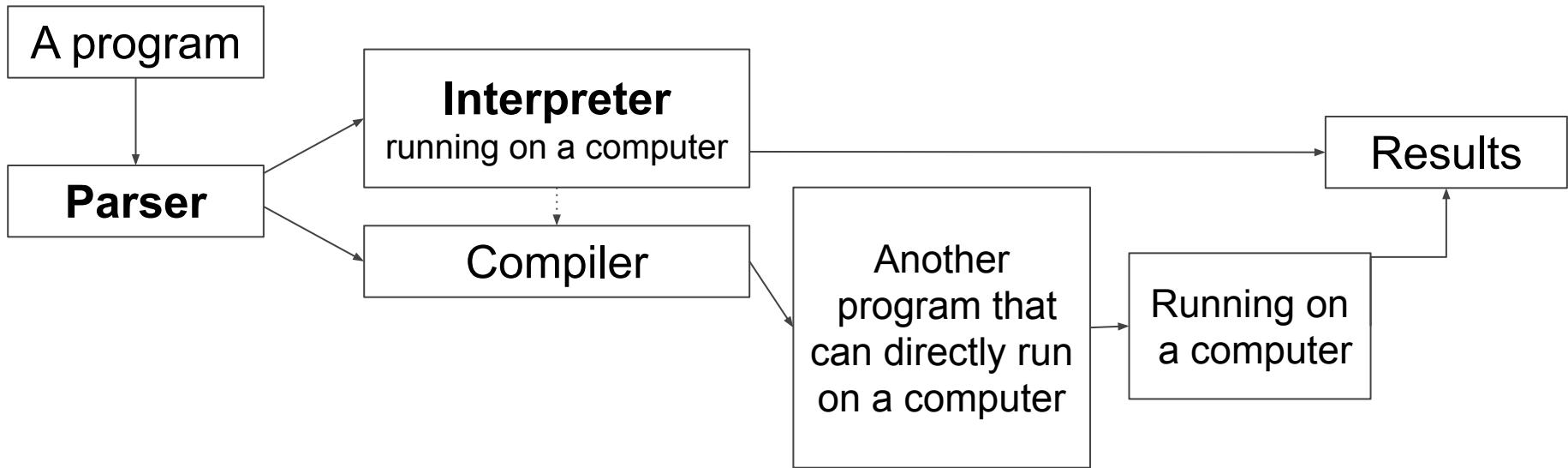


Agenda (Important PL knowledge)

- Syntax
- Semantics
- Parser
- Interpreter (we start to implement an interpreter from Lecture 5. Please, be ready!)



Big Picture (with a natural language example)



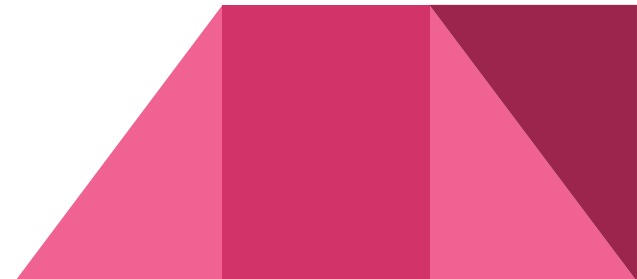
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What does PL consist of?

Programing Languages (by Krishnamurthi)

- Peculiar syntax
- Some behaviors associated with each syntax
- Numerous useful libraries
- A collection of idioms that programmers of that language use



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Which one is most significant to learn PLT?



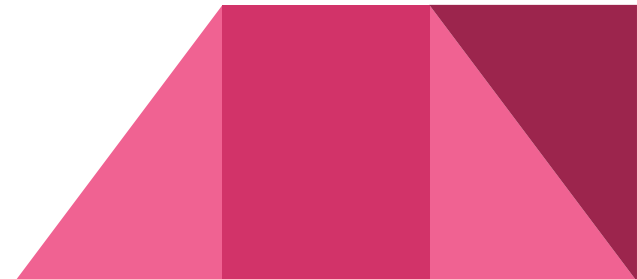
Syntax??

- Which two are most alike?
 - `a[25]` in Java
 - `(vector-ref a 25)` in Racket
 - `a[25]` in C
 - `a[25]` in ML or Haskell
- It's quite distracting to study a language.
 - So, we are going to use a uniform syntax for a new language we implement in our lectures.



The size of a language's library?

- Might be very important for developers to complete their tasks.
- Also distracting to study PL theories as the library is not the core of the language.



Idioms?

- Expressing a special feature of a recurring construct in one or more programming languages
 - See some examples: <http://wiki.c2.com/?JavaIdioms>
- Might be incomplete, dangerous,...
 - Should be careful to not read too much into it
- Developer-oriented but not language-oriented



Then, just semantics!!!

Behaviors associated with each Syntax

Behaviors associated with each Syntax
SEMANTICS!!

Modeling Semantics



The most precise languages in
terms of semantics?

Mathematics?

- Denotational semantics
(https://en.wikipedia.org/wiki/Denotational_semantics)
- Operational semantics
(https://en.wikipedia.org/wiki/Operational_semantics)
- Axiomatic semantics
(https://en.wikipedia.org/wiki/Axiomatic_semantics)

⇒ Too advanced

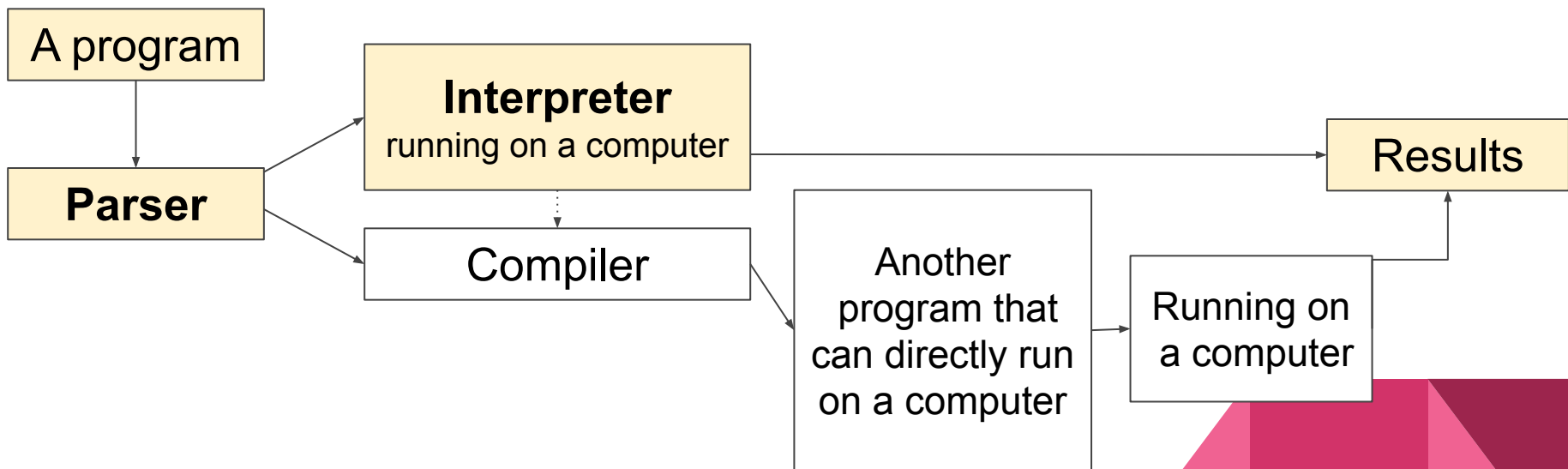


Interpreter semantics

for modeling languages
(A 'cousin' of the operational semantics)

It's simple~!

- Just write an interpreter to explain a language.
- By writing an interpreter, we can understand the language!
- Interpreter can be converted into a compiler!!!






An interpreter is a program.



An interpreter is a program.

Then, what language do we use to implement the interpreter?????



"Others have already worked out
the mathematical semantics of
the simple language."

So, we just start from here...

Modeling Syntax

(Semantics are most significant but we need syntax anyway.)

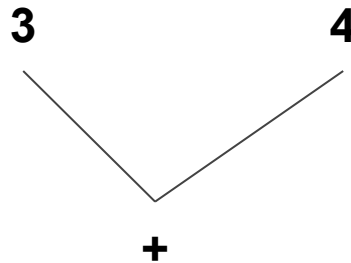
Modeling syntax

- Concrete Syntax ('expression')
 - $3 + 4$ (infix)
 - $3\ 4 +$ (postfix)
 - $(+ 3\ 4)$ (parenthesized prefix)
 - ⇒ Each of these notations is in use by at least one programming language.

Can we have a general from of these syntax??

Modeling syntax

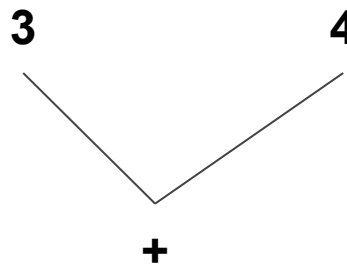
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- Abstract syntax in a tree form (essence in a tree form)



(abstract syntax tree)

Modeling syntax

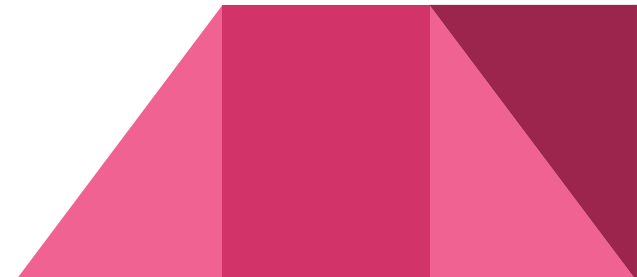
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- Abstract syntax in a tree form (essence in a tree form)



- 'Representation' with the 'right data definition' in Racket
 - `(add (num 3) (num 4))`

Modeling syntax

- Another example
 - $(3 - 4) + 7$ (infix)
 - $3\ 4 - 7 +$ (postfix)
 - $(+ (-\ 3\ 4)\ 7)$ (parenthesized prefix)
- Representation with the 'right data definition' (abstract syntax) in Racket
 - `(add (sub (num 3) (num 4))
 (num 7))`





Why do we need abstract syntax?

Modeling syntax

- Abstract syntax representation: 'one' data definition for the example above in Racket

```
(define-type AE  
  [num (n number?)]  
  [add (lhs AE?)  
        (rhs AE?)]  
  [sub (lhs AE?)  
        (rhs AE?)])
```

⇒ AE stands for "Arithmetic Expression".

Modeling syntax

- Why do we use the *lhs* and *rhs* sub-expressions of type AE rather than those of type *num*?

```
(define-type AE
  [num (n number?)]
  [add (lhs AE?)
        (rhs AE?)])
[sub (lhs AE?)
      (rhs AE?)])
```

```
(define-type AE
  [num (n number?)]
  [add (lhs num?)
        (rhs num?)])
[sub (lhs num?)
      (rhs num?)])
```

- Provide sample expressions permitted by both, and permitted by the former but rejected by the later, and argue that our choice is reasonable.

Modeling syntax

```
(define-type AE
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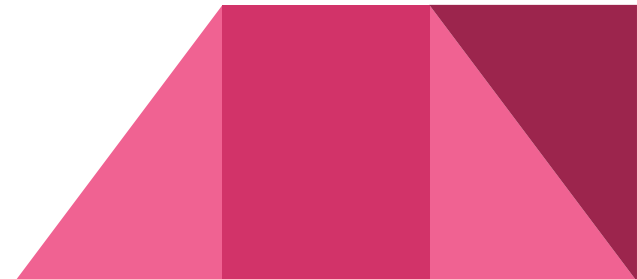
- Provide sample expressions permitted by both, and permitted by the former but rejected by the later, and argue that our choice is reasonable.

```
(add (num 1) (num 1))      (sub (num 1) (num 1))
(sub (add (num 1) (num 1)) (num 1))
```

Parser

Revisit important concepts in PLs

- Syntax
- Semantics
- Grammar
 - Backus-Naur Form



Parser

- A parser is a component in an interpreter or compiler.
 - Identifies what kinds of program code it is examining, and
 - Converts concrete syntax (what we type) into abstract syntax.
- To do this, we need a clear specification of the concrete syntax of the language!!
 - How to specify???
 - We use Backus-Naur Form (BNF)



Specify the concrete syntax of the language

- An algebraic grammar in BNF (Backus-Naur Form):

$\langle \text{expr} \rangle ::= (\langle \text{expr} \rangle + \langle \text{expr} \rangle)$
 $\quad \quad \quad | (\langle \text{expr} \rangle - \langle \text{expr} \rangle)$
 $\quad \quad \quad | \langle \text{num} \rangle$

$\langle \text{num} \rangle ::= 1, 42, 17, \dots$

- **<expr>**: Non-terminal (can rewrite it as one for the things on the right-hand side)
Meta-variable
- **::=**: "Can be written as"
- **|**: "one more choice" (a production)
- **<...>**: literal syntax
- Terminal

Specify the concrete syntax of the language (2)

- An algebraic grammar in BNF (Backus-Naur Form):

$$\begin{aligned}\langle \text{expr} \rangle &::= (\langle \text{expr} \rangle + \langle \text{expr} \rangle) \\ &\quad | (\langle \text{expr} \rangle - \langle \text{expr} \rangle) \\ &\quad | \langle \text{num} \rangle\end{aligned}$$
$$\langle \text{num} \rangle ::= 1, 42, 17, \dots$$

Each meta variable, such as $\langle \text{expr} \rangle$, defines a set

Specify the concrete syntax of the language (3)

- Using a BNF Grammar: $\langle \text{num} \rangle$

$\langle \text{num} \rangle ::= 1, 42, 17, \dots$ number

The set $\langle \text{num} \rangle$ is the set of all numbers.

To make an example $\langle \text{num} \rangle$, pick an element from it:

2 $\in \langle \text{num} \rangle$

298 $\in \langle \text{num} \rangle$

Specify the concrete syntax of the language (4)

- Using a BNF Grammar: $\langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= (\langle \text{expr} \rangle + \langle \text{expr} \rangle)$
 $| (\langle \text{expr} \rangle - \langle \text{expr} \rangle)$
 $| \langle \text{num} \rangle$

addition
subtraction
number

To make an example $\langle \text{expr} \rangle$:

- Choose one case in the grammar
- Pick an example for each meta variable
- Combine the examples with literal text

Specify the concrete syntax of the language (5)

- Using a BNF Grammar: $\langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= (\langle \text{expr} \rangle + \langle \text{expr} \rangle)$
 $| (\langle \text{expr} \rangle - \langle \text{expr} \rangle)$
 $| \langle \text{num} \rangle$

addition
subtraction
number

To make an example $\langle \text{expr} \rangle$:

- Choose one case in the grammar
- Pick an example for each meta variable
- Combine the examples with literal text

$\langle \text{num} \rangle$
 $7 \in \langle \text{num} \rangle$
 $7 \in \langle \text{num} \rangle$

Specify the concrete syntax of the language (6)

- Using a BNF Grammar: $\langle \text{expr} \rangle$

$\langle \text{expr} \rangle ::= (\langle \text{expr} \rangle + \langle \text{expr} \rangle)$	addition
$\quad \quad \quad (\langle \text{expr} \rangle - \langle \text{expr} \rangle)$	subtraction
$\quad \quad \quad \langle \text{num} \rangle$	number

To make an example $\langle \text{expr} \rangle$:

- Choose one case in the grammar $(\langle \text{expr} \rangle + \langle \text{expr} \rangle)$
- Pick an example for each meta variable $8 \in \langle \text{num} \rangle \subseteq \langle \text{expr} \rangle$
- Combine the examples with literal text $(8 + 8) \in \langle \text{expr} \rangle$

Example: A Grammar for Arithmetic Expressions

(our preliminary language that can support simple arithmetic computation.)

- Example syntax of new arithmetic expressions (AE) we want to use.

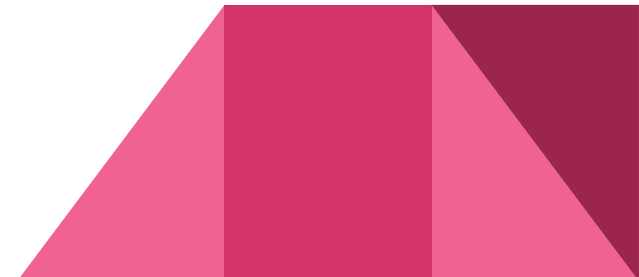
$\{+ \{- 3 4\} 7\}$

- Specify in BNF

$\langle \text{AE} \rangle ::= \langle \text{num} \rangle$

$| \{+ \langle \text{AE} \rangle \langle \text{AE} \rangle\}$

$| \{- \langle \text{AE} \rangle \langle \text{AE} \rangle\}$



Example: A Grammar for Arithmetic Expressions

- Example syntax of new arithmetic expressions (AE) we want to use.

`{+ {- 3 4 } 7}`

- Specify in BNF

`<AE> ::= <num>`

`| {+ <AE> <AE>}`

`| {- <AE> <AE>}`

- Abstract syntax representation In Racket

`(define-type AE`

`[num (n number?)]`

`[add (lhs AE?)`

`(rhs AE?)]`

`[sub (lhs AE?)`

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Example: A Grammar for Arithmetic Expressions

- Example syntax of new arithmetic expressions (AE) we want to use.

`{+ {- 3 4 } 7}`

- Specify in BNF

`<AE> ::= <num>`

`| {+ <AE> <AE>}`

`| {- <AE> <AE>}`

- Abstract syntax representation in Racket

`(define-type AE`

`[num (n number?)]`

`[add (lhs AE?)`

`(rhs AE?)]`

`[sub (lhs AE?)`

`(rhs AE?)])`

*** Example usages based on AE.**

`(define ae1 (add (sub (num 3) (num 4)) (num 7)))`

`(sub? ae1) ; Checking type`

`; retrieving expressions`

`(add-rhs ae1)`

`(sub-rhs (add-lhs ae1))`

BNF captures both **the concrete syntax** and **a default abstract syntax!**

(That is why BNF has been used in definitions of languages.
Let's see some examples...)

<https://users-cs.au.dk/amoeller/RegAut/JavaBNF.html>

<https://cs.wmich.edu/~gupta/teaching/cs4850/sum1106/The%20syntax%20of%20C%20in%20Backus-Naur%20form.htm>

<https://docs.python.org/3/reference/grammar.html>

JC

TODO

Read Chapter 2. Interpreting arithmetic

jcnam@handong.edu
<https://lifove.github.io>

* Slides are from Prof. Sukyoung Ryu's PL class in 2018 Spring
or created by JC based on the main text book.

