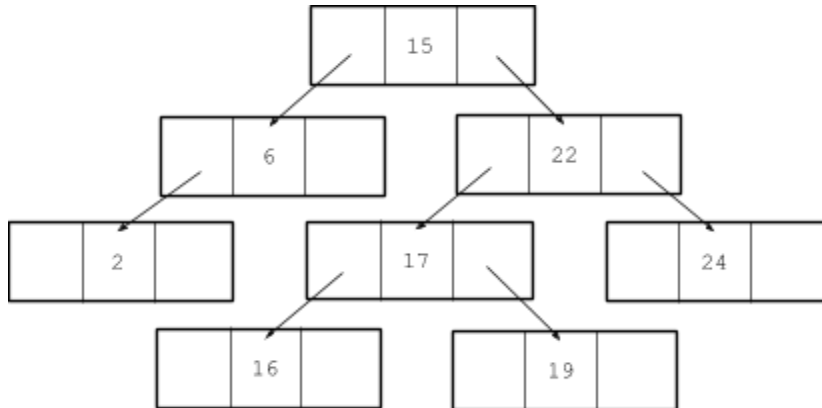


Hannah Zhang

Binary Search Tree Problems

0. Draw a picture of bst.



1. Write the function contains? which takes a binary search tree of numbers and a datum as its input and returns #t if the datum is in the tree, #f otherwise.

```
> (contains? bst 17)
```

```
#t
```

```
> (contains? bst 18)
```

```
#f
```

```
; empty tree must be false
```

```
; if the datum of a node is equal to the datum inputted → true
```

```
; if not, we keep on looking
```

```
; use previously defined abstraction functions
```

```
; this way is not logarithmic
```

```
(define (contains? bst num)
```

```
  (cond ((empty-tree? bst) #f)
```

```
        ((equal? (datum bst) num) #t)
```

```
        (else (or (contains? (left bst) num) (contains? (right bst) num))))
```

```
; logarithmically
```

```
; test left, test right, else return true
```

```
(define (contains2? bst num)
```

```
  (cond ((empty-tree? bst) #f)
```

```
        ((> num (datum bst)) (contains2? (right bst) num))
```

```
        ((< num (datum bst)) (contains2? (left bst) num))
```

```
        (else #t)))
```

(2 6 15 16 17 19 22 24)

; it is a binary search tree so everything is organized

```
; use append
```

```
; append all of the datum of the left side, the datum of the
root, and all of the datum of the right side
```

```
(define (inorder bst)
```

```
(cond ((empty-tree? bst) ' ()))
```

```
(else
```

```
(append (inorder (left bst)) (append (list (datum bst))
```

```
(inorder (right bst))))))
```

3. Write the function `count-nodes` which takes a binary tree (does not have to be a binary search tree) as its input and returns the number of nodes in the tree.

```
> (count-nodes bst)
```

8

```
; if empty, add zero and terminate
```

```
; if it is not empty then there is a node so add 1
```

```
(define (count-nodes bst)
```

```
(if (empty-tree? bst)
```

0

```
(+ 1 (count-nodes (left bst)) (count-nodes (right bst))))
```

4. Write the function `square-tree` which takes a binary tree that contains numbers as its input and returns a binary tree with the same structure and the numbers squared.

```
> (datum (left (left (right (square-tree bst)))))
```

256

```
; returns a tree
```

; the left and right stay the same but the datum is squared

```

; call recursion on left and right of the node

```

```
(define (square-tree bst)
```

```
(cond ((empty-tree? bst) ' ()))
```

```
(else (make-bintree (square (datum bst)) (square-tree
```

```
(left bst)) (square-tree (right bst))))))
```