

Hannah Zhang

## 2.19 Extra Credit

Answers in black

### 2.19

Change `cc` so that it will access its second argument differently

```
(define (cc amount coin-values)
  (cond ((= amount 0) 1)
        ((or (< amount 0) (no-more? coin-values)) 0)
        (else
         (+ (cc amount
                 (except-first-denomination coin-values))
            (cc (- amount
                    (first-denomination coin-values))
                coin-values)))))
```

; input this as `coin-values`

```
(define us-coins (list 50 25 10 5 1))
```

```
(define uk-coins (list 100 50 20 10 5 2 1 0.5))
```

Write `first-denomination`, `except-first-denomination` & `no-more?`

`First-denomination`

; finds the first value in the list of `coin-values`

```
(define (first-denomination coin-values)
  (car coin-values))
```

`Except-first-denomination`

; finds the values in the list of `coin-values` except the first

```
(define (except-first-denomination coin-values)
  (cdr coin-values))
```

`No-more?`

; if there are no more values in the list inputted, return `#t`

```
(define (no-more? coin-values)
  (if (empty? coin-values) #t #f))
```

Does the order of the list `coin-values` affect the answer produced by `cc`? Why or why not?

- No, because eventually the program will count all the combinations of coins. It does not matter which denomination it starts with first.

## Notes on how cc works

- The number of ways to generate the change of amount  $a$  using  $n$  kinds of coins is equal to
  - The number of ways to give amount  $a$  using all but the first kind of coin, plus
  - The number of ways give amount  $a - d$  using all  $n$  kinds of coins, where  $d$  is the denomination of the first kind of coin
- Example: amount = 6, coin-values are 5, 1
  - First group is not using 5
    - Using 1, we have one possible combo to make 6
  - Second group is  $6 - 5$ , using coin-values 5 and 1
    - We have 1 way to create an amount of 1
  - $1 + 1 \rightarrow 2$
- Second example: amount = 7, coin-values are 10, 5, 1
  - First group is not using 10
    - Using 5 and 1 there are 2 ways
  - Second group is  $7 - 10$  which is  $-3 \rightarrow$  less than zero so add zero
  - $2 + 0 \rightarrow 2$