

Outliers Exercise

Question

Using crime data from the file `uscrime.txt` (<http://www.statsci.org/data/general/uscrime.txt>, description at <http://www.statsci.org/data/general/uscrime.html>), test to see whether there are any outliers in the last column (number of crimes per 100,000 people). Use the `grubbs.test` function in the `outliers` package in R.

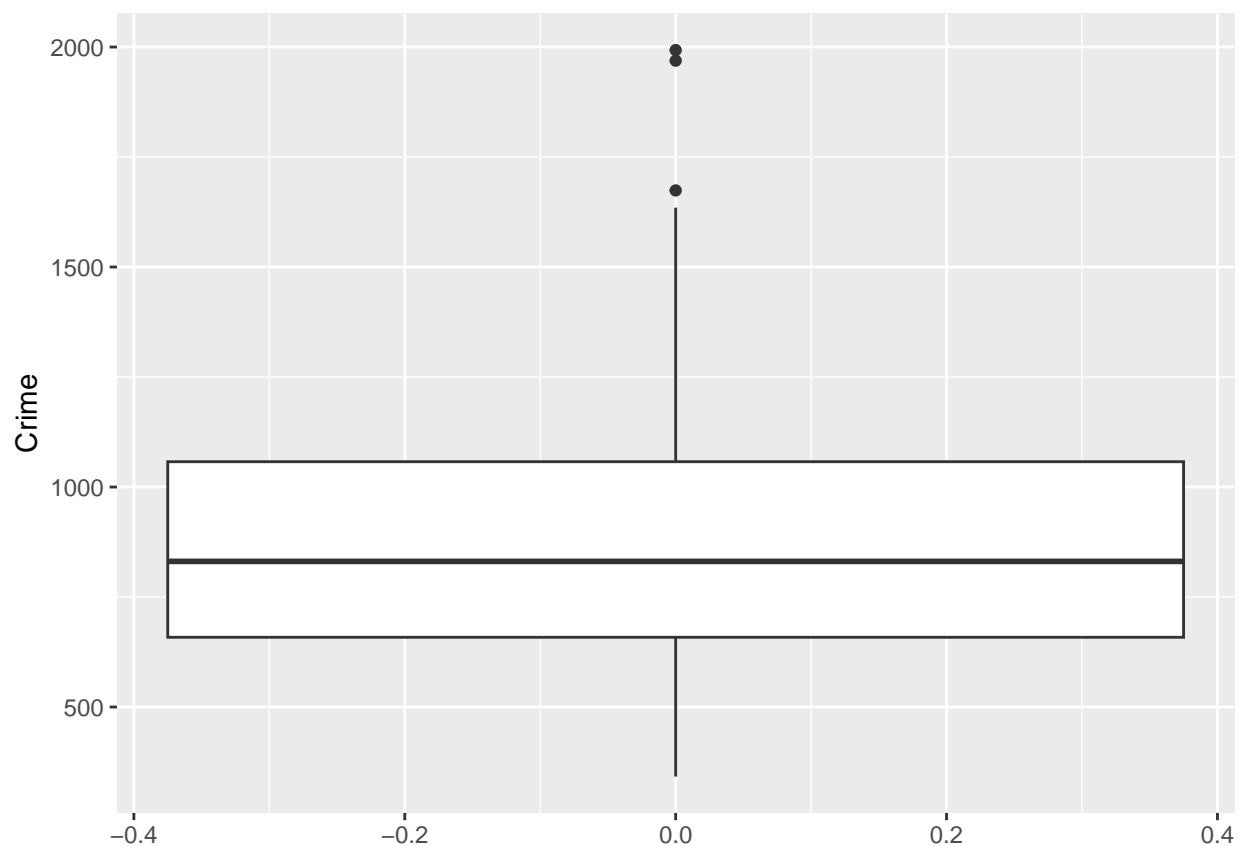
Solution

To check for outliers, the first step is to do an EDA of the data. I begin with the summary.

```
##      Min. 1st Qu.  Median    Mean 3rd Qu.    Max.
##      342.0   658.5   831.0   905.1  1057.5  1993.0
```

First inspection shows a Max that is 1,100 points higher than the Median and 900 points higher than the third quantile. This suggests there are upper outliers. The lower numbers are less extreme.

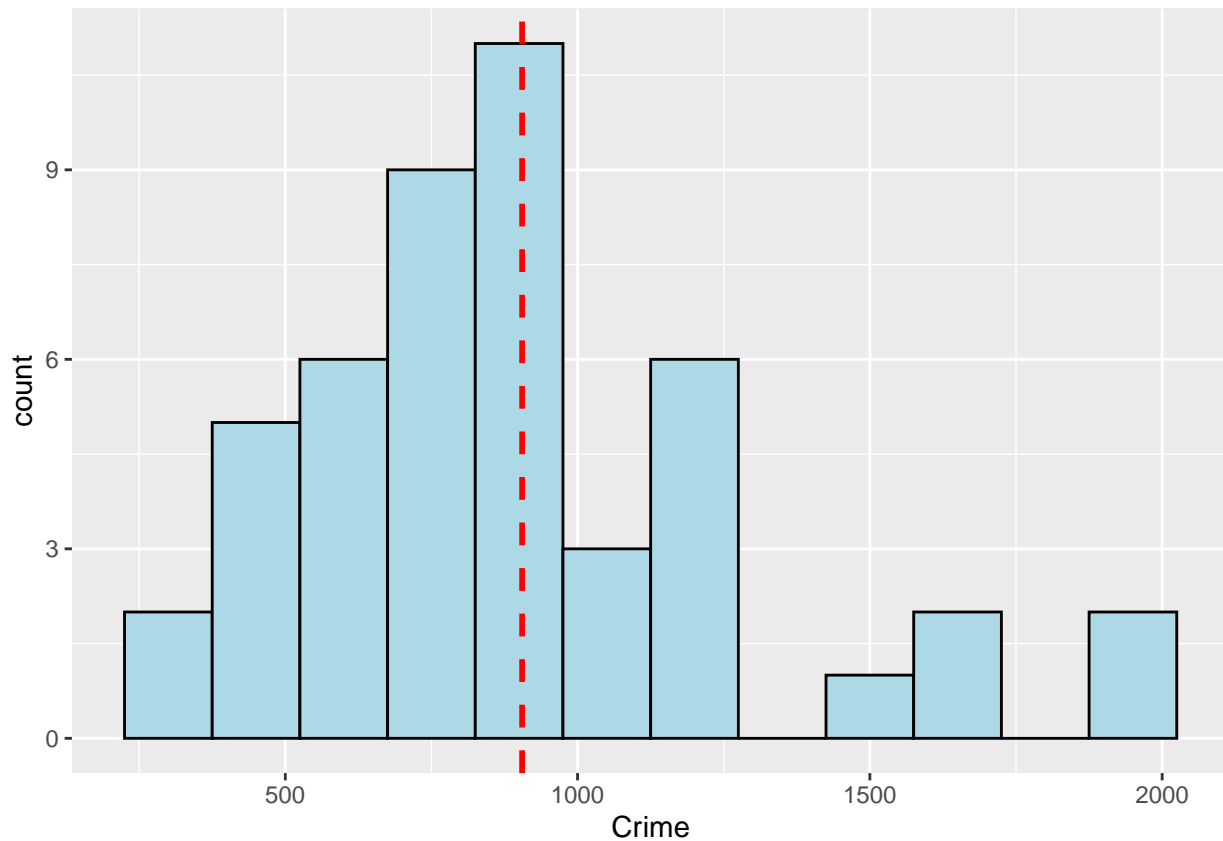
Next, I make a boxplot to inspect the data



The boxplot is similar to our summary. By visual inspection, I can posit that there are at least two upper outliers.

My last EDA is with a histogram

```
## Warning: Using 'size' aesthetic for lines was deprecated in ggplot2 3.4.0.
## i Please use 'linewidth' instead.
## This warning is displayed once every 8 hours.
## Call 'lifecycle::last_lifecycle_warnings()' to see where this warning was
## generated.
```



The histogram above plots the Crime data against count, with the red dashed line showing the mean of Crimes. Again, we can see that this histogram is right-side heavy, suggesting outliers.

Next, I will apply the grubbs test to see if these points are actually outliers, and to see if they will change the data.

```
## [1] "Grubbs Test for Highest Value:"

##
## Grubbs test for one outlier
##
## data: crimedata$Crime
## G = 2.81287, U = 0.82426, p-value = 0.07887
## alternative hypothesis: highest value 1993 is an outlier

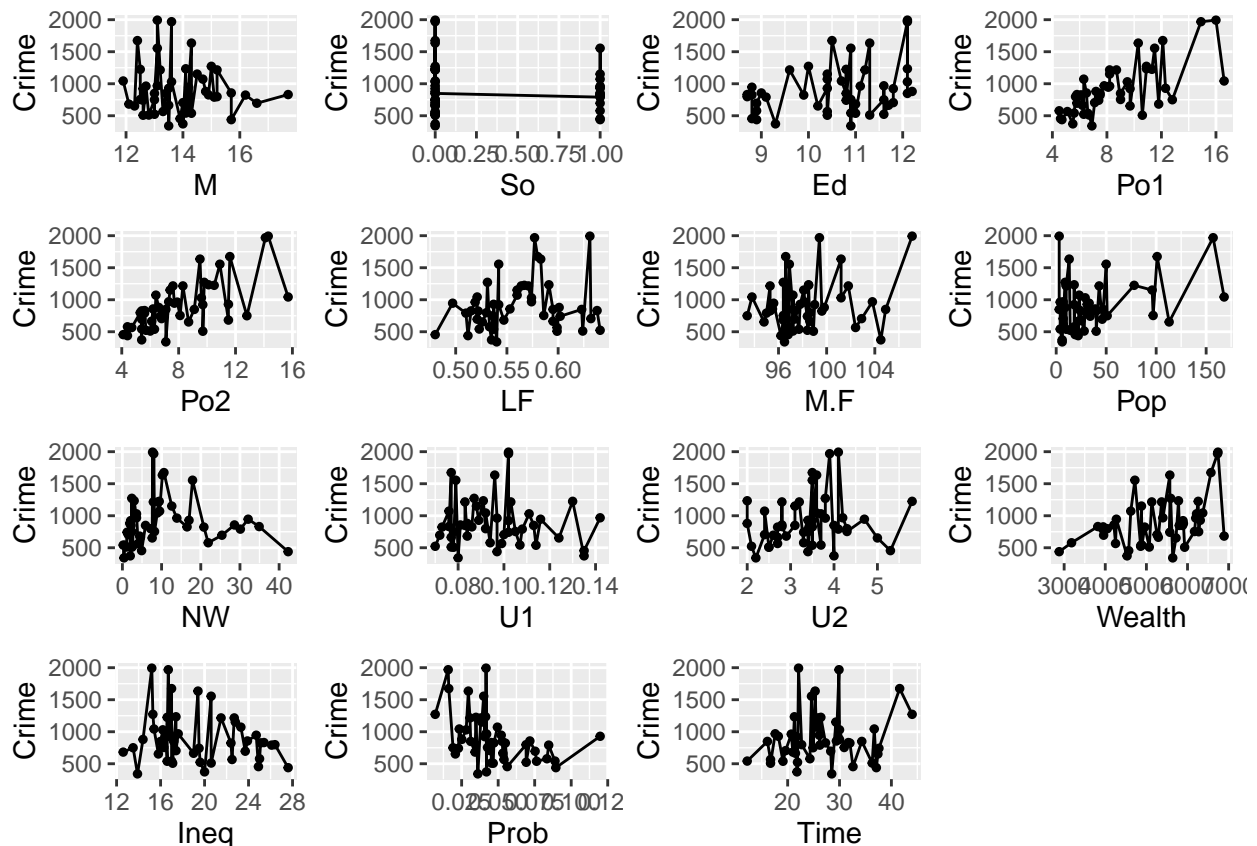
## [1] "Grubbs Test for Lowest Value"

##
## Grubbs test for one outlier
```

```
##
## data:  crimedata$Crime
## G = 1.45589, U = 0.95292, p-value = 1
## alternative hypothesis: lowest value 342 is an outlier
```

Above, I ran the Grubbs Tests to check for outliers on the highest and lowest ends. According to this test, our high point 1993 is NOT an outlier with $\alpha = 0.05$. Watching Sokol's lecture, this would make sense based on what we know about large amounts of data and the likelihood of points outside the norm.

To be certain, I wanted to plot the crime data against the other predictors, one by one.



By quick inspection, plots against Po1 and Po2 imply some sort of linearity. While not getting too deep into this, I can reject the hypothesis that an outlier exists.

CUSUM Exercise

Question

Part 1

1. Using July through October daily-high-temperature data for Atlanta for 1996 through 2015, use a CUSUM approach to identify when unofficial summer ends (i.e., when the weather starts cooling off) each year. You can get the data that you need from the file `temps.txt` or online, for example at <http://www.iweather.net.com/atlanta-weather-records> or <https://www.wunderground.com/history/airport/KFTY/2015/7/1/CustomHistory.html>. You can use R if you'd like, but it's straightforward enough that an Excel spreadsheet can easily do the job too.

Part 1 Solution

For this I used an excel spreadsheet where I could input various values of C and T into my table. I used dates July 1 - September 4 for my “summer dates.” I decided that summer would end after labor day, which is about September 4.

I wrote a function to calculate the St values using inputs C and T. The function is commented below.

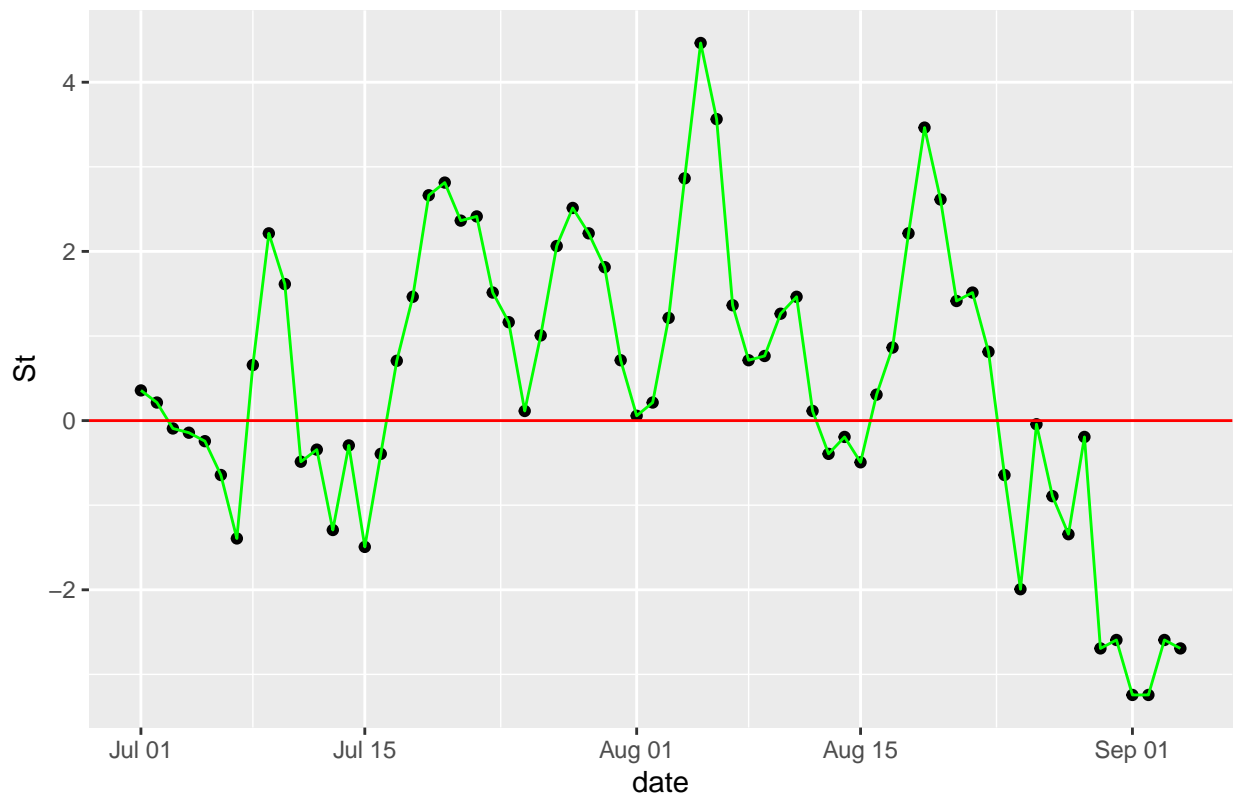
| ## | | date | mean | helper | St |
|-------|--|------------|-------|-------------|-------------|
| ## 1 | | 2023-07-01 | 88.85 | 0.35681818 | 0.35681818 |
| ## 2 | | 2023-07-02 | 88.35 | -0.14318182 | 0.21363636 |
| ## 3 | | 2023-07-03 | 88.40 | -0.09318182 | -0.09318182 |
| ## 4 | | 2023-07-04 | 88.35 | -0.14318182 | -0.14318182 |
| ## 5 | | 2023-07-05 | 88.25 | -0.24318182 | -0.24318182 |
| ## 6 | | 2023-07-06 | 87.85 | -0.64318182 | -0.64318182 |
| ## 7 | | 2023-07-07 | 87.10 | -1.39318182 | -1.39318182 |
| ## 8 | | 2023-07-08 | 89.15 | 0.65681818 | 0.65681818 |
| ## 9 | | 2023-07-09 | 90.05 | 1.55681818 | 2.21363636 |
| ## 10 | | 2023-07-10 | 88.55 | 0.05681818 | 1.61363636 |
| ## 11 | | 2023-07-11 | 87.95 | -0.54318182 | -0.48636364 |
| ## 12 | | 2023-07-12 | 88.15 | -0.34318182 | -0.34318182 |
| ## 13 | | 2023-07-13 | 87.20 | -1.29318182 | -1.29318182 |
| ## 14 | | 2023-07-14 | 88.20 | -0.29318182 | -0.29318182 |
| ## 15 | | 2023-07-15 | 87.00 | -1.49318182 | -1.49318182 |
| ## 16 | | 2023-07-16 | 88.10 | -0.39318182 | -0.39318182 |
| ## 17 | | 2023-07-17 | 89.20 | 0.70681818 | 0.70681818 |
| ## 18 | | 2023-07-18 | 89.25 | 0.75681818 | 1.46363636 |
| ## 19 | | 2023-07-19 | 90.40 | 1.90681818 | 2.66363636 |
| ## 20 | | 2023-07-20 | 89.40 | 0.90681818 | 2.81363636 |
| ## 21 | | 2023-07-21 | 89.95 | 1.45681818 | 2.36363636 |
| ## 22 | | 2023-07-22 | 89.45 | 0.95681818 | 2.41363636 |
| ## 23 | | 2023-07-23 | 89.05 | 0.55681818 | 1.51363636 |
| ## 24 | | 2023-07-24 | 89.10 | 0.60681818 | 1.16363636 |
| ## 25 | | 2023-07-25 | 88.00 | -0.49318182 | 0.11363636 |
| ## 26 | | 2023-07-26 | 89.50 | 1.00681818 | 1.00681818 |
| ## 27 | | 2023-07-27 | 89.55 | 1.05681818 | 2.06363636 |
| ## 28 | | 2023-07-28 | 89.95 | 1.45681818 | 2.51363636 |
| ## 29 | | 2023-07-29 | 89.25 | 0.75681818 | 2.21363636 |
| ## 30 | | 2023-07-30 | 89.55 | 1.05681818 | 1.81363636 |
| ## 31 | | 2023-07-31 | 88.15 | -0.34318182 | 0.71363636 |
| ## 32 | | 2023-08-01 | 88.55 | 0.05681818 | 0.05681818 |
| ## 33 | | 2023-08-02 | 88.65 | 0.15681818 | 0.21363636 |
| ## 34 | | 2023-08-03 | 89.55 | 1.05681818 | 1.21363636 |
| ## 35 | | 2023-08-04 | 90.30 | 1.80681818 | 2.86363636 |
| ## 36 | | 2023-08-05 | 91.15 | 2.65681818 | 4.46363636 |
| ## 37 | | 2023-08-06 | 89.40 | 0.90681818 | 3.56363636 |
| ## 38 | | 2023-08-07 | 88.95 | 0.45681818 | 1.36363636 |
| ## 39 | | 2023-08-08 | 88.75 | 0.25681818 | 0.71363636 |
| ## 40 | | 2023-08-09 | 89.00 | 0.50681818 | 0.76363636 |
| ## 41 | | 2023-08-10 | 89.25 | 0.75681818 | 1.26363636 |
| ## 42 | | 2023-08-11 | 89.20 | 0.70681818 | 1.46363636 |
| ## 43 | | 2023-08-12 | 87.90 | -0.59318182 | 0.11363636 |
| ## 44 | | 2023-08-13 | 88.10 | -0.39318182 | -0.39318182 |
| ## 45 | | 2023-08-14 | 88.30 | -0.19318182 | -0.19318182 |

```

## 46 2023-08-15 88.00 -0.49318182 -0.49318182
## 47 2023-08-16 88.80 0.30681818 0.30681818
## 48 2023-08-17 89.05 0.55681818 0.86363636
## 49 2023-08-18 90.15 1.65681818 2.21363636
## 50 2023-08-19 90.30 1.80681818 3.46363636
## 51 2023-08-20 89.30 0.80681818 2.61363636
## 52 2023-08-21 89.10 0.60681818 1.41363636
## 53 2023-08-22 89.40 0.90681818 1.51363636
## 54 2023-08-23 88.40 -0.09318182 0.81363636
## 55 2023-08-24 87.85 -0.64318182 -0.64318182
## 56 2023-08-25 86.50 -1.99318182 -1.99318182
## 57 2023-08-26 88.45 -0.04318182 -0.04318182
## 58 2023-08-27 87.60 -0.89318182 -0.89318182
## 59 2023-08-28 87.15 -1.34318182 -1.34318182
## 60 2023-08-29 88.30 -0.19318182 -0.19318182
## 61 2023-08-30 85.80 -2.69318182 -2.69318182
## 62 2023-08-31 85.90 -2.59318182 -2.59318182
## 63 2023-09-01 85.25 -3.24318182 -3.24318182
## 64 2023-09-02 85.25 -3.24318182 -3.24318182
## 65 2023-09-03 85.90 -2.59318182 -2.59318182
## 66 2023-09-04 85.80 -2.69318182 -2.69318182

```

C = 0 T= 0



```

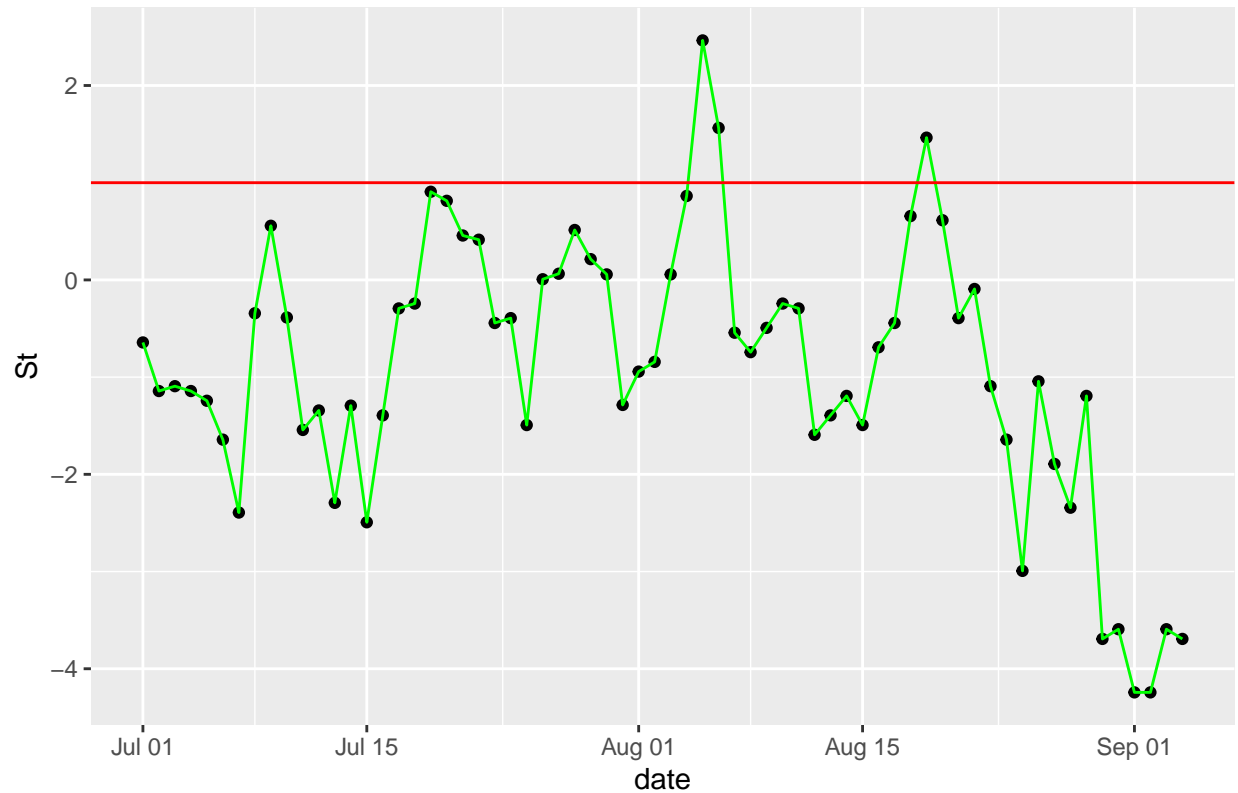
##          date  mean      helper      St
## 1  2023-07-01 88.85 -0.643181818 -0.643181818
## 2  2023-07-02 88.35 -1.143181818 -1.143181818
## 3  2023-07-03 88.40 -1.093181818 -1.093181818

```

| | | | | |
|-------|------------|-------|--------------|--------------|
| ## 4 | 2023-07-04 | 88.35 | -1.143181818 | -1.143181818 |
| ## 5 | 2023-07-05 | 88.25 | -1.243181818 | -1.243181818 |
| ## 6 | 2023-07-06 | 87.85 | -1.643181818 | -1.643181818 |
| ## 7 | 2023-07-07 | 87.10 | -2.393181818 | -2.393181818 |
| ## 8 | 2023-07-08 | 89.15 | -0.343181818 | -0.343181818 |
| ## 9 | 2023-07-09 | 90.05 | 0.556818182 | 0.556818182 |
| ## 10 | 2023-07-10 | 88.55 | -0.943181818 | -0.386363636 |
| ## 11 | 2023-07-11 | 87.95 | -1.543181818 | -1.543181818 |
| ## 12 | 2023-07-12 | 88.15 | -1.343181818 | -1.343181818 |
| ## 13 | 2023-07-13 | 87.20 | -2.293181818 | -2.293181818 |
| ## 14 | 2023-07-14 | 88.20 | -1.293181818 | -1.293181818 |
| ## 15 | 2023-07-15 | 87.00 | -2.493181818 | -2.493181818 |
| ## 16 | 2023-07-16 | 88.10 | -1.393181818 | -1.393181818 |
| ## 17 | 2023-07-17 | 89.20 | -0.293181818 | -0.293181818 |
| ## 18 | 2023-07-18 | 89.25 | -0.243181818 | -0.243181818 |
| ## 19 | 2023-07-19 | 90.40 | 0.906818182 | 0.906818182 |
| ## 20 | 2023-07-20 | 89.40 | -0.093181818 | 0.813636364 |
| ## 21 | 2023-07-21 | 89.95 | 0.456818182 | 0.456818182 |
| ## 22 | 2023-07-22 | 89.45 | -0.043181818 | 0.413636364 |
| ## 23 | 2023-07-23 | 89.05 | -0.443181818 | -0.443181818 |
| ## 24 | 2023-07-24 | 89.10 | -0.393181818 | -0.393181818 |
| ## 25 | 2023-07-25 | 88.00 | -1.493181818 | -1.493181818 |
| ## 26 | 2023-07-26 | 89.50 | 0.006818182 | 0.006818182 |
| ## 27 | 2023-07-27 | 89.55 | 0.056818182 | 0.063636364 |
| ## 28 | 2023-07-28 | 89.95 | 0.456818182 | 0.513636364 |
| ## 29 | 2023-07-29 | 89.25 | -0.243181818 | 0.213636364 |
| ## 30 | 2023-07-30 | 89.55 | 0.056818182 | 0.056818182 |
| ## 31 | 2023-07-31 | 88.15 | -1.343181818 | -1.286363636 |
| ## 32 | 2023-08-01 | 88.55 | -0.943181818 | -0.943181818 |
| ## 33 | 2023-08-02 | 88.65 | -0.843181818 | -0.843181818 |
| ## 34 | 2023-08-03 | 89.55 | 0.056818182 | 0.056818182 |
| ## 35 | 2023-08-04 | 90.30 | 0.806818182 | 0.863636364 |
| ## 36 | 2023-08-05 | 91.15 | 1.656818182 | 2.463636364 |
| ## 37 | 2023-08-06 | 89.40 | -0.093181818 | 1.563636364 |
| ## 38 | 2023-08-07 | 88.95 | -0.543181818 | -0.543181818 |
| ## 39 | 2023-08-08 | 88.75 | -0.743181818 | -0.743181818 |
| ## 40 | 2023-08-09 | 89.00 | -0.493181818 | -0.493181818 |
| ## 41 | 2023-08-10 | 89.25 | -0.243181818 | -0.243181818 |
| ## 42 | 2023-08-11 | 89.20 | -0.293181818 | -0.293181818 |
| ## 43 | 2023-08-12 | 87.90 | -1.593181818 | -1.593181818 |
| ## 44 | 2023-08-13 | 88.10 | -1.393181818 | -1.393181818 |
| ## 45 | 2023-08-14 | 88.30 | -1.193181818 | -1.193181818 |
| ## 46 | 2023-08-15 | 88.00 | -1.493181818 | -1.493181818 |
| ## 47 | 2023-08-16 | 88.80 | -0.693181818 | -0.693181818 |
| ## 48 | 2023-08-17 | 89.05 | -0.443181818 | -0.443181818 |
| ## 49 | 2023-08-18 | 90.15 | 0.656818182 | 0.656818182 |
| ## 50 | 2023-08-19 | 90.30 | 0.806818182 | 1.463636364 |
| ## 51 | 2023-08-20 | 89.30 | -0.193181818 | 0.613636364 |
| ## 52 | 2023-08-21 | 89.10 | -0.393181818 | -0.393181818 |
| ## 53 | 2023-08-22 | 89.40 | -0.093181818 | -0.093181818 |
| ## 54 | 2023-08-23 | 88.40 | -1.093181818 | -1.093181818 |
| ## 55 | 2023-08-24 | 87.85 | -1.643181818 | -1.643181818 |
| ## 56 | 2023-08-25 | 86.50 | -2.993181818 | -2.993181818 |
| ## 57 | 2023-08-26 | 88.45 | -1.043181818 | -1.043181818 |

```
## 58 2023-08-27 87.60 -1.893181818 -1.893181818
## 59 2023-08-28 87.15 -2.343181818 -2.343181818
## 60 2023-08-29 88.30 -1.193181818 -1.193181818
## 61 2023-08-30 85.80 -3.693181818 -3.693181818
## 62 2023-08-31 85.90 -3.593181818 -3.593181818
## 63 2023-09-01 85.25 -4.243181818 -4.243181818
## 64 2023-09-02 85.25 -4.243181818 -4.243181818
## 65 2023-09-03 85.90 -3.593181818 -3.593181818
## 66 2023-09-04 85.80 -3.693181818 -3.693181818
```

C = 1 T= 1



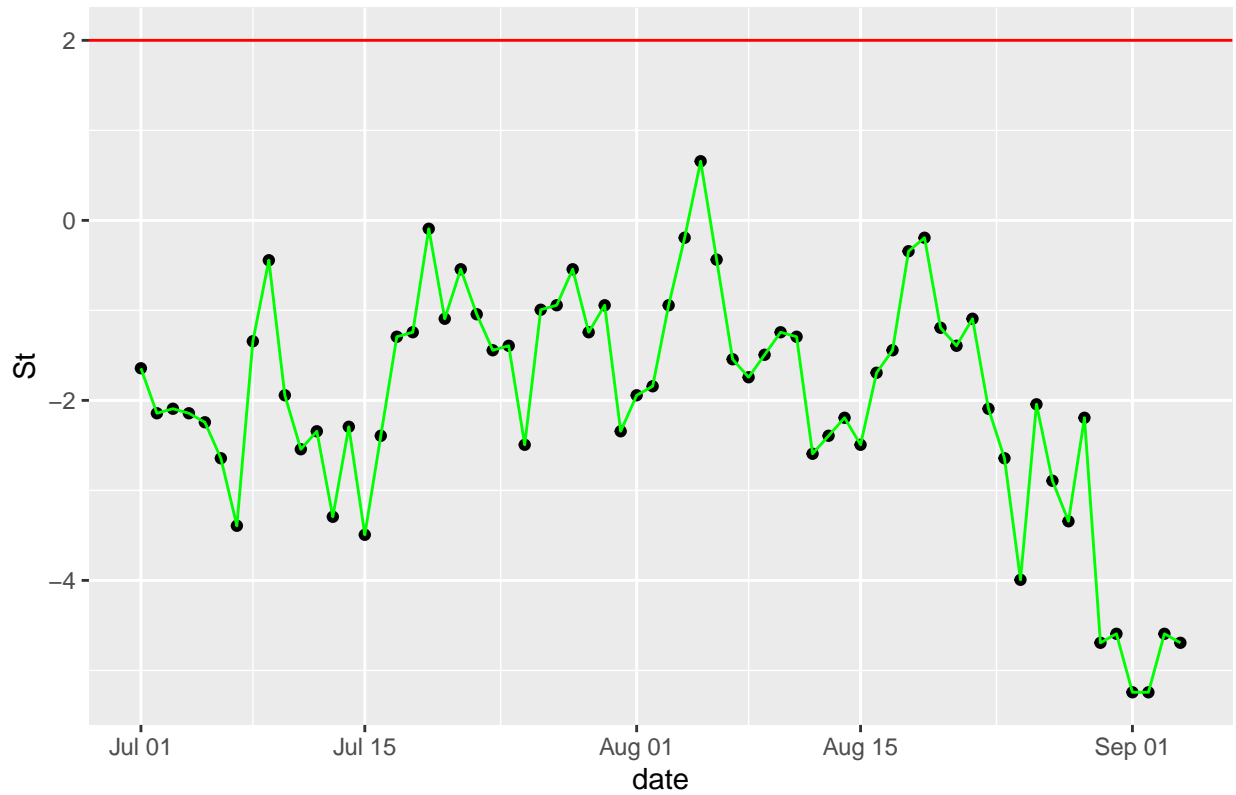
```
##      date  mean  helper      St
## 1 2023-07-01 88.85 -1.64318182 -1.64318182
## 2 2023-07-02 88.35 -2.14318182 -2.14318182
## 3 2023-07-03 88.40 -2.09318182 -2.09318182
## 4 2023-07-04 88.35 -2.14318182 -2.14318182
## 5 2023-07-05 88.25 -2.24318182 -2.24318182
## 6 2023-07-06 87.85 -2.64318182 -2.64318182
## 7 2023-07-07 87.10 -3.39318182 -3.39318182
## 8 2023-07-08 89.15 -1.34318182 -1.34318182
## 9 2023-07-09 90.05 -0.44318182 -0.44318182
## 10 2023-07-10 88.55 -1.94318182 -1.94318182
## 11 2023-07-11 87.95 -2.54318182 -2.54318182
## 12 2023-07-12 88.15 -2.34318182 -2.34318182
## 13 2023-07-13 87.20 -3.29318182 -3.29318182
## 14 2023-07-14 88.20 -2.29318182 -2.29318182
## 15 2023-07-15 87.00 -3.49318182 -3.49318182
```

```

## 16 2023-07-16 88.10 -2.39318182 -2.39318182
## 17 2023-07-17 89.20 -1.29318182 -1.29318182
## 18 2023-07-18 89.25 -1.24318182 -1.24318182
## 19 2023-07-19 90.40 -0.09318182 -0.09318182
## 20 2023-07-20 89.40 -1.09318182 -1.09318182
## 21 2023-07-21 89.95 -0.54318182 -0.54318182
## 22 2023-07-22 89.45 -1.04318182 -1.04318182
## 23 2023-07-23 89.05 -1.44318182 -1.44318182
## 24 2023-07-24 89.10 -1.39318182 -1.39318182
## 25 2023-07-25 88.00 -2.49318182 -2.49318182
## 26 2023-07-26 89.50 -0.99318182 -0.99318182
## 27 2023-07-27 89.55 -0.94318182 -0.94318182
## 28 2023-07-28 89.95 -0.54318182 -0.54318182
## 29 2023-07-29 89.25 -1.24318182 -1.24318182
## 30 2023-07-30 89.55 -0.94318182 -0.94318182
## 31 2023-07-31 88.15 -2.34318182 -2.34318182
## 32 2023-08-01 88.55 -1.94318182 -1.94318182
## 33 2023-08-02 88.65 -1.84318182 -1.84318182
## 34 2023-08-03 89.55 -0.94318182 -0.94318182
## 35 2023-08-04 90.30 -0.19318182 -0.19318182
## 36 2023-08-05 91.15 0.65681818 0.65681818
## 37 2023-08-06 89.40 -1.09318182 -0.43636364
## 38 2023-08-07 88.95 -1.54318182 -1.54318182
## 39 2023-08-08 88.75 -1.74318182 -1.74318182
## 40 2023-08-09 89.00 -1.49318182 -1.49318182
## 41 2023-08-10 89.25 -1.24318182 -1.24318182
## 42 2023-08-11 89.20 -1.29318182 -1.29318182
## 43 2023-08-12 87.90 -2.59318182 -2.59318182
## 44 2023-08-13 88.10 -2.39318182 -2.39318182
## 45 2023-08-14 88.30 -2.19318182 -2.19318182
## 46 2023-08-15 88.00 -2.49318182 -2.49318182
## 47 2023-08-16 88.80 -1.69318182 -1.69318182
## 48 2023-08-17 89.05 -1.44318182 -1.44318182
## 49 2023-08-18 90.15 -0.34318182 -0.34318182
## 50 2023-08-19 90.30 -0.19318182 -0.19318182
## 51 2023-08-20 89.30 -1.19318182 -1.19318182
## 52 2023-08-21 89.10 -1.39318182 -1.39318182
## 53 2023-08-22 89.40 -1.09318182 -1.09318182
## 54 2023-08-23 88.40 -2.09318182 -2.09318182
## 55 2023-08-24 87.85 -2.64318182 -2.64318182
## 56 2023-08-25 86.50 -3.99318182 -3.99318182
## 57 2023-08-26 88.45 -2.04318182 -2.04318182
## 58 2023-08-27 87.60 -2.89318182 -2.89318182
## 59 2023-08-28 87.15 -3.34318182 -3.34318182
## 60 2023-08-29 88.30 -2.19318182 -2.19318182
## 61 2023-08-30 85.80 -4.69318182 -4.69318182
## 62 2023-08-31 85.90 -4.59318182 -4.59318182
## 63 2023-09-01 85.25 -5.24318182 -5.24318182
## 64 2023-09-02 85.25 -5.24318182 -5.24318182
## 65 2023-09-03 85.90 -4.59318182 -4.59318182
## 66 2023-09-04 85.80 -4.69318182 -4.69318182

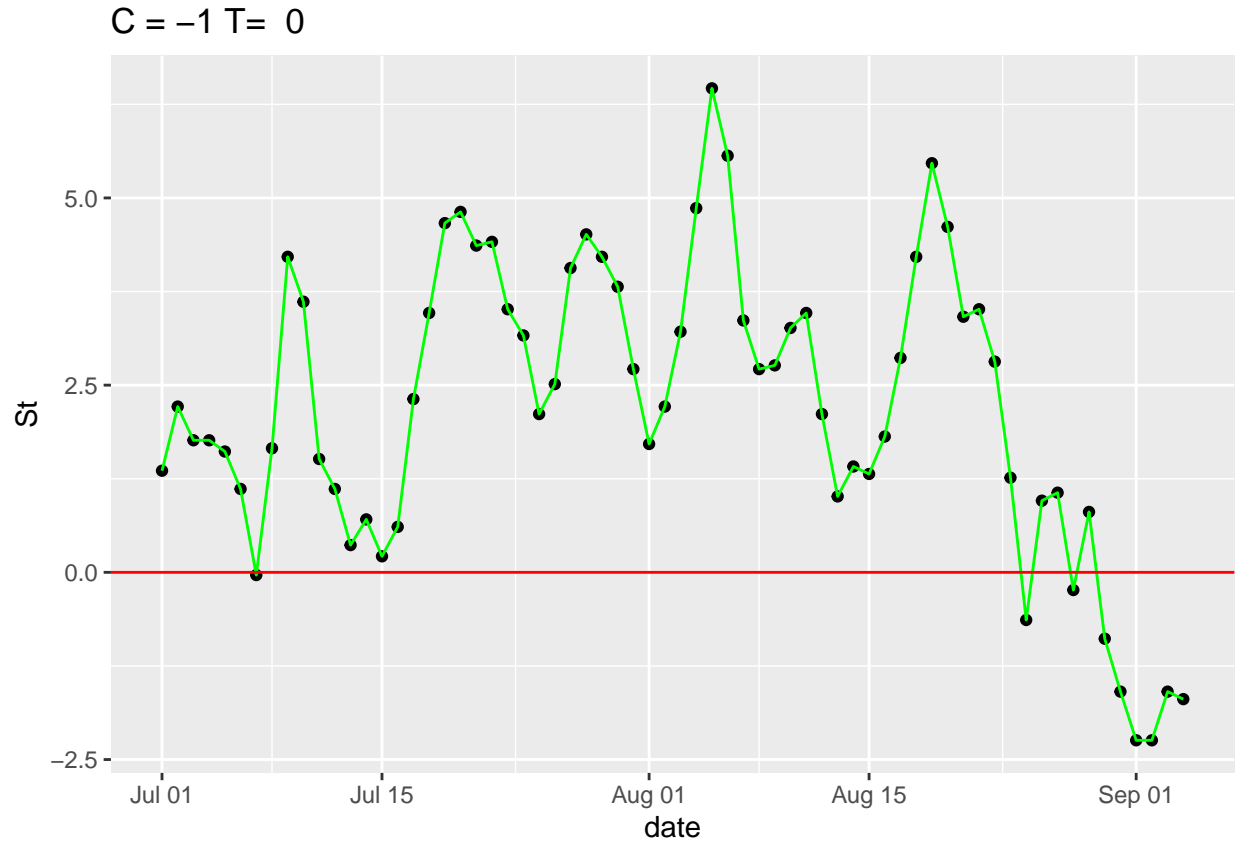
```


C = 2 T= 2



| ## | date | mean | helper | St |
|-------|------------|-------|------------|-------------|
| ## 1 | 2023-07-01 | 88.85 | 1.3568182 | 1.35681818 |
| ## 2 | 2023-07-02 | 88.35 | 0.8568182 | 2.21363636 |
| ## 3 | 2023-07-03 | 88.40 | 0.9068182 | 1.76363636 |
| ## 4 | 2023-07-04 | 88.35 | 0.8568182 | 1.76363636 |
| ## 5 | 2023-07-05 | 88.25 | 0.7568182 | 1.61363636 |
| ## 6 | 2023-07-06 | 87.85 | 0.3568182 | 1.11363636 |
| ## 7 | 2023-07-07 | 87.10 | -0.3931818 | -0.03636364 |
| ## 8 | 2023-07-08 | 89.15 | 1.6568182 | 1.65681818 |
| ## 9 | 2023-07-09 | 90.05 | 2.5568182 | 4.21363636 |
| ## 10 | 2023-07-10 | 88.55 | 1.0568182 | 3.61363636 |
| ## 11 | 2023-07-11 | 87.95 | 0.4568182 | 1.51363636 |
| ## 12 | 2023-07-12 | 88.15 | 0.6568182 | 1.11363636 |
| ## 13 | 2023-07-13 | 87.20 | -0.2931818 | 0.36363636 |
| ## 14 | 2023-07-14 | 88.20 | 0.7068182 | 0.70681818 |
| ## 15 | 2023-07-15 | 87.00 | -0.4931818 | 0.21363636 |
| ## 16 | 2023-07-16 | 88.10 | 0.6068182 | 0.60681818 |
| ## 17 | 2023-07-17 | 89.20 | 1.7068182 | 2.31363636 |
| ## 18 | 2023-07-18 | 89.25 | 1.7568182 | 3.46363636 |
| ## 19 | 2023-07-19 | 90.40 | 2.9068182 | 4.66363636 |
| ## 20 | 2023-07-20 | 89.40 | 1.9068182 | 4.81363636 |
| ## 21 | 2023-07-21 | 89.95 | 2.4568182 | 4.36363636 |
| ## 22 | 2023-07-22 | 89.45 | 1.9568182 | 4.41363636 |
| ## 23 | 2023-07-23 | 89.05 | 1.5568182 | 3.51363636 |
| ## 24 | 2023-07-24 | 89.10 | 1.6068182 | 3.16363636 |
| ## 25 | 2023-07-25 | 88.00 | 0.5068182 | 2.11363636 |

| | | | | | |
|----|----|------------|-------|------------|-------------|
| ## | 26 | 2023-07-26 | 89.50 | 2.0068182 | 2.51363636 |
| ## | 27 | 2023-07-27 | 89.55 | 2.0568182 | 4.06363636 |
| ## | 28 | 2023-07-28 | 89.95 | 2.4568182 | 4.51363636 |
| ## | 29 | 2023-07-29 | 89.25 | 1.7568182 | 4.21363636 |
| ## | 30 | 2023-07-30 | 89.55 | 2.0568182 | 3.81363636 |
| ## | 31 | 2023-07-31 | 88.15 | 0.6568182 | 2.71363636 |
| ## | 32 | 2023-08-01 | 88.55 | 1.0568182 | 1.71363636 |
| ## | 33 | 2023-08-02 | 88.65 | 1.1568182 | 2.21363636 |
| ## | 34 | 2023-08-03 | 89.55 | 2.0568182 | 3.21363636 |
| ## | 35 | 2023-08-04 | 90.30 | 2.8068182 | 4.86363636 |
| ## | 36 | 2023-08-05 | 91.15 | 3.6568182 | 6.46363636 |
| ## | 37 | 2023-08-06 | 89.40 | 1.9068182 | 5.56363636 |
| ## | 38 | 2023-08-07 | 88.95 | 1.4568182 | 3.36363636 |
| ## | 39 | 2023-08-08 | 88.75 | 1.2568182 | 2.71363636 |
| ## | 40 | 2023-08-09 | 89.00 | 1.5068182 | 2.76363636 |
| ## | 41 | 2023-08-10 | 89.25 | 1.7568182 | 3.26363636 |
| ## | 42 | 2023-08-11 | 89.20 | 1.7068182 | 3.46363636 |
| ## | 43 | 2023-08-12 | 87.90 | 0.4068182 | 2.11363636 |
| ## | 44 | 2023-08-13 | 88.10 | 0.6068182 | 1.01363636 |
| ## | 45 | 2023-08-14 | 88.30 | 0.8068182 | 1.41363636 |
| ## | 46 | 2023-08-15 | 88.00 | 0.5068182 | 1.31363636 |
| ## | 47 | 2023-08-16 | 88.80 | 1.3068182 | 1.81363636 |
| ## | 48 | 2023-08-17 | 89.05 | 1.5568182 | 2.86363636 |
| ## | 49 | 2023-08-18 | 90.15 | 2.6568182 | 4.21363636 |
| ## | 50 | 2023-08-19 | 90.30 | 2.8068182 | 5.46363636 |
| ## | 51 | 2023-08-20 | 89.30 | 1.8068182 | 4.61363636 |
| ## | 52 | 2023-08-21 | 89.10 | 1.6068182 | 3.41363636 |
| ## | 53 | 2023-08-22 | 89.40 | 1.9068182 | 3.51363636 |
| ## | 54 | 2023-08-23 | 88.40 | 0.9068182 | 2.81363636 |
| ## | 55 | 2023-08-24 | 87.85 | 0.3568182 | 1.26363636 |
| ## | 56 | 2023-08-25 | 86.50 | -0.9931818 | -0.63636364 |
| ## | 57 | 2023-08-26 | 88.45 | 0.9568182 | 0.95681818 |
| ## | 58 | 2023-08-27 | 87.60 | 0.1068182 | 1.06363636 |
| ## | 59 | 2023-08-28 | 87.15 | -0.3431818 | -0.23636364 |
| ## | 60 | 2023-08-29 | 88.30 | 0.8068182 | 0.80681818 |
| ## | 61 | 2023-08-30 | 85.80 | -1.6931818 | -0.88636364 |
| ## | 62 | 2023-08-31 | 85.90 | -1.5931818 | -1.59318182 |
| ## | 63 | 2023-09-01 | 85.25 | -2.2431818 | -2.24318182 |
| ## | 64 | 2023-09-02 | 85.25 | -2.2431818 | -2.24318182 |
| ## | 65 | 2023-09-03 | 85.90 | -1.5931818 | -1.59318182 |
| ## | 66 | 2023-09-04 | 85.80 | -1.6931818 | -1.69318182 |



From here, I inspected the different graphs and say that $T=0$ and $C=-1$ gave me the best respoes. $C=-1$ allowed me to align the graph with the lowest temperature in July, and when the temperature was beginning to plummet in August. July is officially summer, so when the temperature drops below the July mark and stays below, the summer is over.. According to the graph, this was about August 28. Thus, the official end of summer is August 28.

Part 2

2. Use a CUSUM approach to make a judgment of whether Atlanta's summer climate has gotten warmer in that time (and if so, when).

Part 2 Solution

To start this question, I had to decided how I would approach it. The summer climate has great variation, and I didn't want to pick just one date and risk losing valuable information. I decided to chose the median date for each summer through the years. I chose the median because the mean could be skewed by heat waves or cold spells.

I can see how this is not a perfect method for this calculation, but it will work in this situation.

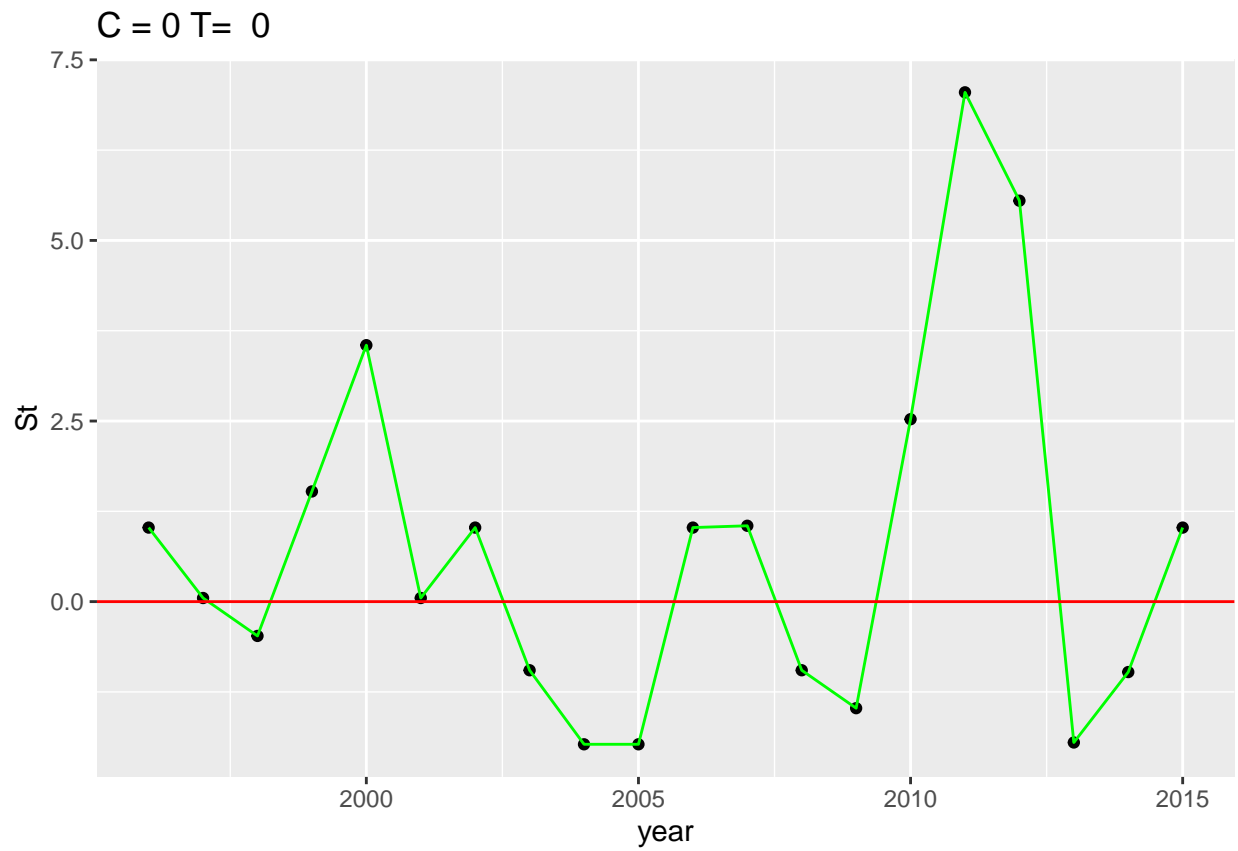
I started by transforming the data to be in a similar to what was done in the previous problem.

```
##      year median
## X1996 1996   90.0
## X1997 1997   88.0
## X1998 1998   88.5
```

```
## X1999 1999 90.5
## X2000 2000 91.0
## X2001 2001 87.0
## X2002 2002 90.0
## X2003 2003 87.0
## X2004 2004 87.0
## X2005 2005 87.0
## X2006 2006 90.0
## X2007 2007 89.0
## X2008 2008 88.0
## X2009 2009 87.5
## X2010 2010 91.5
## X2011 2011 93.5
## X2012 2012 90.0
## X2013 2013 86.0
## X2014 2014 88.0
## X2015 2015 90.0
```

We now have a data frame that has the median temperature across the summer for all years. Using the function from the last question, I created a cusum function.

```
##      year median helper      St
## X1996 1996  90.0  1.025  1.025
## X1997 1997  88.0 -0.975  0.050
## X1998 1998  88.5 -0.475 -0.475
## X1999 1999  90.5  1.525  1.525
## X2000 2000  91.0  2.025  3.550
## X2001 2001  87.0 -1.975  0.050
```

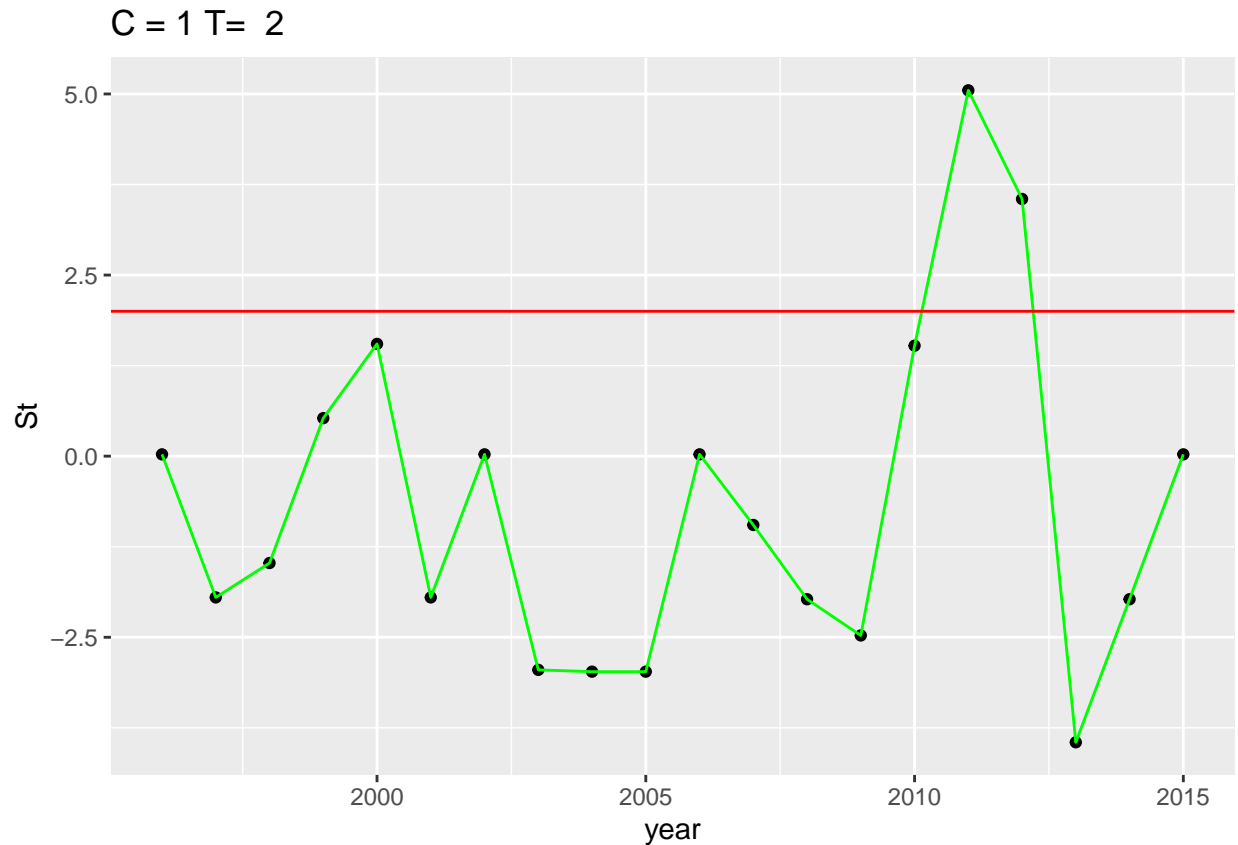


```
##      year median helper    St
## X1996 1996    90.0 -0.975 -0.975
## X1997 1997    88.0 -2.975 -2.975
## X1998 1998    88.5 -2.475 -2.475
## X1999 1999    90.5 -0.475 -0.475
## X2000 2000    91.0  0.025  0.025
## X2001 2001    87.0 -3.975 -3.950
```

C = 2 T= 2



```
##      year median helper    St
## X1996 1996   90.0  0.025  0.025
## X1997 1997   88.0 -1.975 -1.950
## X1998 1998   88.5 -1.475 -1.475
## X1999 1999   90.5  0.525  0.525
## X2000 2000   91.0  1.025  1.550
## X2001 2001   87.0 -2.975 -1.950
```



The plots here are strange. The plot I most like is the one where $C=1$ and $T=2$. We see a huge spike in 2011, crossing the arbitrary threshold, but then it dips back down and seems to be rising again. The timeline is inconclusive for this period.

What is instead of taking the median of all days, I chose one day in each year? I start with a new dataset, holding a list of data frames

```
## [[1]]
## [[1]][[1]]
##      year  X9.Aug
## X1996 1996      90
## X1997 1997      73
## X1998 1998      82
## X1999 1999      91
## X2000 2000      96
## X2001 2001      87
## X2002 2002      86
## X2003 2003      86
## X2004 2004      84
## X2005 2005      85
## X2006 2006      95
## X2007 2007     103
## X2008 2008      85
## X2009 2009      93
## X2010 2010      94
## X2011 2011      91
## X2012 2012      88
```

```

## X2013 2013      89
## X2014 2014      89
## X2015 2015      93
##
##
## [[2]]
##      year X20.Jul
## X1996 1996      99
## X1997 1997      90
## X1998 1998      91
## X1999 1999      90
## X2000 2000      99
## X2001 2001      87
## X2002 2002      91
## X2003 2003      88
## X2004 2004      88
## X2005 2005      89
## X2006 2006      93
## X2007 2007      86
## X2008 2008      94
## X2009 2009      82
## X2010 2010      91
## X2011 2011      91
## X2012 2012      84
## X2013 2013      86
## X2014 2014      76
## X2015 2015      93
##
## [[3]]
##      year X24.Aug
## X1996 1996      88
## X1997 1997      91
## X1998 1998      93
## X1999 1999      91
## X2000 2000      92
## X2001 2001      86
## X2002 2002      82
## X2003 2003      89
## X2004 2004      87
## X2005 2005      85
## X2006 2006      90
## X2007 2007      89
## X2008 2008      89
## X2009 2009      86
## X2010 2010      84
## X2011 2011      93
## X2012 2012      86
## X2013 2013      92
## X2014 2014      92
## X2015 2015      81

```

I can then use my previous function and apply it to three random dates

```
##      year median helper  St
```



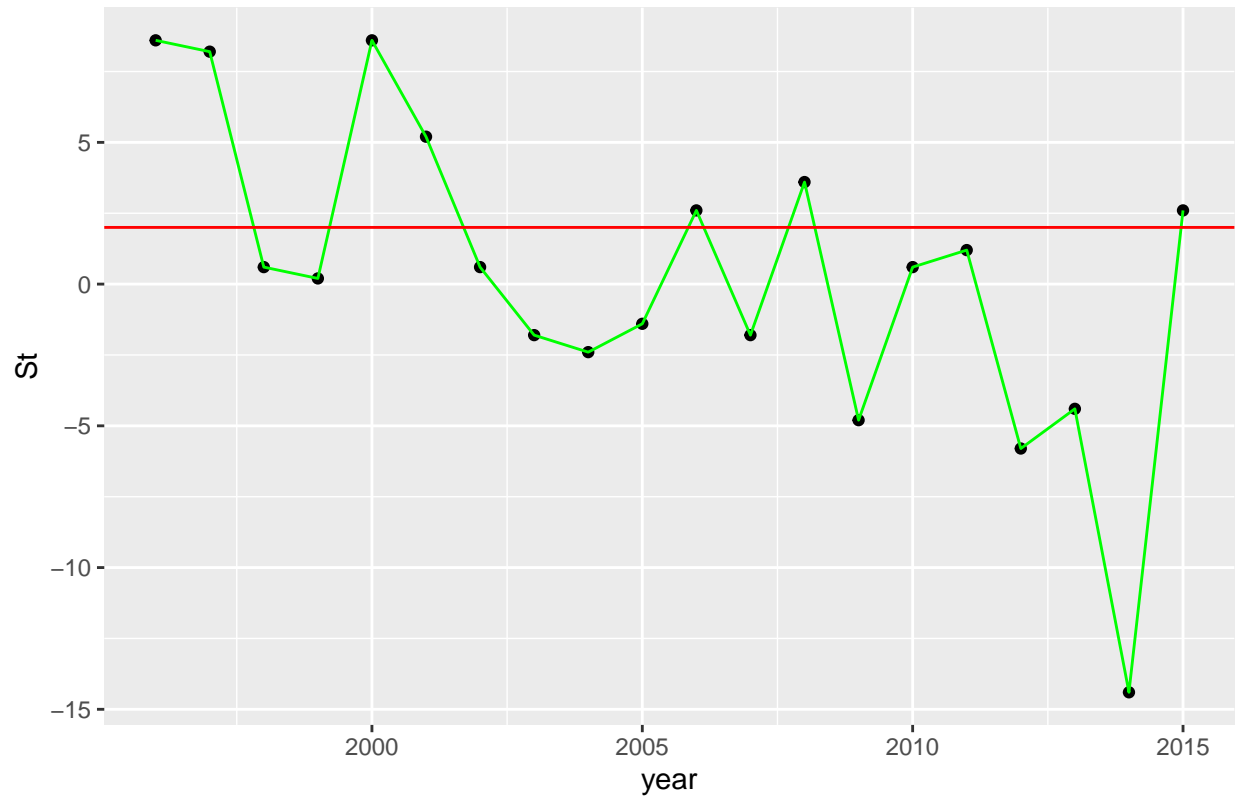
```
## X1996 1996 90.0 0 0
## X1997 1997 88.0 -17 -17
## X1998 1998 88.5 -8 -8
## X1999 1999 90.5 1 1
## X2000 2000 91.0 6 7
## X2001 2001 87.0 -3 3
```

C = 1 T= 2

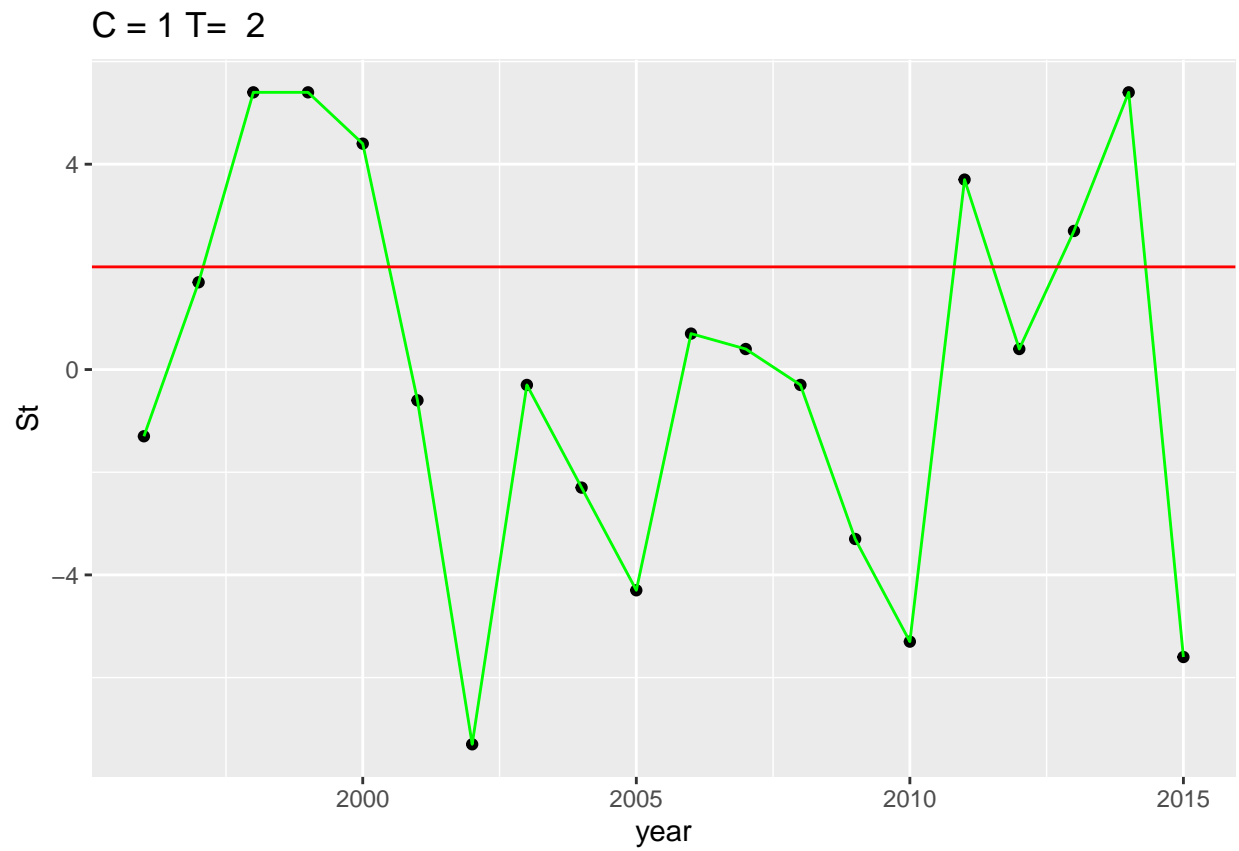


```
##      year median helper  St
## X1996 1996 90.0 8.6 8.6
## X1997 1997 88.0 -0.4 8.2
## X1998 1998 88.5 0.6 0.6
## X1999 1999 90.5 -0.4 0.2
## X2000 2000 91.0 8.6 8.6
## X2001 2001 87.0 -3.4 5.2
```

C = 1 T= 2



```
##      year median helper  St
## X1996 1996   90.0   -1.3 -1.3
## X1997 1997   88.0    1.7  1.7
## X1998 1998   88.5    3.7  5.4
## X1999 1999   90.5    1.7  5.4
## X2000 2000   91.0    2.7  4.4
## X2001 2001   87.0   -3.3 -0.6
```



Again, the data is inconclusive. I would love to say the world is getting warmer, but we are not showing data for enough years to make any well-informed decisions.