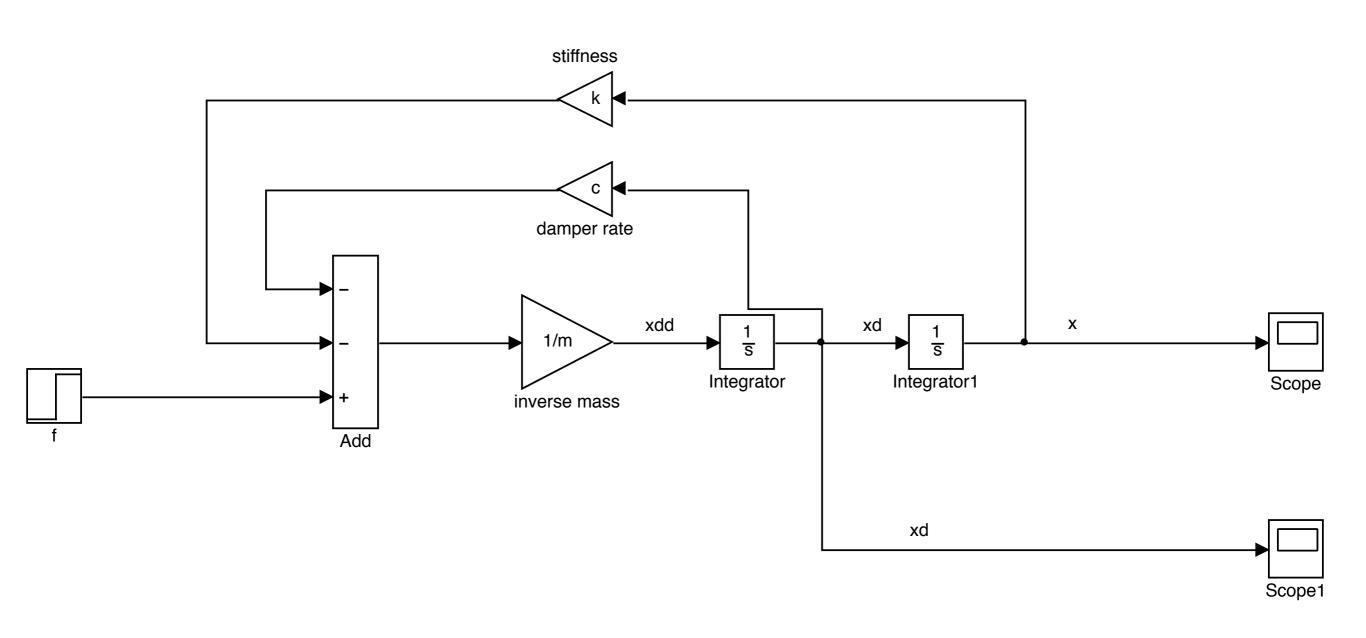
ME40064: System Modelling & Simulation ME50344: Engineering Systems Simulation Lecture 18

Dr Andrew Cookson University of Bath, 2019-20

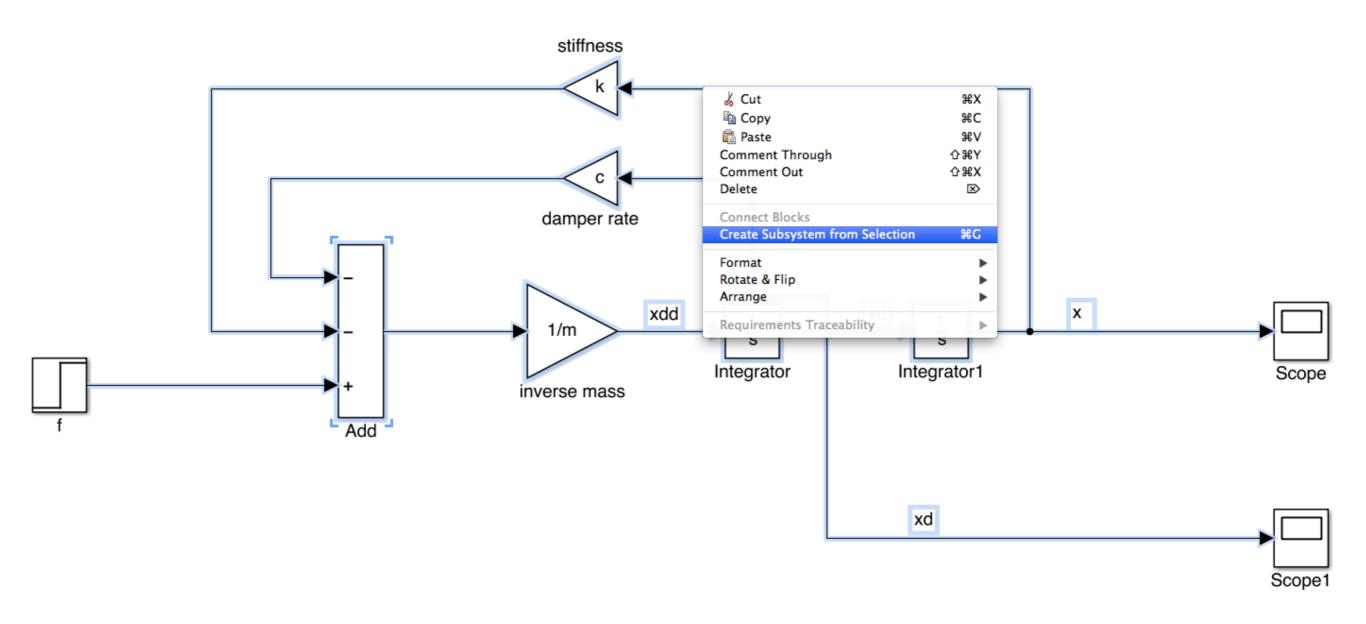
LECTURE 18 Simulink: A Closer Look

- Understand how to build a subsystem model in Simulink
- Appreciation of potential complexity and sophistication of Simulink models
- Understand some of Simulink's solvers and relevant settings

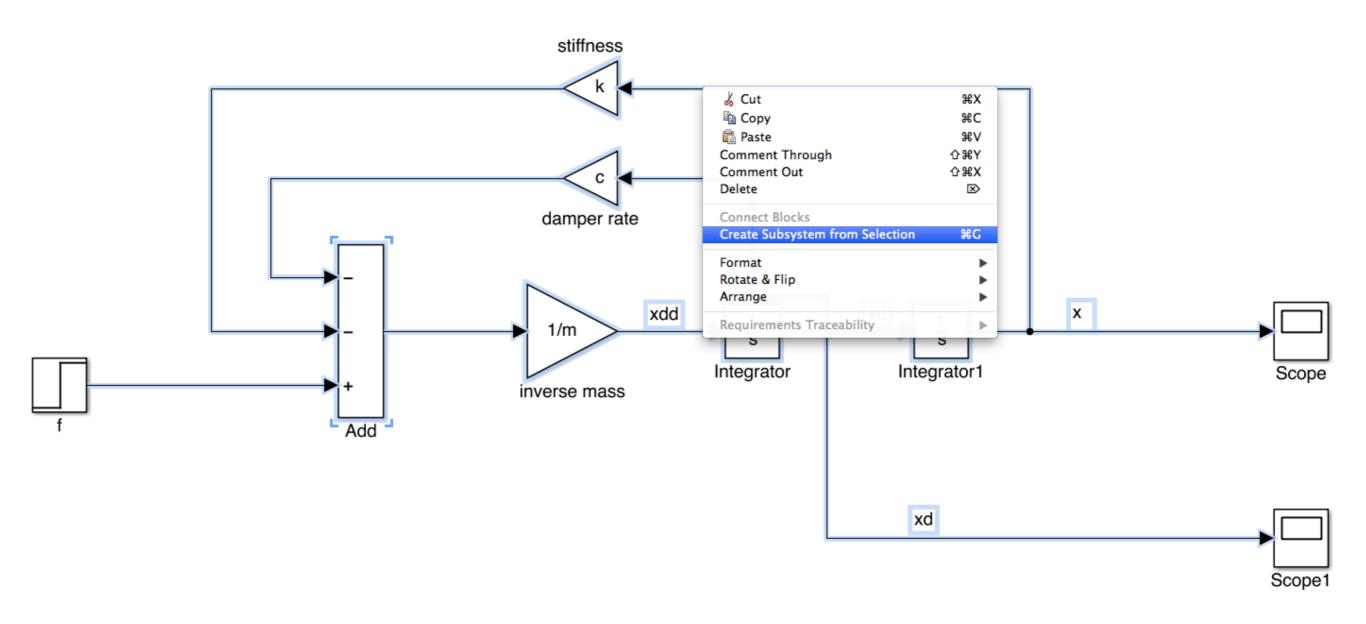
Start with a block diagram model



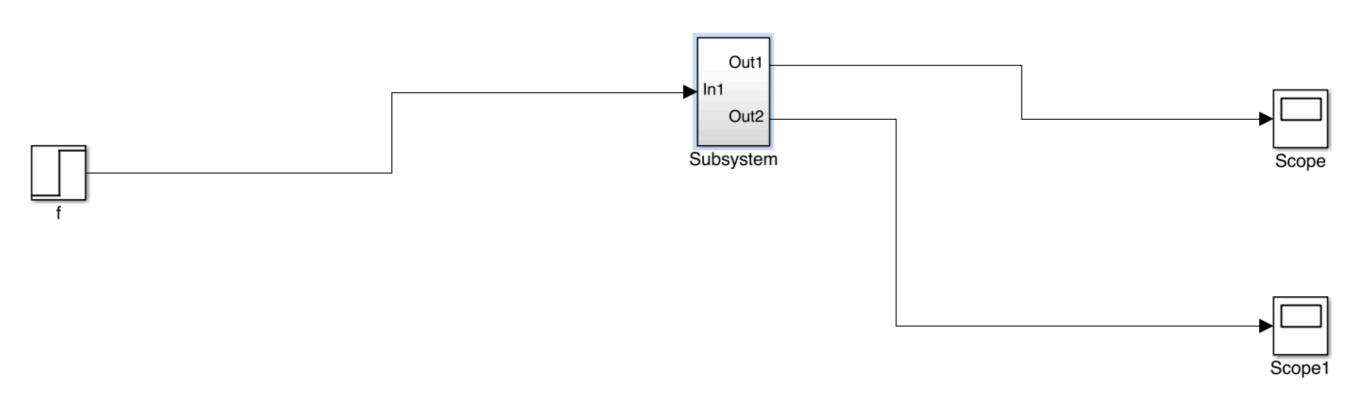
Select the model - excluding inputs and outputs, then click the "Build subsystem option"



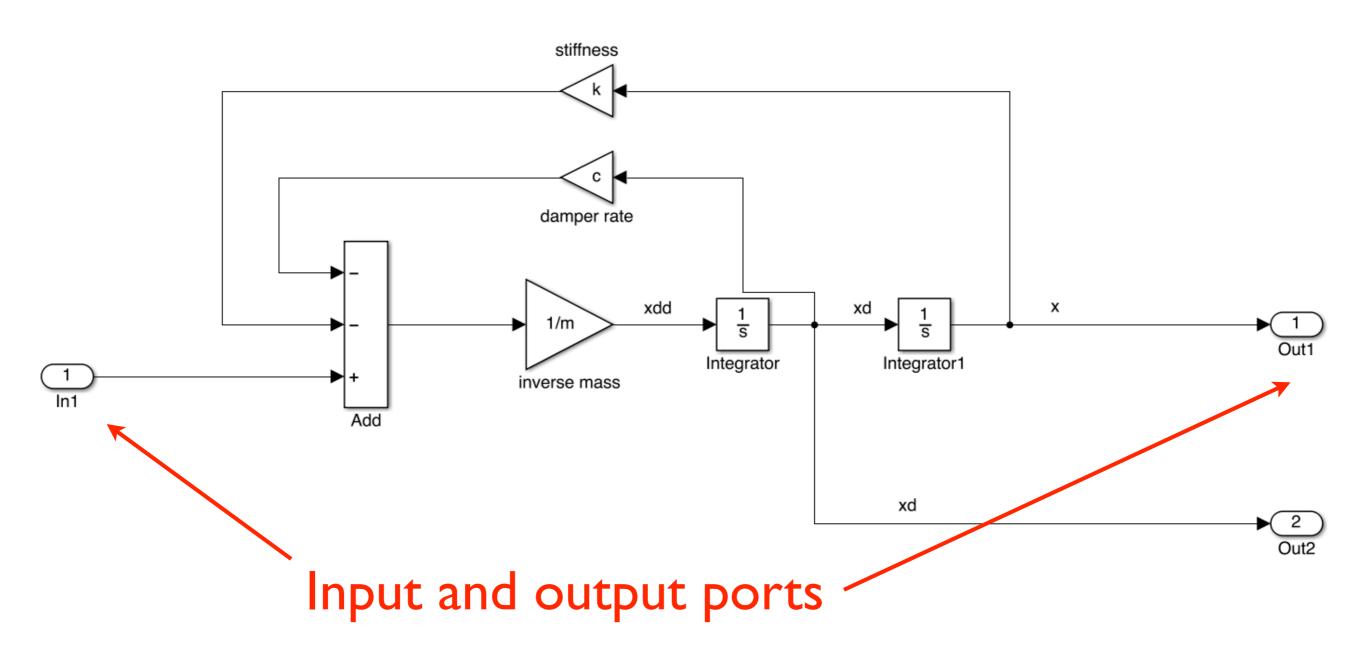
Select the model - excluding inputs and outputs, then click the "Build subsystem option"



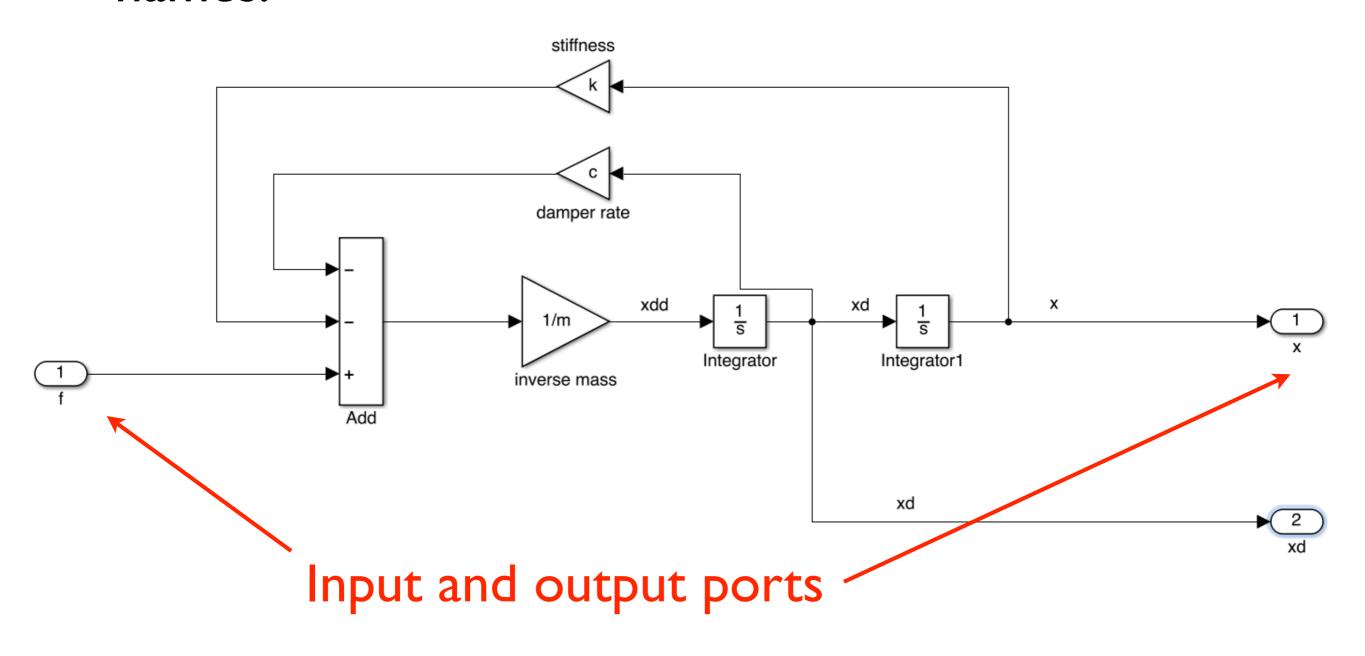
Produces the following:



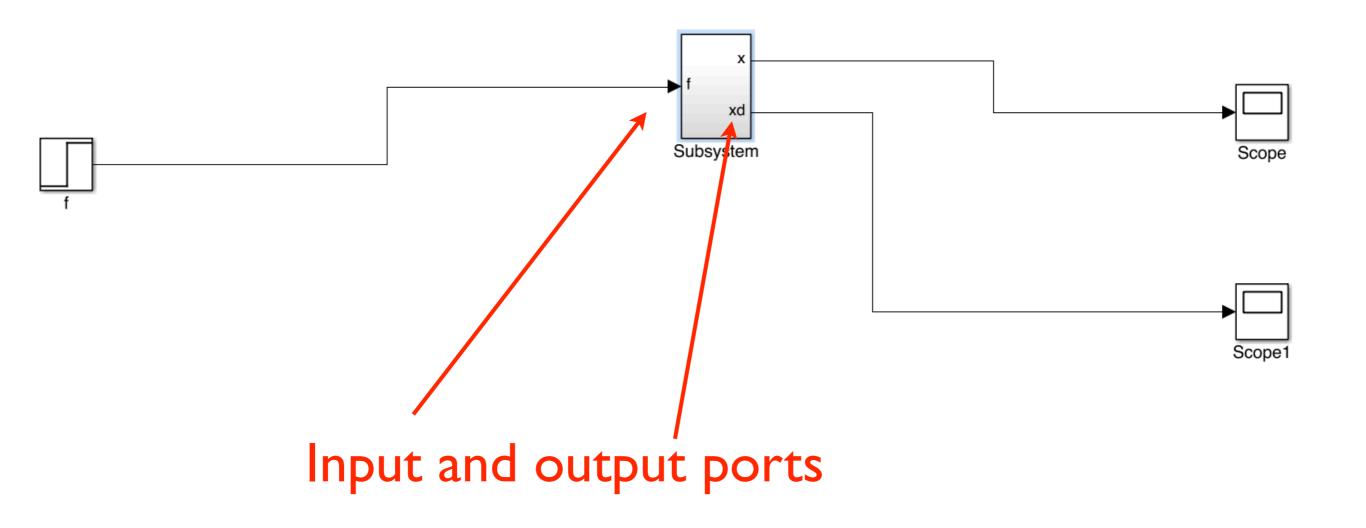
Clicking inside the subsystem block:



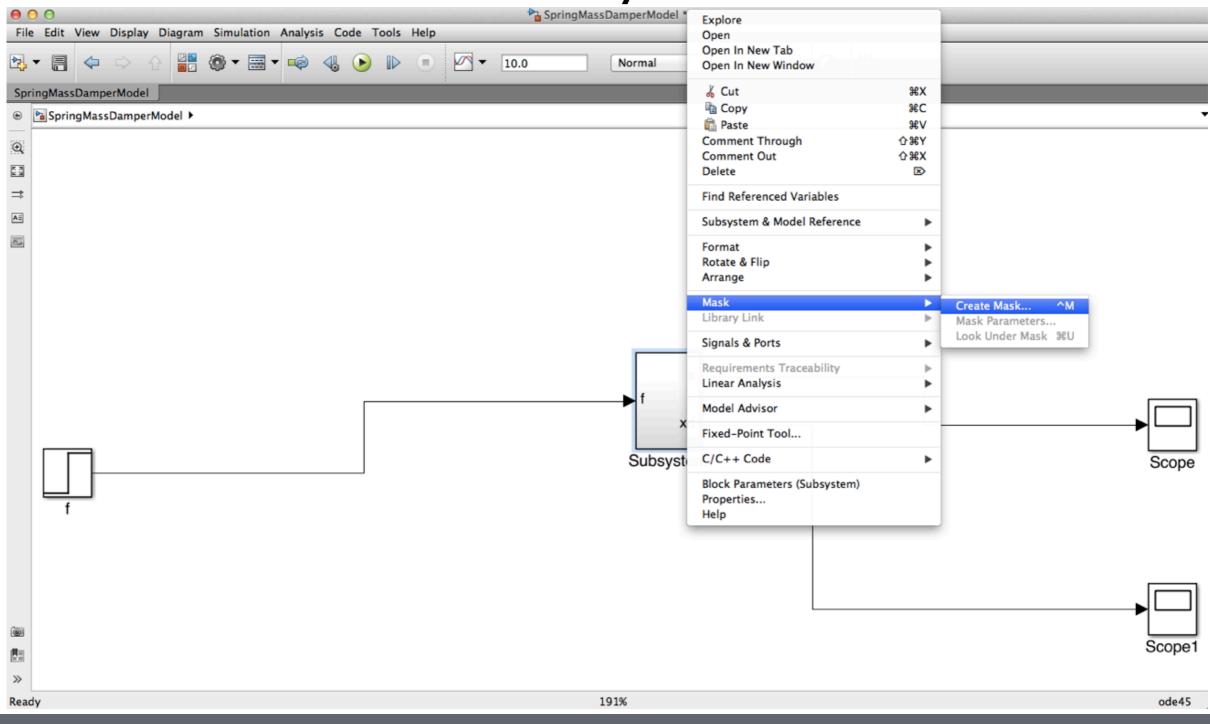
Relabel these input and output ports to variable names:



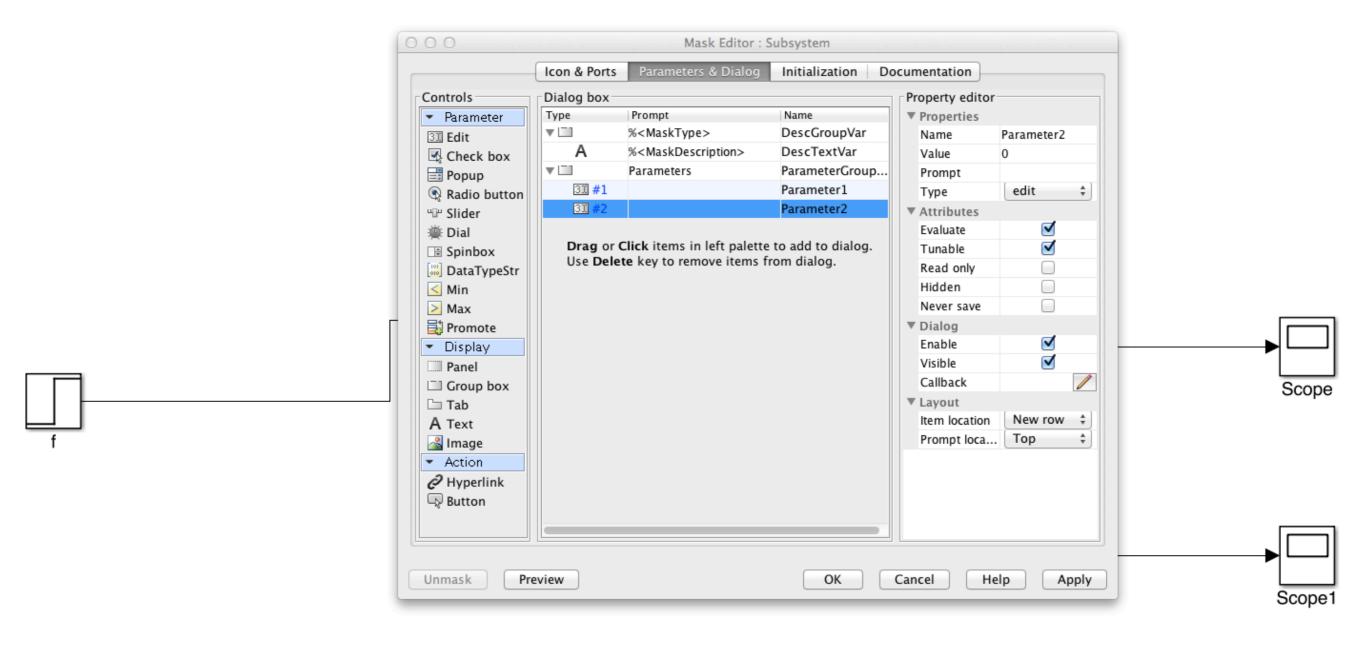
Produces the following subsystem block:



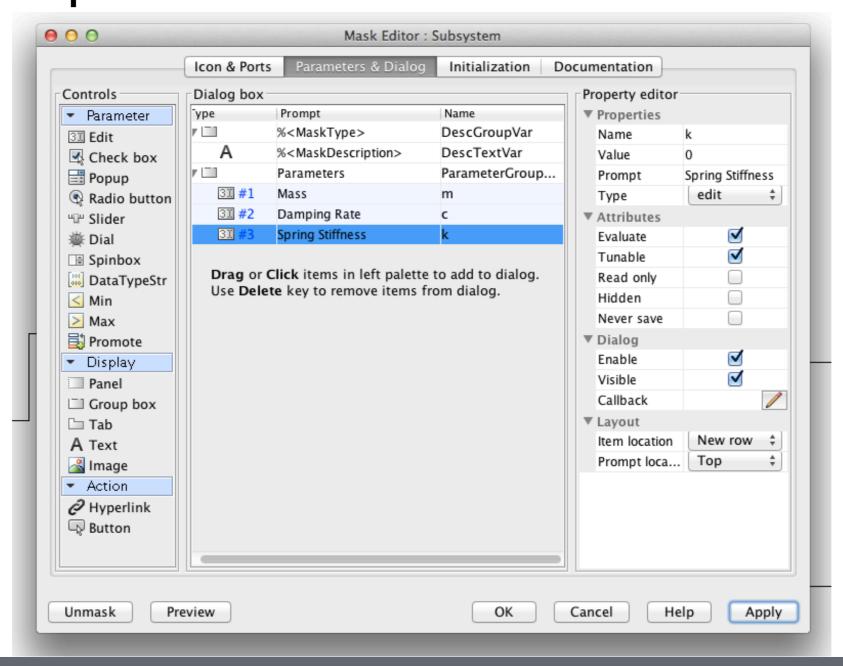
Now will mask this subsystem:



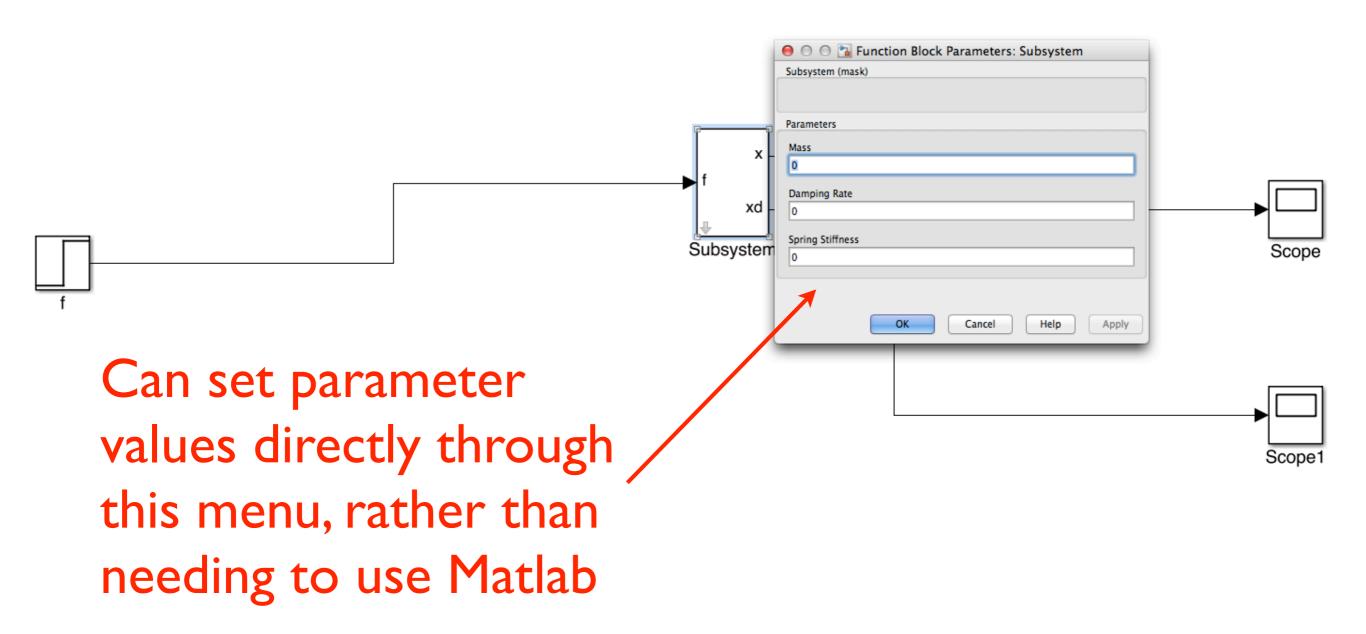
Click "edit" to add the parameters:



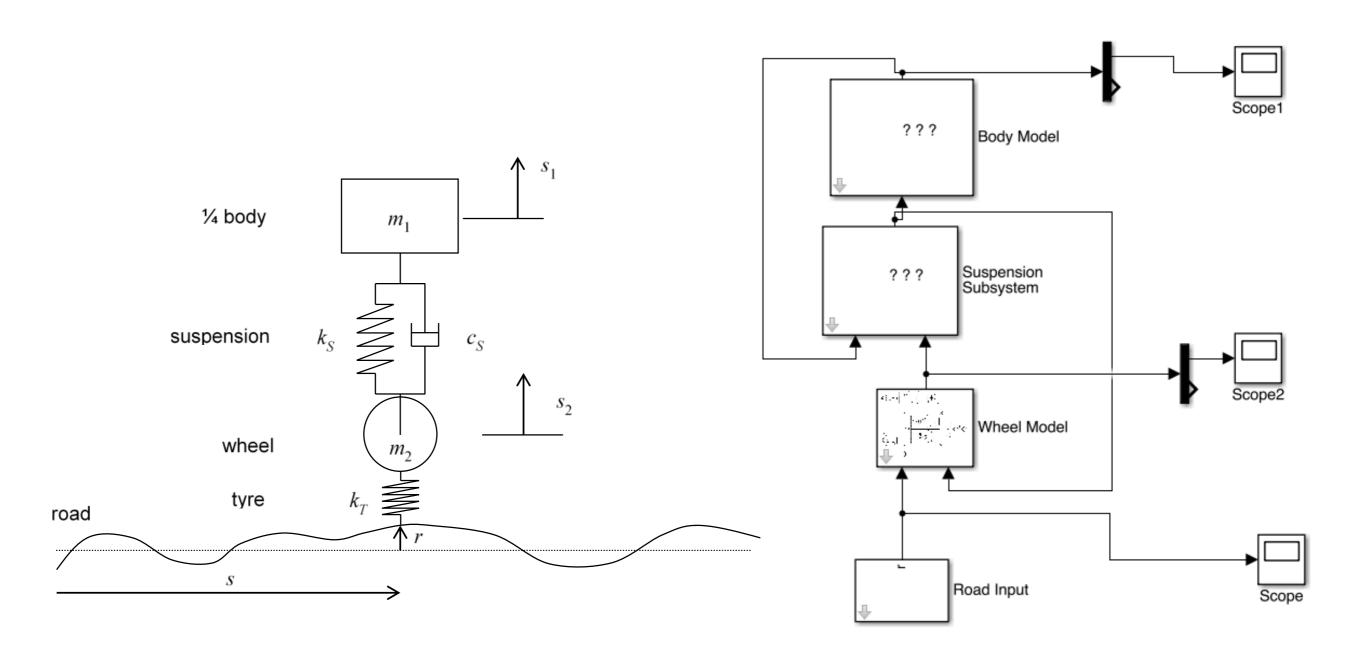
Now define a label and specify the variable name for each parameter:



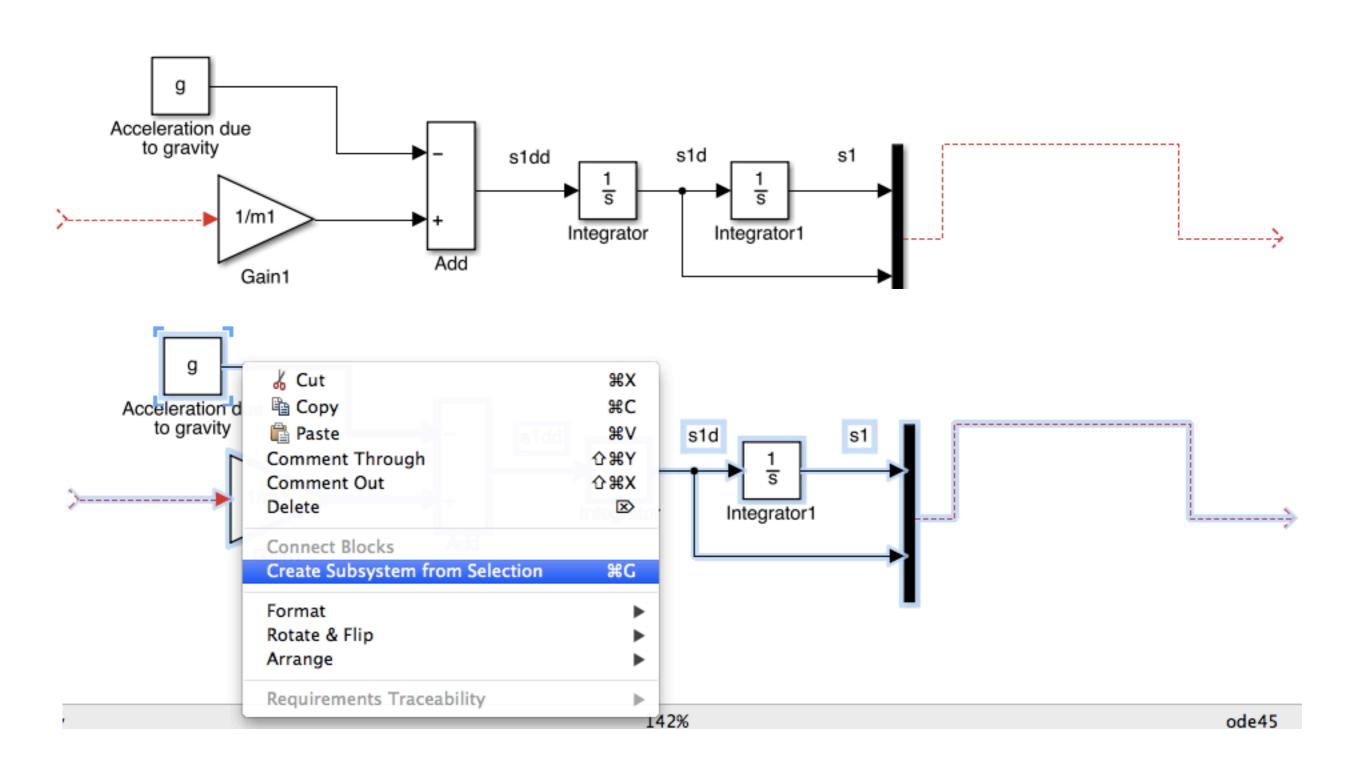
Double clicking on the subsystem block produces following menu:



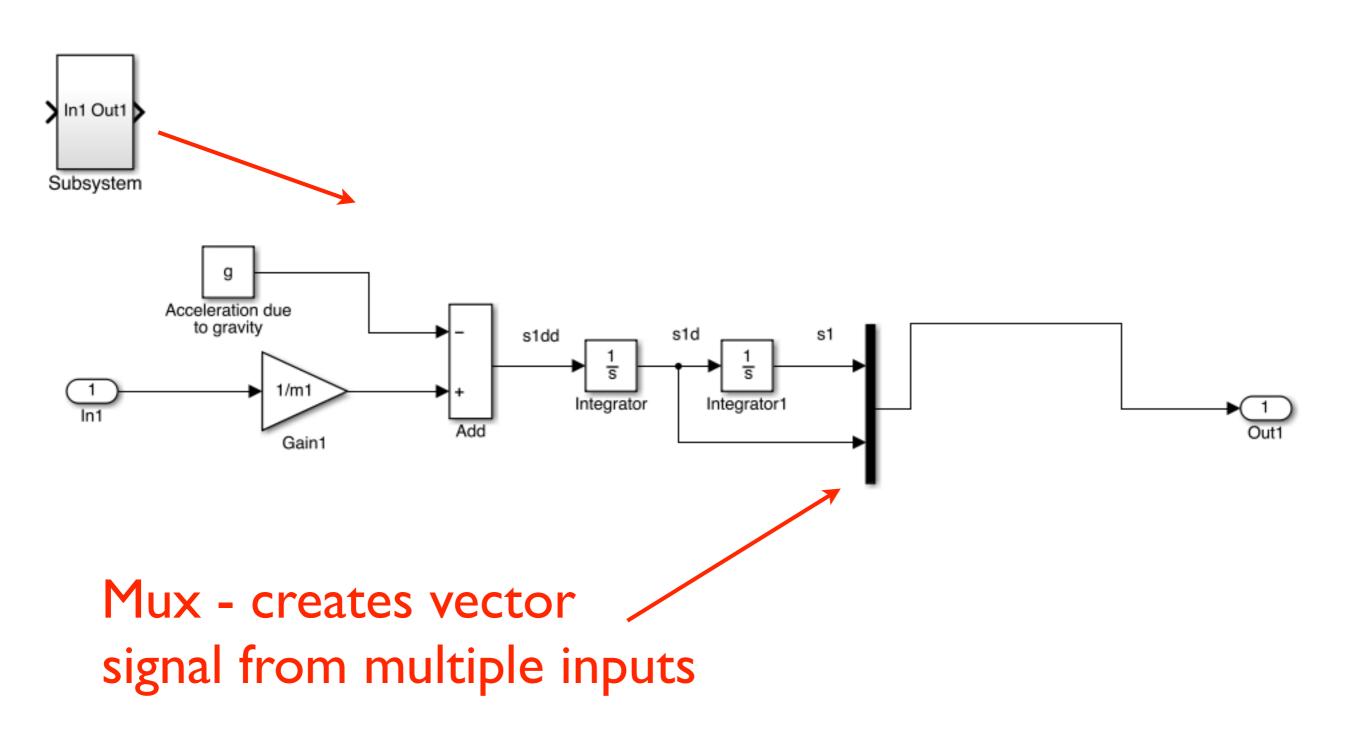
SUBSYSTEM MODELS Recap Of 1/4 Car Model



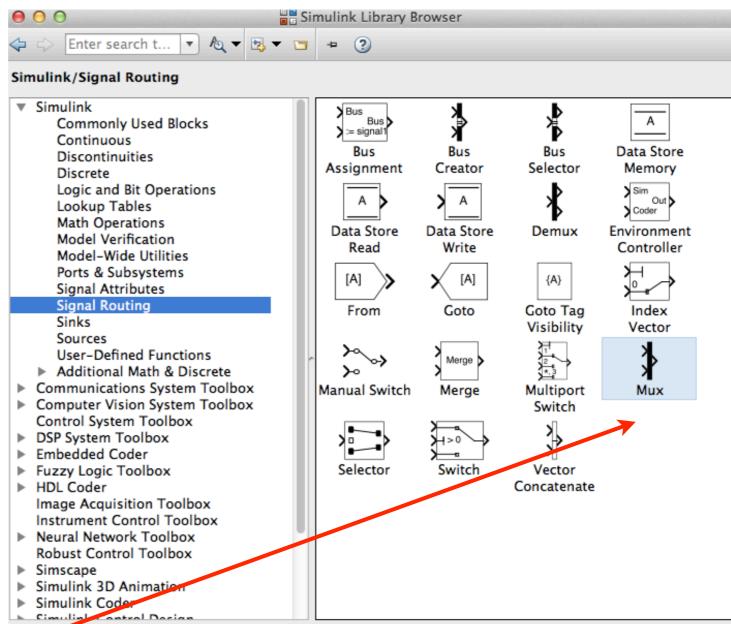
SUBSYSTEM MODELS Building The Body Model Subsystem



SUBSYSTEM MODELS Building The Body Model Subsystem



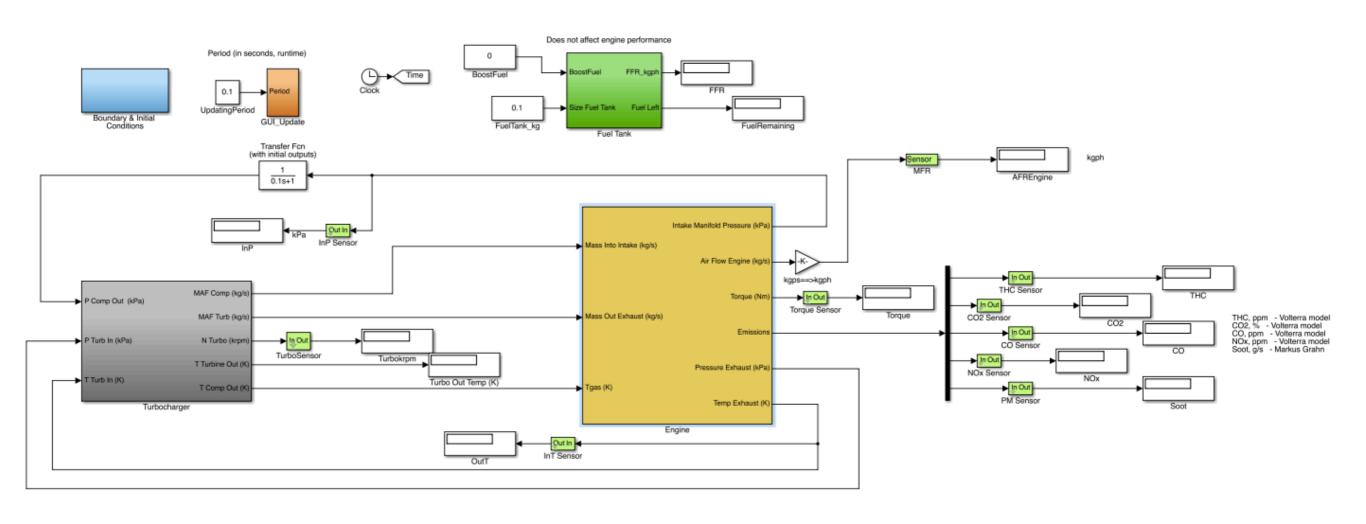
SUBSYSTEM MODELS Building The Body Model Subsystem



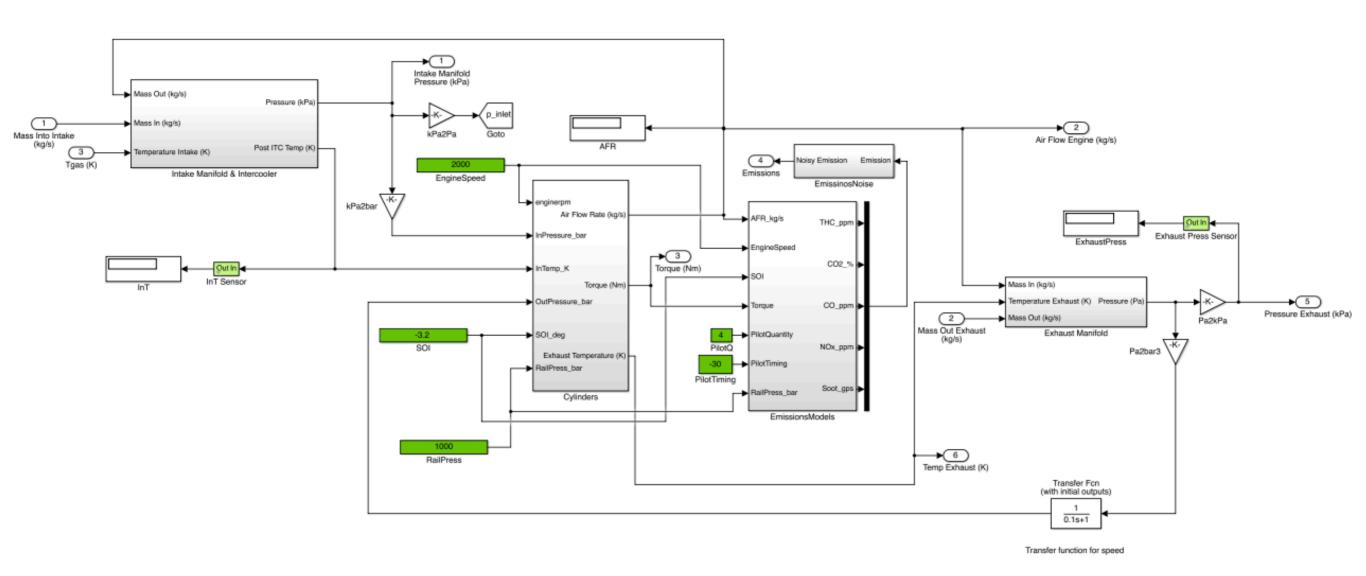
Mux - creates vector signal from multiple inputs

 Following slides show just a few of the blocks and subsystems from an engine model created by Dr. R. Burke

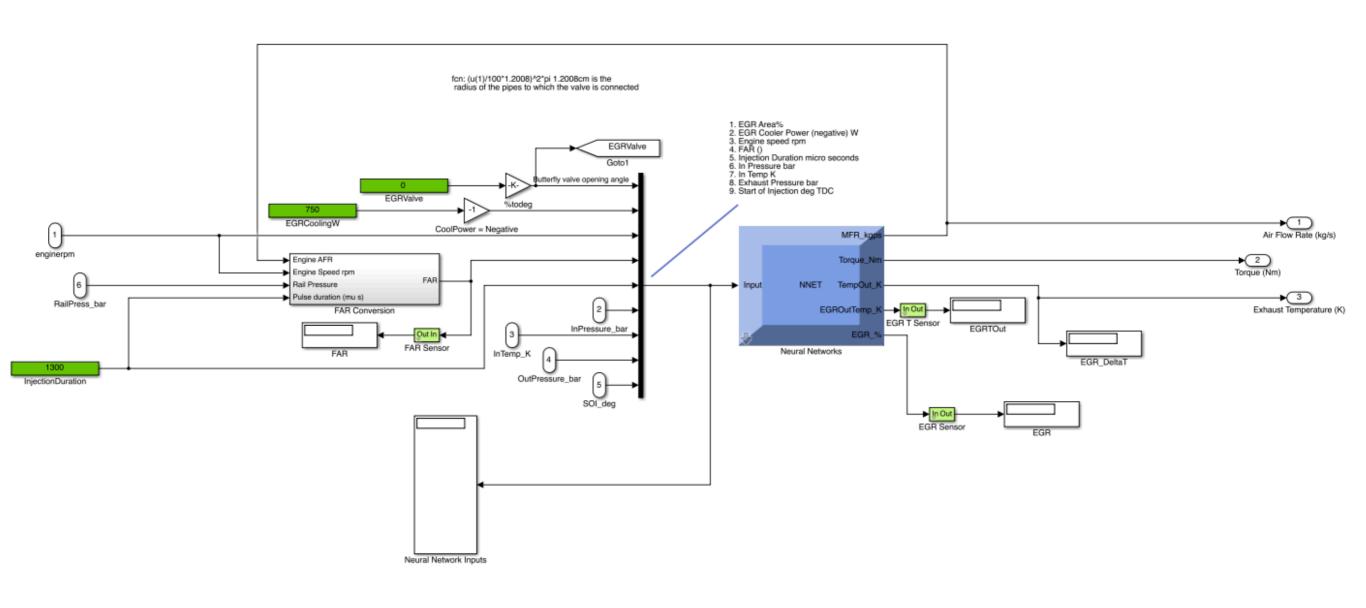
Engine control system model (Dr. R. Burke)



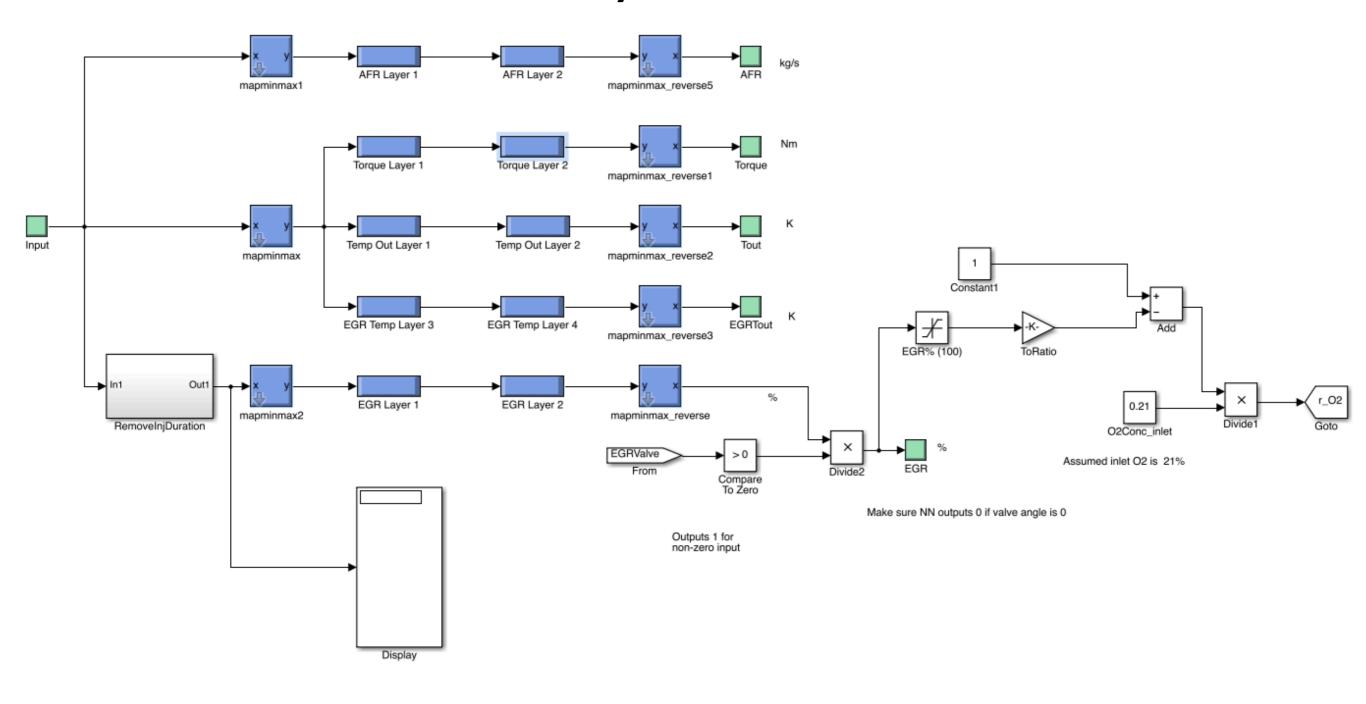
Engine subsystem



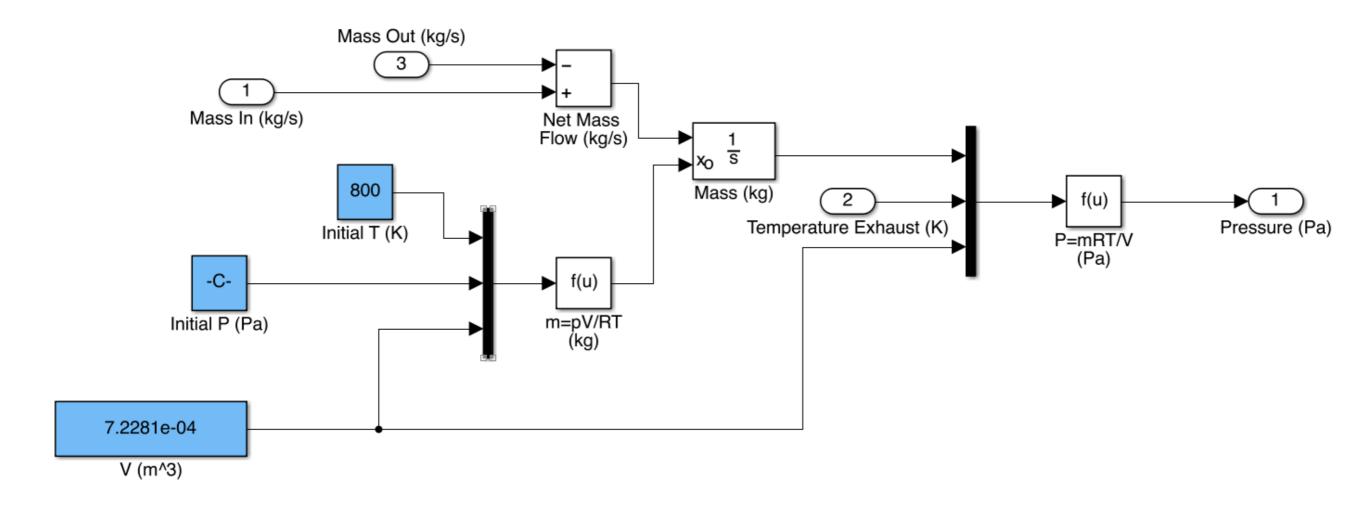
Cylinders subsystem



Neural networks subsystem



Exhaust manifold

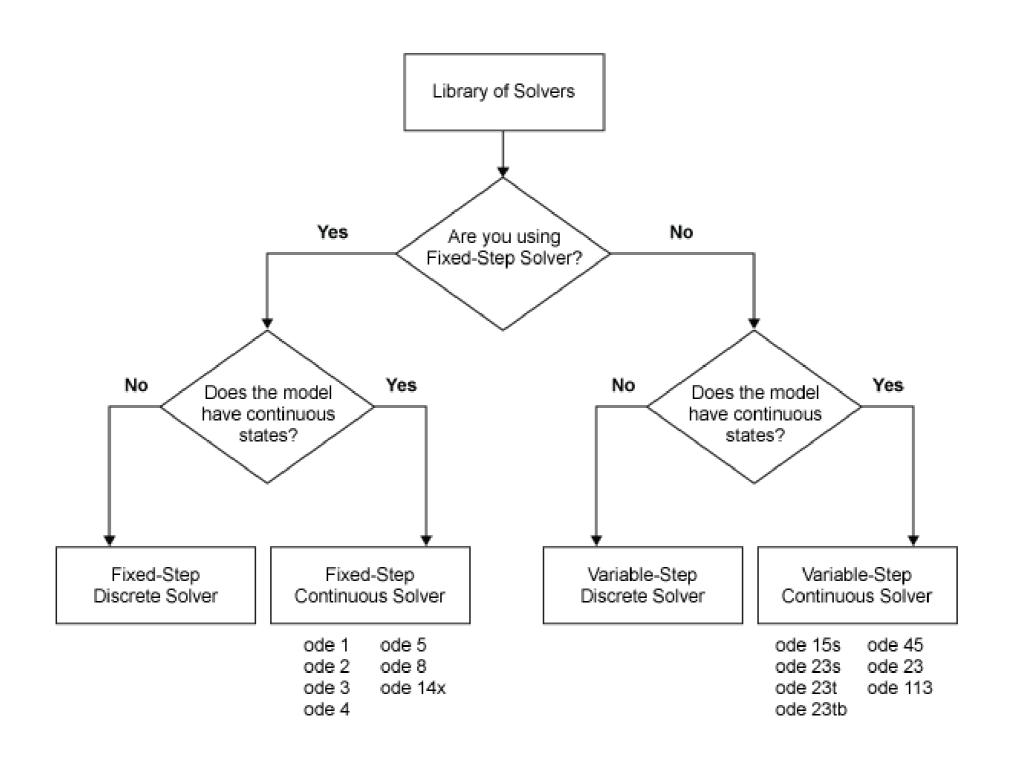


made 10x bigger for system stabilisation

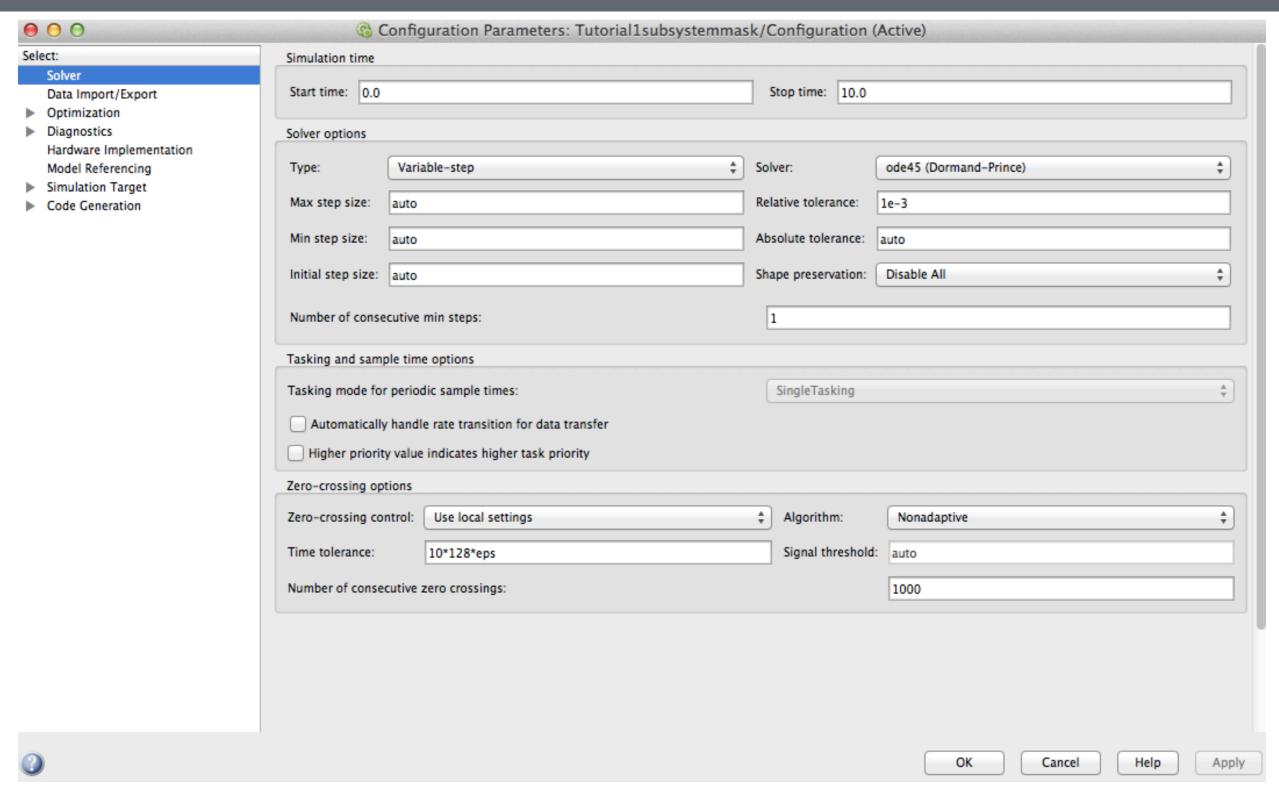
SIMULINK'S SOLVERS

What are the solvers and their options?

SIMULINK'S SOLVERS The Options



SIMULINK'S SOLVERS The Options



SIMULINK'S SOLVERS Runge-Kutta 4 Scheme

Multi-stage scheme - an explicit method, therefore has stability restrictions

To solve the following types of ordinary differential equations:

$$\frac{dy}{dt} = f(y,t), \quad y(t_0) = y_0$$

For one time step:

$$t_{n+1} = t_n + \Delta t$$

The solution at that next time point is the following weighted sum:

$$y_{n+1} = y_n + \frac{\Delta t}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

These values of k are defined on the following slide:

SIMULINK'S SOLVERS Runge-Kutta 4 Scheme

$$y_{n+1} = y_n + \frac{\Delta t}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

The solution at that next time point is the following weighted sum:

$$k_{1} = f(y_{n}, t_{n})$$

$$k_{2} = f(y_{n} + \Delta t \frac{k_{1}}{2}, t_{n} + \frac{\Delta t}{2})$$

$$k_{3} = f(y_{n} + \Delta t \frac{k_{2}}{2}, t_{n} + \frac{\Delta t}{2})$$

$$k_{4} = f(y_{n} + \Delta t k_{3}, t_{n} + \Delta t)$$

This is a 4th order method

SIMULINK'S SOLVERS Runge-Kutta 4 Scheme

$$y_{n+1} = y_n + \frac{\Delta t}{6}(k_1 + 2k_2 + 2k_3 + k_4)$$

The solution at that next time point is the following weighted sum:

Estimates of the slope

Start point of step
$$\underbrace{k_1 = f(y_n, t_n)}_{k_2 = f(y_n + \Delta t)} \underbrace{\frac{k_1}{2}}_{t_n}, t_n + \frac{\Delta t}{2} \underbrace{\frac{\Delta t}{2}}_{t_n} \underbrace{\text{Mid-point estimated from step I}}_{t_n}$$

$$\underbrace{k_3 = f(y_n + \Delta t)}_{t_n} \underbrace{\frac{\Delta t}{2}}_{t_n}, t_n + \frac{\Delta t}{2} \underbrace{\text{Updated estimate of mid-point}}_{t_n}$$

$$\underbrace{k_4 = f(y_n + \Delta t)}_{t_n} \underbrace{t_n + \Delta t}_{t_n} \underbrace{\text{End point of step using updated y estimate}}_{t_n}$$

SIMULINK'S SOLVERS Ode45 (Dormand-Prince)

This is the default solver in Simulink and Matlab - good for many problems

A variant of the Runge-Kutta scheme described previously

This version computes a 4th and 5th order accurate solution - the difference between the solutions indicates the size of the error

The time step can then be adapted to suit this error size for each step of the solution

This kind of adaptive time stepping provides a good balance of accuracy and computational cost

More information available at:

https://uk.mathworks.com/help/matlab/ref/ode45.html

https://uk.mathworks.com/help/simulink/gui/solver.html

SIMULINK'S SOLVERS Further Reading

Use Auto Solver to Select A Solver

https://uk.mathworks.com/help/simulink/ug/use-auto-solver-to-select-a-solver-1.html

Checking Accuracy Through Multiple Solutions

https://uk.mathworks.com/help/simulink/ug/improving-simulation-accuracy.html