# Advanced applied econometrics

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### Next week

- next and final lecture: 12.7; 9-12
- 2 Graded PS (send to phaan@diw.de and mblesch@diw.de) August 4
- 3 prepare Blundell et al. (2016)

## Plan for today

- Keane & Wolpin: Set-up
  - Structure of Model
  - Identification
  - Model fit & fix
- 2 K&W: Solution and Estimation
  - compare to Rust
  - Simulate & Interpolating value function
- 3 Practical session: Intro homework (Max)

# Motivation of Keane & Wolpin

What is the research question?

Set-up

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### Explain schooling & career choices ("human K investment")

- school
- white / blue collar work
- military
- home production

Policy Evaluations: Impact of tuition subsidy

# Motivation of Keane & Wolpin

**Assumptions?** Alternatives? Atheoretic answers?

What **choices** does paper model?



Set-up

### Rewards of choice

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Set-up

■ How are the rewards of choices modelled?

### Rewards of choice

### (1) Wage

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- $\blacksquare$  occupation-specific skill heterogeneity  $e_m(a)$
- $\blacksquare$  schooling g(a)
- $\blacksquare$  experience in occupation  $x_m(a)$  quadratic
- unobserved endowments at age 16  $e_m(16)$
- cross-experience terms (what?)- see Section (III)
- (2) non-monetary "rewards"
  - effort cost of schooling
  - home "production" (what?)

# Unobserved heterogeneity

How modelled in Keane & Wolpin?

Set-up

# <u>Unobserved</u> heterogeneity (types)

#### Individual "fixed" effects very **interactive**

- $\bullet$   $e_{mk}$  are K types of initial endowments in diff occupations
- initial diffs create diff comp advantage
- link to initial schooling (initial conditions)?

Set-up

# Schooling choices & technology

Schooling in model?

Set-up

# Schooling choices & technology

### **Costs of schooling**

- monetary tuition fees (college & graduate)
- current period effort cost
- individual cost of schooling via  $e_4(16)$

What are benefits of schooling?

Set-up

# State-space

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Set-up

What is state-space?

## State-space

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Set-up

At any point in time t, observe

- past choices
- initial conditions
- current shocks

... how do individuals choose what to do?

### Choices

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Set-up

#### Choices made subject to

- draw shocks
- compare expected value of actions Value functions.

(more on **solution method** in a minute)

### Structure of Model

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Set-up

Assumptions, **Alternatives**, Atheoretic answers? What alternative assumptions could you imagine?

- Preferences
- Technology/ Market
- General structure are processes missing?

### **Alternatives**

Set-up

#### **Preferences**

- non-monetary prefs over activities (edu ?) may change over time
- people care not only about themselves
  - people conform to norms
- people may care about risk
- people may be myopic or backwardlooking
- people may dislike specific occupation

### Alternatives II

Set-up

### **Technology**

- information maybe imperfect
- hours choice may be possible

#### Market

- labour demand?
- transitions not always voluntary (labor market frictions)
- single agent model (cf. BLP or search model)

### Structure of Model

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Assumptions, Alternatives, **Atheoretic answers**? What atheoretic strategies for this research question?

1 OLS

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- Exogenous schooling & occupations Quasi-experimental IV- and panel literature.
- 3 Static discrete choice: model multinomial choice

# Less structural approaches II

Estimates of rates of return to education (RORE) are...

Set-up

**OLS-estimated returns** to educ'n/experience/occupations: biased if **unobserved factors** influence

- schooling choice & earnings
- **2 selection** into work & experience.
- selection into occupations

Here: **model selection** into schooling, experience, occupational choice.

Alternative?



Set-up

### Identification

How is the model identified?

Set-up

## Transitions between activities over age

- schooling becomes less frequent
- working increases.

### Occupational differences in transition trends

- blue-collar work occurs often at low ages
- blue-collars hardly increase after age of 22

### Earnings evolution over age & transitions

- voluntary transitions / persistence must be incentivised
- what about non-monetary costs/rewards?



### Identification

- What can explain wage growth in occupation?
- What role for measurement error in wages?
- What can explain high persistence in activities ?
- What can identify discount factor?

### Identification

Set-up

What can explain wage growth in occupation?

- experience & age
- no job-to-job transitions (no wage variance in occup'n)
- no bargaining, no promotions

What role for **measurement error** in wages?

variance of measurem't error smooths predictions (deal with outlier) - see FN 25.

#### Persistence?



How to get a good fit? see Figures 1-5 in paper.

## Extended model: More persistence

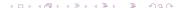
Persistence in choices **stronger than model** predicts.

How to fix the fit?



### Extended model: More persistence

- Occupation switching costs. Drop in earnings on leaving sector for a year
- Occupation-specific non-monetary costs interpretation ?
- 3 age-specific home term (young people couch premium ?) or involuntary unemployment?
- 4 "psychic" graduation effect non-monetary schooling return



# Results of augmented model

- Importance of initial endowments (types) for w-var
- Measurement error "accounts for" 40% of total w-var
- 3 Experience terms are important and heterogenous.
- No diploma effect on wages (warm glow? employment?)
- Monetary job search costs are significant.
- 6 How to interpret Table 12?

### Solution methods

Compare Rust to Keane & Wolpin solution methods.

# Keane & Wolpin

Set-up

Dynamic Bellman equation:

$$V_{t}(S_{i,t},\theta) = \max_{d(S_{i,t})} E\left[\sum_{t=\tau}^{T} \beta^{t-\tau} u_{\tau}(d_{t}, X_{i,t}, \theta) + \varepsilon\right]$$
$$= \max_{d(S_{i,t})} \left[u_{t}(d_{t}, X_{i,t}, \theta) + \beta E\left[V_{t+1}(S_{i,t}, \theta) | X_{i,t}, d_{t}\right]\right]$$

### Conditional independence:

- Dynamic term  $\beta E \left[ V_{t+1}(S_{i,t},\theta) | X_{i,t}, d_t \right]$  indep of shock
- choice-reward combinations dep on current state-space

How to calculate  $\beta E[V_{t+1}(S_{i,t},\theta)|X_{i,t},d_t]$ ?



# Solving for values

Set-up

Infinite horizon (Rust)

seek fixed point

Finite horizon (Keane & Wolpin)

backward induction

### Backward induction

(1) Optimal policy  $\delta^*$  for final period problem simple

$$V_{t}(S_{i,t},\theta) = \max_{d(S_{i,t})} \left[ u_{t}(d_{t}, X_{i,t}, \theta) \right]$$
  
$$\delta_{T}^{*}(S_{i,T}, \theta) = \operatorname{argmax}_{dT} \left[ u_{T}(d_{T}, X_{i,T}, \theta) + \varepsilon_{i,d_{T}} \right]$$

(2) in period T-1

$$E\left[V_{t}(S_{i,t},\theta)|X_{i,T-1},d_{i,T-1}\right] = \int \int \left[u_{T}(\delta_{T}^{*}(S_{i,T},\theta),X_{i,t},\theta) + \varepsilon_{i,\delta_{T}^{*}}\right] dF_{\varepsilon} dF_{X}(X_{T}|X_{i,T-1},d_{T-1})$$

What to do about those integrals?

### Backward induction II

What to do about those integrals?

Integrate idiosyncratic shock: assume  $\varepsilon$  is EV(1)

$$\int \left[ u_{T}(.), X_{i,t}, \theta) + \varepsilon_{i,\delta_{T}^{*}} \right] dF_{\varepsilon} = log \left( \sum_{d_{T}} e^{u_{T}(d_{T}, X_{i,T,\theta})} \right) + \gamma$$

Integrate future state space (over  $F(X_T|X_{i,T-1},d_{T-1}))$ ?

### Backward induction II

Theory: **Evaluate** choice prob's at **all points**.

- $\blacksquare$  if  $X_{i,t}$  has 5 binary variables
- $\blacksquare$  if  $X_{i,t}$  has 10 variables with 3 values

By how much does state space grow?

### Backward induction III

Theory: **Evaluate** choice prob's at **all points**.

- if  $X_{i,t}$  has 5 binary variables =2<sup>5</sup>=32 values for each t.
- if  $X_{i,t}$  has 10 variables with 3 values =  $3^{10}$  = **59,049** values for each t.

Numerical challenge increases (fast!) in state space

# Interpolating

Set-up

Backward induction in practice:

- Solve at subset of grid points
- Impute value (interpolate) at other points

With optimal policy at T-1, go to T-2...

Keane & Wolpin interpolate **both integrals** - why?

- 1 Draw R vectors of shocks (one for each alternative)  $\varepsilon_{1,T},...,\varepsilon_{M,T}$  for T.
- 2 Evaluate the maximum for each draw of R.
- 3 Average of R draws: expected maximum (EMAX)

$$V_T(x) = \frac{1}{R} \sum_{r=1}^{R} max_d \ u_T(d, x, \epsilon_T^r(d))$$

4 then calculate  $V_{T-1}(x)$  in T-1

$$= \frac{1}{R} \sum_{r=1}^{R} max_{d} \left[ u_{T-1}(d, x, \epsilon_{T-1}^{r}(d)) + \beta \sum_{x} {}_{i,T}V_{T}(x_{i,T}) F(x_{i}, T | x_{i,T-1}, d) \right]$$

This simulates EMAX for R specific points  $\varepsilon$ .



## Simulate & Interpolate II

Select R grid-points (specific values of X) and impute EMAX for others, e.g.

$$V_t(x_1 = 1, x_2 = 10, x_3 = ln(1000)) = 125$$
  
 $V_t(x_1 = 2, x_2 = 100, x_3 = ln(2000)) = 500$ 

Establish link between **EMAX** and state space

$$V_t(x_{k,t}) = \alpha_1 x + \alpha_2 x^2 + ... + \xi_{k,t}$$

# Simulate & Interpolate (last slide)

Then, estimate predicted EMAX for actual individuals using  $\hat{\alpha}$ .

$$\hat{V}_t(x_{i,t}) = \hat{\alpha_1} x_{i,t} + \hat{\alpha_2} x^2 + \dots$$
 (1)

10 minutes break