# Structural Econometrics in Labour and IO Job Search II - Equilibrium Job Search

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7th July 2022



# Organisation

#### Some organizational points:

- Exam on Thursday 14th July, 2-5pm (if you must)
- please bring pen & paper (maybe a crayon for figures?)
- Please evaluate your teachers
   Evaluation forms will be made available on github.
   Email Juliane JMetzner@diw.de
   (Evaluation is anonymous as far as possible.)

#### Outline

- Motivation of B-M
- Assumptions of B-M
- 3 Equilibrium: Discussion of problem set
- 4 Identification and Estimation

#### Motivation of Burdett-Mortensen Model

What can Burdett & Mortensen explain?



#### Motivation of Burdett-Mortensen Model

#### What can Burdett & Mortensen explain?

- Wage inequality despite equal characteristics
- involuntary unemployment
- the "firm-size effect" in wages
- the "experience effect" in wages
- the "firm effect" in wage

#### Motivation of Burdett-Mortensen Model

- (1) Wage inequality despite
  - (ex ante) homogeneous workers
  - (ex ante) homogeneous firms
- (2) Good & bad luck in stochastic labour market
  - why people are happy to get job
  - search unemployment is involuntary & random



#### Motivation of Burdett-Mortensen II

- (3) "firmsize effect" in wages
  - what is this?
- (4) "experience effect" in wages
- (5) "firm effect" in wages

#### Assumptions of Burdett & Mortensen

Characterize the assumptions made by Burdett & Mortensen.

#### Assumptions of Burdett & Mortensen

#### **Assumptions**

- homogeneous workers & firms
- wage posting no bargaining
- job offers arrive for unemployed at Poisson rate  $\lambda_0$
- on-the-job search: offers arrive at rate  $\lambda_1$
- jobs destroyed at Poisson rate  $\delta$
- constant benefits in unemplyment wages & (Why ?)

## Alternative assumptions

Who is competing in the labour market in Burdett & Mortensen?

## Alternative assumptions

How does Burdett & Mortensen relate to models with **more** / **less competition**?

#### Alternative assumptions II

Perfect Competition & Monopsony **nested in B-M** 

- Monopsony:  $\lambda_1 = 0$
- Perfect competition:  $\lambda_1 = \infty$

What happens in the B-M framework if we set  $\lambda_1 = 0$  ?

# Diamond paradox

Without on-the-job search ( $\lambda_1 = 0$ )...

**firms set**  $w = w^R$  - despite frictions.

Why?

# Diamond paradox II

Why do firms set monopsony wage despite search?

#### Firms have no benefit of higher wage

- Cannot attract more individuals.
- $\bullet$  I(w) = I

What might induce firms to set higher wages?

# Diamond paradox III

#### Rationale: Reservation wage heterogeneity

- among unemployed (Albrecht-Axell 1984)
- by on-the-job search (Burdett-Mortensen)

Alternative solutions?

# Diamond paradox III

#### Rationale: Reservation wage heterogeneity

- among unemployed
- by on-the-job search

Alternative solutions for supra- $w^R$  wages?

Efficiency wages (Lazear, Akerlof, Stiglitz)



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# Equilibrium in BM model

What does it mean that BM is an "equilibrium model"?

## Equilibrium in BM model

Equilibrium between workers' and firms' strategies

- workers choose res-wage given wage distribution
- firm set wages given (i) workers' (ii) other firms' strategies

Steady state conditions?

#### (Q1.1) Lowest wage on market

Distinguish equilibrium wage ( $\geq w^R$ ) from other wage strategies.

# (Q1.2) Briefly describe workers' strategies

What is unemployed workers' strategy?

# Unemployed workers' strategy

Strategy in stationary infinite horizon...

- To find  $w^R$ , evaluate value functions... (how ?)
- using  $\overline{F} \equiv 1 F$  find:

$$w^R = b + (\lambda_0 - \lambda_1) \int_{w^R} \frac{\overline{F}(w')}{r + \delta + \lambda_1 \overline{F}(w')} dw'$$

- What is the intuition for this expression?
- Why is  $w^R = b$  if  $\lambda_0 = \lambda_1$ ?



# (Q1.2) Employed Workers' strategy

What is employed workers' strategy?

# Employed Workers' strategy II

#### What is workers' strategy?

- Workers' reservation wage is current wage.
- Why?

## (Q1.3) Duration in a job

How long do people stay in a job?

#### (Q1.3) Duration in a job

Depends on the wage...

$$\frac{1}{\delta + \lambda_1 \left( 1 - F(w) \right)} \tag{1}$$

# (Q1.4) What is population wage density?

Strategies to transform offer to population distribution:

Strategy 1: Consider flows of workers earning w

$$\left[\delta + \lambda_1 \; \overline{F}(w)\right] \; g(w) \; (1-u) = u \; \lambda_0 \; f(w) + (1-u) \; G(w) \; \lambda_1 \; f(w)$$

then use flows of workers earning up to w

$$u \lambda_0 F(w) = (1 - u) G(w) \left[\delta + \lambda_1 \overline{F}(w)\right] G(w) = \frac{F(w)}{\left(1 + \frac{\lambda_1}{\delta} \overline{F}(w)\right)}$$

using  $u = \frac{\delta}{\delta + \lambda_0}$ .

Strategy 2: Use expression of G(w) and differentiate. (1. or 2.) find:

$$g(w) = \frac{f(w)}{\left[1 + \kappa_1 \; \overline{F}(w)\right]^2}$$

## Pop'n w-density to get profits

Now have I(w) as function of **observables** 

- firm may see g(w) (statistics / market research)
- can get f(w) from g(w) and transitional dynamics
- => Now have  $\pi$  as function of observables

Which wage level maximizes profits?



#### Wage inequality

**Wage dispersion** with equal profits: margin vs. volume:

- - more employees
  - less profits per employee
- **2** low wage-firms  $\Pi_b$ 
  - fewer employees
  - higher profits per employee

Explains true wage inequality Explains correlates of wages:

• firm, firm-size, experience effects

Logic. Is it realistic?



# Wage dispersion

Firms w diff. strategies appears realistic

- Large firms pay & retain
- small firms exploit & let go.
- worker density increasing on support of F(.)

Random matching of workers maybe less realistic

What about the "**tenure effects**" in wages? What about counter-offers?



# (Q1.5) What if counter-offers possible?

Search model with **counter-offers** (Postel-Vinay & Robin 2002)

- no incentive to pay above-w<sup>R</sup>
- still get wage inequality what will it depend on?

# (Q1.5) What if counter-offers possible?

Search model with counter-offers (Postel-Vinay & Robin 2002)

- no incentive to pay above-w<sup>R</sup>:
   can now wait until firm with higher wage comes
- still get wage inequality what will it depend on? wages rise with tenure - why?

#### Problem set

Any questions on theory part of problem set?

Motivation of B-M
Assumptions of B-M
Equilibrium: Discussion of problem set

#### Pausa

10 min break

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#### Identification

What is identification?

#### Identification of BM model

What data do we need to identify the model?

#### Identification from cross-sectional data

In the problem set, you simulated **observed wages and unemployment durations**.

Can we recover all **model primitives from the simulated** data?

#### Identification from cross-sectional data

Can we identify the model from the simulated data?

- Not non-parametrically, unless we observe all wages sampled from F (Flinn and Heckman, 1982)
- Parametrically, yes. We have to assume that F belongs to some parametric family (e.g. Normal distribution).