

Class 24 加强练习 3 (Recursion III)

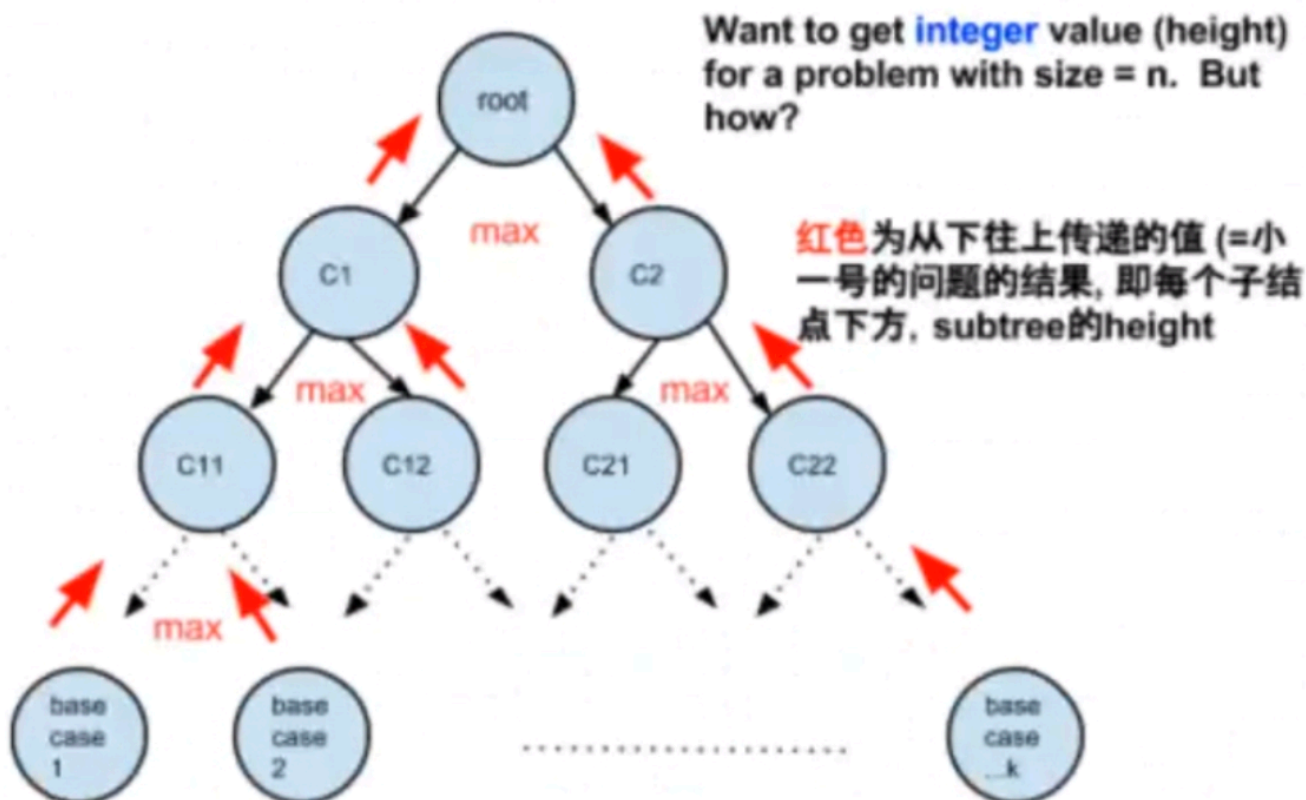
Q1. Tree + Recursion 第一类问题:

Use recursion to return values in a bottom-up way in binary tree

Q1.1 Determine whether a binary tree is a balanced binary tree (**$O(n \log n)$** solution).

What's the definition of "balanced"? It could be:

- the tree has a minimum possible overall height
- no leaf is too further away, i.e. 0 or 1, from root than any other leaf
- **left and right sub-trees have similar height, i.e. difference is 0 or 1 (balanced height)**

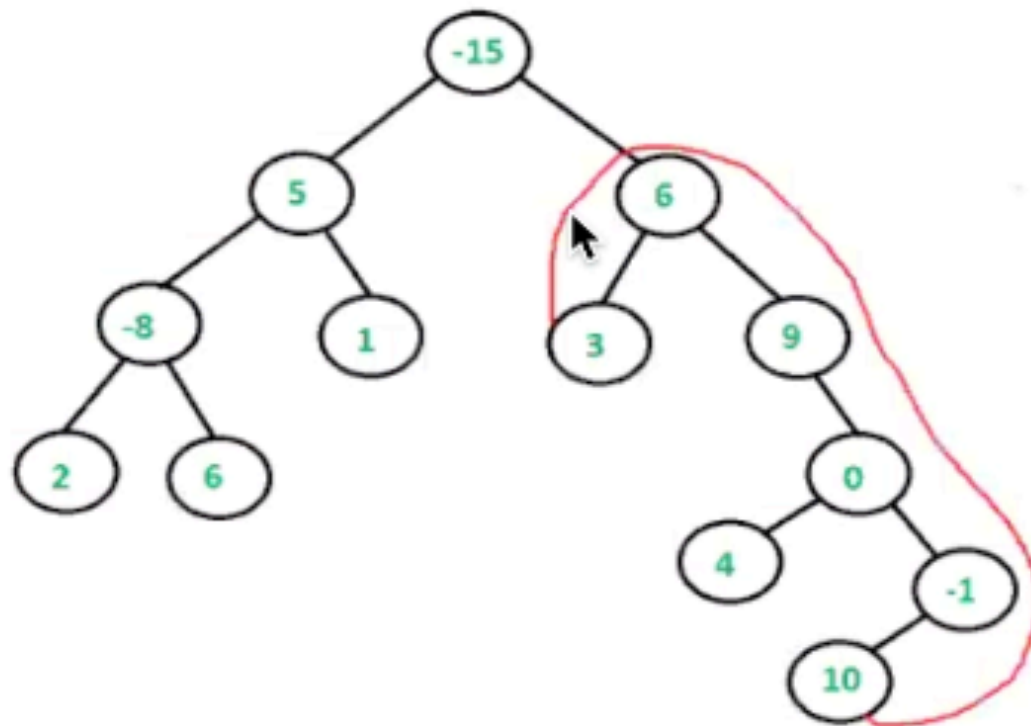


Q1.3 Midterm 2 question 2 (重复强调, 简要复习)

Given a binary tree in which each node element contains a number. Find the maximum possible sum **from one leaf node to another**.

The maximum sum path may or may not go through root. For example, in the following binary tree, the maximum sum is 27($3 + 6 + 9 + 0 - 1 + 10$). Expected time complexity is $O(n)$.





Way of thinking (Tricks)

1. What do you expect from your lchild / rchild?

Max single path in my left subtree (1)

Max single path in my right subtree (2)

2. What do you want to do in the current layer?

update `global_max` = `left` + `right` + `root.value` if feasible

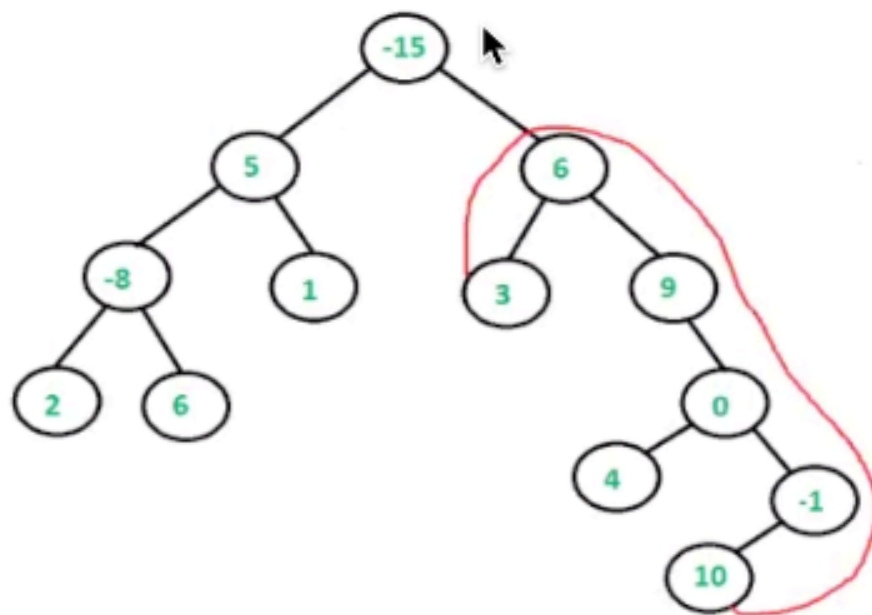
3. What do you want to report to your parent? (same as Q1 == Q3)

it is usually the return type of the Recursion function

Q1.4 (人字形path 问题)

Laicode.com Class 20 (Maximum Path Sum Binary Tree II)

Get Maximum sum of the path cost from **any node to any node** (not necessarily from leaf to leaf)



Way of thinking (Tricks)

1. What do you expect from your lchild / rchild?

Max single path in my left subtree [ended at the left child node] , if this value is negative, we discard it

Max single path in my right subtree [ended at the right child node] , if this value is negative, we discard it

2. What do you want to do in the current layer?

update `global_max = left + right + root.value` if feasible

3. What do you want to report to your parent? (same as Q1 == Q3)

it is usually the return type of the Recursion function

Q2. Tree + Recursion 第二类问题: (Path Problem in binary tree)

Discussion:

Note that: Tree 相关问题, 路径种类可以分为两大类

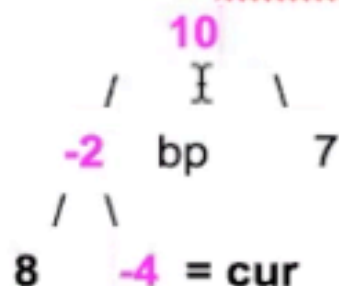
Class 1: 人字形path, 这类题一般需要从下往上传integer value (E.g., Q1.1 - 1.4 above)

Class 2: 从root 往下 (直上直下) path

Key point: carry a 直上直下 path prefix (非人字形) while traversing the tree:

a. complete path from leaf to root

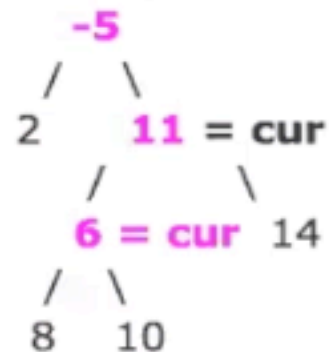
b. sub-section of complete path from leaf to root



Prefix_of_path = {10, -2, -4}

Q2.2 (laicode.com Class 20) Given a binary tree in which each node contains an integer number. Determine if there exists a path from any node to any node (**the two nodes can be the same node and they can only be on the path from root to one of the leaf nodes**), the sum of the numbers on the path is equal to the given target number.

Examples



If target = 17, There exists a path 11 + 6, the sum of the path is target,
 If target = 100, There does not exist any paths sum of which is target.

Solution 1:

path_prefix = {-5 11 6}
 ← cur
 6
 11 + 6
 (-5) + 11 + 6

Time = $O(n^2)$

Pre-order to iterate the whole tree, and for each current node X, we do a for loop in {X root}

Solution 2:

Pre-order to iterate the whole tree, and for each current node X, we do a for loop in {X root}.

path_prefix = {-5 11 6}

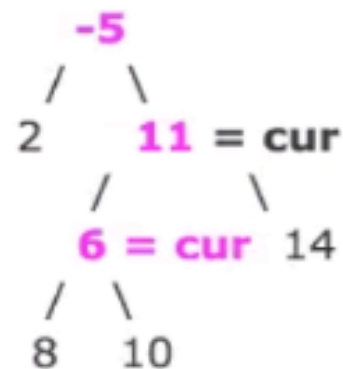
11+6=17



root
cur
 path_prefix = xxxxxxxxxxxx xxxxxxxxxxxxxxxxxxxxxxxx
another_path_prefix
target

another_path_prefix + target == path_prefix_to_current

another_path_prefix == path_prefix_to_current - target
12
17
= -5



path_prefix = {-5, 11, 6}

HashSet<path_prefix_sum> = {-5 6 12}

12 - target (17) = -5

We use a HashSet to store all path_prefix_sum.

Time = O(n)

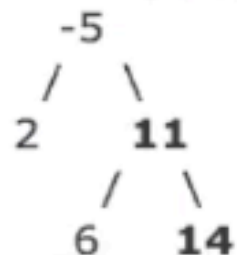
Q2.3 (laicode.com Class 20) **Maximum Path Sum Binary Tree III**

Given a binary tree in which each node contains an integer number. Find the maximum possible sum **from any node to any node (the two nodes can be the same node and they can only be on the path from root to one of the leaf nodes)**.

Assumptions

- The root of given binary tree is not null

Examples



The maximum path sum is $11 + 14 = 25$

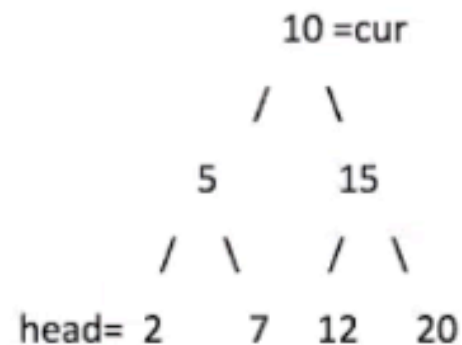
Solution 1 (DP max subarray sum) :

root cur
input = { x x x x **X X X X X X** x x x x x x x x x x }
sum →

```
public void helper(TreeNode root, int[] max, int sum) {  
    // base case  
    if (root == null) {  
        return;  
    }  
  
    if (sum < 0) {  
        sum = root.value;  
    } else {  
        sum += root.value;  
    }  
    max[0] = Math.max(max[0], sum); // this is actually a pre-order traversal. that's it!  
  
    helper(root.left, max, sum);  
    helper(root.right, max, sum);  
}
```

Q3. Tree + Recursion 第三类问题: Tree Serialization Problem

Q3.1. Given a Binary Tree, convert it to a Doubly Linked List(DLL) in in-order sequence.



Output: 2 <-> 5 <-> 7 <-> 10 <-> 12 <-> 15 <-> 20

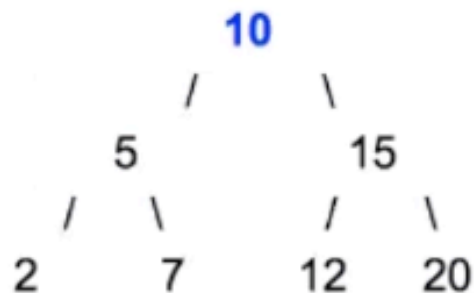
Discussion:

Reconstruct a tree by using xxx-order and **in-order** traversal sequences .

此类问题的要点就是把global 的问题一分为二(recursively), 每半边返回一个subtree的root node.



Q4.1 How to reconstruct a tree (with no duplicate values) with pre-order and **in-order** sequences of all nodes.



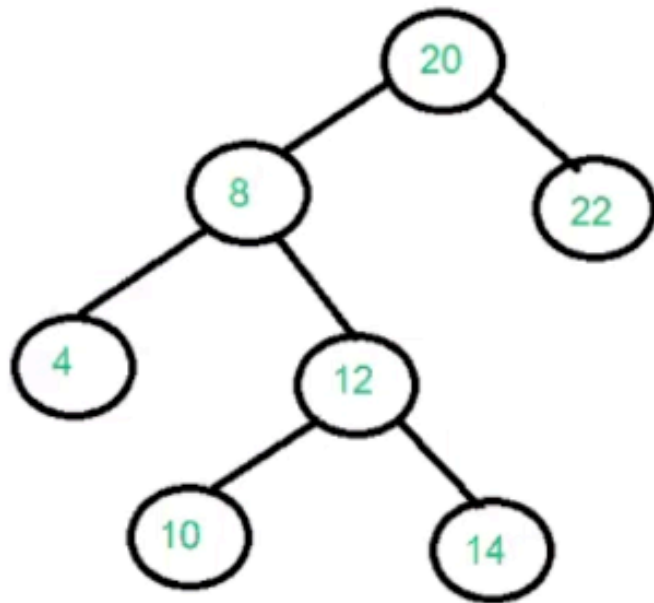
Index	0	1	2	3	4	5	6
Preorder:	10	5	2	7	15	12	20
<u>Inorder:</u>	2	5	7	10	12	15	20

inLeft == 0 idxMap[10] == 3 inRight

idxMap[10] - inLeft = 3 - 0 = 3 == leftSize

Q4.3 Construct a tree from **Inorder** and **Level** order traversals of **binary tree**

Given the inorder and level-order traversal sequences of a Binary Tree (**you can assume all unique numbers in the tree**), how to re-construct the Binary Tree.



Input: Two arrays that represent Inorder and level

order traversals of a Binary Tree

index= 0 1 2 3 4 5 6

in-order[] = {4, 8, 10, 12, 14, 20, 22};

level-order[] = {20, 8, 22, 4, 12, 10, 14};