



Crypto

Version 0.3

HANS@LAMMDA.SE 2023

Purpose of this presentation

Cryptography is generic and finds its way into components and processes.

Slides and code resides on github.

https://github.com/hans-lammda/azure_lab.git

Feel free to contact me for ideas and corrections.

hans@lammda.se

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Agenda

- **Intro**

- Cryptologi
- Cryptoanalysis

- **Symmetric keys**

- Historic encryption
- AES

- **Asymmetric keys**

- RSA

- **Hash**

- SHA, SALT

- **Applications**

- Certificate Authority
 - Policies, templates
 - Generate keypair , Certificate Sign Request, Issue certificates
 - Chain of trust
 - Revocation

Cryptography

Cryptography is the study of mathematical techniques related to aspects of information security such as confidentiality, data integrity, entity authentication, and data origin authentication.

Bruce Schneier Applied Cryptography

(The art of designing strong protocols and algorithms)

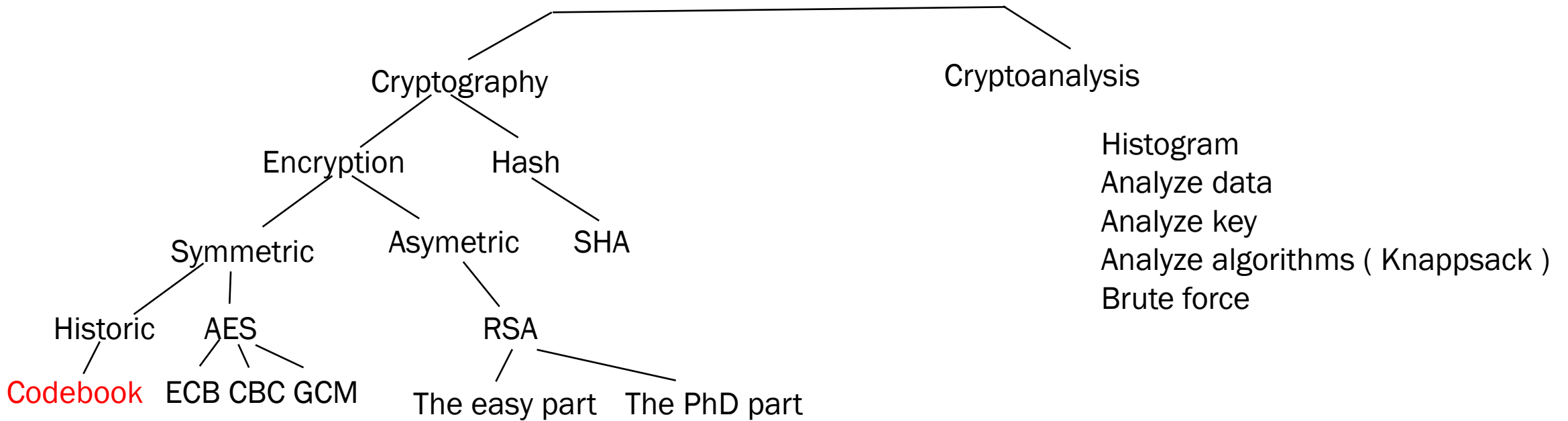
Cryptoanalysis

Cryptanalysis is the study of mathematical techniques for attempting to defeat cryptographic techniques, and, more generally, information security services.

Bruce Schneier Applied Cryptography

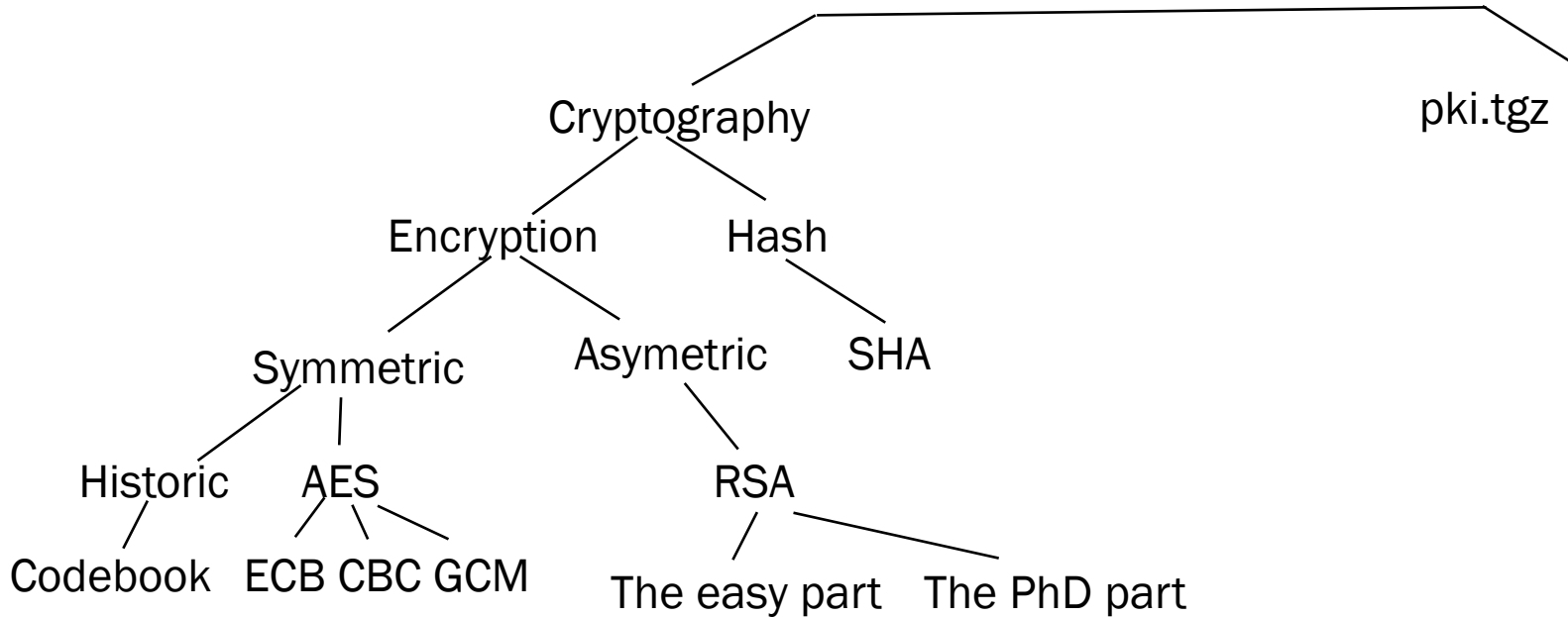
(The art of breaking strong protocols and algorithms)

Cryptology



[Knapsack problem - Wikipedia](#)

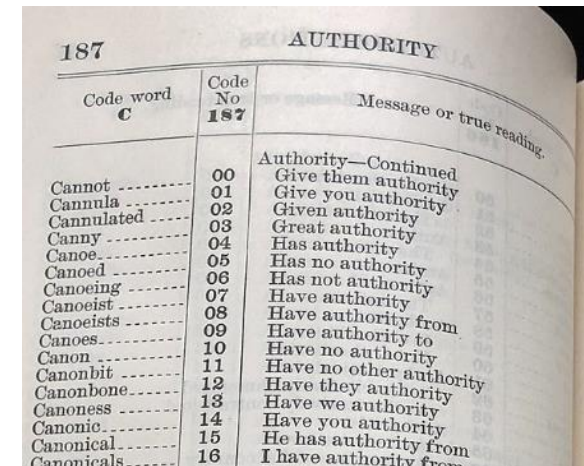
Code related to crypto



```
crypto/
├── aes
│   ├── aes_cbc.py
│   ├── aes_cgm.py
│   ├── aes_ecb.py
│   ├── crypt_decrypt.py
│   ├── Makefile
│   └── tux.bmp
├── ca
│   ├── ca.conf
│   ├── keygen.py
│   ├── Makefile
│   ├── openssl.cnf
│   ├── README.md
│   └── req.cnf
├── format
│   ├── keygen.py
│   ├── Makefile
│   └── ntoken.py
├── hash
│   ├── Makefile
│   └── sha256.py
└── rsa
    ├── Makefile
    ├── rsa.py
    └── simple.py
```

Codebook

substitution cipher, [data encryption](#) scheme in which units of the plaintext (generally single letters or pairs of letters of ordinary text) are replaced with other symbols or groups of symbols



Code word C	Code No 187	Message or true reading.
		Authority—Continued
Cannot	00	Give them authority
Cannula	01	Give you authority
Cannulated	02	Given authority
Canny	03	Great authority
Canoe	04	Has authority
Canoeed	05	Has no authority
Canoeing	06	Has not authority
Canoeist	07	Have authority
Canoeists	08	Have authority from
Canoes	09	Have authority to
Canon	10	Have no authority
Canonbit	11	Have no other authority
Canonbone	12	Have they authority
Canoneess	13	Have we authority
Canonic	14	Have you authority
Canonical	15	He has authority from
Canonicals	16	I have authority from

[substitution cipher](#) | [cryptology](#) | [Britannica](#)
[Codebook - Wikipedia](#)

Code books

Code is the ultimate method for "encryption"

Each letter in the plain text message is mapped to book with a table, where each entry is generated by true random

Each new letter , means new page

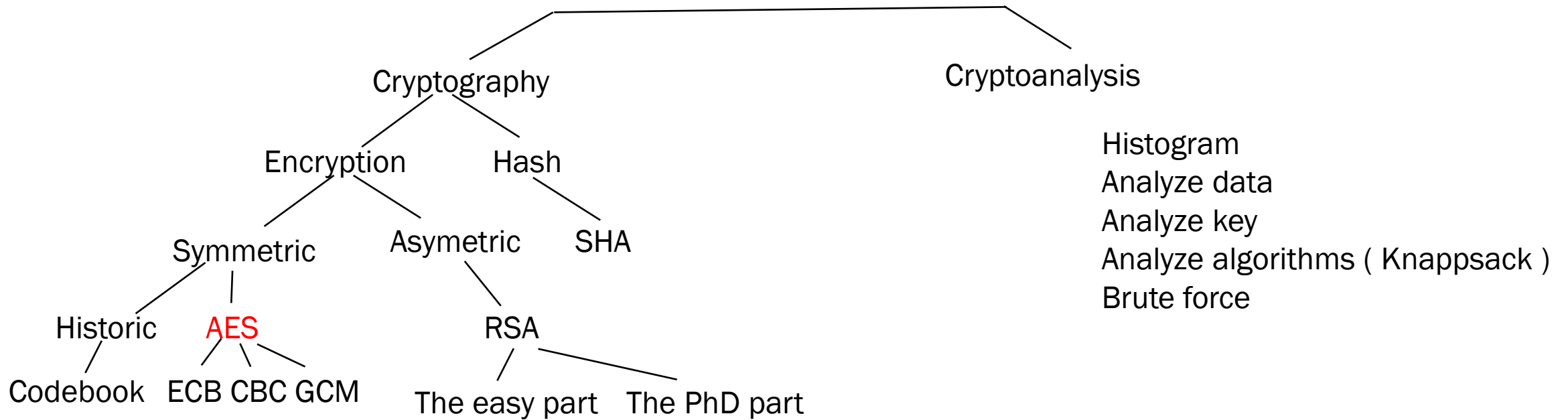
Never reuse the same page

Problem: Key distribution, performance



[Entropy - Wikipedia](#)

Cryptology



[Knapsack problem - Wikipedia](#)

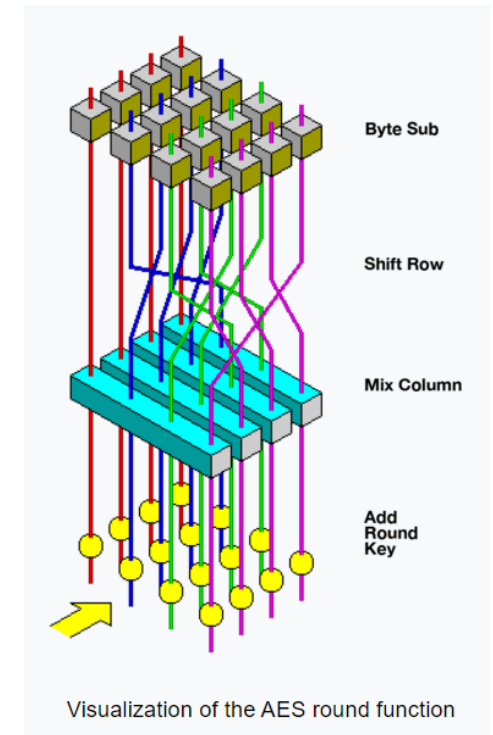
AES

High speed and low RAM requirements were some of the criteria of the AES selection process.

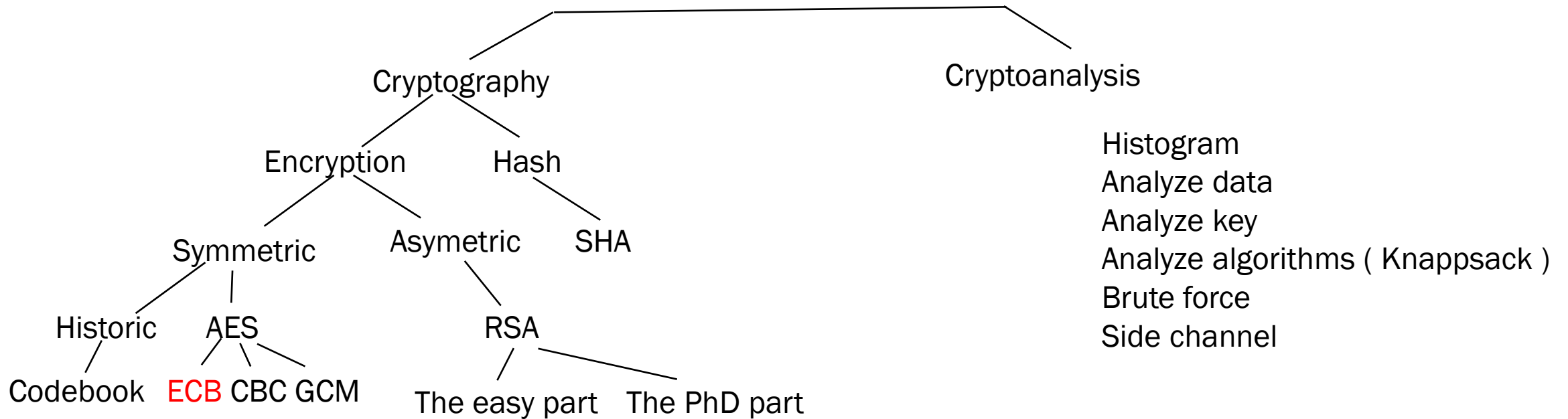
AES is included in the [ISO/IEC 18033-3](#)

Sidechannel attacks mostly related to software implementation.

[AES instruction set - Wikipedia](#)



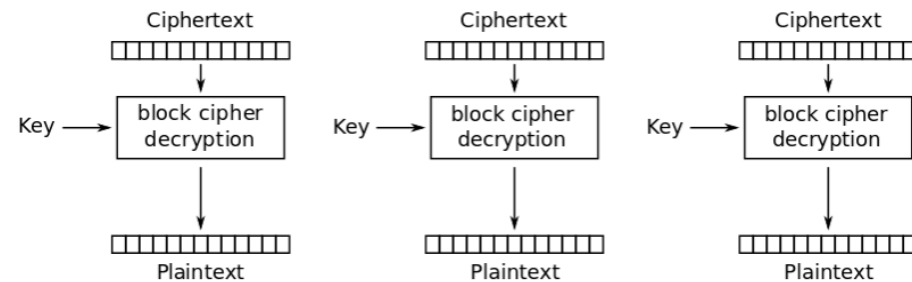
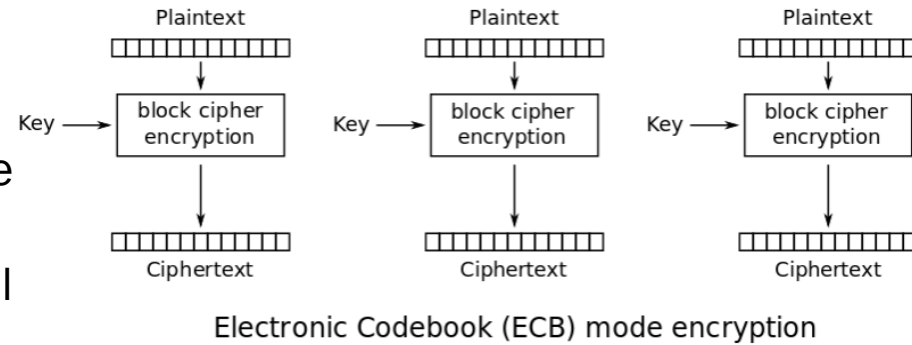
Cryptology



[Knapsack problem - Wikipedia](#)

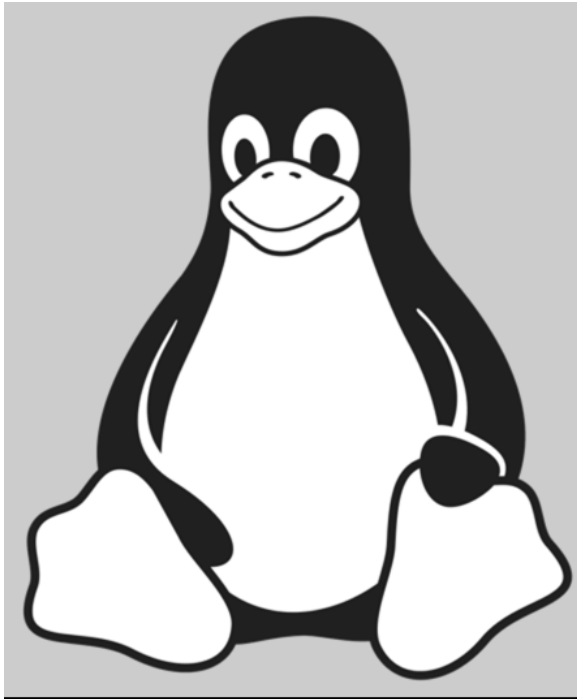
ECB

The simplest (and **not to be used anymore**) of the encryption modes is the **electronic codebook** (ECB) mode (named after conventional physical codebooks).



[Block cipher mode of operation - Wikipedia](#)

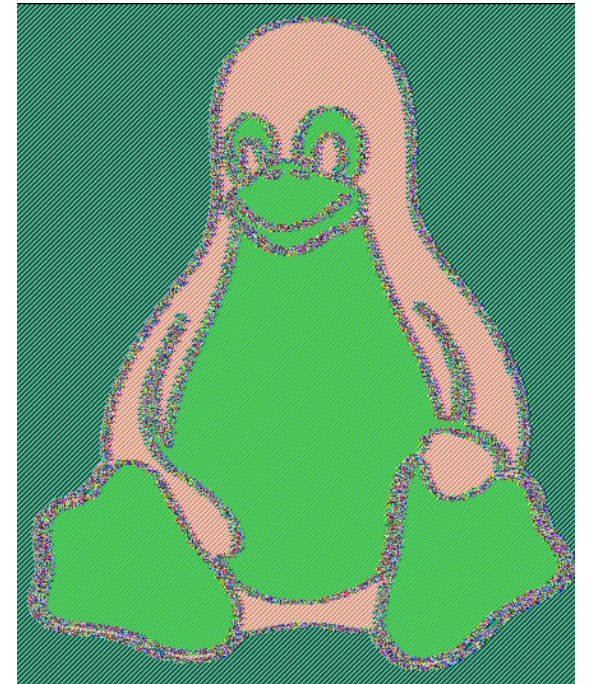
AES.MODE_ECB



```
from Crypto.Cipher import AES
import os

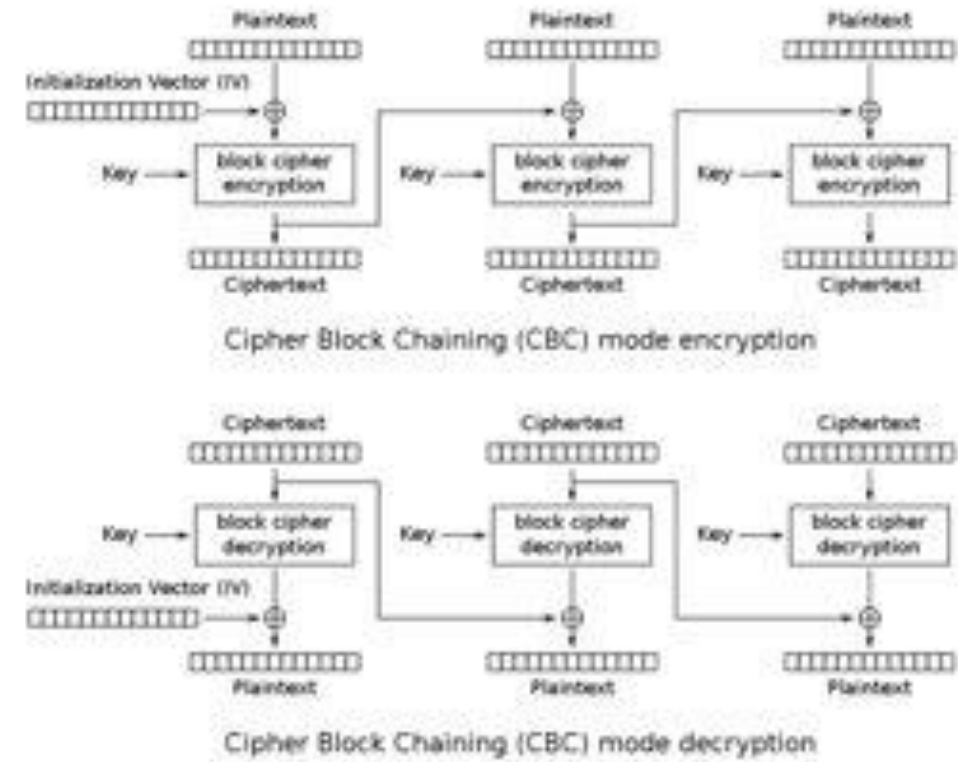
key=b"PASSWORDASSWORDASSWORDASSWORDXXX"
cipher = AES.new(key, AES.MODE_ECB)
with open("tux.bmp", "rb") as f:
    clear = f.read()
clear_trimmed = clear[64:-2]
ciphertext = cipher.encrypt(clear_trimmed)
ciphertext = clear[0:64] + ciphertext + clear[-2:]
with open("tux_ecb.bmp", "wb") as f:
    f.write(ciphertext)
```

Beware: AES library may contain deprecated encryption protocols like ECB



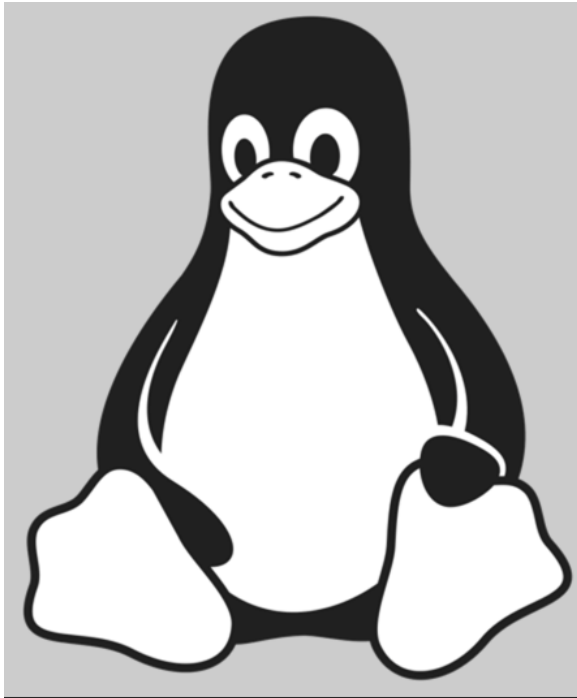
CBC

In CBC mode, each block of plaintext is [XORed](#) with the previous ciphertext block before being encrypted. This way, each ciphertext block depends on all plaintext blocks processed up to that point. To make each message unique, an [initialization vector](#) must be used in the first block.



[Block cipher mode of operation - Wikipedia](#)

AES.MODE_CBC



```
from Crypto.Cipher import AES
import os

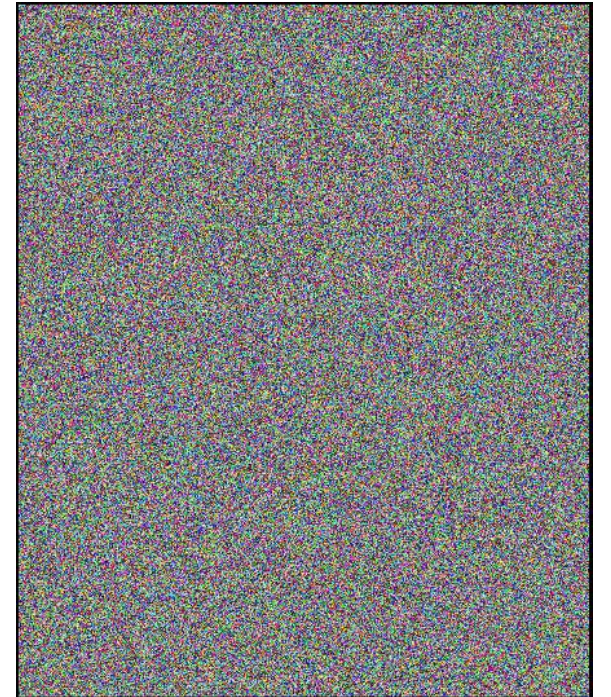
key=b"PASSWORDASSWORDASSWORDASSWORDXXX"

iv = b"0000111122223333"

cipher = AES.new(key, AES.MODE_CBC,iv)
with open("tux.bmp", "rb") as f:
    clear = f.read()

clear_trimmed = clear[64:-2]
ciphertext = cipher.encrypt(clear_trimmed)
ciphertext = clear[0:64] + ciphertext + clear[-2:]
with open("tux_cbc.bmp", "wb") as f:
    f.write(ciphertext)
```

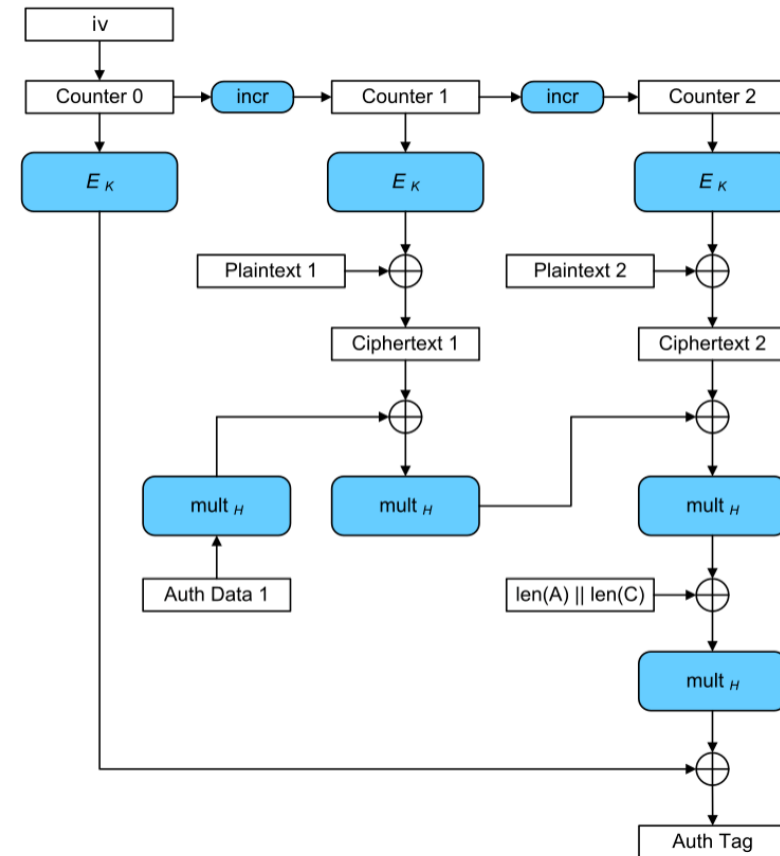
The initial vector should be randomized.



Galois Counter Mode

GCM is defined for block ciphers with a block size of 128 bits. Galois message authentication code (GMAC) is an authentication-only variant of the GCM which can form an incremental message authentication code. Both GCM and GMAC can accept initialization vectors of arbitrary length. GCM can take full advantage of parallel processing and implementing GCM can make efficient use of an [instruction pipeline](#) or a hardware pipeline.

[Block cipher mode of operation - Wikipedia](#)



AES.MODE_GCM

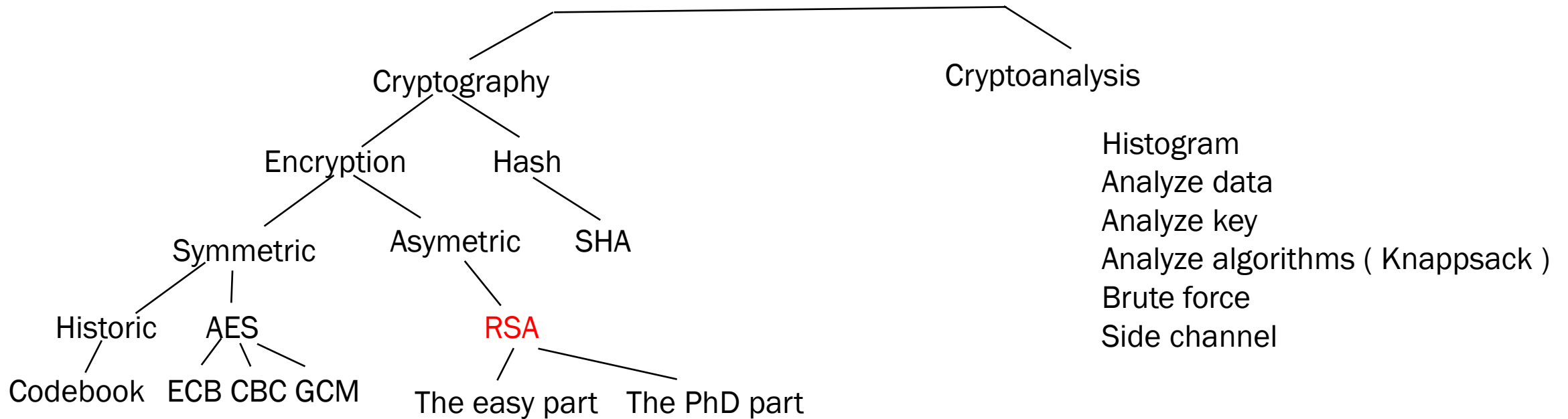
Note: Authenticated with salted password

```
import hashlib
import os
from Crypto.Cipher import AES
from Crypto.Random import get_random_bytes

password=b"Very_secret"
salt = get_random_bytes(32)
key = hashlib.scrypt(password, salt=salt, n=2**14, r=8, p=1, dklen=32)

mode = AES.MODE_GCM
plain = b"Nackademin 2022"
cipher = AES.new(key, mode)
ciphertext, tag = cipher.encrypt_and_digest(plain)
file_out = open("aes_cgm.bin", "wb")
[ file_out.write(x) for x in (cipher.nonce, tag, ciphertext) ]
file_out.close()
```

Cryptology



[Knapsack problem - Wikipedia](#)

RSA

Rivest
Shamir
Adleman

Inventor: [Ronald L. Rivest](#), [Adi Shamir](#), [Leonard M. Adleman](#)

Current Assignee : [Massachusetts Institute of Technology](#)

Worldwide applications

1977 • [US](#)

Application US05/860,586 events ⓘ

1977-12-14 • Application filed by Massachusetts Institute of Technology

1977-12-14 • Priority to US05/860,586

1983-09-20 • Application granted

1983-09-20 • Publication of US4405829A

2000-09-20 • Anticipated expiration

Status • Expired - Lifetime

[US4405829A - Cryptographic communications system and method - Google Patents](#)

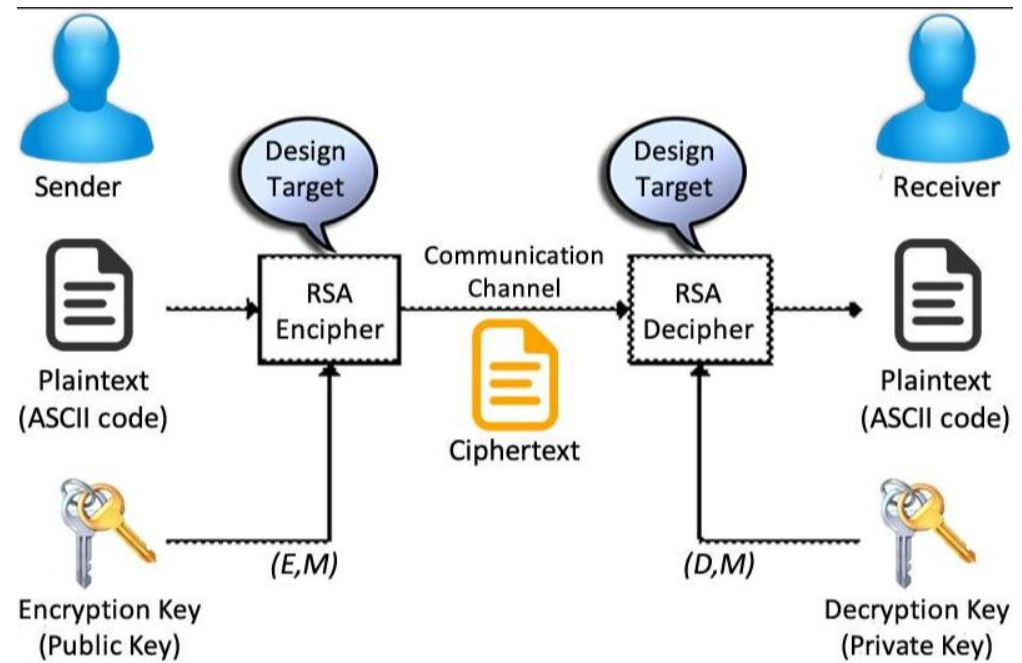
RSA inventive steps

One keypair for encryption
Another keypair for decryption

The encryption key is **public**, and could be distributed without risk

The decryption key is **private** should never be distributed

The private (D) and public (E) key have a common modulus (M). Therefore keypair.



Basic Math in Python

Short form of multiplication

Given two positive numbers, a and n, a modulo n is the **remainder** of the division of a by n, where a is the dividend and n is the divisor.

Power function

$$2^{**}2 = 4 \text{ (} 2*2 \text{)}$$

$$2^{**}3 = 8 \text{ (} 2*2*2 \text{)}$$

$$2^{**}4 = 16 \text{ (} 2*2*2*2 \text{)}$$

Modulo operator (%)

$$0 \% 2 = 0$$

$$1 \% 2 = 1$$

$$2 \% 2 = 0$$

$$3 \% 2 = 1$$

$$4 \% 2 = 0$$

$$5 \% 2 = 1$$

RSA keys are pair of integers

For practical use the numbers must be very large, for learning we keep it short.

The three integers are $e = 5$ $d = 11$ and $m = 14$

The private keypair is (11,14)

The public keypair is (5, 14)

RSA in python

```
def rsa(key, n, data):  
    return data ** key % n  
  
public    = 5  
private   = 11  
n = 14  
  
data = 2  
encrypted_data = rsa(public, n, data)  
decrypted_data = rsa(private, n, encrypted_data)  
  
print (f"\nInput: {data} encrypted with keypair ({public},{n}) becomes {encrypted_data}\n")  
print (f"\nInput: {encrypted_data} decrypted with keypair ({private},{n}) becomes {decrypted_data}\n")
```


Encrypt with RSA (1)

```
def rsa(key, n, data):  
    return data ** key % n
```

```
public   = 5  
private  = 11  
n = 14
```

```
data = 2  
encrypted_data = rsa(public, n, data)
```

```
rsa(5, 14, 2):  
    return 2 ** 5 % 14
```

```
2**5 = 32  
32 % 14 = 4
```

The encrypted data (2) becomes 4

Decrypt with RSA (1)

```
def rsa(key, n, data):  
    return data ** key % n
```

```
public    = 5  
private   = 11  
n         = 14
```

```
data      = 2  
encrypted_data = 4
```

```
rsa(11, 14, 4):  
    return 4 ** 11 % 14
```

```
4**11 = 4194304  
4194304 % 14 = 2
```

The decrypted data (4) becomes 2

Same algorithm
different
keypairs

Seems to simple, why grant them a patent ?

How about encrypting with the private key and decrypt with the public.

Encrypt with RSA (2)

```
def rsa(key, n, data):  
    return data ** key % n
```

```
public   = 5  
private  = 11  
n = 14
```

```
data = 2  
encrypted_data = rsa(public, n, data)
```

```
rsa(11, 14, 2):  
    return 2 ** 11 % 14
```

```
2**11 = 2048  
2048 % 14 = 4
```

The encrypted data (2) becomes 4

Encrypt with private key (11) instead of public (5)

Decrypt with RSA (2)

```
def rsa(key, n, data):  
    return data ** key % n
```

```
public    = 5  
private   = 11  
n = 14
```

```
data = 2  
encrypted_data = 4
```

```
rsa(5, 14, 4):  
    return 4 ** 5 % 14
```

```
4**5 = 1024  
1024 % 14 = 2
```

The decrypted data (4) becomes 2

Decrypt with public key (5) instead of private (11)

Math on PhD level

How does $e(5)$, $d(11)$ and (14) relates to each other

It starts with two numbers $p(2)$ and $q(7)$ where $p \cdot q = n(14)$

Claims (41)

Hide Dependent ^

We claim:

1. A cryptographic communications system comprising:

A. a communications channel,

B. an encoding means coupled to said channel and adapted for transforming a transmit message word signal M to a ciphertext word signal C and for transmitting C on said channel,

where M corresponds to a number representative of a message and

$$0 \leq M \leq n-1$$

where n is a composite number of the form

$$n = p \cdot q$$

where p and q are prime numbers, and

where C corresponds to a number representative of an enciphered form of said message and corresponds to

$$C \equiv M \cdot \text{sup} \cdot e \pmod{n}$$

where e is a number relatively prime to $1 \text{ cm}(p-1, q-1)$, and

Math on PhD level

5,11 and 14 could be used for encrypt / decrypt

$$2 * 7 = 14$$

How do get e (5) , two criteria

1. $1 < e < ((p-1) * (q-1))$
2. e should be coprime with $n(14)$ and $((p-1) * (q-1))$

Lets list all number between 1 and 6

1 , 2 , 3 . 4 . 5 . 6

1 should be excluded by nature

All even numbers higher than 2 are not prime numbers

2 and 3 are factors of 6

e must be smaller than $(2-1) * (7-1) = 6$

5 is the only candidate left , e is 5

Math on PhD level

(Coprimes)

How do we find all coprimes for n (14) ?

1. Start by listing all numbers between 1 and 14

1,2,3,4,5,6,7,8,9,10,11,12,13,14

2. Exclude even numbers

1,3,5,7,9,11,13

3. Skip q (7) since this is a factor in n .

Six numbers left in the list

1,3,5,9,11,13

$$2 * 7 = 14$$

$$(2-1) * (7-1) = 6$$

This formula is generic and is the inventive step.

$$(p-1) * (q-1)$$

Math on PhD level

Criteria for d according to the patent

$$d * e \% ((p-1)*(q-1)) = 1$$

Let's insert the numbers from our example $e=5$, $p=2$, $q=7$

$$e * 5 \% 6 = 1$$

Let's step e

$$e=1 > 1 * 5 \% 6 > 5$$

$$e=2 > 2 * 5 \% 6 > 4$$

$$e=3 > 3 * 5 \% 6 > 3$$

$$e=4 > 4 * 5 \% 6 > 2$$

$$e=5 > 5 * 5 \% 6 > 1$$

d and e have the same value (5) , lets continue

..

$$e=10 > 10 * 5 \% 6 > 2$$

$$e=11 > 11 * 5 \% 6 > 1 \quad (\text{Yes, we pick 11 for d})$$

Infinite number of prime numbers

Definition prime number: "A whole number greater than 1 that cannot be exactly divided by any whole number other than itself and 1"

Example: 1,2,3,5,7

Proof by contradiction: "If it is true that infinite number of primes exists, lets proof that there is not a finite number (n) of primes $P_1, P_2, P_3, \dots, P_n$.
"

$$N = P_1 * P_2 .. * P_{n-1} * P_n + 1$$

$$N/P_n = P_1 * P_2 * .. * P_{n-1} * P_n / P_n + 1/P_n = P_1 * P_2 * .. P_{n-1} + 1/P_n$$

Proof: If P_n is larger than 1 , then $1/P_n$ could not be a whole number.

Infinite number of prime numbers

Assume all prime numbers are [2,3,5,7]

$$N = P_1 * P_2 * P_{n-1} .. P_n + 1$$

$$N = 2*3*5*7 = 210 + 1 = 211$$

$$N/P_n = P_1*P_2*P_{(n-1)} + 1/P_n$$

$$211/7 = (2*3*5) + 1/7$$

$$30.1428571 = 30 + 0.1428571$$

Factors: 1, 11, 121

Factor Pairs: (1, 121) (11, 11)

Prime factors: 121 = 11 × 11

```
121
 | \
11 11
```

<https://www.calculator.net/factor-calculator.htm>

Future of RSA

Breaking RSA with a Quantum Computer

A group of Chinese researchers have [just published](#) a paper claiming that they can—although they have not yet done so—[break 2048-bit RSA](#). This is something to take seriously. It might not be correct, but it's not obviously wrong.

We have long known from Shor's algorithm that factoring with a quantum computer is easy. But it takes a big quantum computer, on the orders of millions of qubits, to factor anything resembling the key sizes we use today. What the researchers have done is combine classical lattice reduction factoring techniques with a quantum approximate optimization algorithm. This means that they only need a quantum computer with 372 qubits, which is well within what's possible today. (The [IBM Osprey](#) is a 433-qubit quantum computer, for example. Others are on their way as well.)

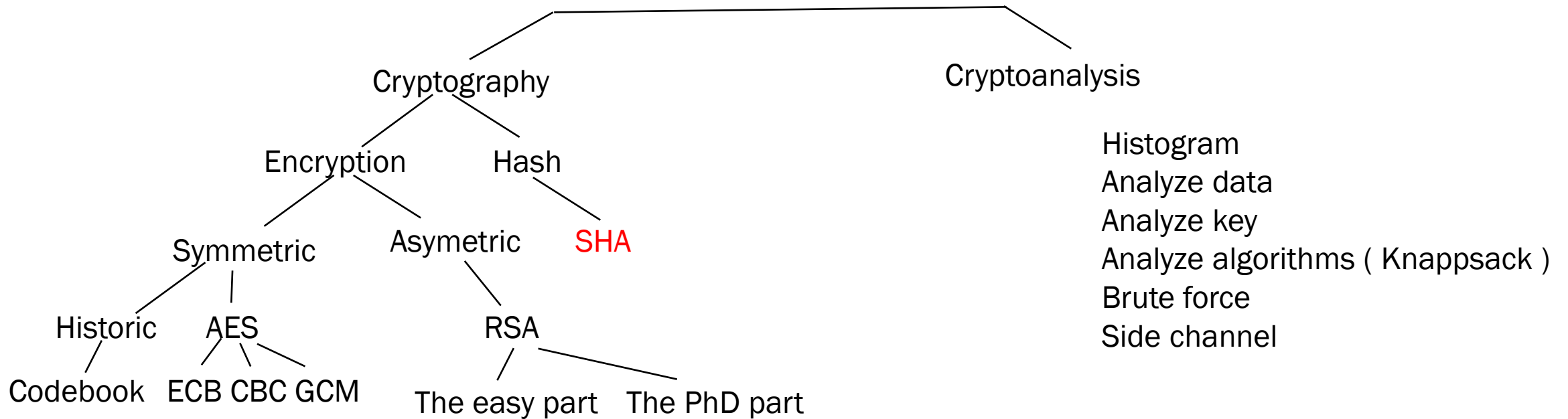
The Chinese group didn't have that large a quantum computer to work with. They were able to factor 48-bit numbers using a 10-qubit quantum computer. And while there are always potential problems when scaling something like this up by a factor of 50, there are no obvious barriers.

Honestly, most of the paper is over my head—both the lattice-reduction math and the quantum physics. And there's the nagging question of why the Chinese government didn't classify this research.

But...wow...maybe...and yikes! Or not.

<https://www.schneier.com/blog/archives/2023/01/breaking-rsa-with-a-quantum-computer.html>

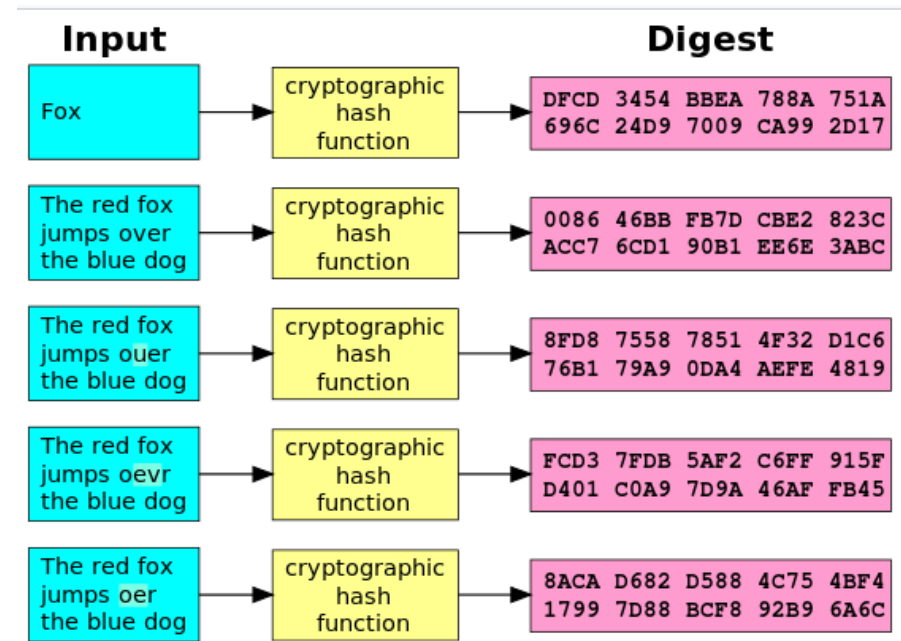
SHA (256, 384 , 512)



[Knapsack problem - Wikipedia](#)

HASH functions

A cryptographic hash function (specifically [SHA-1](#)) at work. A small change in the input (in the word "over") drastically changes the output (digest). This is the so-called [avalanche effect](#).



HASH and passwords

To authenticate a user, the password presented by the user is hashed and compared with the stored hash.

Testing a trial password or passphrase typically requires one hash operation. But if key stretching was used, the attacker must compute a strengthened key for each key they test, meaning there are 65,000 hashes to compute per test. This increases the attacker's workload by a factor of 65,000, approximately 2^{16} , which means the enhanced key is worth about 16 additional bits in key strength

[Key stretching - Wikipedia](#)

Brute force attacks:

Common [graphics processing units](#) can try billions of possible passwords each second.

HASH, Password and Salt

If users have the same password on many sites. The hashvalue will guide the attacker.

Username	String to be hashed	Hashed value = SHA256
user1	password123	57DB1253B68B6802B59A969F750FA32B60CB5CC8A3CB19B87DAC28F541DC4E2A
user2	password123	57DB1253B68B6802B59A969F750FA32B60CB5CC8A3CB19B87DAC28F541DC4E2A

Salt prevents simple reuse for the attacker.

Username	Salt value	String to be hashed	Hashed value = SHA256 (Password + Salt value)
user1	D;%yL9TS:5Pa1S/d	password123D;%yL9TS:5Pa1S/d	9C9B913EB1B6254F4737CE947EFD16F16E916F9D6EE5C1102A2002E48D4C88BD
user2)<,-<U(jLezy4j>*	password123)<,-<U(jLezy4j>*	6058B4EB46BD6487298B59440EC8E70EAE482239FF2B4E7CA69950DFBD5532F2

[Salt \(cryptography - Wikipedia\)](#)

Example

```
import hashlib

filename = "sha256.py"
with open(filename,"rb") as f:
    bytes = f.read()
    hash = hashlib.sha256(bytes).hexdigest();
print(hash)
```

```
cat sha256.py | sha256sum
```

```
cli: @cat sha256.py | sha256sum | awk '{print $$1}'
python: @python3 sha256.py
~
```

Formats for PKI

- **Overview**

- Same algorithms , different formats
- PEM
- JOSE

- **Applications for PKI**

- Encryption
- Signing
- CA Structure

Openssl

Not included by default in Windows
WSL2 offers integration with Linux
De-facto standard tool for crypto developers
Generate keys
Encrypt, hash, sign, CA etc



openssl.org

<https://learn.microsoft.com/en-us/azure/iot-hub/tutorial-x509-openssl>

[Create certificates for Azure Stack Edge Pro GPU via Azure PowerShell](#)

Generate keypair

RSA keys generated once,
exported in two different
formats

- PEM
- JWK

```
def keygen(pub_path, priv_path, kid):  
  
    public_key = jwk.JWK()  
  
    private_key = jwk.JWK.generate(kty='RSA', size=2048, kid=kid)  
  
    public_key.import_key(**json_decode(private_key.export_public()))  
  
    pem_pub = public_key.export_to_pem(private_key=False, password=None)  
    pem_pub = pem_pub.decode("utf-8")  
    pem_priv = private_key.export_to_pem(private_key=True, password=None)  
    pem_priv = pem_priv.decode("utf-8")  
  
    # openssl rsa -noout -text -inform PEM -in pub.pem -pubin  
  
    fp = open("%s.pem" % pub_path, "w")  
    fp.write(pem_pub)  
    fp.close()  
  
    fp = open("%s.jwk" % pub_path, "w")  
    fp.write(public_key.export())  
    fp.close()  
  
    fp = open("%s.pem" % priv_path, "w")  
    fp.write(pem_priv)  
    fp.close()  
  
    fp = open("%s.jwk" % priv_path, "w")  
    fp.write(private_key.export())  
    fp.close()  
    return
```

PEM Format

PEM is text files where the keys are base64 encoded

Example from a unencrypted private key.

----- BEGIN PRIVATE KEY -----

```
-----BEGIN PRIVATE KEY-----
MIIEvgIBADANBgkqhkiG9w0BAQEFAASCBgwggSkAgEAAoIBAQDaVH1je5dJZXeF
v1oq24AbJ09dQHqFT1rJIpd6fsrud0M2qBx+8lBTg9pTt05GP5fqDq02KjPYNqzP
8qTzANDFSr1WobZT+QgS5bVX+nhGLaUuw86LYvx5tmRMpjgRnj0/S0CJjggLwkS/
QCwFJq4gh+G9DrwoP0eo0dbksAJA9rzKBuwsAkJPMwdG5C8zRY7upwAsgYjHDcK6
pSD29M/CQeNCcLugZLHorwGo/ajxwVfGmBf0lVMc2UJsft7P3PKsgJ1vQFm4KuT
agz3LWqjzcf36nJAjJayL1krCQSuUn456PE3Re09d1pzW6/Ewrjli/CwoMT631JE
89+0Pb8PAgMBAECggEAE7hLG9L/U8DKoXwqfItKfQ+PLmdBjBjsMUlV9//Y/BFh
MvmbzheJPwULKw5avmH8d0aPr8AmFW+MZYfo2cE6gIEDEv6u0KcNcwkc1QjcsWU3
PnJiVIVxTakDH2BppgwhEHhCjw0shSHEPD+Wk9+6tvN7y/2EHy18Tkva jHNQimXU
F8GpLOVo2v5lefQ180rElNua/xJW5D25Gv4q/Xue/9kRCt5dX6hWmQ2TYpqf7c4
x8VhnqLSFPBTQxJAatrg4pbBBIIJvMcHCiJaJlJEDl8Y6FtXi/EhvlNhgqOg5hV
zlcFLUDXNIWKBWvt0FIkFKSL4UYL+4sVwgaBC2ebcQKBgQD1BlCf8jeTsG/EnLxc
jFpL6ET2uTt7pca4Q6Qjc62Wo0KZ5Gqy9y97J6xKz4gHje+c/nLgE2gZ4ELCKKDL
HR7qeytcQyMP06Q+POCL9QpGs9FGM2ItwVH0fkBCKCurbzMecnfStGT+YmkspI91
tTlOYc01K3DLGc08+Gd20GF96QKBgQDkHBGL5+PGxzSnFEogZwmBiuckYa7rcxe9
Ku2Zsd7up4KDZLXgMo/RMtTKM1Kq1pE51/nFgygAcPP00N/WGSJj1E/R0IWgU4/I
JmPQL6eblJSHDNuDYcz9Vuz99Bfk4vfoA7TL8ab3r4dwaXUvqoeOWOpBIggyXIop
Aaq3ioTiNwKBgB9cQ411Lu/UMTn05MHppNT6UXlSk+5rdVe4MJXpBFq3YprXxWBK
luU0WrTogvyUigqJ9qH/Wd+V+UpicNVi0MbCJPawETKt640bvXGqtzn9YdeeU/6P
M7IbRpy+ZMN+ZAiNlhB9zj9Q0S1JkqL6Tu+JS8cwXC62crJPCM70wGWhAoGBAN/e
yFc52SsaEIu1dvaMCSFQ8H6d0+2p2+90tREPfbLFRWquQb0yC8F1kK8NZaFyyb6q
P2Df0p90020LTVKzAJRVhyzU6IAR4l29h5InYuhnDsnoDxwtnjJAYIDwUY76TfEv
yf2qIYLOiy8A4NiyFS3YB7d6re63MYUDNMfDM51LAoGBAK8yQgCwccMRcxS2bBhi
tq+E0XIekYJP7ZW/cimU6s4QSHFgNMMAQoejBcB0L+C9cMVYQbgUUgToyw3RLQ0X
c33np7eTjGrQnsLyFc5fncB7PlyrUMRtutaeV97UzdWHsm47K76NsRX623gvlll
koyg2L6iSfTlYICl99FtLYtTV
-----END PRIVATE KEY-----
```

[Privacy-Enhanced Mail - Wikipedia](#)

PEM Format

RSA , e, d and n could be extracted with openssl
`openssl rsa -noout -modulus -in priv.pem`

```
Modulus=DA547D637B9749657785BF5A2ADB801B24EF5D407A9F4F5AC922977A7ECAEE774336A81C7EF2505383DA53B4EE463F97EA0EAD362A33D  
836ACFF2A4F300D0C54ABD56A1B653F90812E5B557FA78462DA52EC3CEA562FC79B6644CA638119E3D3F4B40898E080BC244BF402C0526AE2087  
E1BD0EBC283CE7A8D1D6E4B00240F6BCCA06EC2C02424F330746E42F33458EEEA7002C8188C70DC2BAA520F6F4CFC241E34270BBA064B1E8AF01A  
8FDA8F1C157C69817CE95531CD9426C7E9B7B3F73CAB20275BD0166E0AB936A0CF72D6AA3CDC7F7EA72408C96B22F592B0904AE527E39E8F13745  
E3BD775A735BAFC4C2B8E28BF0B0A0C4FADF5244F3DFB43DBF0F
```

JWK Format

If kty (Keytype is RSA) e, d and n
Are included in JSON.

(Also p and q)

```
{
  "d": "E7hLG9L_U8DKoXwqfItKfQ-PLmDbjBjsMUiv9__Y_BFhMvmbzheJPwULKw5avmH8d0aPr8AmFW-MZYfo2cE6gIEDEv6u_Xue_9kRCt5dX6hwWmQ2TYpqf7c4x8VhnqLSFPBTQxJAatrg4pbBBIIJvMCHCijaJljEDl8Y6FtXi_Ehvlinhqq0g5hVzlcflUDX",
  "dp": "H1xDjXUu79QxOfTkwenk1PpReVKT7mt1V7gwlekEWrdimtFYEqK5TRat0iC_JSKCon2of9Z35X5SmJw1WI4xsIk9pY",
  "dq": "397IVznZKxoQi7V29owJIVDwfp077anb73S1EQ8VssVFaq5Bs7ILwXWQrw1loXLJvqo_YN_Sn3Q7Y4tNurMCNFWHLNT",
  "e": "AQAB",
  "kid": "nackademin",
  "kty": "RSA",
  "n": "2lR9Y3uXSWV3hb9aKtuAGyTvXUB6n09aySKXen7K7ndDNqgcFvJQU4PaU7TuRj-X6g6tNioz2Dasz_Kk8wDQxUq9VqG29vTPwkHjQnC7oGSx6K8BqP2o8cFXxpgXzpVTHNlCbH6bez9zyrICdb0BZuCrk2oM9y1qo83H9-pyQIyWsi9ZKwkErLJ-OejxN0Xj",
  "p": "9QZQn_I3k7BvxJy13IxaS-hE9rk7e6XGuE0kI30tlqNCmeRqsvcveyesSs-IB43vnP5y4BNoGeBJQiig5R0e6nsrXEMj",
  "q": "5BwRpefjxsc0pxRKIGcJgYrnJGGu63MXvSrtmUne7qeCg2ZV4DKP0TLUyjnSqtAR0df5xYMoAHDzztDf1hkiY9RP0dCF",
  "qi": "rzJCALBxwxFzGzZsGGK2r4TRch6Rgk_tlb9yKZTqzhBIcWA0wxCgSMFwHQv4L1wxVhBuBRsB0jLDdEtDRdzfeent50"
}
```

[Javascript Object Signing and Encryption \(JOSE\) — jose 0.1 documentation](https://8gwifi.org/jwkconvertfunctions.jsp)
<https://8gwifi.org/jwkconvertfunctions.jsp>

CA

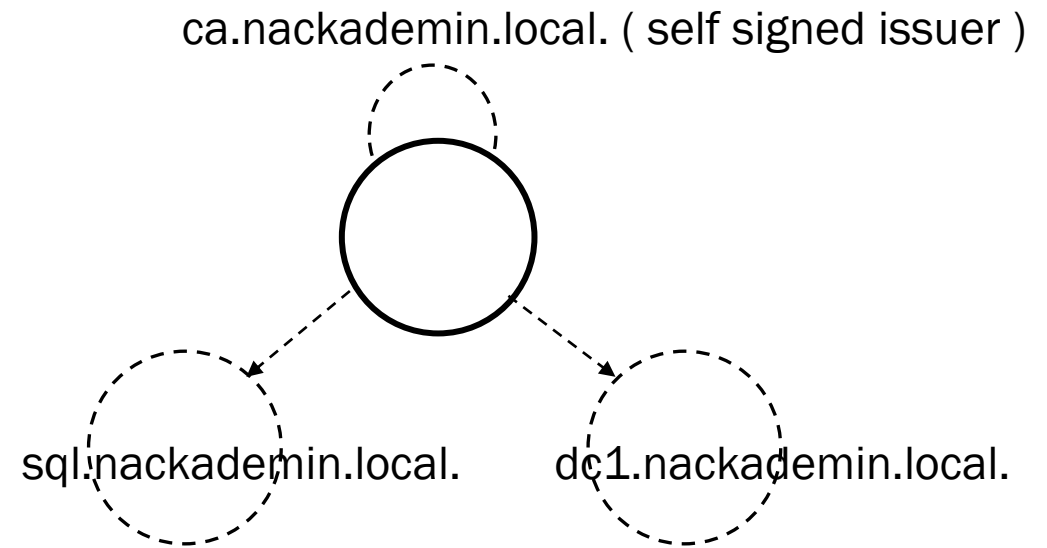
- **Overview**

- Signing

PKI

PKI is short for Public Key Infrastructure

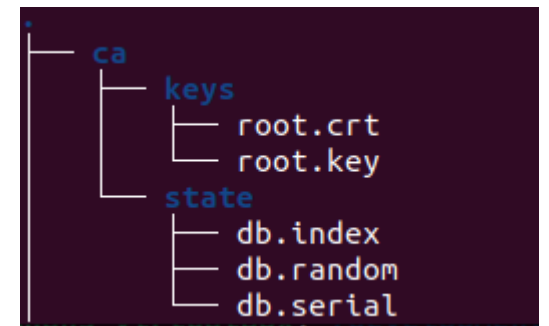
First step is to create a Certificate Authority that issues certificates for objects in the tree of domains.



PKI with Openssl

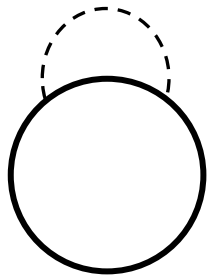
Openssl have functionality and templates for acting as a CA

```
touch ca/state/db.index
touch ca/state/db.random
openssl rand -hex 16 > ca/state/db.serial
openssl genrsa -out ca/keys/root.key 2048
openssl req -x509 -sha256 -new -nodes -key ca/keys/root.key -days 3650 -out
ca/keys/root.crt -config openssl.cnf
```



Self signed root certificate

Subject and Issuer are the same



ca.nackademin.local

```
Certificate:
Data:
  Version: 3 (0x2)
  Serial Number:
    0b:6e:7c:b3:a2:57:ab:0a:ce:a4:55:b5:c4:22:98:e7:bb:b7:e7:0c
  Signature Algorithm: sha256WithRSAEncryption
  Issuer: C = SE, ST = Stockholm, L = Nacka, O = Nackademin, OU = education, CN = ca.nackademin.local, emailAddress = hans.lamm@nackademin.se
  Validity
    Not Before: Nov 16 18:26:06 2022 GMT
    Not After : Nov 13 18:26:06 2032 GMT
  Subject: C = SE, ST = Stockholm, L = Nacka, O = Nackademin, OU = education, CN = ca.nackademin.local, emailAddress = hans.lamm@nackademin.se
  Subject Public Key Info:
    Public Key Algorithm: rsaEncryption
    Public-Key: (2048 bit)
    Modulus:
      00:c9:63:8d:6d:15:fe:90:e9:73:c6:e3:16:80:92:
      16:ad:2b:ac:46:6b:b6:b8:c1:8d:0d:a4:f8:57:84:
      2c:94:63:37:ab:1b:05:2d:1f:5f:80:03:87:64:d5:
      cb:fd:30:3c:73:73:34:94:a9:3e:3f:8b:00:c4:29:
      19:73:19:4d:39:31:20:82:58:24:77:6e:48:47:f5:
      f5:72:43:92:cc:f7:c1:8f:ad:32:7c:b7:1f:e7:75:
      b4:90:53:ca:4d:ce:54:46:3e:38:34:ab:c9:05:db:
      03:1d:f0:4e:cb:af:1e:c2:1e:6c:21:32:6a:6b:a0:
      04:f0:03:40:ef:bd:19:ca:5a:eb:f5:01:a8:15:57:
      4c:69:55:91:10:81:ed:db:af:38:6f:50:77:cf:0c:
      47:00:5b:0f:51:c6:c0:1e:1d:71:09:15:d2:d2:94:
      1b:8e:c8:74:2e:96:08:eb:d3:7c:fb:fd:fe:8c:31:
      9f:9e:1c:59:df:3e:82:de:3f:45:a6:da:04:e8:68:
      2d:4e:42:1e:ac:a9:fc:a1:12:3b:f8:8e:3d:62:ba:
      72:15:a4:60:7a:eb:b7:94:c6:dc:7c:7e:57:e1:db:
      c9:fc:ae:72:4c:4c:99:31:0f:1d:c6:ac:1f:77:c7:
      80:7f:f5:77:62:0e:aa:4a:3e:e1:54:31:8f:da:f9:
      f0:b7
    Exponent: 65537 (0x10001)
```

Policy / template for openssl

openssl req -x509 -sha256 -new -nodes -key ca/keys/root.key -days 3650 -out ca/keys/root.crt -config openssl.cnf

Some options passed as commands,
But most of them specified in policy file.

```
[ req_distinguished_name ]
countryName               = Country Name (2 letter code)
countryName_default       = SE
countryName_min           = 2
countryName_max           = 2

stateOrProvinceName       = State or Province Name (full name)
stateOrProvinceName_default = Stockholm

localityName              = Locality Name
localityName_default       = Nacka

0.organizationName        = Organization Name (eg, company)
0.organizationName_default = Nackademin

# we can do this but it is not needed normally :-)
#1.organizationName       = Second Organization Name (eg, company)
#1.organizationName_default = World Wide Web Pty Ltd

organizationalUnitName     = Organizational Unit Name (eg, section)
organizationalUnitName_default = education

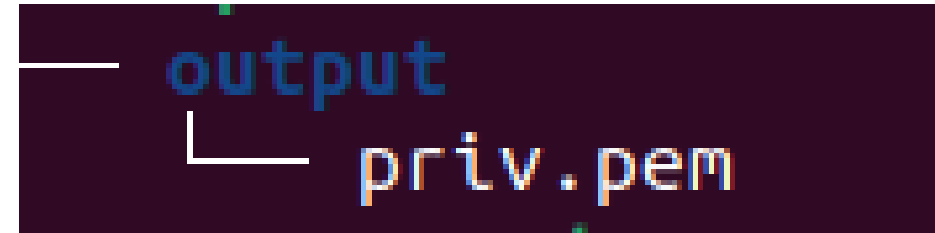
commonName                = Common Name (e.g. server FQDN or YOUR name)
commonName_max            = 64
commonName_default        = ca.nackademin.local

emailAddress              = Email Address
emailAddress_max          = 64
emailAddress_default       = hans.lamm@nackademin.se

# SET-ex3                 = SET extension number 3
```

Generate keypair with openssl

```
openssl genrsa -out output/priv.pem 2048
```



Private (and public keys) created and stored in priv.pem

Certificate sign request PKCS#10

`openssl req -new -key output/priv.pem -out output/csr.pem -config req.cnf`

A new file is written to output

The command above could be executed over and over since no states are preserved.

The CSR/PKCS#10 is just a request to the CA to issue a certificate

```
output
├── csr.pem
└── priv.pem
```

Signature is described as
Sha256WithRSAEncryption

The public key is added to the CSR
together with attributes from policy
under the Data section.

The section is then hashed and
encrypted against client private key.

The private is not submitted to CA !!!

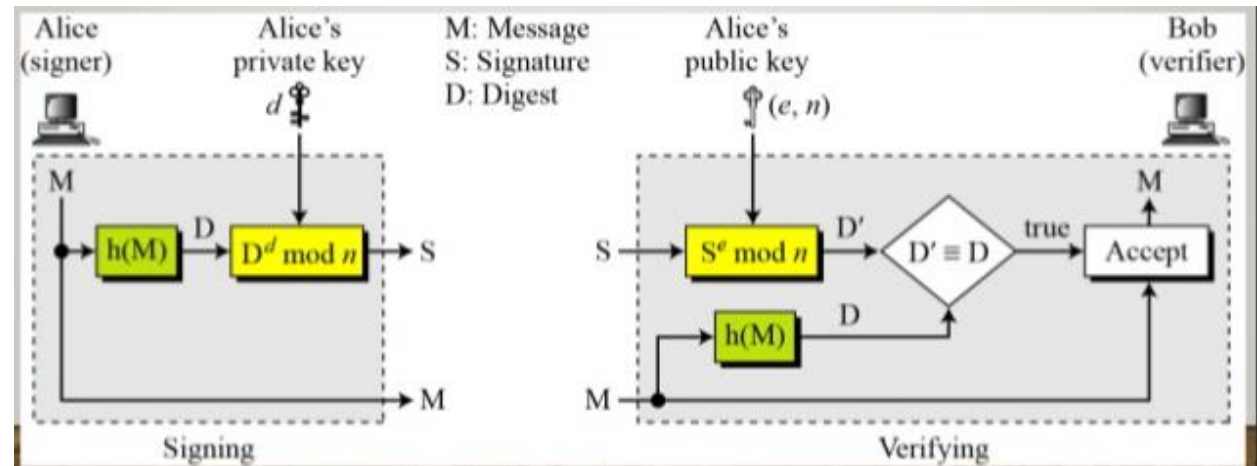
```
Certificate Request:
Data:
  Version: 1 (0x0)
  Subject: C = SE, ST = Stockholms Lan, L = Nacka, O = nackademin, OU = education, CN = dc1.nackademin.local
  Subject Public Key Info:
    Public Key Algorithm: rsaEncryption
    Public-Key: (2048 bit)
    Modulus:
      00:a2:d9:ad:f3:8a:f5:6a:f2:44:4d:f1:43:64:54:
      16:dc:80:f3:31:1f:ba:9e:16:0f:6b:2b:a4:68:32:
      28:bb
    Exponent: 65537 (0x10001)
  Attributes:
    Requested Extensions:
      X509v3 Extended Key Usage:
        TLS Web Client Authentication, Code Signing
      X509v3 Basic Constraints:
        CA:TRUE
      X509v3 Key Usage:
        Digital Signature, Non Repudiation, Key Encipherment
  Signature Algorithm: sha256WithRSAEncryption
  Signature Value:
    69:47:8b:2c:dd:2e:ef:2d:18:17:7a:3a:6c:dc:2d:0f:62:da:
    16:d7:67:9e
```

Signatures and RSA

Signing is based on hash/digest and encryption.

The message is passed from Alice to Bob, together with an encrypted hash.

When Bob compares the decrypted hash with the received hash, message is accepted.



Certificate Sign Request template

Attributes in the CSR originates from request template.

The validity interval of the certificate is defined by the CA

In this scenario there is no validation of the request.

In front of the CA where is often a RA (registration authority) to check that the request owns the domain for the CN in the request.

(Let`s encrypt , uses text record in DNS)

```
[req]
default_bits = 2048
prompt = no
default_md = sha256
distinguished_name = dn
x509_extensions = usr_cert
req_extensions = v3_req

[ dn ]
C=SE
ST=Stockholms Lan
L=Nacka
O=nackademin
OU=education
CN = dc1.nackademin.local

[ usr_cert ]
basicConstraints=CA:FALSE
nsCertType = client, server
keyUsage = nonRepudiation, digitalSignature, keyEncipherment
extendedKeyUsage = serverAuth, clientAuth, codeSigning
subjectKeyIdentifier=hash
authorityKeyIdentifier=keyid,issuer

[ v3_req ]
extendedKeyUsage = clientAuth, codeSigning
basicConstraints = CA:TRUE
keyUsage = nonRepudiation, digitalSignature, keyEncipherment
```


Submit the CSR/PKSC#10 to the CA

```
openssl ca -config ca.conf -in output/csr.pem -out output/cert.pem -notext -batch
Using configuration from ca.conf
Check that the request matches the signature
Signature ok
The Subject's Distinguished Name is as follows
countryName             :PRINTABLE:'SE'
stateOrProvinceName     :ASN.1 12:'Stockholms Lan'
localityName            :ASN.1 12:'Nacka'
organizationName        :ASN.1 12:'nackademin'
organizationalUnitName  :ASN.1 12:'education'
commonName              :ASN.1 12:'dc1.nackademin.local'
Certificate is to be certified until Nov 13 19:21:48 2032 GMT (3650 days)

Write out database with 1 new entries
Data Base Updated
openssl rsa -in output/priv.pem -pubout > output/pubkey.pem
writing RSA key
```

output

- cert.pem
- csr.pem
- priv.pem
- pubkey.pem

Issued certificate

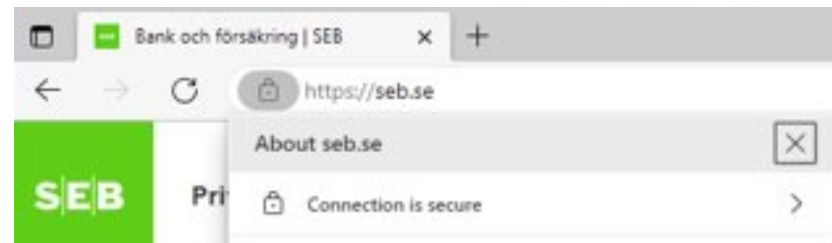
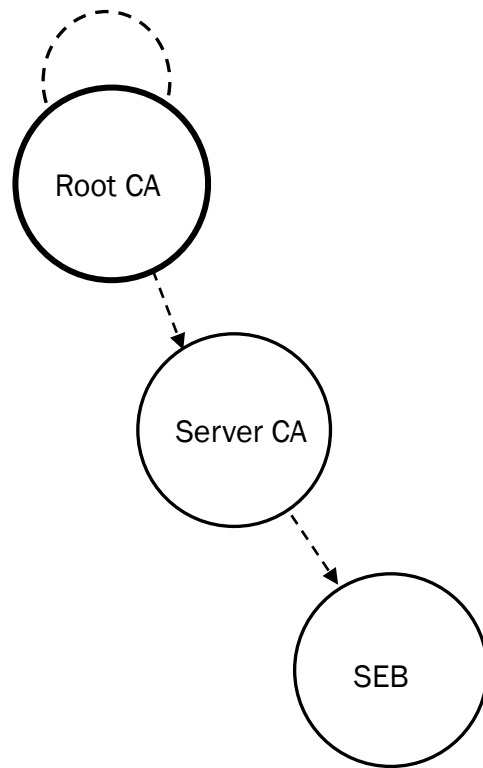
The issuer and subject CN:s differs.

The certificate is now issued and ready to use.

- Format .pfx / PKCS#12
- Revocation
- Distribution of CA root.crt

```
Certificate:
Data:
  Version: 3 (0x2)
  Serial Number:
    03:27:c3:1d:77:9a:ae:3a:60:80:93:61:ef:38:e7:f0
  Signature Algorithm: sha256WithRSAEncryption
  Issuer: C = SE, ST = Stockholm, L = Nacka, O = Nackademin, OU = education, CN = ca.nackademin.local, emailAddress = hans.lamm@nackademin.se
  Validity
    Not Before: Nov 16 19:21:48 2022 GMT
    Not After : Nov 13 19:21:48 2032 GMT
  Subject: C = SE, ST = Stockholms Lan, L = Nacka, O = nackademin, OU = education, CN = dc1.nackademin.local
  Subject Public Key Info:
    Public Key Algorithm: rsaEncryption
    Public-Key: (2048 bit)
    Modulus:
      00:a2:d9:ad:f3:8a:f5:6a:f2:44:4d:f1:43:64:54:
      22:02:07:c8:68:c9:8f:ab:97:a5:2a:5a:0f:a6:7a:
      28:bb
    Exponent: 65537 (0x10001)
  X509v3 extensions:
    X509v3 Extended Key Usage:
      TLS Web Client Authentication, Code Signing
    X509v3 Basic Constraints:
      CA:TRUE
    X509v3 Key Usage:
      Digital Signature, Non Repudiation, Key Encipherment
    X509v3 Subject Key Identifier:
      A8:DE:5C:46:03:D7:4A:4A:35:2A:B0:B5:73:3A:93:C7:96:67:F2:80
    X509v3 Authority Key Identifier:
      04:03:6C:F9:F8:7F:CE:FA:45:37:F2:7D:A7:B5:00:96:2C:96:1A:FC
  Signature Algorithm: sha256WithRSAEncryption
  Signature Value:
    87:05:a1:f1:85:f3:be:0a:10:cb:8b:54:3d:ae:a4:67:49:63:
    b5:e2:ee:cd:38:d5:bd:68:7b:ea:7c:2d:b7:d6:f1:16:7b:84:
    ec:c1:66:79
```

Chain of Trust



Certificate Viewer: seb.se

General

Details

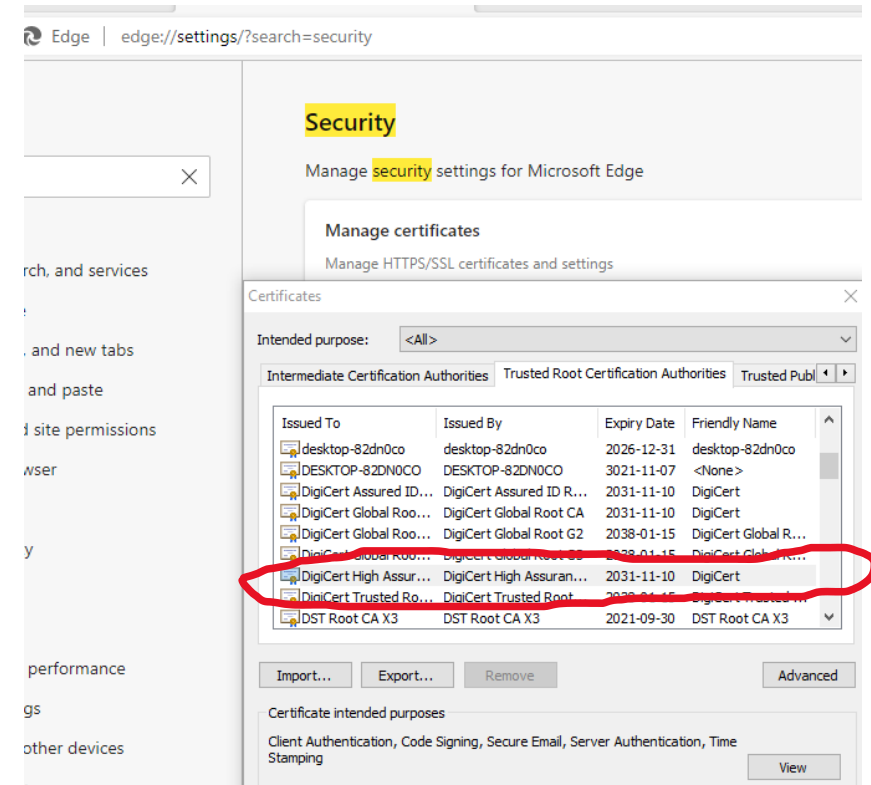
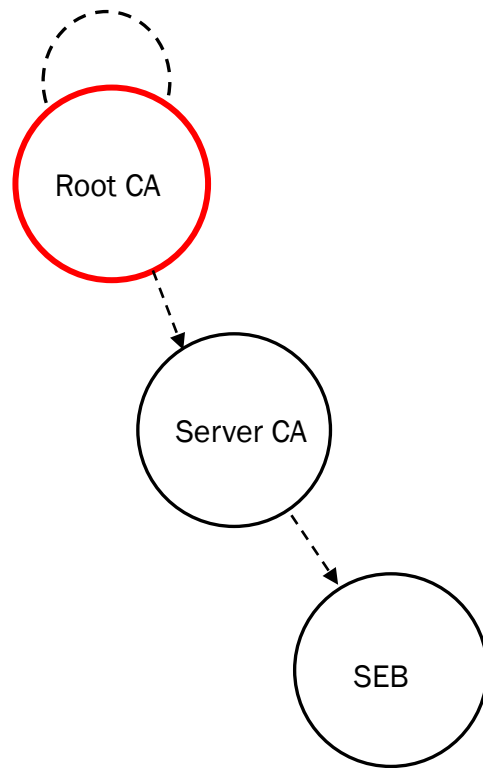
Certificate Hierarchy

▼ DigiCert High Assurance EV Root CA

▼ DigiCert SHA2 Extended Validation Server CA

seb.se

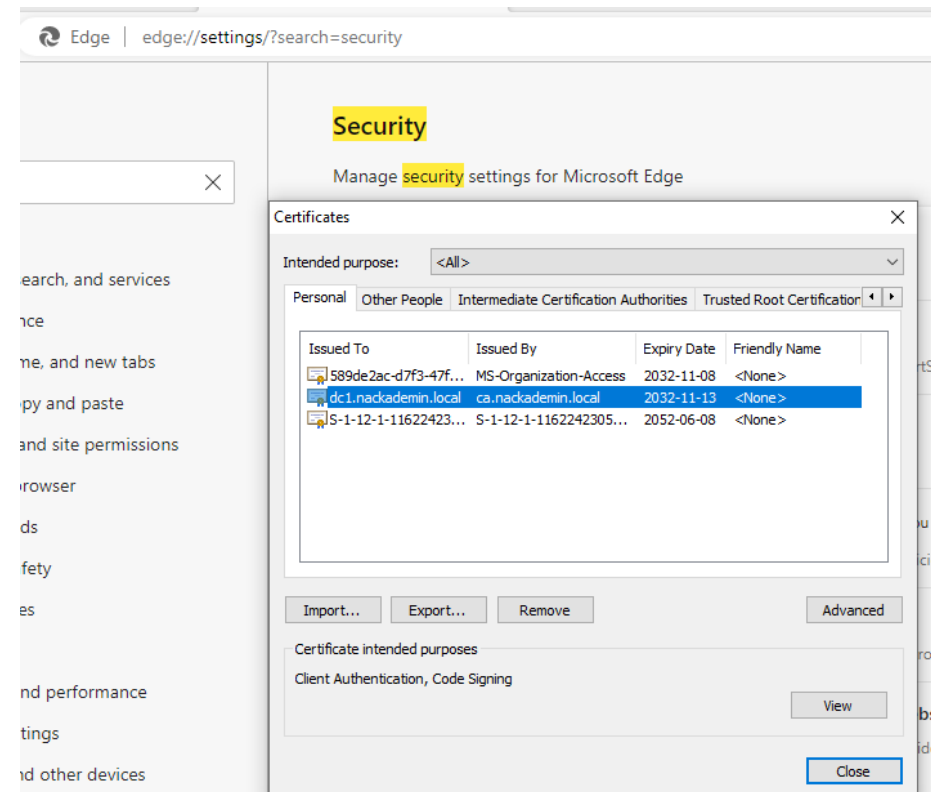
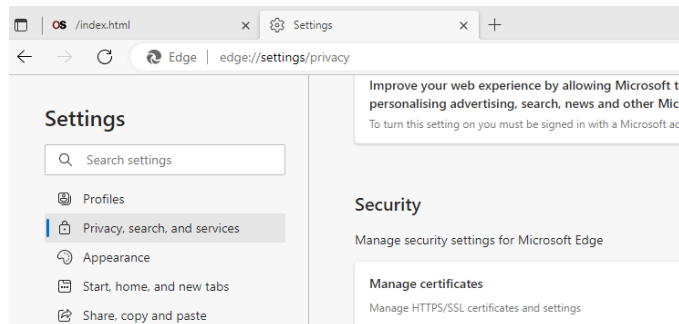
Root of Trust



Import certificates in Edge

Personal certificates includes private key

Trusted CA , certs with public key only



Generate PKCS#12 / *.pfx

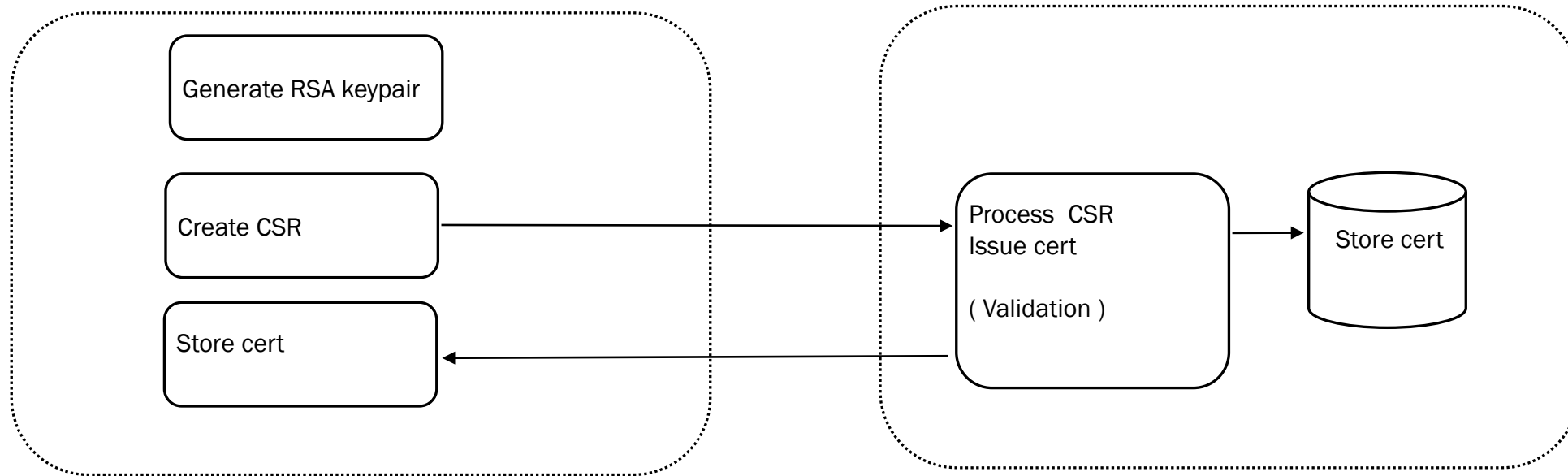
Format used by browsers for mutual authentication

*.pfx is the standard format in Windows

Could also be used in Java key store (JKS)

```
openssl pkcs12 -export -passout pass:qwerty -out output/certificate.pfx -inkey output/priv.pem -in output/cert.pem -certfile output/cert.pem
```

Separation of duty with RSA



Validity period for Java Web Tokens

Encoded

PASTE A TOKEN HERE

eyJhbGciOiJSUzI1NiIsImN1c3RvbVNPZ0hlYWRLciI6ImN1c3RvbUhlYWRLckNvbRlbnQifQ.eyJleHAiOiIxNjY4NTg5NDMzIiwiaWF0IjoiMTY2ODU4OTMzMjMyImlzc3VlciI6ImF1dGh1bnRyY2F0aW9uLm5hY2thZGVtaW4ubG9jYyWiLCJ1cG4iOiJoYW5zLmXhbw1AbmFja2FkZW1pb3ZlZS99.igRhvDYwsJsuU7Wcsm08P_hs5gBHkr1xKYFThT0509Uc-Oz6UABfmI7VRHiQVdgsjfZ1jg1u-jHsAKRrK-xLaWoSUSMexXZTJXW5IKyRpIIu7E253ILT60nX91VpuUCHBkJjSkGwNo_SdJw_kU9vDYqTqV0mB8Ne nOuJPNZ25XN2oM3jHS9YIRxuxRMD41xhh18CRW-S58skzzYVvBdS7MGsgAu3IJckby7-Y4-zvFsrAXZ25MqW7PxgtJMTXoHd8jSuDqRQQQaCWSLHjnT5Z5GBWTJ-jrVAvupwBppHnqbW1Ykxx5wN5f_7iL2qo3_T2dx9-pV9oI4vG64ZWSAzCg|

Decoded

EDIT THE PAYLOAD AND SECRET

HEADER: ALGORITHM & TOKEN TYPE

```
{
  "alg": "RS256",
  "customSigHeader": "customHeaderContent"
}
```

PAYLOAD: DATA

```
{
  "exp": "1668589433",
  "iat": "1668589333",
  "issuer": "authentication.nackademin.local",
  "upn": "hans.lamm@nackademin.se"
}
```

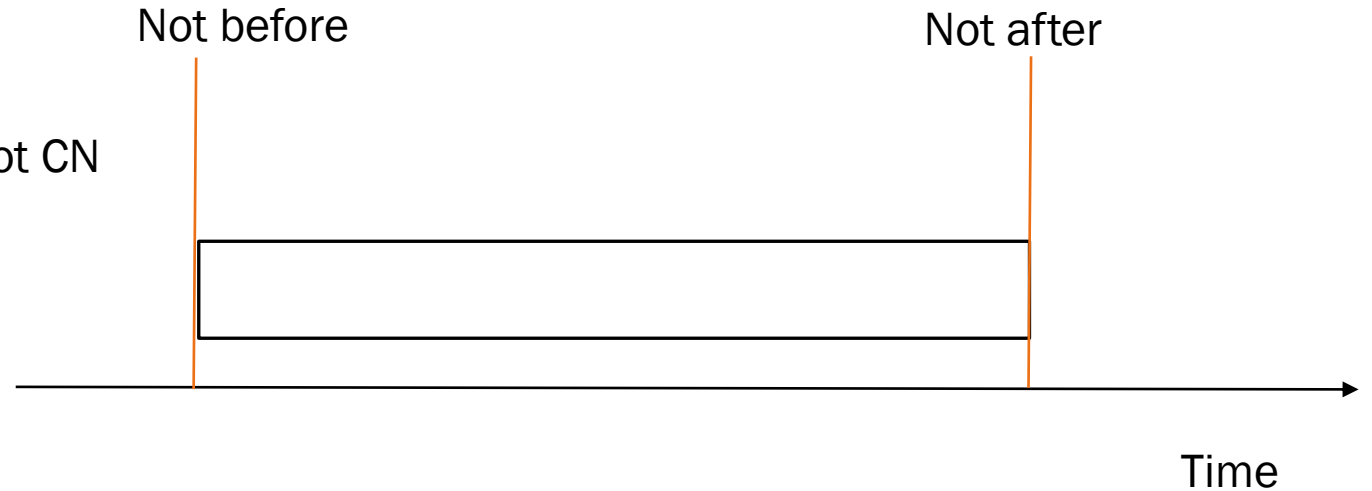
VERIFY SIGNATURE

```
RSASHA256(  
    base64UrlEncode(header) + "." +  
    base64UrlEncode(payload),  
    Public Key in SPKI, PKCS #1,  
    X.509 Certificate, or PKCS #1
```

Javascript Object Signing and Encryption (JOSE) — jose 0.1 documentation

Revocation

- If certificate is issued for 10 years
- Private key gets compromised
- Premature termination of validity required
- CRL integrated into CA
- All clients must check revocation lists
- Revocation associated with serial number, not CN



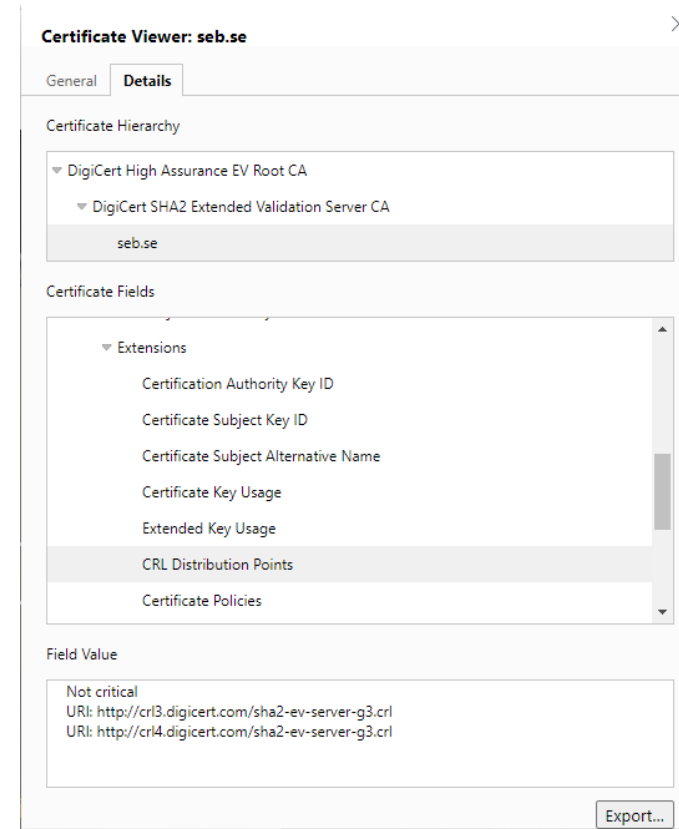
Revocation

Distribution points for revocation of certificates are included in CA cert

It is the client that checks for revocation

All intermedia certs must be checked.

[Certificate revocation list - Wikipedia](#)

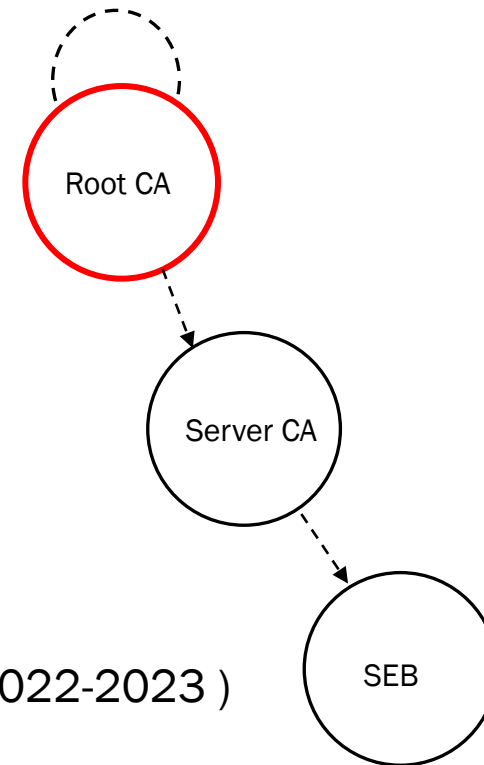


Validity time for certs in the tree

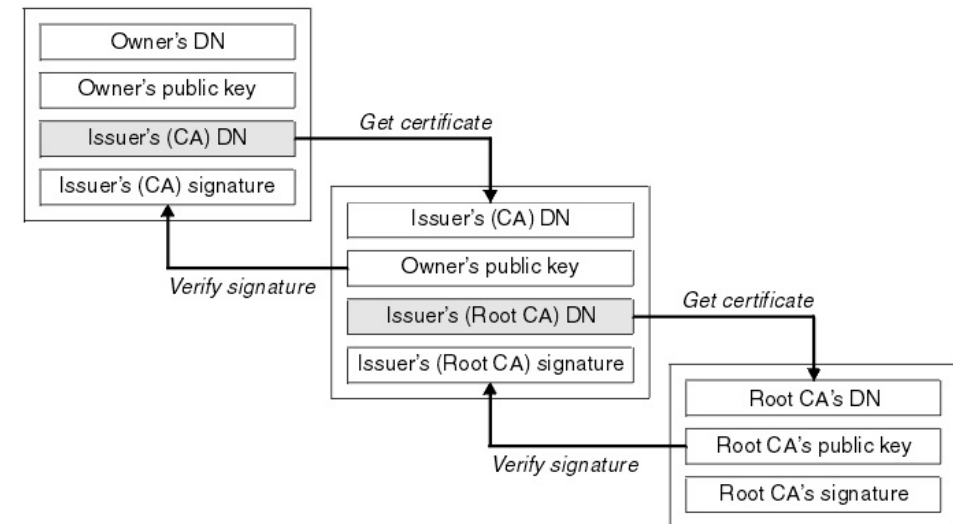
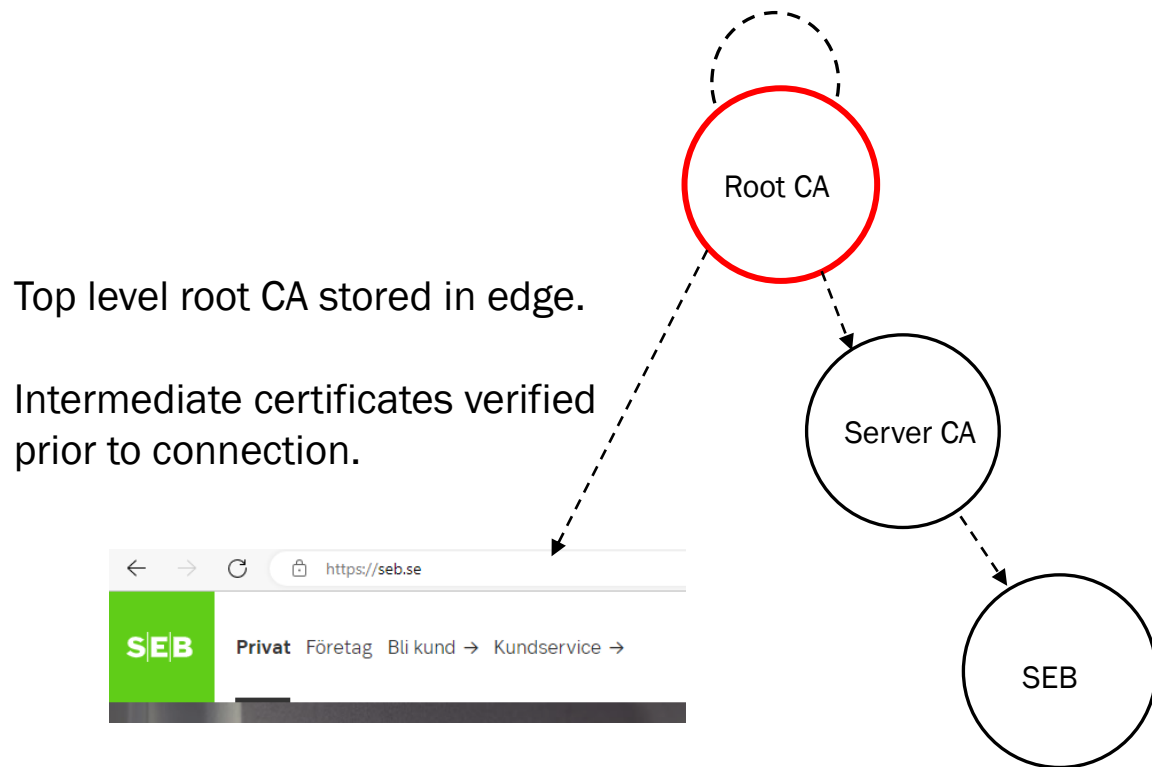
Root CA only used to issue cert for server CA (2006-2031)
If this key gets compromised, the impact will be massive

Server CA:s used to issue cert for customers (2013-2028)

Customers get cert only (2022-2023)



RSA solved the problem with key distribution



[How Certificate Chains Work \(digicert.com\)](https://www.digicert.com)

Thankyou