

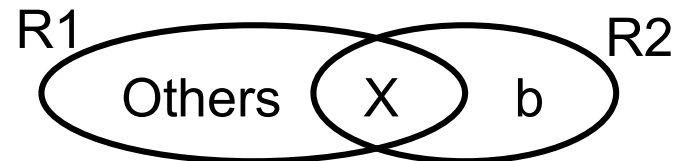
CPSC 304 – Administrative notes

October 2 & October 3, 2024

- New “in class” exercise started today
- October 15: [Milestone 2](#) due
- October 22: Midterm @ 6PM
 - Do you have a conflict? If so fill out the midterm conflict form on Piazza by the end of Monday
 - More information on Piazza ~1 week before the midterm.

Now where were we...

- We'd been discussing normalization
- We'd discussed BCNF (for all FDs of the form $X \rightarrow b$, X must be a superkey for the relation)
- We'd discussed how to decompose relations into BCNF. Repeatedly do:



Let's revisit a discussion that we had about which FDs hold after a decomposition...

Revisiting a previous clicker question:

- Take the closure of the attributes using *all* FDs
- For an FD $X \rightarrow b$, if the decomposed relation S contains $\{X \cup b\}$, then the FD holds for S :
- For example. Consider relation $R(A,B,C,D,E)$ with functional dependencies $AB \rightarrow C$, $BC \rightarrow D$, $CD \rightarrow E$, $DE \rightarrow A$, and $AE \rightarrow B$.

Project these FD's onto the relation $S(A,B,C,D)$.

- Which of the following hold in S ?

A. $A \rightarrow B$

$A^+ = A$

B. $AB \rightarrow E$

$AB^+ = ABCDE$, but E is not in S

C. $AE \rightarrow B$

$AE^+ = ABCDE$, but E is not in S

D. $BCD \rightarrow A$

Yes. $BCD^+ = ABCDE$; all in S

E. None of the above

Why do we need to consider FDs that aren't present in decomposed relations? (1/3)

Consider a relation $R(A, B, C, D)$ with FDs $A \rightarrow B$, and $B \rightarrow C$.

Consider the following set of tuples that may or may not adhere to the FDs above:

A	B	C	D
1	3	1	1
1	3	2	2
2	4	3	3
2	4	4	4

Which of the following FDs hold in the above tuples?

- A. $A \rightarrow B$ only
- B. $B \rightarrow C$ only
- C. Both $A \rightarrow B$ and $B \rightarrow C$
- D. Neither $A \rightarrow B$ nor $B \rightarrow C$

Does $A \rightarrow C$ hold? No!

Why do we need to consider FDs that aren't present in decomposed relations? (2/3)

Consider a relation $R(A, B, C, D)$ with FDs $A \rightarrow B$, and $B \rightarrow C$.

Consider a new set of tuples where $A \rightarrow B$ and $B \rightarrow C$:

A	B	C	D
1	3	5	1
1	3	5	2
2	4	6	3
2	4	6	4

Does $A \rightarrow C$ hold for this instance of R ?

A. Yes

B. No

Is it possible, given that $A \rightarrow B$ and $B \rightarrow C$, hold to create a set of tuples where $A \rightarrow C$ does *NOT* hold?

A. Yes

B. No

Why do we need to consider FDs that aren't present in decomposed relations? (3/3)

Consider a relation $R(A, B, C, D)$ with FDs $A \rightarrow B$, and $B \rightarrow C$.
Consider the same set of tuples where the FDs hold, *including* $A \rightarrow C$:
Let's assume that we decompose on $A \rightarrow B$, resulting in two relations:
 $R_1(A, B)$, $R_2(A, C, D)$

A	B	C	D
1	3	5	1
1	3	5	2
2	4	6	3
2	4	6	4

R_1

A	B
1	3
2	4

R_2

A	C	D
1	5	1
1	5	2
2	6	3
2	6	4

Does $A \rightarrow C$ hold for this instance of R_2 ?

A. Yes

B. No

Is it possible to create a set of tuples for R_2 where $A \rightarrow C$ does *NOT* hold?

A. Yes

B. No

Yet Another BCNF Example: Is it in BCNF? If so, why? If not, decompose.

$R(A,B,C,D,E,F)$

FD = $A \rightarrow B$

$DE \rightarrow F$,

$B \rightarrow C$

$A^+ = \{A,B,C\}$

$B^+ = \{B,C\}$

$DE^+ = \{D,E,F\}$

ADE is the only key

Decompose on $A \rightarrow B$

$CDEF$ A B

$R1(\underline{A}, B)$, $R2(\underline{A}, C, \underline{D}, \underline{E}, F)$

Decompose $R2$ on $DE \rightarrow F$

AC DE F

$R3(\underline{D}, \underline{E}, F)$, $R4(\underline{A}, C, \underline{D}, \underline{E})$

What is A^+ on $R4$?

A. A

B AC

C. ABC

D. Other

Decompose again:

DE A C

$R5(\underline{A}, C)$, $R6(\underline{A}, \underline{D}, \underline{E})$

Final answer: $R1(\underline{A}, B)$, $R3(\underline{D}, \underline{E}, F)$, $R5(\underline{A}, C)$, $R6(\underline{A}, \underline{D}, \underline{E})$

Clicker exercise: More BCNF

- Let $R(ABCD)$ be a relation with functional dependencies $A \rightarrow B$, $C \rightarrow D$, $AD \rightarrow C$, $BC \rightarrow A$
- Decompose into BCNF.

Clicker exercise: More BCNF

- Let $R(ABCD)$ be a relation with functional dependencies $A \rightarrow B$, $C \rightarrow D$, $AD \rightarrow C$, $BC \rightarrow A$
 - Decompose into BCNF. Which of the following is a lossless-join decomposition of R into BCNF?
- A. $\{AB, AC, BD\}$
 - B. $\{AB, AC, CD\}$
 - C. $\{AB, AC, BCD\}$
 - D. All are
 - E. None are

Clicker exercise: More BCNF Explained

- Let $R(ABCD)$ be a relation with functional dependencies $A \rightarrow B$, $C \rightarrow D$, $AD \rightarrow C$, $BC \rightarrow A$
- Decompose into BCNF. Which of the following is a lossless-join decomposition of R into BCNF?

Closures:

- $A^+ = \{AB\}$
- $C^+ = \{CD\}$
- $AD^+ = \{ADBC\} \leftarrow \text{Key}$
- $BC^+ = \{BCDA\} \leftarrow \text{Key}$

$A \rightarrow B$ violates BCNF in R : Decompose to $R1(\underline{A}, B)$, $R2(\underline{A}, \underline{C}, D)$

$C \rightarrow D$ violates BCNF in $R2$: Decompose to $R3(\underline{C}, D)$, $R4(\underline{C}, \underline{A})$

All are two attribute relations, all are in BCNF. Final answer:

$R1(\underline{A}, B)$, $R3(\underline{C}, D)$, $R4(\underline{C}, \underline{A})$

Clicker Exercise: Option 'A' exposed

- Let $R(ABCD)$ be a relation with functional dependencies $A \rightarrow B$, $C \rightarrow D$, $AD \rightarrow C$, $BC \rightarrow A$

Is $\{AB, AC, BD\}$ a lossless join?

Imagine tuples:

A	B	C	D
1	2	5	6
1	2	3	7
8	2	9	4

decompose



A	B
1	2
8	2

A	C
1	5
1	3
8	9

B	D
2	6
2	7
2	4

join



A	B	C	D
1	2	5	6
1	2	3	7
8	2	9	4
1	2	3	4

In class exercise

- Do Normalization #2 now

This BCNF stuff is great and easy!

- Guaranteed that there will be no redundancy of data
- Easy to understand (just look for superkeys)
- Easy to do.
- So what is the main problem with BCNF?
 - For one thing, BCNF may not preserve all dependencies

An illustrative BCNF example

Unit	Company	Product

$\text{Unit} \rightarrow \text{Company}$
 $\text{Company, Product} \rightarrow \text{Unit}$

Is Unit a key?

Unit	Company

$\text{Unit} \rightarrow \text{Company}$

Unit	Product

We lose the FD: $\text{Company, Product} \rightarrow \text{Unit}$!!

So What's the Problem (1/2)?

Assume that we start with a table with a single tuple:

Unit	Company	Product
SKYWill	UBC	Databases

We decompose on Unit \rightarrow Company:

<u>Unit</u>	Company
SKYWill	UBC

Unit	Product
SKYWill	Databases

Now someone adds a new team, Team Meat to each table:

<u>Unit</u>	Company
SKYWill	UBC
Team Meat	UBC

Unit	Product
SKYWill	Databases
Team Meat	Databases

So What's the Problem (2/2)?

<u>Unit</u>	Company
SKYWill	UBC
Team Meat	UBC

Unit	Product
SKYWill	Databases
Team Meat	Databases

Unit → Company

No problem so far. All *local* FD's are satisfied.
Let's put all the data back into a single table again:

Unit	Company	Product
SKYWill	UBC	Databases
Team Meat	UBC	Databases

Violates the FD:

Company, Product → Unit

3NF to the rescue!



A relation R is in 3NF if:

If $X \rightarrow b$ is a non-trivial dependency in R ,
then X is a superkey for R

or b is part of a (minimal) key.

} BCNF

(must be true for every such functional dependency)

Note: b must be part of a **key** *not* part of a **superkey** (if a key exists, *all* attributes are part of a superkey)

Example: $R(\text{Unit}, \text{Company}, \text{Product})$

- $\text{Unit} \rightarrow \text{Company}$
 - $\text{Company}, \text{Product} \rightarrow \text{Unit}$
- Keys: $\{\text{Company}, \text{Product}\}, \{\text{Unit}, \text{Product}\}$

BCNF or 3NF? The clicker question

- 3NF retains all functional dependencies
 - Rule: for all non-trivial functional dependencies in a relation R of the form $X \rightarrow b$, it must be the case that X is a superkey of R **or b is part of a key**
 - Ex: is R(ABCD) in BCNF, 3NF, or both given the following FDs:
 - $AB \rightarrow C$
 - $CD \rightarrow A$
- A. Both BCNF and 3NF
B. BCNF but not 3NF
C. 3NF but not BCNF
D. Neither BCNF nor 3NF