```
AttributeError Traceback (most recent call last)
 <ipython-input-3-296913ab6e35> in <module>()
 ----> 1 data.type
 AttributeError: 'list' object has no attribute 'type'
 In [4]: data.type()
        -----
 AttributeError Traceback (most recent call last)
 <ipython-input-4-f5d544e46bb2> in <module>()
 ---> 1 data.type()
 AttributeError: 'list' object has no attribute 'type'
 In [5]: data.
 data.append data.extend data.insert data.remove data.sort
 data.count data.index data.pop data.reverse
 In [5]: data1 = [6, 7.5, 8, 0, 1]
 In [6]: ls
Applications/ Library/ Public/ curl
Creative Cloud Files/ MDIGB0_ideal.xbgf PycharmProjects/ experiments/
Desktop/ Mathematica/ Untitled.ipynb nohup.out
Developer/ Movies/ amber_test/ requirement.txt
Documents/ Music/ anaconda/ seaborn-data/
Downloads/ Parallels/ android/ solarized/
Dropbox/ Pictures/ bin/ texput.log
 Applications/ Library/
 In [7]: arr1 = np.array(data1)
In [8]: arr1.

arr1.T arr1.copy arr1.imag arr1.ravel arr1.sum

arr1.all arr1.ctypes arr1.item arr1.real arr1.swapaxes

arr1.any arr1.cumprod arr1.itemset arr1.repeat arr1.take

arr1.argmax arr1.cumsum arr1.itemsize arr1.reshape arr1.tobytes

arr1.argmin arr1.data arr1.max arr1.resize arr1.tofile

arr1.argpartition arr1.diagonal arr1.mean arr1.round arr1.tolist

arr1.argsort arr1.dot arr1.min arr1.searchsorted arr1.tostring

arr1.astype arr1.dtype arr1.nbytes arr1.setfield arr1.trace

arr1.base arr1.dump arr1.ndim arr1.setflags arr1.transpose

arr1.byteswap arr1.dumps arr1.newbyteorder arr1.shape arr1.var

arr1.choose arr1.fill arr1.nonzero arr1.size arr1.view

arr1.compress arr1.flat arr1.prod arr1.squeeze

arr1.conj arr1.flatten arr1.ptp arr1.std

arr1.strides
 In [8]: arr1.
 In [8]: arr1.dtype
 Out[8]: dtype('float64')
 In [9]: arr1.shape
 Out[9]: (5,)
 In [10]: arr1.size
 Out[10]: 5
 In [11]: arr.ndim
 NameError Traceback (most recent call last)
 <ipython-input-11-ff9c433e9bba> in <module>()
 ---> 1 arr.ndim
 NameError: name 'arr' is not defined
 In [12]: a
In [12]: a
%alias %autoindent all and apply assert
```

```
%alias_magic %automagic
                           amber_test/ android/
                                                        arr1
%autocall
                           anaconda/
                                         any
                                                        as
In [12]: arr1.ndim
Out[12]: 1
In [13]: str1 = 'kkk'
In [14]: arr2 = np.array(str1)
In [15]: arr2
Out[15]:
array('kkk',
     dtype='IS3')
In [16]: print arr2
kkk
In [17]: calibers = np.array([.22, .270, .357, .380, .44, .50], dtype = np.float64)
In [18]: calibers
Out[18]: array([ 0.22 , 0.27 , 0.357, 0.38 , 0.44 , 0.5 ])
In [19]: caliber.dtype
NameError
                                         Traceback (most recent call last)
<ipython-input-19-6e1e056b5924> in <module>()
---> 1 caliber.dtype
NameError: name 'caliber' is not defined
In [20]: calibers.dtype
Out[20]: dtype('float64')
In [21]: int_array.astype(calibers.dtype)
                                         Traceback (most recent call last)
<ipython-input-21-bbc3393af524> in <module>()
---> 1 int_array.astype(calibers.dtype)
NameError: name 'int_array' is not defined
In [22]: np.empty?
Docstring:
empty(shape, dtype=float, order='C')
Return a new array of given shape and type, without initializing entries.
Parameters
shape : int or tuple of int
   Shape of the empty array
dtype : data-type, optional
   Desired output data-type.
order : {'C', 'F'}, optional
   Whether to store multi-dimensional data in row-major
   (C-style) or column-major (Fortran-style) order in
   memory.
Returns
-----
out : ndarray
   Array of uninitialized (arbitrary) data of the given shape, dtype, and
   order. Object arrays will be initialized to None.
See Also
empty_like, zeros, ones
```

```
Notes
`empty`, unlike `zeros`, does not set the array values to zero,
and may therefore be marginally faster. On the other hand, it requires
the user to manually set all the values in the array, and should be
used with caution.
Examples
_____
>>> np.empty([2, 2])
array([[ -9.74499359e+001,
                            6.69583040e-309],
       [ 2.13182611e-314, 3.06959433e-309]])
                                                        #random
>>> np.empty([2, 2], dtype=int)
array([[-1073741821, -1067949133],
      [ 496041986,
                      19249760]])
                                                        #random
Type:
          builtin_function_or_method
In [23]: np.empty??
Docstring:
empty(shape, dtype=float, order='C')
Return a new array of given shape and type, without initializing entries.
Parameters
shape: int or tuple of int
   Shape of the empty array
dtype : data-type, optional
   Desired output data-type.
order : {'C', 'F'}, optional
   Whether to store multi-dimensional data in row-major
    (C-style) or column-major (Fortran-style) order in
   memory.
Returns
out : ndarray
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See Also
empty_like, zeros, ones
Notes
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Examples
>>> np.empty([2, 2])
array([[ -9.74499359e+001, 6.69583040e-309],
      [ 2.13182611e-314, 3.06959433e-309]])
                                                        #random
>>> np.empty([2, 2], dtype=int)
array([[-1073741821, -1067949133],
       [ 496041986,
                       19249760]])
                                                        #random
          builtin_function_or_method
In [24]: np.empty(8, dtype = 'u4')
Out[24]:
                     0,
array([
                                        0, 4194308,
                                                          1, 4233920,
            1], dtype=uint32)
```

```
In [25]: np.empty(8, dtype = '4')
                   Traceback (most recent call last)
TypeError
<ipython-input-25-0c729741e9ef> in <module>()
---> 1 np.empty(8, dtype = '4')
TypeError: data type "" not understood
In [26]: np.empty(8, dtype = 'i4')
Out[26]: array([0, 0, 0, 0, 0, 0, 0], dtype=int32)
In [27]: np.empty(8, dtype = 'i4')
Out[27]: array([0, 0, 0, 0, 0, 0, 0], dtype=int32)
In [28]: np.empty(8, dtype = 'f4')
Out[28]: array([ 0., 0., 0., 0., 0., 0., 0.], dtype=float32)
In [29]: np.empty(8, dtype = 'int')
Out[29]: array([0, 0, 0, 0, 0, 0, 0, 0])
In [30]: np.empty([2,2,2], dtype = 'int')
Out[30]:
array([[[0, 0],
       [0, 0]],
      [[0, 0],
       [0, 0]]])
In [31]: np.empty([2,2,2], dtype = int)
Out[31]:
array([[[0, 0],
       [0, 0]],
      [[0, 0],
       [0, 0]]])
In [32]: np.empty([2,2], dtype = int)
Out[32]:
array([[0, 0],
      [0, 0]])
In [33]: arr3d = np.array([[[1,2,3],[4,5,6]],[[7,8,9], [10,11,12]]])
In [34]: arr3d
Out[34]:
array([[[ 1, 2, 3],
       [ 4, 5, 6]],
      [[ 7, 8, 9],
       [10, 11, 12]])
In [35]: names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])
In [36]: data = randn(7,4)
NameError
                                         Traceback (most recent call last)
<ipython-input-36-cb7c4b32d8ce> in <module>()
---> 1 data = randn(7,4)
NameError: name 'randn' is not defined
In [37]: randn
NameError
                                         Traceback (most recent call last)
<ipython-input-37-398a9a52c608> in <module>()
---> 1 randn
```

```
NameError: name 'randn' is not defined
In [38]: data = np.randn(7, 4)
AttributeError
                                        Traceback (most recent call last)
<ipython-input-38-999554d4bcda> in <module>()
---> 1 data = np.randn(7, 4)
AttributeError: 'module' object has no attribute 'randn'
In [39]: data = np.random.randn(7, 4)
In [40]: data
Out[40]:
array([[-1.52433546, -0.32703791, -0.84868919, 1.09946958],
       [-0.88259789, -0.06316187, -0.15245984, 0.04303572],
       [ 1.3625452 , -1.12694417, 0.31368561, 0.56077444],
       [-0.53090207, -0.99261563, -0.79623224, 0.0475795],
       [1.0203938, -1.28077757, -0.5116905, -0.35825162],
       [0.9362092, 1.0289195, 1.26334767, 0.98402902],
       [-1.32131556, -0.91838682, -0.4337269 , 0.15345908]])
In [41]: names
Out[41]:
array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'],
     dtype='|S4')
In [42]: data[name == 'Bob', 3]
NameError
                                         Traceback (most recent call last)
<ipython-input-42-1fc590ae27e9> in <module>()
----> 1 data[name == 'Bob', 3]
NameError: name 'name' is not defined
In [43]: data[names == 'Bob', 3]
Out[43]: array([ 1.09946958, 0.0475795 ])
In [44]: data[(0, 3), 3]
Out[44]: array([ 1.09946958, 0.0475795 ])
In [45]: np.
Display all 583 possibilities? (y or n)
np.ALLOW_THREADS np.empty_like
                                                           np.nested_iters
np.BUFSIZE
                             np.equal
                                                           np.newaxis
np.CLIP
                             np.errstate
                                                           np.newbuffer
np.ComplexWarning
                             np.euler_gamma
                                                           np.nextafter
np.DataSource
                             np.exp
                                                           np.nonzero
np.ERR_CALL
                             np.exp2
                                                           np.not_equal
np.ERR_DEFAULT
                             np.expand_dims
                                                           np.nper
np.ERR_IGNORE
                             np.expm1
                                                           np.npv
np.ERR_LOG
                             np.extract
                                                           np.numarray
np.ERR_PRINT
                             np.eye
                                                           np.number
                             np.fabs
np.ERR_RAISE
                                                           np.obj2sctype
np.ERR_WARN
                             np.fast Copy And Transpose \\
                                                           np.object
np.FLOATING_POINT_SUPPORT
                             np.fft
                                                           np.object0
np.FPE_DIVIDEBYZERO
                             np.fill_diagonal
                                                           np.object_
np.FPE_INVALID
                             np.find_common_type
                                                           np.ogrid
np.FPE_OVERFLOW
                             np.finfo
                                                           np.oldnumeric
np.FPE_UNDERFLOW
                             np.fix
                                                           np.ones
np.False_
                             np.flatiter
                                                           np.ones_like
np.Inf
                             np.flatnonzero
                                                           np.outer
np.Infinity
                             np.flexible
                                                           np.packbits
np.MAXDIMS
                             np.fliplr
                                                           np.pad
np.MAY_SHARE_BOUNDS
                             np.flipud
                                                           np.partition
                                                           np.percentile
np.MAY_SHARE_EXACT
                             np.float
np.MachAr
                             np.float128
                                                           np.pi
np.ModuleDeprecationWarning
                             np.float16
                                                           np.piecewise
```

nn MAN	np.float32	np.pkgload
np.NAN np.NINF	np.float64	np.pkgtodd np.place
·	·	
np.NZERO	np.float_	np.pmt
np.NaN	np.floating	np.poly
np.PINF	np.floor	np.poly1d
np.PZERO	np.floor_divide	np.polyadd
np.PackageLoader	np.fmax	np.polyder
np.RAISE	np.fmin	np.polydiv
np.RankWarning	np.fmod	np.polyfit
np.SHIFT_DIVIDEBYZERO	np.format_parser	np.polyint
np.SHIFT_INVALID	np.frexp	np.polymul
np.SHIFT_OVERFLOW	np.frombuffer	np.polynomial
np.SHIFT_UNDERFLOW	np.fromfile	np.polysub
np.ScalarType	np.fromfunction	np.polyval
np.Tester	np.fromiter	np.power
np.TooHardError	np.frompyfunc	np.ppmt
np.True_	np.fromregex	np.print_function
np.UFUNC_BUFSIZE_DEFAULT	np.fromstring	np.prod
np.UFUNC_PYVALS_NAME	np.full	np.product
np.VisibleDeprecationWarning	np.full_like	np.promote_types
np.WRAP	np.fv	np.ptp
np.abs	np.generic	np.put
np.absolute	np.genfromtxt	np.putmask
np.absolute_import	np.get_array_wrap	np.pv
np.add	np.get_include	np.r_
np.add_docstring	np.get_printoptions	np.rad2deg
np.add_newdoc	np.getbuffer	np.radians
np.add_newdoc_ufunc	np.getbufsize	np.random
np.add_newdocs	np.geterr	np.rank
np.alen	np.geterrcall	np.rate
np.all	np.geterrobj	np.ravel
np.allclose	np.gradient	np.ravel_multi_index
np.alltrue	np.greater	np.real
np.alterdot	np.greater_equal	np.real_if_close
np.amax	np.half	np.rec
np.amin	np.hamming	np.recarray
np.angle	np.hanning	np.recfromcsv
np.any	np.histogram	np.recfromtxt
np.append	np.histogram2d	np.reciprocal
np.apply_along_axis	np.histogramdd	np.record
np.apply_over_axes	np.hsplit	np.remainder
np.arange	np.hstack	np.repeat
np.arccos	np.hypot	np.require
np.arccosh	np.i0	np.reshape
np.arcsin	np.identity np.iinfo	np.resize
np.arcsinh np.arctan	· · ·	<pre>np.restoredot np.result_type</pre>
•	np.imag	
np.arctan2 np.arctanh	np.in1d np.index_exp	np.right_shift np.rint
np.argmax	np.indices	np.roll
np.argmin	np.inexact	np.rollaxis
np.argpartition	np.inf	np.roots
np.argsort	np.info	np.rot90
np.argwhere	np.infty	np.round
np.around	np.inner	np.round_
np.array	np.insert	np.row_stack
np.array2string	np.int	np.s_
np.array_equal	np.int0	np.safe_eval
np.array_equiv	np.int16	np.save
np.array_equiv	np.int32	np.savetxt
np.array_repr np.array_split	np.int64	np.savez
np.array_str	np.int8	np.savez_compressed
np.asanyarray	np.int_	np.sctype2char
np.asarray	HP · LIIC_	
np.usurruy	nn int ashuffer	nn sctyneDict
	np.int_asbuffer	np.sctypeDict
np.asarray_chkfinite	np.intc	np.sctypeNA
np.asarray_chkfinite np.ascontiguousarray	np.intc np.integer	np.sctypeNA np.sctypes
np.asarray_chkfinite	np.intc	np.sctypeNA

nn acmatniv	nn intn	nn sot numeris ens
np.asmatrix np.asscalar	np.intp np.invert	<pre>np.set_numeric_ops np.set_printoptions</pre>
np.atleast_1d	np.ipmt	np.set_string_function
np.atleast_2d	np.irr	np.setbufsize
np.atleast_3d	np.is_busday	np.setdiff1d
np.average	np.isclose	np.seterr
np.bartlett	np.iscomplex	np.seterrcall
np.base_repr	np.iscomplexobj	np.seterrobj
np.bench	np.isfinite	np.setxor1d
np.binary_repr	np.isfortran	np.shape
np.bincount	np.isinf	np.shares_memory
np.bitwise_and	np.isnan	np.short
np.bitwise_not	np.isneginf	np.show_config
np.bitwise_or	np.isposinf	np.sign
np.bitwise_xor	np.isreal	np.signbit
np.blackman	np.isrealobj	np.signedinteger
np.bmat	np.isscalar	np.sin
np.bool	np.issctype	np.sinc
np.bool8	np.issubclass_	np.single
np.bool_	np.issubdtype	np.singlecomplex
np.broadcast	np.issubsctype	np.sinh
np.broadcast_arrays	np.iterable	np.size
np.broadcast_to	np.ix_	np.sometrue
np.busday_count	np.kaiser	np.sort
np.busday_offset	np.kron	np.sort_complex
np.busdaycalendar	np.ldexp	np.source
np.byte	np.left_shift	np.spacing
np.byte_bounds	np.less	np.split
np.bytes_	np.less_equal	np.sqrt
np.c_	np.lexsort	np.square
np.can_cast	np.lib	np.squeeze
np.cast	np.linalg	np.stack
np.cbrt	np.linspace	np.std
np.cdouble	np.little_endian	np.str
np.ceil	np.load	np.str_
np.cfloat	np.loads	np.string0
np.char	np.loadtxt	np.string_
np.character	np.log	np.subtract
np.chararray	np.log10	np.sum
np.choose	np.log1p	np.swapaxes
np.clip	np.log2	np.take
np.clongdouble	np.logaddexp	np.tan
np.clongfloat	np.logaddexp2	np.tanh
np.column_stack	np.logical_and	np.tensordot
np.common_type	np.logical_not	np.test
np.compare_chararrays	np.logical_or	np.testing
np.compat	np.logical_xor	np.tile
np.complex	np.logspace	np.timedelta64
np.complex128	np.long	np.trace
np.complex256	np.longcomplex	np.transpose
np.complex64	np.longdouble	np.trapz
np.complex_	np.longfloat	np.tri
np.complexfloating	np.longlong	np.tril
np.compress	np.lookfor	np.tril_indices
np.concatenate	np.ma	np.tril_indices_from
np.conj	np.mafromtxt	np.trim_zeros
np.conjugate	np.mask_indices	np.triu
np.convolve	np.mat	np.triu_indices
np.copy	np.math	np.triu_indices_from
np.copysign	np.matmul	np.true_divide
np.copyto	np.matrix	np.trunc
np.core	np.matrixlib	np.typeDict
np.corrcoef	np.max	np.typeNA
np.correlate	np.maximum	np.typecodes
np.cos	np.maximum_sctype	np.typename
np.cosh	np.may_share_memory	np.ubyte
np.count_nonzero np.cov	np.mean np.median	np.ufunc np.uint
пр.соч	np.meatan	np.utnc

```
np.cross
                              np.memmap
                                                            np.uint0
np.csingle
                              np.meshgrid
                                                            np.uint16
np.ctypeslib
                              np.mgrid
                                                            np.uint32
                              np.min
np.cumprod
                                                            np.uint64
                              np.min_scalar_type
np.cumproduct
                                                            np.uint8
np.cumsum
                              np.minimum
                                                            np.uintc
np.datetime64
                              np.mintypecode
                                                            np.uintp
np.datetime_as_string
                              np.mirr
                                                            np.ulonglong
np.datetime_data
                              np.mod
                                                            np.unicode
np.deg2rad
                              np.modf
                                                            np.unicode0
np.degrees
                              np.moveaxis
                                                            np.unicode_
np.delete
                              np.msort
                                                            np.union1d
np.deprecate
                              np.multiply
                                                            np.unique
np.deprecate_with_doc
                              np.nan
                                                            np.unpackbits
np.diag
                              np.nan_to_num
                                                            np.unravel_index
np.diag_indices
                              np.nanargmax
                                                            np.unsignedinteger
np.diag_indices_from
                              np.nanaramin
                                                            np.unwrap
np.diagflat
                              np.nanmax
                                                            np.ushort
np.diagonal
                              np.nanmean
                                                            np.vander
np.diff
                              np.nanmedian
                                                            np.var
np.digitize
                              np.nanmin
                                                            np.vdot
np.disp
                              np.nanpercentile
                                                            np.vectorize
np.divide
                              np.nanprod
                                                            np.version
np.division
                              np.nanstd
                                                            np.void
np.dot
                              np.nansum
                                                            np.void0
np.double
                              np.nanvar
                                                            np.vsplit
np.dsplit
                              np.nbytes
                                                            np.vstack
np.dstack
                              np.ndarray
                                                            np.warnings
np.dtype
                              np.ndenumerate
                                                            np.where
np.e
                              np.ndfromtxt
                                                            np.who
np.ediff1d
                              np.ndim
                                                            np.zeros
np.einsum
                              np.ndindex
                                                            np.zeros_like
                              np.nditer
np.emath
np.empty
                              np.negative
In [45]: arr = np.random.randn(7)
In [46]: arr
Out[46]:
array([ 2.70499407, -0.34452092, -0.88641991, -1.25973759, -0.48000149,
       0.78200997, -1.63438477])
In [47]: arr *= 5
In [48]: arr *= 5
In [49]: arr \= 5
 File "<ipython-input-49-c5df5af48126>", line 1
SyntaxError: unexpected character after line continuation character
In [50]: arr /= 5
In [51]: arr
Out[51]:
array([ 13.52497037, -1.72260462, -4.43209957, -6.29868793,
        -2.40000743,
                     3.91004984, -8.17192383])
In [52]: np.modf(arr)
Out[52]:
(array([ 0.52497037, -0.72260462, -0.43209957, -0.29868793, -0.40000743,
         0.91004984, -0.17192383),
array([ 13., -1., -4., -6., -2.,
                                      3., -8.]))
In [53]: np.meshgrid?
```

```
In [54]:
In [54]: points = np.arange(-5, 5, 0.01)
In [55]: po
%popd
        points
                pow
In [55]: points
Out[55]:
array([ -5.00000000e+00,
                           -4.99000000e+00,
                                              -4.98000000e+00,
        -4.97000000e+00,
                           -4.96000000e+00,
                                               -4.95000000e+00,
        -4.94000000e+00,
                           -4.93000000e+00,
                                              -4.92000000e+00,
        -4.91000000e+00,
                           -4.90000000e+00,
                                               -4.89000000e+00
        -4.88000000e+00,
                           -4.87000000e+00.
                                              -4.86000000e+00.
                           -4.84000000e+00,
        -4.85000000e+00.
                                              -4.83000000e+00.
        -4.82000000e+00.
                           -4.81000000e+00.
                                              -4.80000000e+00.
        -4.79000000e+00,
                           -4.78000000e+00,
                                              -4.77000000e+00,
        -4.76000000e+00,
                           -4.75000000e+00,
                                              -4.74000000e+00,
        -4.73000000e+00,
                           -4.72000000e+00,
                                              -4.71000000e+00,
        -4.70000000e+00,
                           -4.69000000e+00,
                                              -4.68000000e+00,
        -4.67000000e+00,
                           -4.66000000e+00,
                                              -4.65000000e+00,
        -4.64000000e+00,
                           -4.63000000e+00,
                                              -4.62000000e+00,
        -4.61000000e+00,
                           -4.60000000e+00,
                                              -4.59000000e+00,
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         4.93000000e+00,
         4.96000000e+00,
                             4.97000000e+00, 4.98000000e+00,
         4.99000000e+00])
In [56]: xs, ys = np.meshgrid(points, points)
In [57]: xs
Out[57]:
array([[-5., -4.99, -4.98, ..., 4.97, 4.98, 4.99],
       [-5., -4.99, -4.98, ..., 4.97, 4.98, 4.99],
[-5., -4.99, -4.98, ..., 4.97, 4.98, 4.99],
              , -4.99, -4.98, ..., 4.97, 4.98, 4.99],
       [-5.
       [-5., -4.99, -4.98, ..., 4.97, 4.98, 4.99],
       [-5., -4.99, -4.98, \ldots, 4.97, 4.98, 4.99]])
In [58]: ys
Out[58]:
array([[-5. , -5. , -5. , -5. , -5. , -5. ],
       [-4.99, -4.99, -4.99, ..., -4.99, -4.99, -4.99],
       [-4.98, -4.98, -4.98, \dots, -4.98, -4.98, -4.98],
       [ 4.97, 4.97, 4.97, ..., 4.97, 4.97, 4.97], [ 4.98, 4.98, 4.98, ..., 4.98, 4.98, 4.98], [ 4.99, 4.99, 4.99, ..., 4.99, 4.99, 4.99]])
In [59]: import matplotlib.pyplot as plt
In [60]: %matplotlib
Using matplotlib backend: MacOSX
In [61]: z = np.sqrt(xs**2 + ys**2)
In [62]: z
Out[62]:
array([[ 7.07106781, 7.06400028, 7.05693985, ..., 7.04988652,
         7.05693985, 7.06400028],
       [7.06400028, 7.05692568, 7.04985815, ..., 7.04279774,
         7.04985815, 7.05692568],
       [7.05693985, 7.04985815, 7.04278354, ..., 7.03571603,
         7.04278354, 7.04985815],
       [7.04988652, 7.04279774, 7.03571603, ..., 7.0286414,
         7.03571603, 7.04279774],
       [ 7.05693985, 7.04985815, 7.04278354, ..., 7.03571603, 7.04278354, 7.04985815], [ 7.06400028, 7.05692568, 7.04985815, ..., 7.04279774, 7.04985815, 7.05692568]])
In [63]: plt.imshow(z, cmap = plt.cm.grey); ply.colorbar()
                                              Traceback (most recent call last)
AttributeError
<ipython-input-63-5a86dbc5197e> in <module>()
---> 1 plt.imshow(z, cmap = plt.cm.grey); ply.colorbar()
AttributeError: 'module' object has no attribute 'grey'
In [64]: plt.imshow(z, cmap = plt.cm.gray); ply.colorbar()
NameError
                                              Traceback (most recent call last)
<ipython-input-64-ebdb61bf9200> in <module>()
---> 1 plt.imshow(z, cmap = plt.cm.gray); ply.colorbar()
NameError: name 'ply' is not defined
In [65]: plt.imshow(z, cmap = plt.cm.gray); plt.colorbar()
Out[65]: <matplotlib.colorbar.Colorbar at 0x114424a10>
```

```
In [66]: arr = np.random.randn(4, 4)
In [67]: arr
Out[67]:
array([[ 0.99715976, -0.99285941, -1.29983152, 0.26311053],
       [ 1.44502703, 0.76717446, 0.45337043, 0.19472739], [ 0.48680544, 0.51659521, -0.17987949, -0.50011625], [ 1.21627682, 1.46086937, 0.4304918, -0.28471634]])
In [68]: arr
Out[68]:
array([[ 0.99715976, -0.99285941, -1.29983152, 0.26311053],
       [ 1.44502703, 0.76717446, 0.45337043, 0.19472739],
       [ 0.48680544, 0.51659521, -0.17987949, -0.50011625],
       [ 1.21627682, 1.46086937, 0.4304918, -0.28471634]])
In [69]: arr = np.array([[0,1,2], [3,4,5], [6,7,8]])
In [70]: arr
Out[70]:
array([[0, 1, 2],
       [3, 4, 5],
       [6, 7, 8]])
In [71]: arr.cumsum(0)
Out[71]:
In [72]: arr.cumprod(0)
Out[72]:
array([[ 0, 1, 2], [ 0, 4, 10],
       [ 0, 28, 80]])
In [73]: arr.cumprod(1)
Out[73]:
array([[ 0, 0, 0],
       [ 3, 12, 60],
       [ 6, 42, 336]])
In [74]: arr.cumprod(2)
ValueError
                                      Traceback (most recent call last)
<ipython-input-74-db4582eaf51a> in <module>()
---> 1 arr.cumprod(2)
ValueError: axis(=2) out of bounds
In [75]: arr.cumprod()
Out[75]: array([0, 0, 0, 0, 0, 0, 0, 0])
In [76]: arr.cumsum()
Out[76]: array([ 0, 1, 3, 6, 10, 15, 21, 28, 36])
In [77]: arr = np.random.randn(8)
In [78]: arr.sort(-1)
In [79]: arr
Out[79]:
array([-1.67419884, -1.0020941 , -0.64800766, 0.5882544 , 0.68288943,
        1.01370844, 1.41173385, 1.69355966])
In [80]: arr.sort()
In [81]: arr
```

```
Out[81]:
array([-1.67419884, -1.0020941 , -0.64800766, 0.5882544 , 0.68288943,
        1.01370844, 1.41173385, 1.69355966])
In [82]: arr.sort(1)
ValueError
                                          Traceback (most recent call last)
<ipython-input-82-e68aa76b5f43> in <module>()
---> 1 arr.sort(1)
ValueError: axis(=1) out of bounds
In [83]: arr.sort(0)
In [84]: arr
Out[84]:
array( \hbox{$[-1.67419884, -1.0020941 , -0.64800766, 0.5882544 , 0.68288943, }
        1.01370844, 1.41173385, 1.69355966])
In [85]: arr.sort?
Docstring:
a.sort(axis=-1, kind='quicksort', order=None)
Sort an array, in-place.
Parameters
axis : int, optional
    Axis along which to sort. Default is -1, which means sort along the
kind : {'quicksort', 'mergesort', 'heapsort'}, optional
    Sorting algorithm. Default is 'quicksort'.
order: str or list of str, optional
    When `a` is an array with fields defined, this argument specifies
    which fields to compare first, second, etc. A single field can
    be specified as a string, and not all fields need be specified,
    but unspecified fields will still be used, in the order in which
    they come up in the dtype, to break ties.
See Also
numpy.sort : Return a sorted copy of an array.
argsort : Indirect sort.
lexsort : Indirect stable sort on multiple keys.
searchsorted : Find elements in sorted array.
partition: Partial sort.
Notes
See ``sort`` for notes on the different sorting algorithms.
Examples
-----
>>> a = np.array([[1,4], [3,1]])
>>> a.sort(axis=1)
>>> a
array([[1, 4],
      [1, 3]])
>>> a.sort(axis=0)
>>> a
array([[1, 3],
       [1, 4]])
Use the `order` keyword to specify a field to use when sorting a
structured array:
>>> a = np.array([('a', 2), ('c', 1)], dtype=[('x', 'S1'), ('y', int)])
>>> a.sort(order='y')
```

```
array([('c', 1), ('a', 2)],
     dtype=[('x', 'IS1'), ('y', '<i4')])</pre>
          builtin_function_or_method
In [86]: np.random.randn?
Docstring:
randn(d0, d1, ..., dn)
Return a sample (or samples) from the "standard normal" distribution.
If positive, int_like or int-convertible arguments are provided,
`randn` generates an array of shape ``(d0, d1, ..., dn)``, filled
with random floats sampled from a univariate "normal" (Gaussian)
distribution of mean 0 and variance 1 (if any of the :math:`d_i` are
floats, they are first converted to integers by truncation). A single
float randomly sampled from the distribution is returned if no
argument is provided.
This is a convenience function. If you want an interface that takes a
tuple as the first argument, use `numpy.random.standard_normal` instead.
Parameters
d0, d1, ..., dn : int, optional
    The dimensions of the returned array, should be all positive.
    If no argument is given a single Python float is returned.
Returns
Z : ndarray or float
    A ``(d0, d1, ..., dn)``-shaped array of floating-point samples from
    the standard normal distribution, or a single such float if
    no parameters were supplied.
See Also
random.standard_normal : Similar, but takes a tuple as its argument.
Notes
For random samples from :math: `N(\mu, \sigma^2)`, use:
``sigma * np.random.randn(...) + mu``
Examples
>>> np.random.randn()
2.1923875335537315 #random
Two-by-four array of samples from N(3, 6.25):
\Rightarrow 2.5 * np.random.randn(2, 4) + 3
array([[-4.49401501, 4.00950034, -1.81814867, 7.29718677], #random
       [ 0.39924804, 4.68456316, 4.99394529, 4.84057254]]) #random
Type:
          builtin_function_or_method
In [87]: np.ones(3)
Out[87]: array([ 1., 1., 1.])
In [88]: np.ones(3,3)
TypeError
                                          Traceback (most recent call last)
<ipython-input-88-370a00780af9> in <module>()
---> 1 \text{ np.ones}(3,3)
/Users/Hansen/anaconda/lib/python2.7/site-packages/numpy/core/numeric.pyc in ones(shape, dtype, order
```

```
188
           .....
   189
--> 190
           a = empty(shape, dtype, order)
          multiarray.copyto(a, 1, casting='unsafe')
   191
   192
           return a
TypeError: data type not understood
In [89]: np.ones([3,3])
Out[89]:
In [90]: %timeit np.random.normal(size = 8)
The slowest run took 180.23 times longer than the fastest. This could mean that an intermediate resul
t is being cached.
100000 loops, best of 3: 2.06 µs per loop
In [91]: %timeit np.random.normal(size = 1000000)
10 loops, best of 3: 38.9 ms per loop
In [92]: nwalks = 5000
In [93]: nsteps = 1000
In [94]: draws = np.random.randint(0, 2, size = (nwalks, nsteps))
In [95]: steps = np.where(de)
%%debug %debug def
                        del
                                  delattr
In [95]: steps = np.where(dr)
        dreload
draws
In [95]: steps = np.where(draws > 0, 1, -1)
In [96]: walks = steps.cumsum(1)
In [97]: walks
Out[97]:
             0, 1, ..., 38, 37, 38],
array([[ -1,
             0, -1, ..., 2, 3, 4],
-2, -3, ..., -56, -55, -54],
      [ -1,
      [ -1,
      [ 1,
             0, -1, ..., 38, 37, 36],
             0, -1, ..., -20, -19, -20],
      [ 1,
             2, 3, ..., 34, 35, 34]])
      [ 1,
In [98]: walks.max(nwalks -1 )
ValueError
                                         Traceback (most recent call last)
<ipython-input-98-63532e358457> in <module>()
---> 1 walks.max(nwalks -1)
/Users/Hansen/anaconda/lib/python2.7/site-packages/numpy/core/_methods.pyc in _amax(a, axis, out, kee
pdims)
     24 # small reductions
     25 def _amax(a, axis=None, out=None, keepdims=False):
         return umr_maximum(a, axis, None, out, keepdims)
     28 def _amin(a, axis=None, out=None, keepdims=False):
ValueError: 'axis' entry is out of bounds
In [99]: walks.max(nteps -1 )
                                         Traceback (most recent call last)
<ipython-input-99-511f61c365aa> in <module>()
```

```
---> 1 walks.max(nteps -1 )
NameError: name 'nteps' is not defined
In [100]: walks.max(nsteps -1 )
                                       Traceback (most recent call last)
<ipython-input-100-1dc7e8d8c620> in <module>()
---> 1 walks.max(nsteps -1)
/Users/Hansen/anaconda/lib/python2.7/site-packages/numpy/core/_methods.pyc in _amax(a, axis, out, kee
pdims)
    24 # small reductions
    25 def _amax(a, axis=None, out=None, keepdims=False):
---> 26 return umr_maximum(a, axis, None, out, keepdims)
    27
    28 def _amin(a, axis=None, out=None, keepdims=False):
ValueError: 'axis' entry is out of bounds
In [101]: walks.size()
______
TypeError
                                        Traceback (most recent call last)
<ipython-input-101-1b6c024318ca> in <module>()
---> 1 walks.size()
TypeError: 'int' object is not callable
In [102]: walks
Out[102]:
      [ -1, 0, 1, ..., 38, 37, 38],
[ -1, 0, -1, ..., 2, 3, 4],
[ -1, -2, -3, ..., -56, -55, -54],
array([[ -1,
      [ 1,
            0, -1, ..., 38, 37, 36],
      [ 1, 0, -1, \ldots, -20, -19, -20],
      [ 1, 2, 3, ..., 34, 35, 34]])
In [103]:
```