

Overlay analysis and Map Algebra

Spatial Data Analysis and Simulation modelling,
2020, Simon Scheider



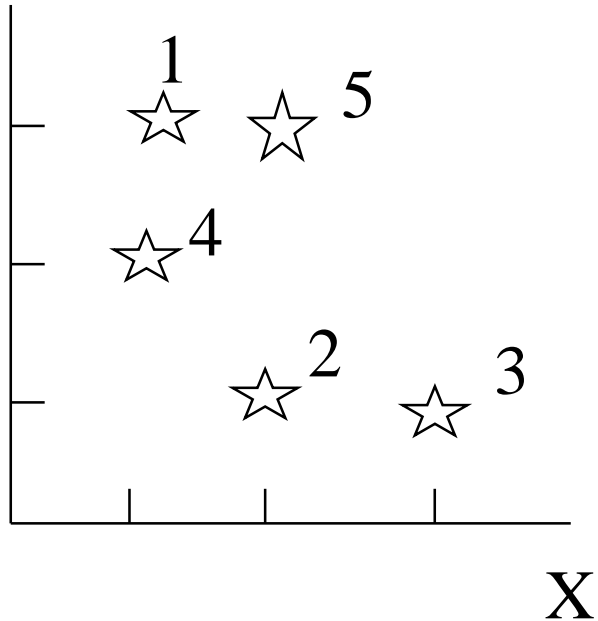
Outline

- Vector Overlay and Analysis:
 - Spatial relations
 - Selection
 - Overlay
 - Spatial Join
- Raster Overlay and Analysis:
 - Local map algebra
 - Zonal map algebra

Vector Overlay and Analysis

Vector data format

e.g. point data



Objects have unique identifiers--
point ID, polygon ID, arc ID, etc

common identifiers provide link to:

—geometry table (for 'where')

—attributes table (for what)

Coordinates Table		
Point ID	x	y
1	1	3
2	2	1
3	4	1
4	1	2
5	3	2

Attributes Table		
Point ID	model	year
1	a	90
2	b	90
3	b	80
4	a	70
5	c	70

Relational (table based) data representation

GIS contain tables (feature classes) in which:

- *rows: entities* (records, observations, features):
 - ‘all’ information about one occurrence of a feature
- *columns: attributes* (fields, data elements, variables, items (ArcGIS))
 - one type of information for all features

The *key* field is an attribute whose values uniquely identify each row

Parcel Table			
Parcel #	Address	Block	\$ Value
8	501 N Hi	1	105,450
9	590 N Hi	2	89,780
36	1001 W. Main	4	101,500
75	1175 W. 1st	12	98,000

Field Calculator

Field calculator

Description: Field calculator

Input layer: 'Added geom info' from algorithm 'Add geometry attributes'


Result field name: 123 product

Field type: 123 Float

Field length: 123 10

Field precision: 123 5

Create new field: 123 Yes

Formula: 123 NULL ELSE attribute(\$currentfeature, 'area') * attribute(\$currentfeature, 'P_65_EO_JR') END 

Calculated: calc

Parent algorithms: 0 elements selected

OK Cancel Help

Formula

Expression Function Editor

= + - / * ^ || () '\n'

Search... Show Help

```
CASE
WHEN attribute($
currentfeature, 'BU_CODE')
IS NULL
OR attribute($
currentfeature,
'P_65_EO_JR') <= 0
THEN NULL
ELSE attribute($
currentfeature, 'area') *
attribute($currentfeature,
'P_65_EO_JR')
END
```

Output preview: NULL

- Add_geometr...
- Add_geometr...
- Add_geometr...
- Add_geometr...
- algorithm_id
- Intersection_...
- Intersection_...
- Intersection_...
- Intersection_...
- Intersection_...
- parameter
- sourcelayer
- sourcelayer_m...
- sourcelayer_m...
- sourcelayer_m...
- sourcelayer_m...
- targetlayer
- targetlayer_m...

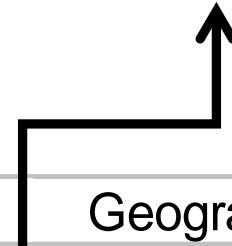
Table join

Produce map of values by district/ neighborhood

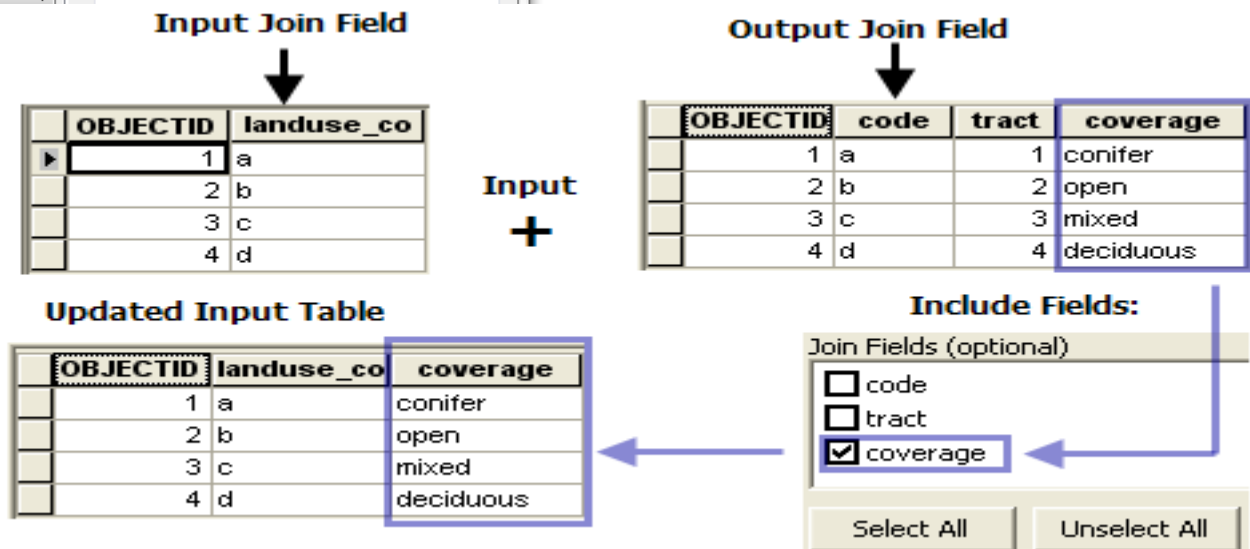
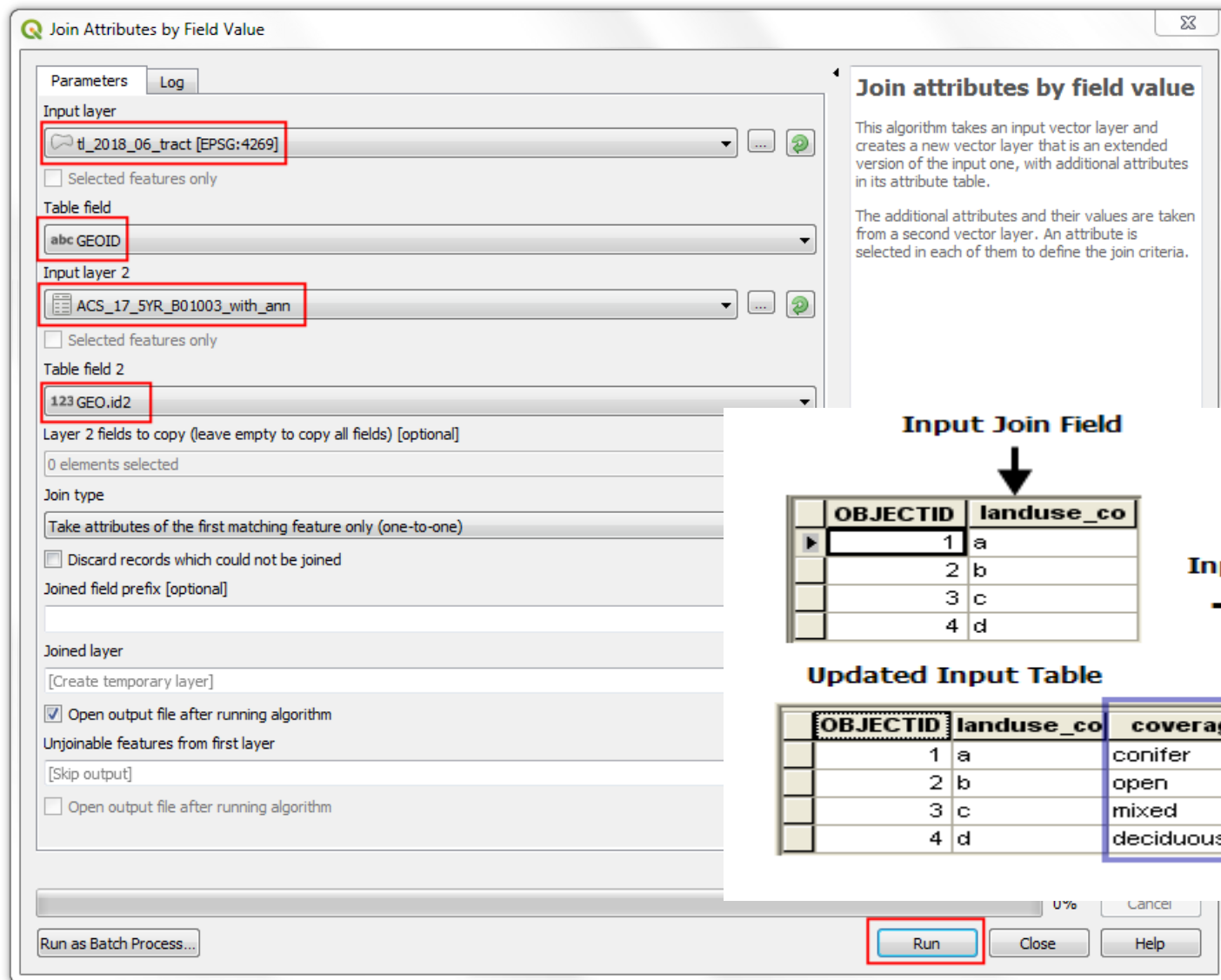
- Problem: no district code available in parcel Table
- Solution: join Parcel Table, containing values, with Geography Table, containing location codings, using Block as key field

Parcel Table			
Parcel #	Address	Block	\$ Value
8	501 N Hi	1	105,450
9	590 N Hi	2	89,780
36	1001 W. Main	4	101,500
75	1175 W. 1st	12	98,000

Geography Table			
Block	District	Tract	City
1	A	101	Dallas
2	B	101	Dallas
4	B	105	Dallas
12	E	202	Garland

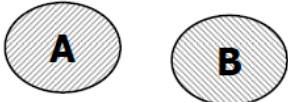



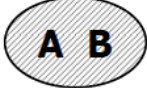





Join Attributes by Field Value

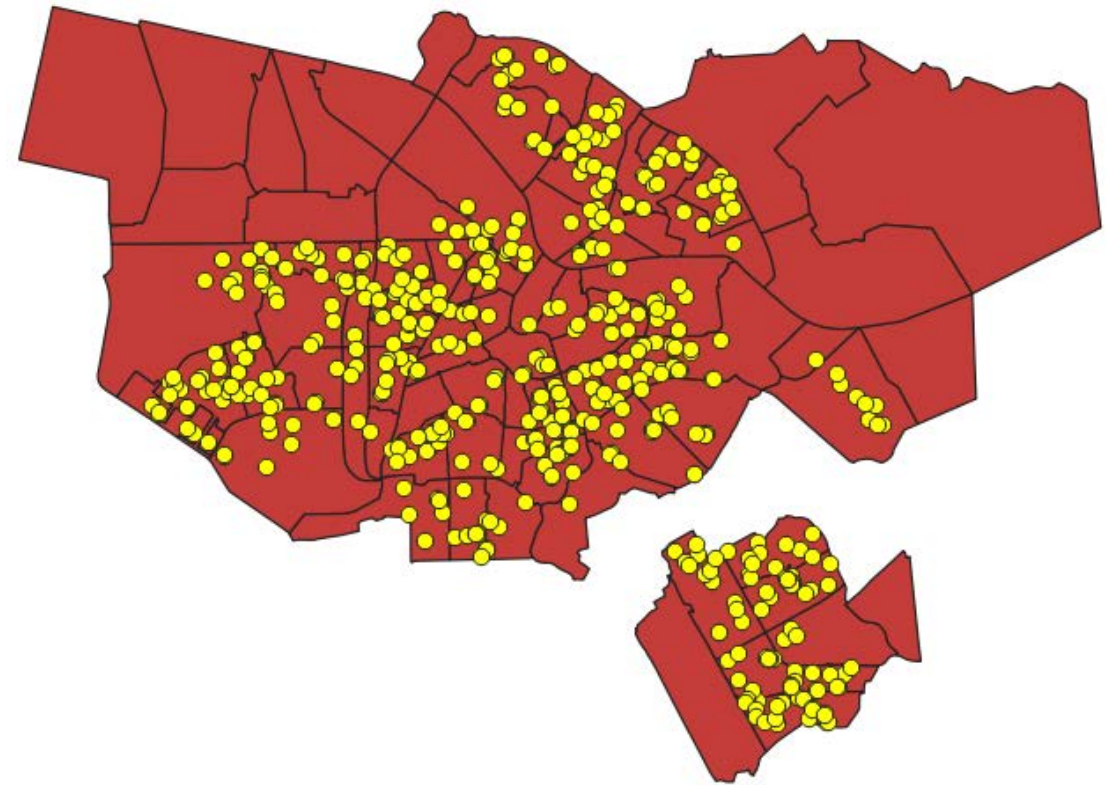
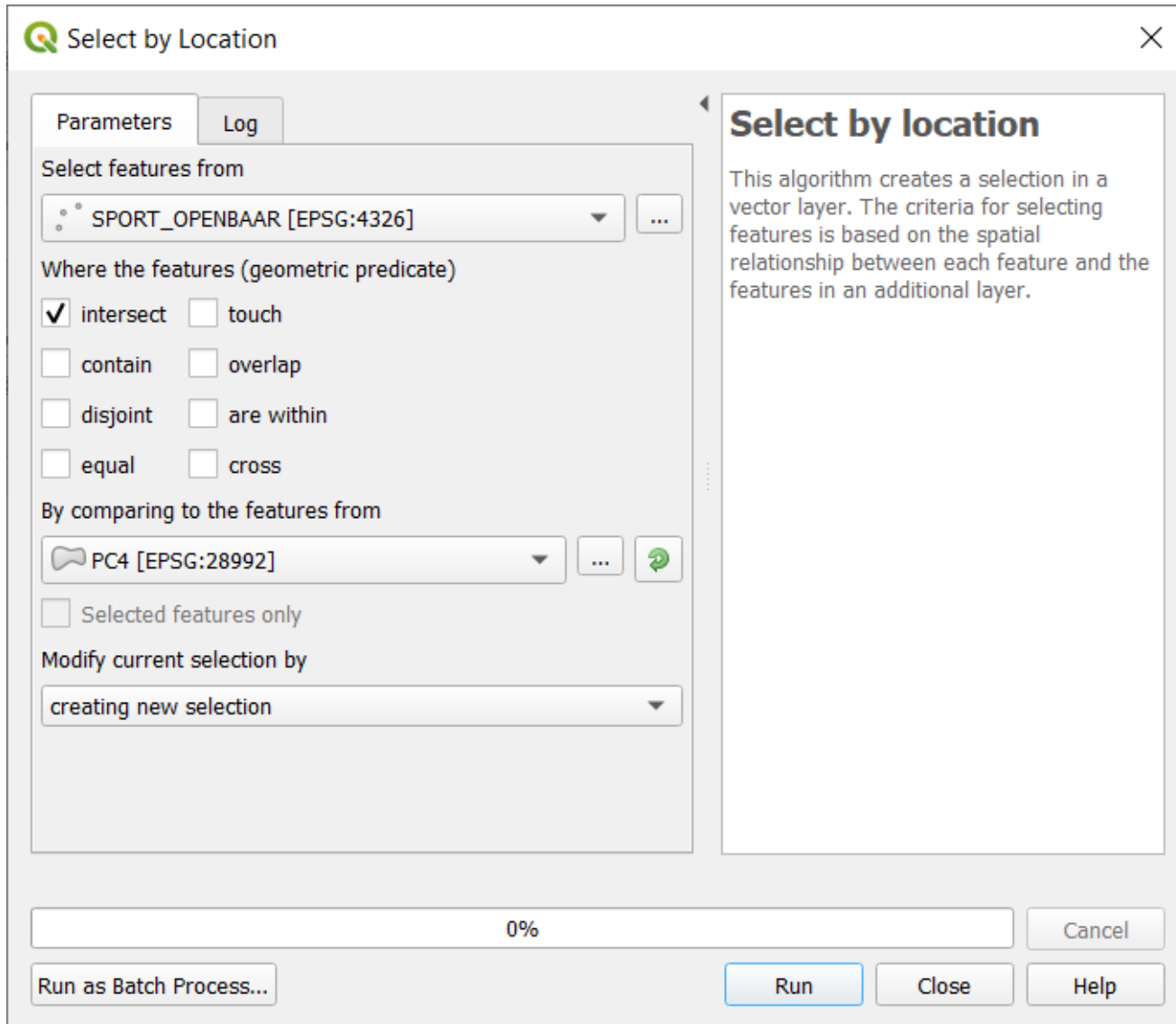


Spatial relations

- Spatial (e.g. topological) relationships can be used for joining features
- Egenhofer's 9-Intersection matrix allows to capture such relations
- Intersect =
All that is not disjoint

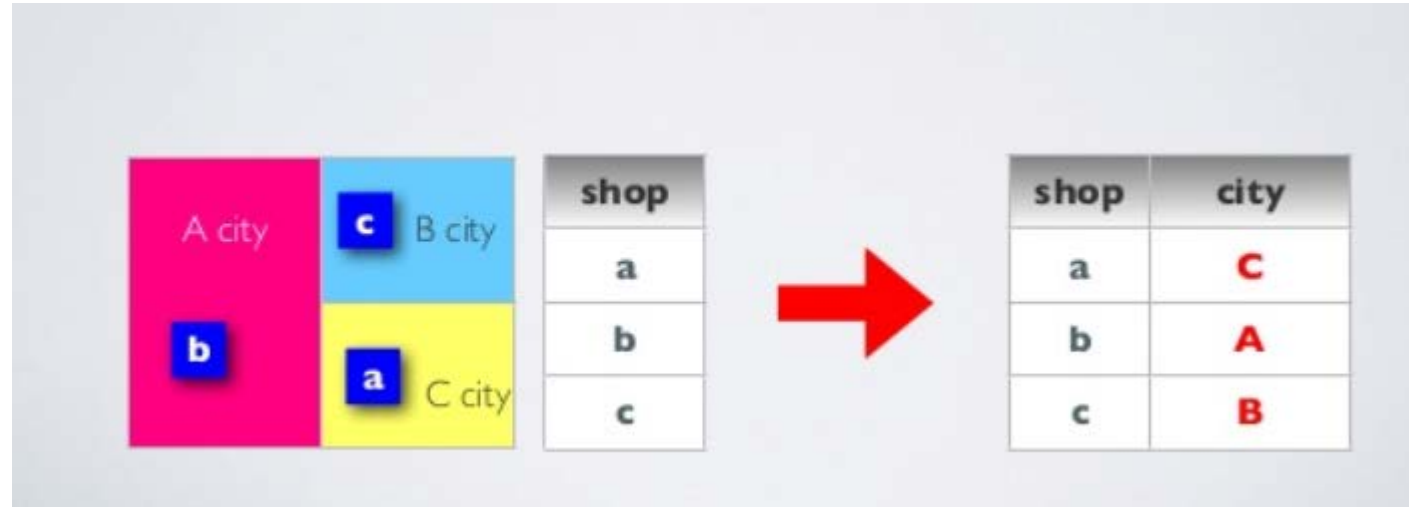
 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \emptyset & \emptyset & \neg \emptyset \\ A^\circ & \emptyset & \emptyset & \neg \emptyset \\ A^- & \neg \emptyset & \neg \emptyset & \neg \emptyset \end{matrix}$ <p>disjoint</p>	 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \neg \emptyset & \emptyset & \neg \emptyset \\ A^\circ & \emptyset & \emptyset & \neg \emptyset \\ A^- & \neg \emptyset & \neg \emptyset & \neg \emptyset \end{matrix}$ <p>meet</p>	 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \emptyset & \emptyset & \neg \emptyset \\ A^\circ & \neg \emptyset & \neg \emptyset & \neg \emptyset \\ A^- & \emptyset & \emptyset & \neg \emptyset \end{matrix}$ <p>contains</p>	 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \neg \emptyset & \emptyset & \neg \emptyset \\ A^\circ & \neg \emptyset & \neg \emptyset & \neg \emptyset \\ A^- & \emptyset & \emptyset & \neg \emptyset \end{matrix}$ <p>covers</p>
 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \neg \emptyset & \emptyset & \emptyset \\ A^\circ & \emptyset & \neg \emptyset & \emptyset \\ A^- & \emptyset & \emptyset & \neg \emptyset \end{matrix}$ <p>equal</p>	 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \neg \emptyset & \neg \emptyset & \neg \emptyset \\ A^\circ & \neg \emptyset & \neg \emptyset & \neg \emptyset \\ A^- & \neg \emptyset & \neg \emptyset & \neg \emptyset \end{matrix}$ <p>overlap</p>	 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \emptyset & \neg \emptyset & \emptyset \\ A^\circ & \emptyset & \neg \emptyset & \emptyset \\ A^- & \neg \emptyset & \neg \emptyset & \neg \emptyset \end{matrix}$ <p>inside</p>	 $\begin{matrix} & \partial B & B^\circ & B^- \\ \partial A & \neg \emptyset & \neg \emptyset & \emptyset \\ A^\circ & \emptyset & \neg \emptyset & \emptyset \\ A^- & \neg \emptyset & \neg \emptyset & \neg \emptyset \end{matrix}$ <p>covered by</p>

Selecting layers by location

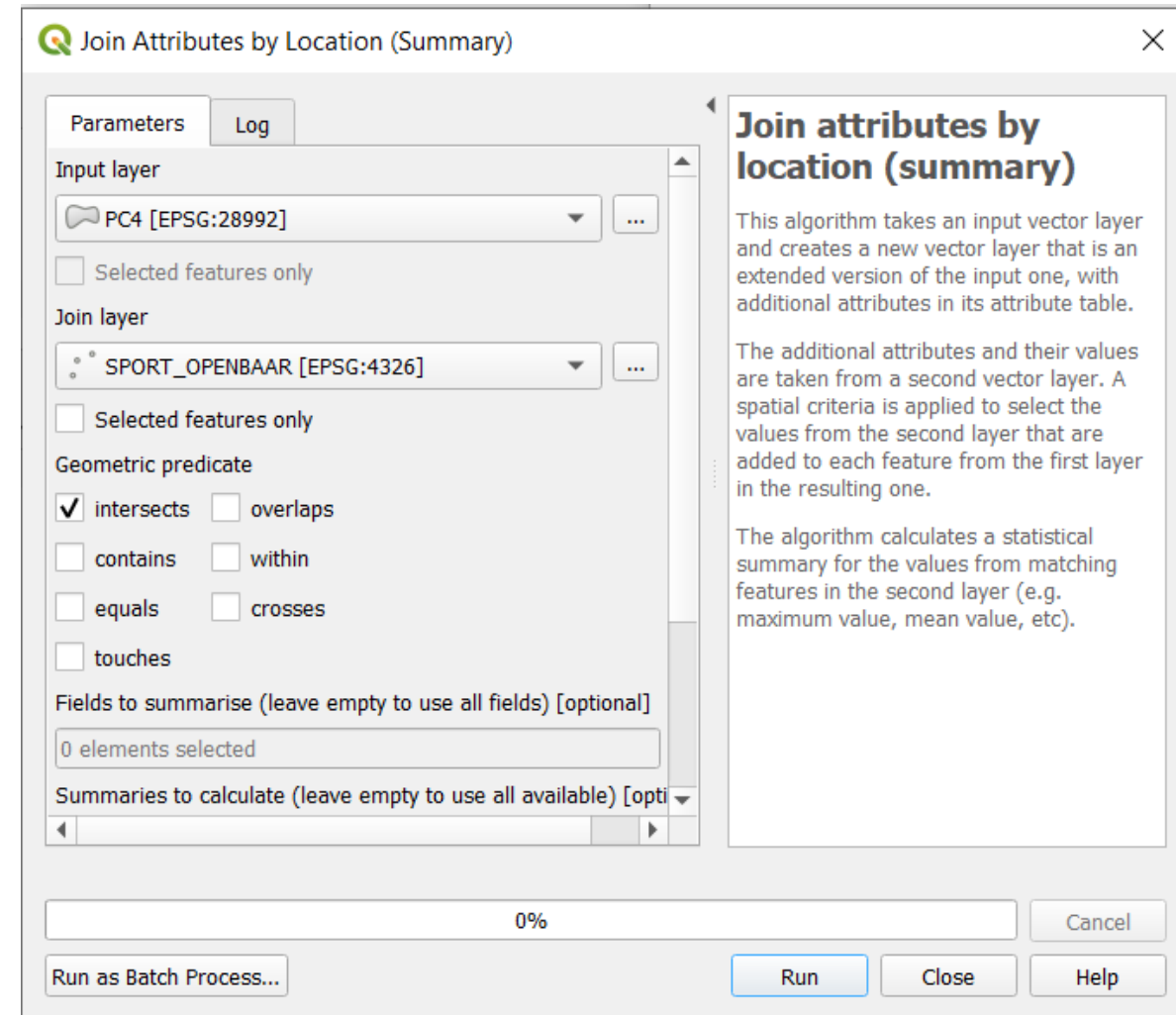
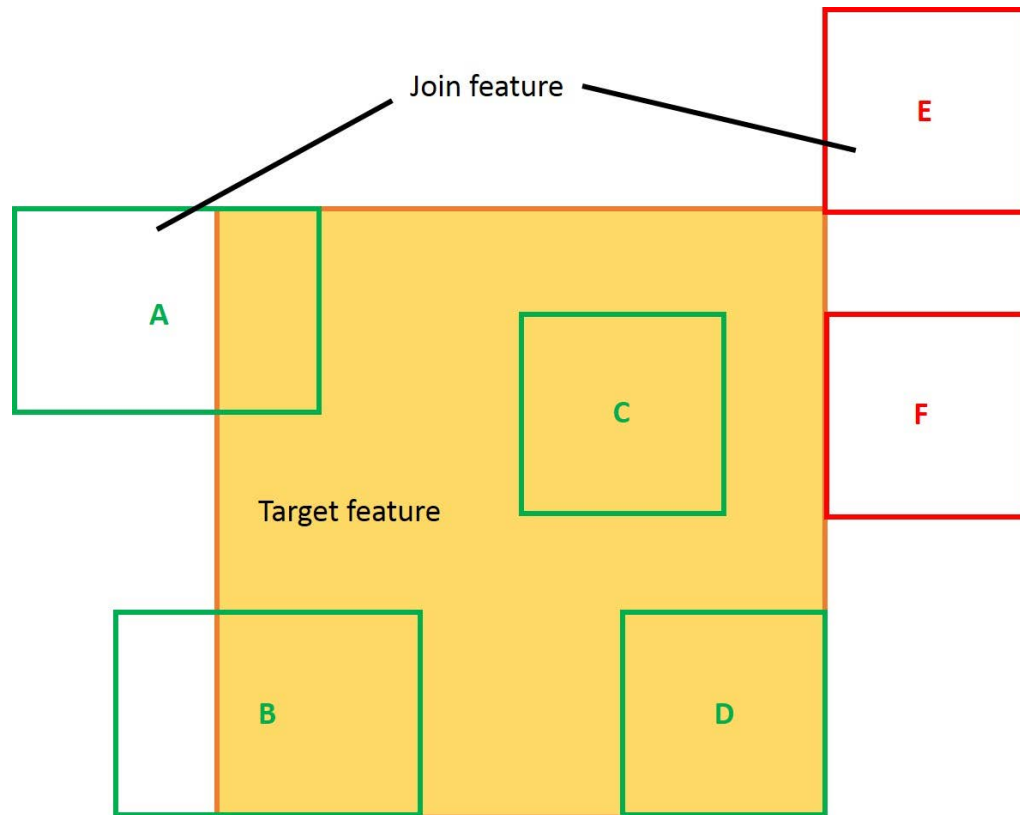


Spatial Join

- Joins attributes from one feature to another based on a spatial relationship. The target features and the joined attributes from the join features are written to the output feature class.

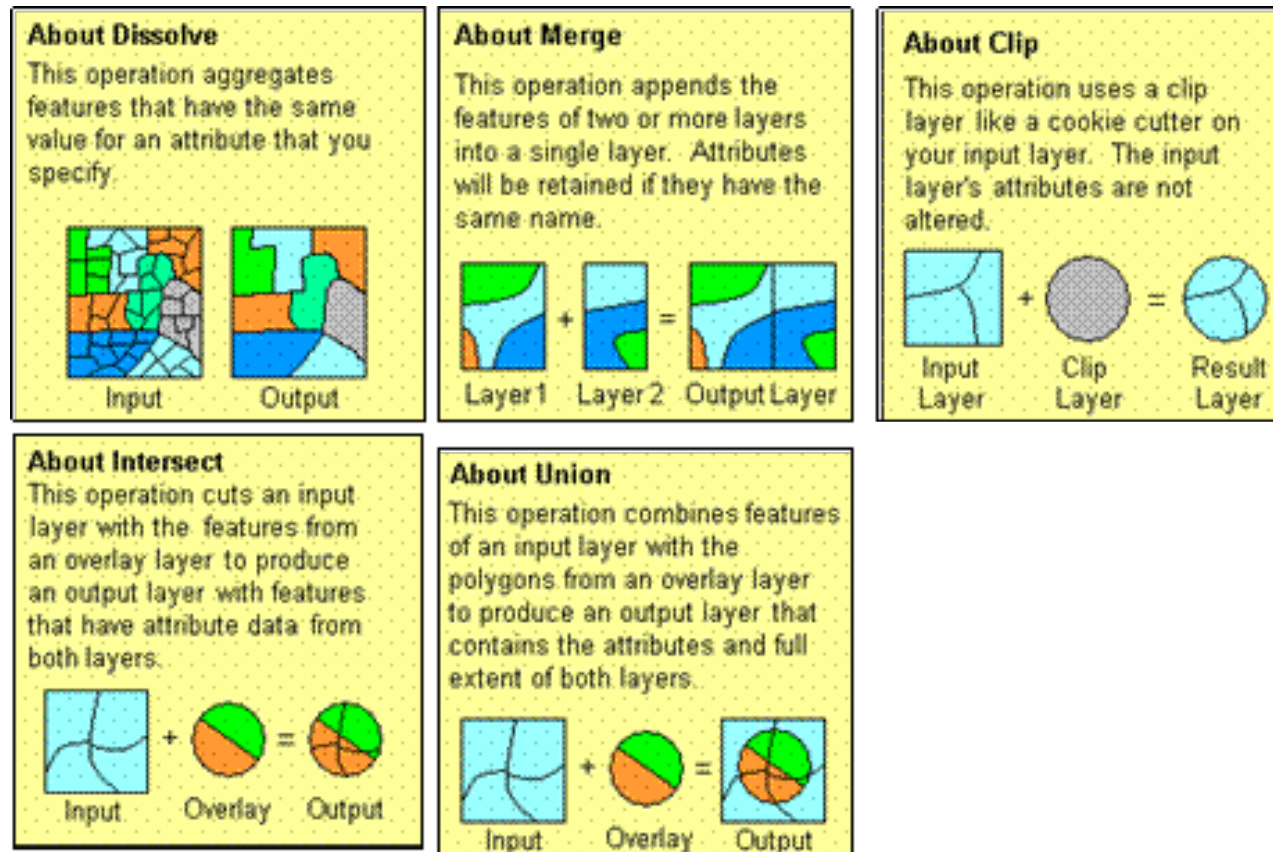


Join Attribute by Location (Summary)



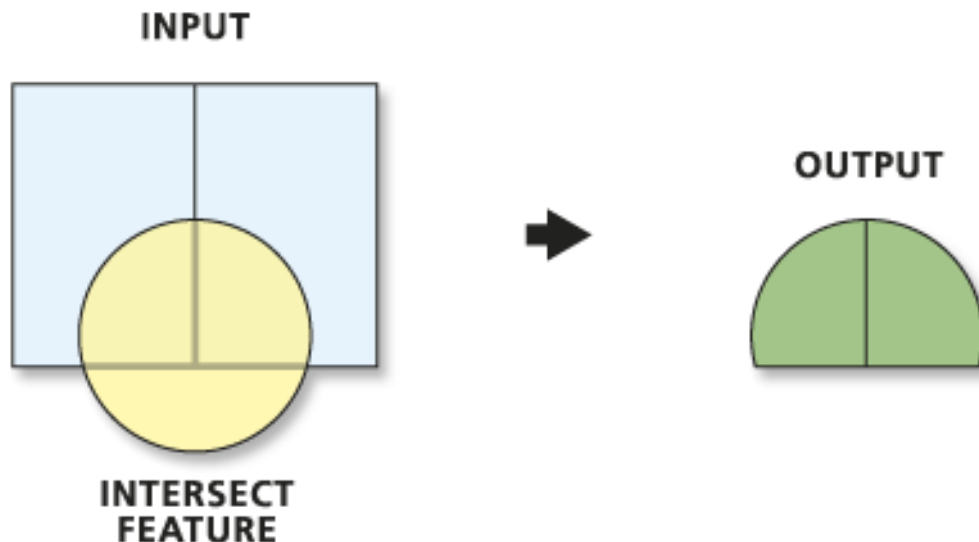
Overlay: Intersect/Clip/Union/Merge/Dissolve

- These are point set operations (intersections or unions of point sets)
- Input are polygons or lines
- Output are new polygons or lines that were generated based on the input



Example: Intersection

- This operation does a geometric intersection and keeps only the parts in both layers



QGIS Intersection

Properties Comments

Description Intersection

Show advanced parameters

Input layer
Using model input Target Layer

Overlay layer
Using model input Source Layer

Input fields to keep (leave empty to keep all fields) [optional]
123

Overlay fields to keep (leave empty to keep all fields) [optional]
123

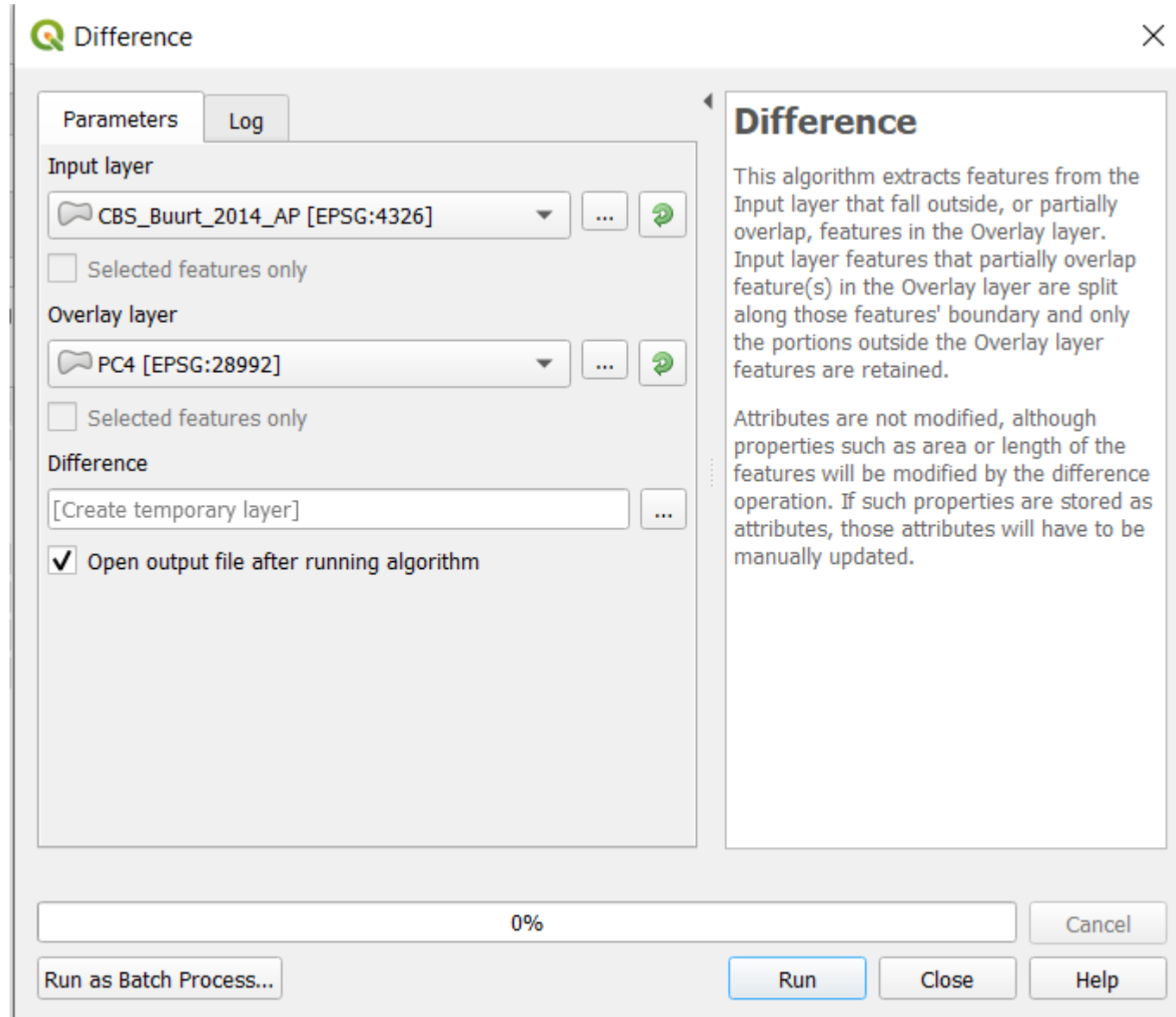
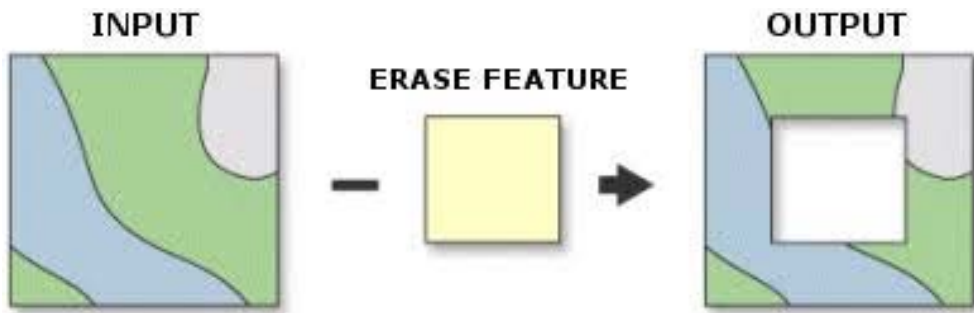
Intersection
[Enter name if this is a final result]

Dependencies
0 dependencies selected

OK Cancel Help

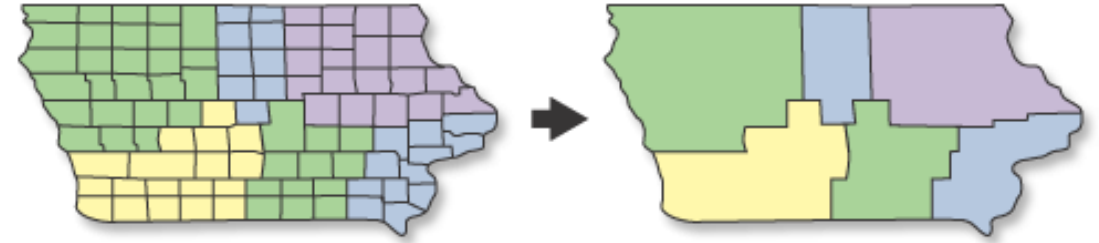
Example: Difference

- This operation subtracts a layer from another one



Example: Aggregate

- This operation aggregates a polygon layer using some attribute and using some statistics
- Sometimes also called “Dissolve”



Aggregate

Properties Comments

Description: Aggregate

Input layer: Using algorithm output "Calculated" from algorithm "Field calculator"

Group by expression (NULL to group all features): 123 Postcode4

Aggregates

	Source Expression	Aggregate Function	Delimiter	Name	Type	Length	Precision
0	abc Postcode4	concatenate_unique	,	Postcode4	Text (string)	254	0
1	123 Opp_m2	sum	,	Opp_m2	Whole number (integer - 64bit)	10	0
2	abc BU_CODE	concatenate	,	BU_CODE	Text (string)	10	0

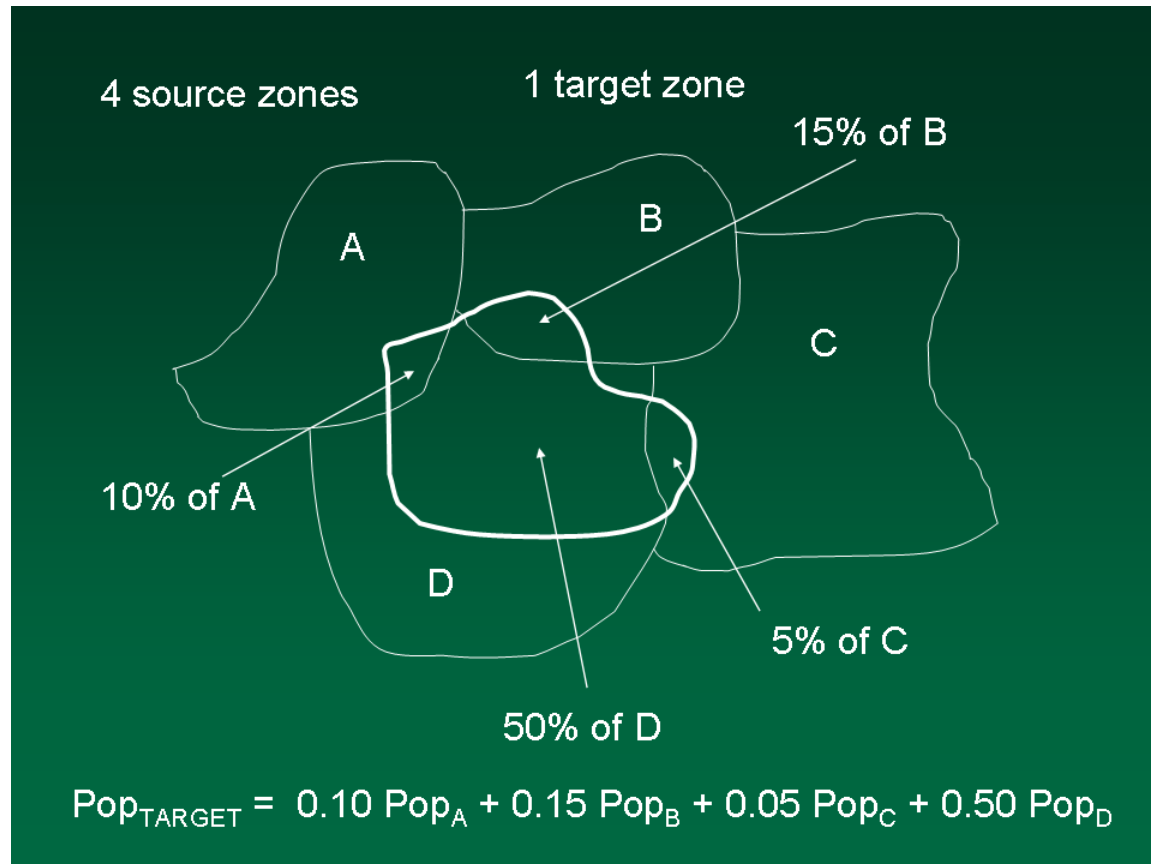
Load fields from template layer: final Load Fields

Aggregated: [Enter name if this is a final result]

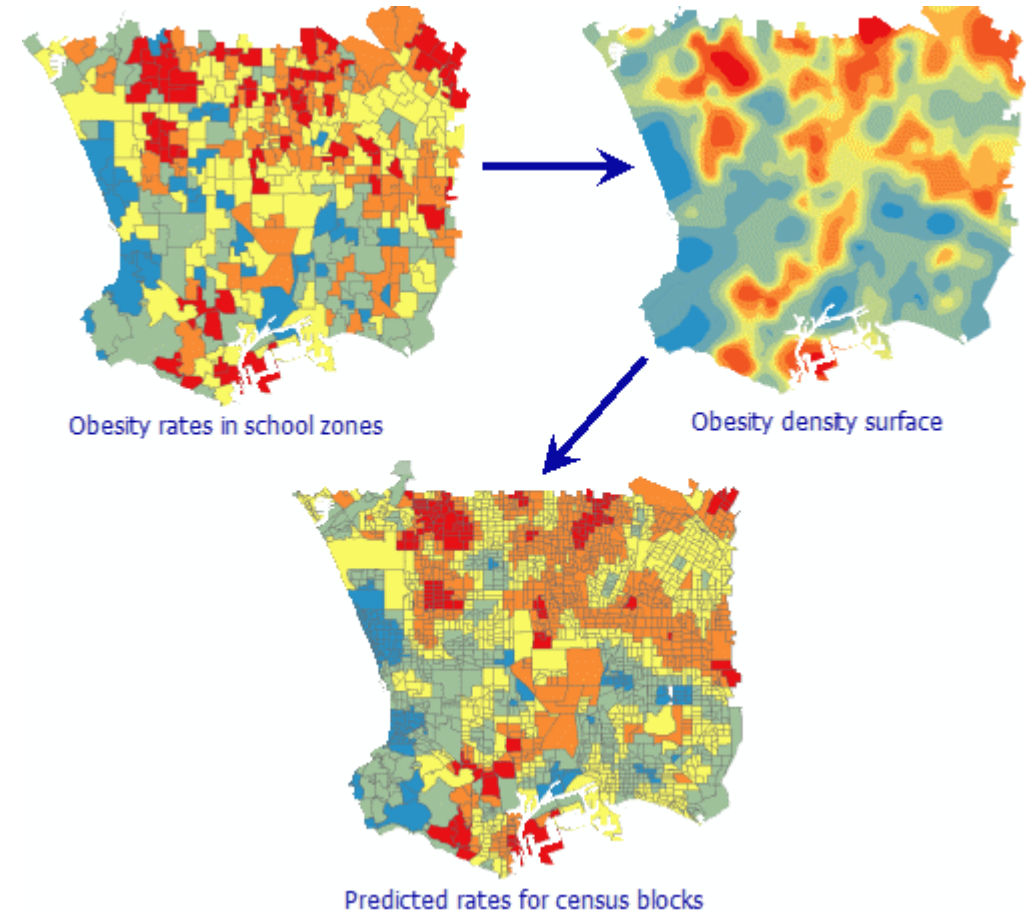
OK Cancel Help

Areal Interpolation

“Simple” approach with overlay

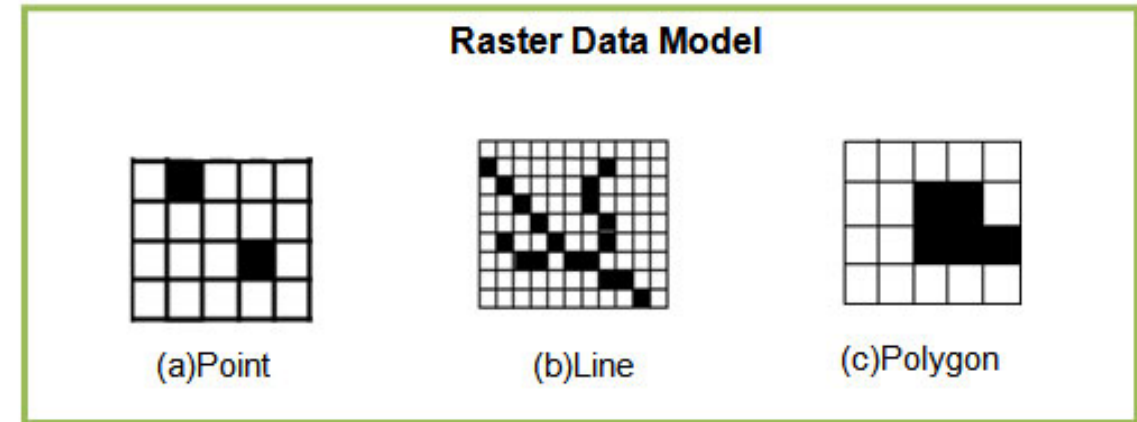


Kriging (Geostatistical Analyst)



Raster Overlay Analysis

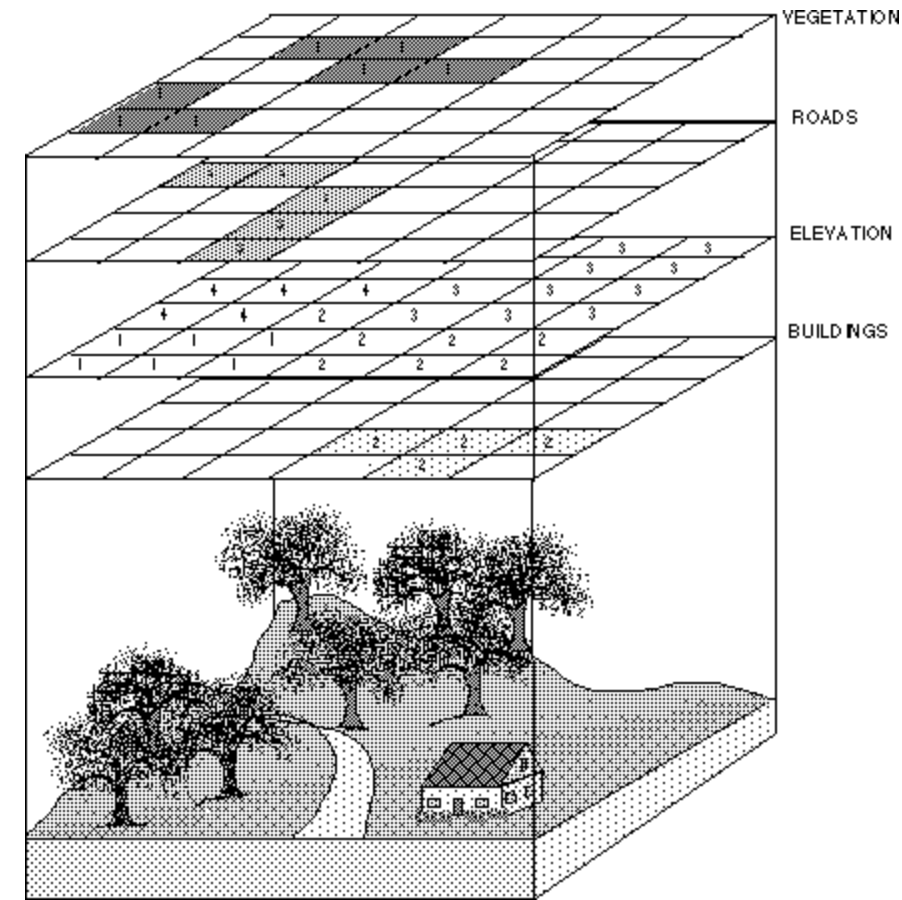
Raster data model



Array of cells or pixels (aka picture elements) which are arranged in rows and columns. Each pixel has a value in the form of integer, floating points or alphanumeric.

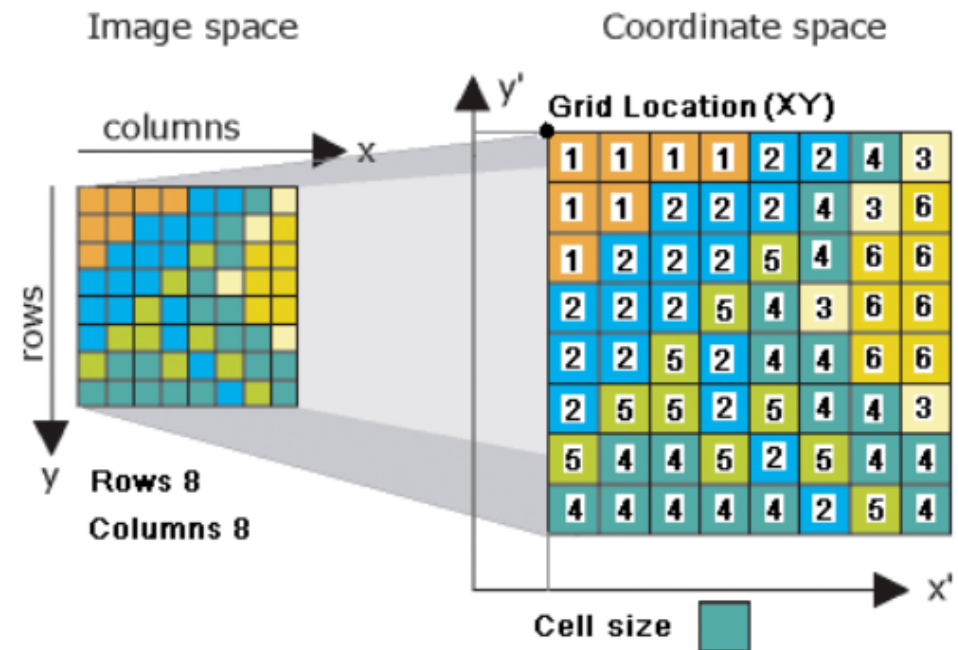
A point can be represented by a single pixel in raster model. A line is a chain of spatially connected cells with the same value.

Similarly, a water body in raster data is represented as a set of contiguous pixels having same value that represents a homogeneous area.



Raster cells: more than pixels

- Rows / columns of pixels
- Cell coordinates and values
- Possible meaning of cell value?
 - feature identifier
 - qualitative characteristic
 - quantitative characteristic
 - representation of zone

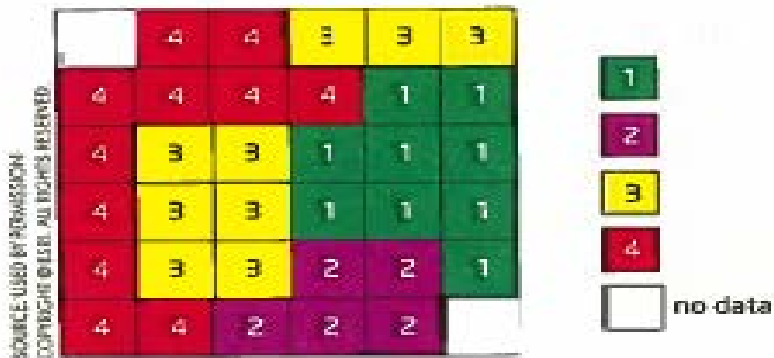


List of cell values

[11112243112224361222546622254366225244662552544354452544444254]

Raster zones, regions and NoData/Null

- Zone: refers to the set of cells sharing a certain value (connected or disconnected)
- Region: zone with connected cells
- NoData/Null \neq 0
- Associated table (in case of integers) (value,count)



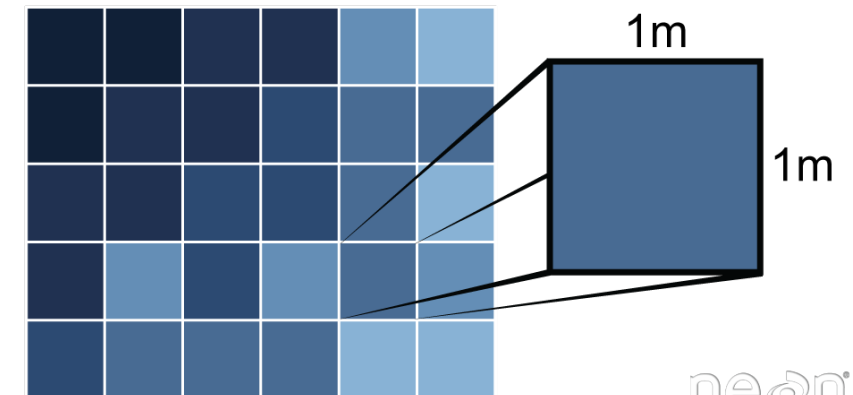
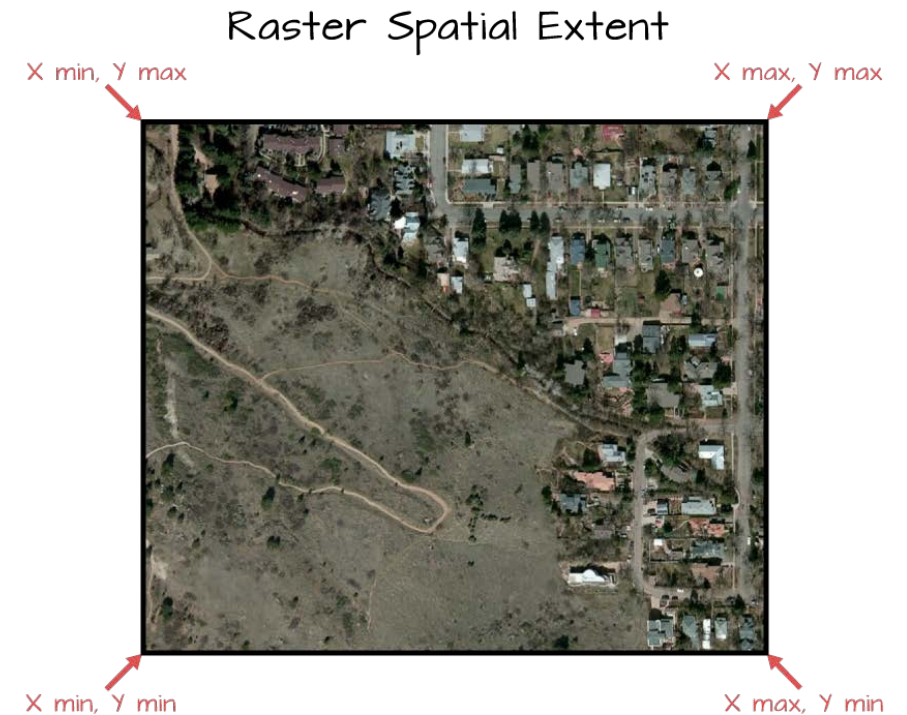
Cell size and extent

How to decide on resolution (cell size)?

- Resolution of input data
- The output needed for your analysis
- Response time (processing speed)
- Kind of application / analysis

Raster resolution increases as the size of the cell decreases

Raster extent: Same as display or layer?



Map Algebra

- Introduced by Dana **Tomlin** and Joseph **Berry** (Tomlin 1990)
- **Cell-by-cell** combination of raster data layers (addition, subtraction, multipl.,...)
- Simple **operations** on numbers stored as values at **raster** cell locations
- Output grids with results at the cell locations **corresponding to input cells**

Map Algebra: Basic elements

Building blocks for Map Algebra language are:

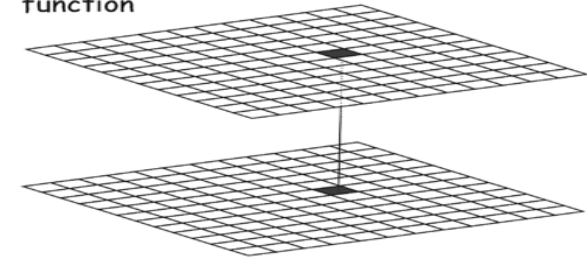
- **Objects** - datasets, layers, values (as inputs or storage location)
- **Operators** (+, -, *, ...)
- **Functions** (loc,foc,zon,glob)
- **Actions** – Result of applying functions with operators to objects
- **Qualifiers on the actions** – parameters determining the conduction of a function

Map Algebra: Functions

Higher-order GIS operation (why?)

- Important building blocks for modeling
- **Parameter-dependent**
- **Local**: cell-by-cell
- **Neighborhood (Focal)**: moving neighborhood
- **Zonal**: within homogeneous zones
- **Global**: incorporation of the full dataset

Local function



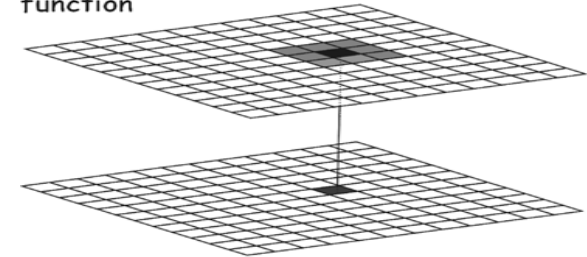
e.g.,

10	12	42
30	9	4
-12	8	15

plus 4

14	16	46
34	13	8
-8	12	19

Neighborhood function



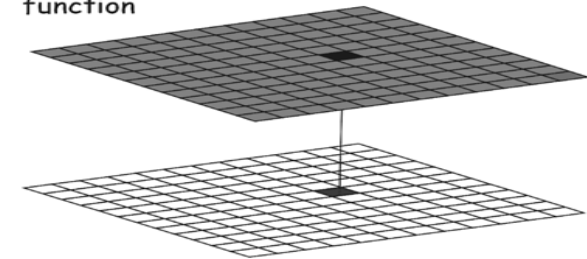
e.g.,

10	12	42
30	9	4
-12	8	15

neighborhood maximum

33	42	42
30	42	42
30	30	17

Global function



e.g.,

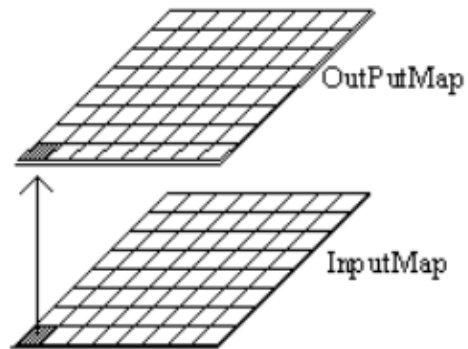
10	12	42
30	9	4
-12	8	15

global maximum

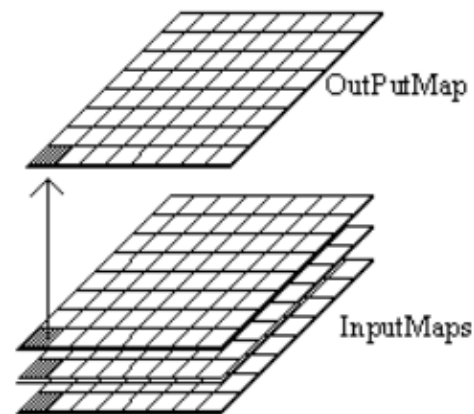
42	42	42
42	42	42
42	42	42

Example: Local Map algebra function

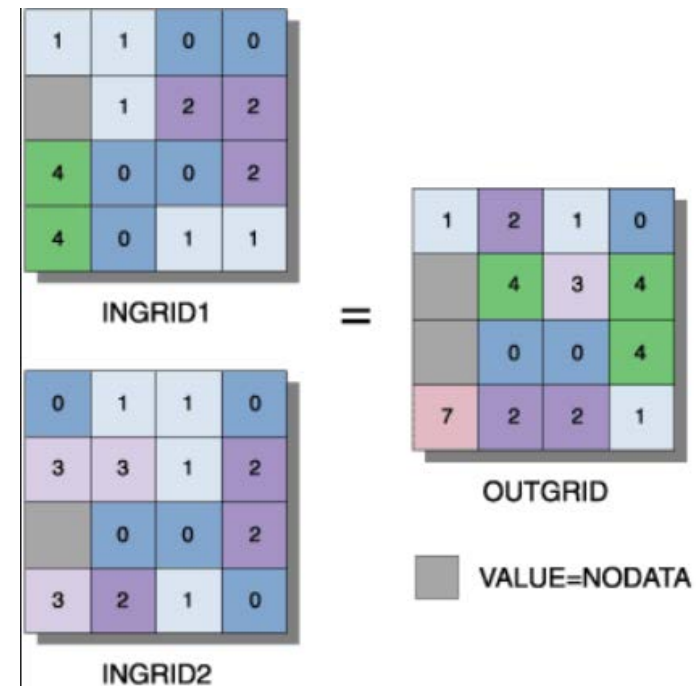
- Local functions: on equivalent cells across raster layers
- Quiz: What arithmetic operator is used in this local function example?
- local sum



a) Single values Associated with Individual Locations

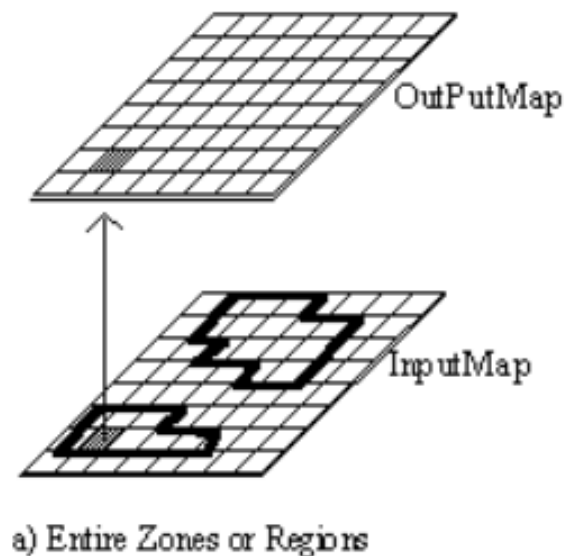


b) Multiple values Associated with Individual Locations



Example: Zonal Map algebra function

- Zonal functions: on cells within specified zones (zones defined by cell values of zone raster)
- Quiz: What operator is used in this zonal function example?
- Zonal maximum



1	1	2	2
	3	2	3
4	3	3	3
4	2	2	4

the zone dataset

3	3	2	4
1	3	2	4
1	2	2	
1	1	3	3

the value dataset

=

3	3	4	4
	4	4	4
3	4	4	4
3	4	4	3

Rasterize/vector to raster (Local Map Algebra)

Rasterize (vector to raster)

Properties Comments

Description: Rasterize (vector to raster)

Show advanced parameters

Input layer

Using model input: Land use

Field to use for a burn-in value [optional]

123 CBScode2

A fixed value to burn [optional]

123 0.000000

Output raster size units

123 Georeferenced units

Width/Horizontal resolution

123 50.000000

Height/Vertical resolution

123 50.000000

Output extent

Using model input: Land use

Assign a specified nodata value to output bands [optional]

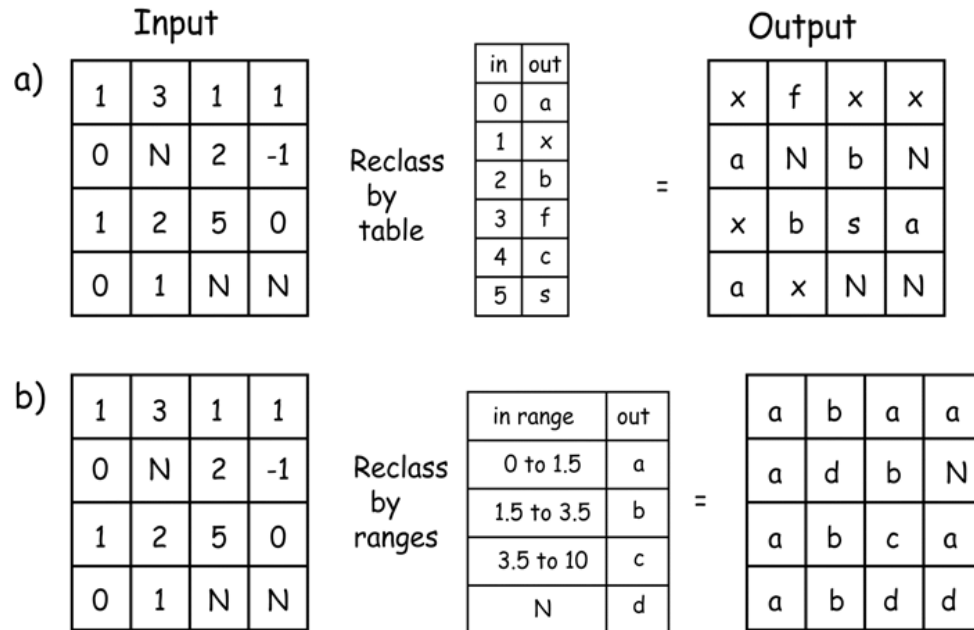
123 0.000000

Rasterized

Land_use_rasterized



Reclassify (Local Map Algebra)



Fixed table

	Minimum	Maximum	
1	40	40	1

Buttons: Add Row, Remove Row(s), Remove All, OK, Cancel

Reclassify by table

Description: Reclassify by table

Show advanced parameters

Raster layer: [Dropdown]

Band number: 1

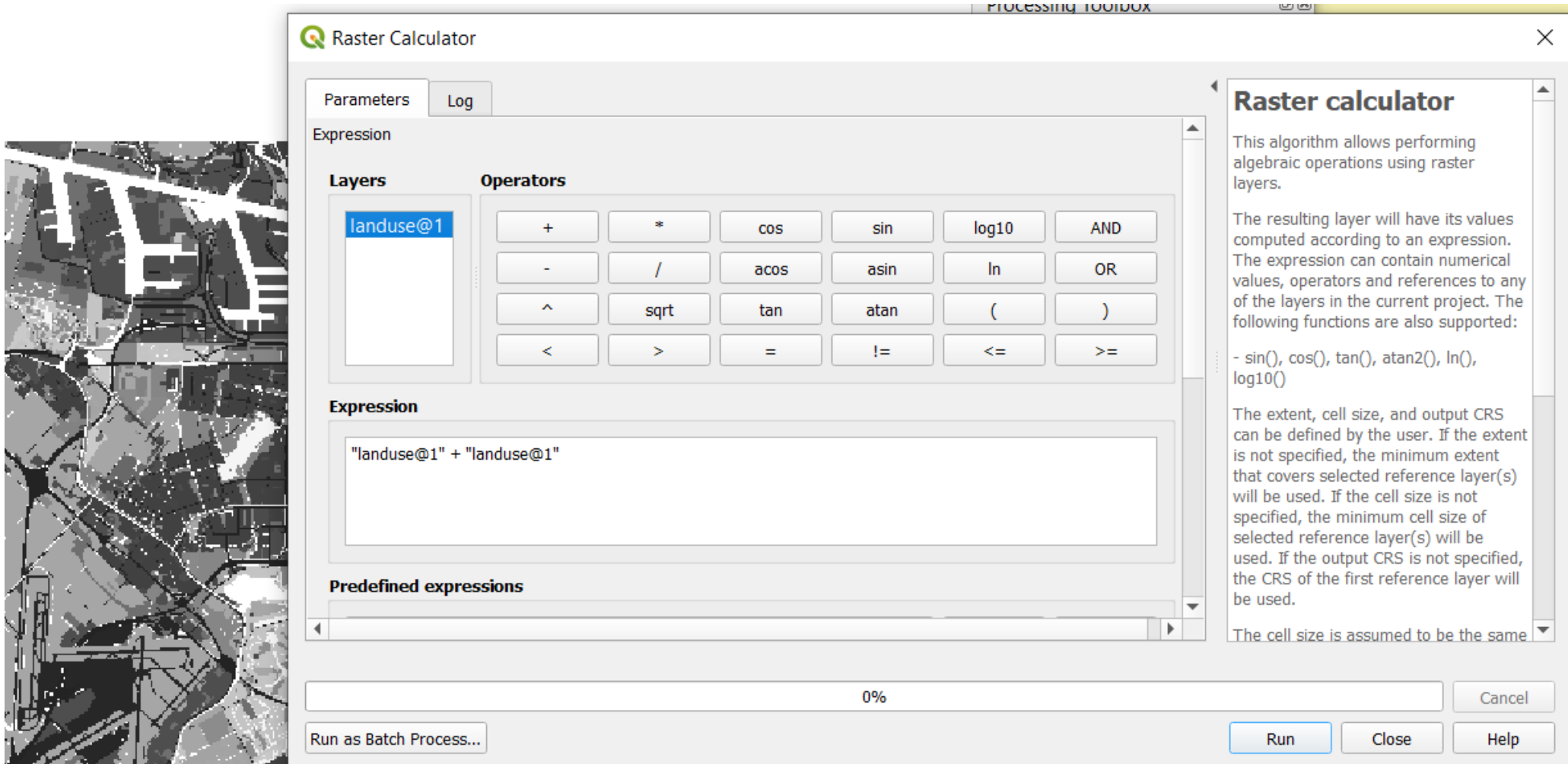
Reclassification table: 123 Fixed table (0x3)

Reclassified raster: [Enter name if this is a final result]


Parent algorithms: 0 elements selected

Buttons: OK, Cancel, Help

Raster Calculator (Local Map Algebra)




Zonal Statistics

 Zonal statistics

Properties Comments

Description Zonal statistics


Raster layer

 Using algorithm output "Reclassified raster" from algorithm "Reclassify by table"

Raster band

123 1

Vector layer containing zones

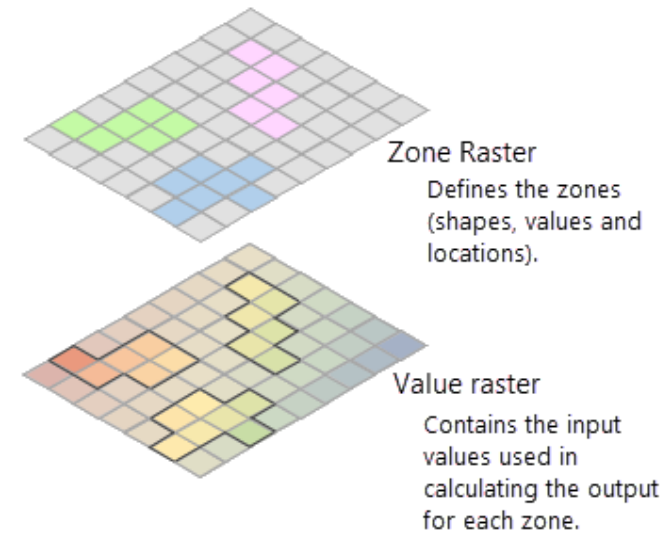
123  PC4

Output column prefix

123 _

Statistics to calculate

123 1 options selected



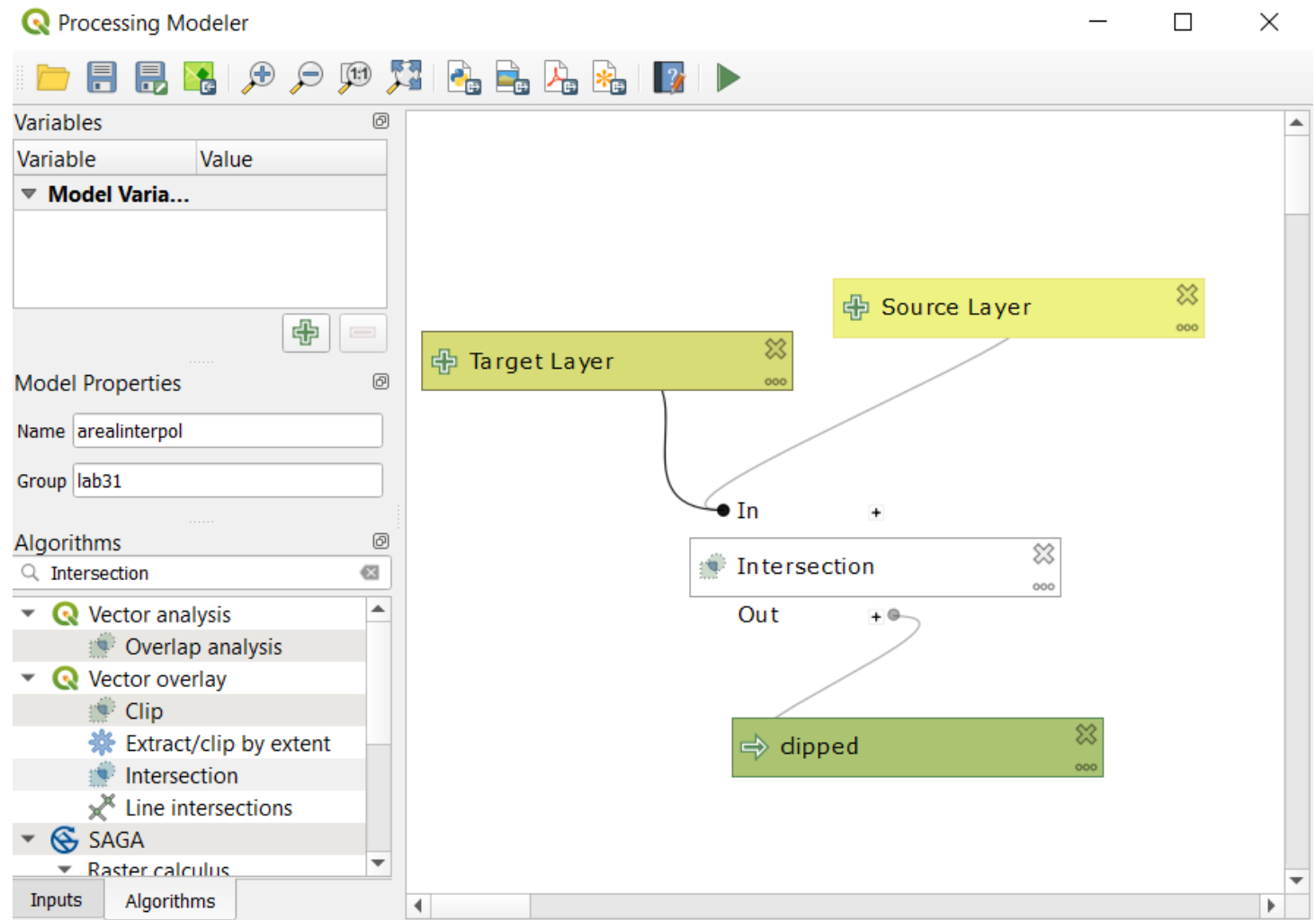
Note:
Zone
Raster
can also
be a
Polygon layer!

Following values calculated for each zone:

- minimum
- maximum
- sum
- count
- mean
- standard deviation
- number of unique values
- range
- variance

Processing models (visual programming)

- Use Processing Modeller to save/rerun processing workflows and export them into Python



Questions?
(Q&A session)

References

- Chrisman (2002): Exploring Geographic Information systems, 2nd edition, Chapter 4 “Attribute based operations” (105-118)
- Chrisman (2002): Exploring Geographic Information systems, 2nd edition, Chapter 5 “Overlay: Integration of disparate sources” (119-152)
- Tomlin, C. D. (1990). Geographic information systems and cartographic modelling. New Jersey, US: Prentice-Hall.
- Egenhofer, M. J., & Franzosa, R. D. (1991). Point-set topological spatial relations. International Journal of Geographical Information System, 5(2), 161-174.