Passager, for string orchestra

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Introduction

This document describes a piece for string orchestra. It is a literate program, which may be read as well as executed.

To convert into a readable Pdf file, install Pandoc and use

```
markdown2pdf -o MusicaVitae.pdf MusicaVitae.lhs
```

To run the program, install the Haskell platform and the Music.Time module. For correct playback of intonation, use a sampler that support Midi Tuning Standard, such as Timidity.

```
{-# LANGUAGE
    TypeSynonymInstances,
    FlexibleInstances,
    MultiParamTypeClasses,
    DeriveFunctor #-}

module Music.Projects.MusicaVitae
(
-- * Preliminaries
-- ** Instruments and tuning
    Part(..),
    Section(..),
    Tuning(..),
```

```
partSection,
    sectionTuning,
   partTuning,
    ensemble,
    sectionParts,
   isViolin, isViola, isCello,
   highParts, lowParts,
   highViolinParts, highViolaParts, highCelloParts,
    lowViolinParts, lowViolaParts, lowCelloParts,
    doubleBass,
   Doubling(..),
   PartFunctor(..),
-- ** Time and pitch
   Dur(..),
   Pitch(..),
   Str(..),
   Scale(..),
    step,
    scaleFromSteps,
   PitchFunctor(..),
-- ** Dynamics
   Level(..),
   Dynamics(..),
   levelAt,
   ppp, pp, p, mf, f, ff, fff,
    cresc,
   dim,
   LevelFunctor(..),
-- ** Articulation
   Articulation(..),
   Phrasing(..),
    staccato,
```

```
tenuto,
    legato,
   portato,
-- ** Playing techniques
   RightHand(..),
   LeftHand(..),
   Stopping(..),
   Stopped,
   Technique,
-- ** Intonation
   Intonation(..),
    intonation,
    cueIntonation,
    raisedIntonation,
-- ** Cues
   Cue(..),
-- * Midi rendering
   renderCue,
-- * High-level constructors
-- ** Open strings
    openString,
   openStringPizz,
    openStringJete,
    openStrings,
-- ** Natural harmonics
   naturalHarmonic,
   naturalHarmonicPizz,
   naturalHarmonicJete,
   naturalHarmonics,
```

```
-- ** Quarter stopped strings
    quarterStoppedString,
    quarterStoppedStrings,
-- ** Stopped strings
    stoppedString,
    stoppedStringPizz,
    stoppedStringJete,
    stoppedStrings,
-- ** Tremolo
    stoppedStringTrem,
   naturalHarmonicTrem,
where
import Prelude hiding ( reverse )
import Control.Applicative
import Data.Convert ( convert )
import qualified Data.List as List
import Music
import Music.Time.Overlay
import Music.Time.Tremolo
import Music.Time.Functors
import Music.Render
import Music.Render.Midi
import Music.Inspect
import Music.Util.List
import Music.Util.Either
```

Preliminaries

In this chapter we will describe the musical preliminaries needed to compose the piece.

Instruments and parts

The instrumentation is as follows:

- Violin I-IV
- Viola I-II
- Cello I-II
- Double Bass

A basic idea of the piece is to combine (slightly) different tunings of the instruments using open-string techniques and harmonics. For this purpose, we will split the ensemble into three sections, each using a different tuning:

- Odd-numbered VI, Vla and Vc parts tunes A4 to 443 Hz (A3 to 221.5 Hz)
- Even-numbered VI, VIa and Vc parts tunes A4 to 437 Hz (A3 to 218.5 Hz)
- Double bass tunes A1 to 55 Hz

The other strings should be tuned in relation to the A-string as usual.

We now define the relation between these types as follows:

```
partSection :: Part -> Section
sectionTuning :: Section -> Tuning
partTuning
            :: Part -> Tuning
partSection ( Violin 1 ) = High
partSection ( Violin 2 ) = Low
partSection ( Violin 3 ) = High
partSection ( Violin 4 ) = Low
partSection ( Viola 1 ) = High
partSection ( Viola 2 ) = Low
partSection ( Cello 1 ) = High
partSection ( Cello 2 ) = Low
partSection DoubleBass = Middle
sectionTuning Low
                     = 440 - 2
sectionTuning Middle = 440
sectionTuning High = 440 + 2
partTuning = sectionTuning . partSection
Then add some utility definitions to quickly access the various parts:
ensemble
             :: [Part]
sectionParts :: Section -> [Part]
isViolin, isViola, isCello, isDoubleBass :: Part -> Bool
highParts, lowParts
    :: [Part]
highViolinParts, highViolaParts, highCelloParts
    :: [Part]
lowViolinParts, lowViolaParts, lowCelloParts
    :: [Part]
doubleBass :: Part
ensemble
```

```
= [ Violin 1, Violin 2, Violin 3, Violin 4
      , Viola 1, Viola 2, Cello 1, Cello 2, DoubleBass ]
sectionParts s = filter (x \rightarrow partSection x == s) ensemble
highParts = sectionParts High
lowParts = sectionParts High
isViolin ( Violin _ )
                              True
isViolin
                            = False
isViola
            ( Viola _ )
                           = True
isViola
                            = False
            ( Cello _ )
isCello
                           = True
isCello
                            = False
isDoubleBass ( DoubleBass ) = True
isDoubleBass _
                            = True
highViolinParts = filter isViolin (sectionParts High)
highViolaParts = filter isViola (sectionParts High)
highCelloParts = filter isCello (sectionParts High)
lowViolinParts
                = filter isViolin (sectionParts Low)
lowViolaParts = filter isViola (sectionParts Low)
lowCelloParts = filter isCello (sectionParts Low)
doubleBass
                = DoubleBass
```

All parts may be doubled. If several parts are doubled but not all, the musicians should strive for a balance between the two main tuning sections (i.e. avoid doubling just the upper parts or vice versa).

Certain cues are required to be played by a single musician even if the parts are doubled, which will be marked *solo*. These passages should be distributed evenly among the musicians, instead of being played by designated soloists.

```
data Doubling = Solo | Tutti
  deriving ( Eq, Show )
```

The PartFunctor class defined useful operations for mapping over part and doubling.

Time and pitch

We will use the temporal operations form Music. Time for composition on both event level and structural level. We use floating point values to represent durations.

```
type Dur = Double
```

For simplicity, we will use Midi numbers for written pitch. Sounding pitch will of course be rendered depending on tuning and playing technique of the given part.

String number will be represented separately using a different type (named Str so as not to collide with String).

```
type Pitch = Int

data Str = I | II | III | IV
    deriving ( Eq, Show, Ord, Enum, Bounded )
```

A scale is conceptually a function from steps to pitches. This relation is captured by the step function, which maps steps to pitches. For example, major 'step' 3 means the third step in the major scale.

The simplest way to generate a scale is to list its relative steps, i.e. 2,2,2,1,2 for the first five pitches in the major scale. This is captured by the function scaleFromSteps.

```
newtype Scale a = Scale { getScale :: [a] }
    deriving ( Eq, Show, Functor )
step :: Scale Pitch -> Pitch -> Pitch
```

```
step (Scale xs) p = xs !! (p 'mod' length xs)
scaleFromSteps :: [Pitch] -> Scale Pitch
scaleFromSteps = Scale . accum
    where
        accum = snd . List.mapAccumL add 0
        add a x = (a + x, a + x)

retrograde :: Scale Pitch -> Scale Pitch
retrograde = Scale . List.reverse . getScale
```

The PitchFunctor class defines a useful operation for mapping over pitch. This generalizes to scales and scores containing pitched elements.

```
class PitchFunctor f where
    setPitch :: Pitch -> f -> f
    mapPitch :: (Pitch -> Pitch) -> f -> f
    setPitch x = mapPitch (const x)

instance PitchFunctor (Pitch) where
    mapPitch f x = f x

instance PitchFunctor (Scale Pitch) where
    mapPitch f = fmap f

invert :: PitchFunctor f => f -> f
invert = mapPitch negate
```

Dynamics

We use a linear representation for dynamic levels. Level 0 corresponds to some medium level dynamic, level 1 to extremely loud and level –1 to extremely soft. A dynamic is a function from time to level, generalizing crescendo, diminuendo and so on.

```
type Level = Double
newtype Dynamics = Dynamics { getDynamics :: Dur -> Level }
```

```
deriving (Eq)
instance Show Dynamics where
    show x = ""
levelAt :: Dynamics -> Dur -> Level
levelAt (Dynamics n) t = n t
ppp, pp, mf, f, ff, fff :: Dynamics
ppp = Dynamics $ const (-0.8)
pp = Dynamics $ const (-0.6)
   = Dynamics $ const (-0.3)
mf = Dynamics $ const 0
    = Dynamics $ const 0.25
ff = Dynamics $ const 0.5
fff = Dynamics $ const 0.7
cresc, dim :: Dynamics
cresc = Dynamics id
dim
      = Dynamics (succ . negate)
instance Num Dynamics where
    (Dynamics x) + (Dynamics y) = Dynamics (t \rightarrow x t + y t)
    (Dynamics x) * (Dynamics y) = Dynamics (t \rightarrow x t * y t)
    signum (Dynamics x)
                                = Dynamics (signum . x)
    abs (Dynamics x)
                                 = Dynamics (abs . x)
                                 = Dynamics (const $ fromInteger n)
    fromInteger n
class LevelFunctor f where
    setLevel :: Level -> f -> f
    mapLevel :: (Level -> Level) -> f -> f
    setLevel x = mapLevel (const x)
    setDynamics :: Dynamics -> f -> f
    mapDynamics :: (Dur -> Level -> Level) -> f -> f
```

```
setDynamics n = mapDynamics (\t _ -> n 'levelAt' t)
instance LevelFunctor Dynamics where
    mapLevel f (Dynamics n) = Dynamics (f . n)
    mapDynamics f (Dynamics n) = Dynamics (t \rightarrow f t n t)
Articulation
data Articulation
    = Straight
    Accent
             Double Articulation
    | Duration Double Articulation
    deriving (Eq, Show)
data Phrasing
    = Phrasing
    | Binding Double Phrasing
    | Begin Articulation Phrasing
    | End Articulation Phrasing
    deriving (Eq, Show)
staccato :: Articulation -> Articulation
staccato = Duration 0.8
tenuto :: Articulation -> Articulation
tenuto = Duration 1.2
legato :: Phrasing -> Phrasing
legato = Binding 1.2
portato :: Phrasing -> Phrasing
```

Playing techniques

portato = Binding 0.8

The piece makes use of different playing techniques in both hands.

The RightHand type is parameterized over time, articulation, phrasing and content. The LeftHand type is parameterized over pitch and string.

```
data RightHand t c r a
   = Pizz ca
   | Single c a
   | Phrase r [(t, a)]
   | Jete r [a]
   deriving (Eq, Show)
data LeftHand p s
   = OpenString
   | NaturalHarmonic
                        рs
   | NaturalHarmonicGliss pps
   | QuarterStoppedString s
   | StoppedString
                        рs
   | StoppedStringTrem
                        ррѕ
   | StoppedStringGliss
                        ррѕ
   deriving (Eq, Show)
leftHand :: RightHand t c r a -> [a]
leftHand (Pizz c x) = [x]
leftHand (Single c x) = [x]
leftHand (Phrase c xs) = map snd xs
leftHand (Jete c xs) = xs
```

As the intonation will be different between open and stopped strings, we define a function mapping each left-hand technique to a stopping. This stopping also distributes over right-hand techniques (for example, an the intonation of a natural harmonic is open, whether played *arco* or *pizz*).

```
data Stopping = Open | QuarterStopped | Stopped
    deriving ( Eq, Show )

class Stopped a where
    stopping :: a -> Stopping
```

```
instance Stopped (LeftHand p s) where
   stopping (OpenString
                                   ) = Open
   stopping ( NaturalHarmonic
                              x s
                                   ) = Open
   stopping ( NaturalHarmonicTrem  x y s ) = Open
   stopping ( NaturalHarmonicGliss x y s ) = Open
   stopping ( QuarterStoppedString s
                                   ) = QuarterStopped
   stopping (StoppedString
                              x s
                                   ) = Stopped
   stopping ( StoppedStringTrem     x y s ) = Stopped
   stopping (StoppedStringGliss x y s ) = Stopped
instance Stopped a => Stopped (RightHand t r p a) where
   stopping ( Pizz c x )
                            = stopping x
   stopping (Single c x)
                            = stopping x
   stopping (Phrase r (x:xs)) = stopping (snd x)
   stopping ( Jete r(x:xs) ) = stopping x
instance PitchFunctor (LeftHand Pitch s) where
   (f x) s
   mapPitch f (StoppedStringTrem x y s) = StoppedStringTrem (f x) (f y) s
   mapPitch f x
instance PitchFunctor a => PitchFunctor (RightHand t c r a) where
   mapPitch f ( Pizz c x )
                           = Pizz
                                   c (mapPitch f x)
   mapPitch f ( Single c x ) = Single c (mapPitch f x)
   mapPitch f (Phrase r xs) = Phrase r (fmap (\((d,p) -> (d, mapPitch f p)) xs)
   mapPitch f ( Jete    r xs ) = Jete
                                   r (fmap (mapPitch f) xs)
```

Intonation

Many playing techiniques in the score calls for open strings. In this case intonation is determined solely by the tuning.

In some cases, open-string techniques are used with an above first-position stop. This should make the open string pitch rise about a quarter-tone step (or at least less than a half-tone step).

Where stopped strings are used, intonation is determined by context:

- In solo passages, intonation is individual. No attempt should be made to synchronize intontation (on long notes et al) for overlapping solo cues.
- In unison passages, common intonation should be used.

```
data Intonation
    = Tuning
    Raised
    | Common
    | Individual
    deriving (Eq, Show)
intonation :: Doubling -> Technique -> Intonation
intonation Tutti t = case stopping t of
                 -> Tuning
    QuarterStopped -> Raised
    Stopped
              -> Common
intonation Solo t = case stopping t of
    Open
                 -> Tuning
    QuarterStopped -> Raised
    Stopped
                 -> Individual
cueIntonation :: Cue -> Intonation
cueIntonation (Cue p d n t) = intonation d t
raisedIntonation :: Cent
raisedIntonation = 23 Cent
Cues
A cue is an action taken by a performer on time.
```

```
type Technique =
   RightHand
```

```
Dur
        Articulation
       Phrasing
        (LeftHand
           Pitch Str)
data Cue
    = Cue
    {
                  :: Part,
        cuePart
        cueDoubling :: Doubling,
        cueDynamics :: Dynamics, -- time is 0 to 1 for the duration of the cue
        cueTechnique :: Technique
    }
    deriving (Eq, Show)
instance PartFunctor Cue where
               f (Cue p d n t) = Cue (f p) d n t
    mapDoubling f (Cue p d n t) = Cue p (f d) n t
instance PitchFunctor Cue where
   mapPitch f (Cue p d n t) = Cue p d n (mapPitch f t)
instance LevelFunctor Cue where
                  (Cue p d n t) = Cue p d (mapLevel f n) t
    mapLevel f
    mapDynamics f (Cue p d n t) = Cue p d (mapDynamics f n) t
instance (Time t, PartFunctor a) => PartFunctor (Score t a) where
    mapPart f = fmap (mapPart f)
    mapDoubling f = fmap (mapDoubling f)
instance (Time t, PitchFunctor a) => PitchFunctor (Score t a) where
    mapPitch f = fmap (mapPitch f)
instance (Time t, LevelFunctor a) => LevelFunctor (Score t a) where
```

```
mapLevel f = fmap (mapLevel f)
mapDynamics f = fmap (mapDynamics f)
```

Midi rendering

We are going to compose the piece as a score of cues. In order to hear the piece and make musical decisions, we need to define a rendering function that renders a cue to a score of Midi notes, which is the object of this chapter.

The MidiNote type is imported from Music.Render.Midi, but we define some extra type synonyms to make the rendering functions somewhat more readable:

Channel

A caveat is that the Midi representation does not handle simultaneous tunings well. We must therefore separete the music into different Midi channels based on part, section and intontation.

```
midiChannel :: Cue -> MidiChannel
midiChannel (Cue part doubling dynamics technique) =
   midiChannel' part section intonation'
    where
                     = partSection part
         section
         intonation' = intonation doubling technique
midiChannel' ( Violin _)
                           High
                                  Tuning
                                                0
midiChannel' (Viola _ )
                          High
                                  Tuning
                                                1
midiChannel' (Cello _ ) High
                                  Tuning
                                                2
midiChannel' ( Violin _)
                           Low
                                                3
                                  Tuning
midiChannel' (Viola _ ) Low
                                  Tuning
midiChannel' (Cello _ ) Low
                                             = 5
                                  Tuning
midiChannel' ( Violin _)
                                  Common
                                                6
midiChannel' ( Viola _ )
                                  Common
                                             = 7
midiChannel' (Cello _ ) _
                                  Common
                                             = 8
```

```
midiChannel' DoubleBass
                                          = 10
midiChannel' ( Violin _)
                               Raised
                                          = 11
midiChannel' ( Viola _ )
                               Raised
                                            11
midiChannel' (Cello _ ) _
                                          = 13
                               Raised
midiChannel' (Violin _)
                        High
                               Individual =
midiChannel' (Viola _ ) High
                               Individual = 1
midiChannel' (Cello _ ) High
                               Individual =
midiChannel' (Violin _)
                        Low
                               Individual =
midiChannel' (Viola _ ) Low
                               Individual = 4
midiChannel' (Cello _ ) Low
                               Individual = 5
```

Instrument

Instrument rendering is simple: if the technique is *pizzicato*, use the pizzicato strings program, otherwise use the program representing the current instrument.

(The standard programs give us solo sounds. We could mix in the *string ensemble* program based on the doubling attribute. I am not sure this is a good idea though.)

Pitch and bending

Table of open string pitches.

```
openStringPitch :: Part -> Str -> MidiPitch
openStringPitch ( Violin _ ) I = 55
openStringPitch ( Violin _ ) II = 62
```

```
openStringPitch ( Violin _ ) III =
openStringPitch ( Violin _ ) IV
                                     76
openStringPitch ( Viola _ )
                                    48
openStringPitch ( Viola _ )
                                    55
openStringPitch ( Viola _ )
                            III =
                                    62
openStringPitch ( Viola _ )
                            ΙV
                                    69
openStringPitch ( Cello _ )
                            Ι
                                    36
openStringPitch ( Cello _ )
                            ΙI
                                    43
openStringPitch ( Cello _ )
                            III =
                                    50
                                    57
openStringPitch ( Cello _ ) IV
openStringPitch DoubleBass
                                    28
                             Ι
openStringPitch DoubleBass
                            ΙI
                                    33
openStringPitch DoubleBass
                                    38
                             III =
openStringPitch DoubleBass
                             ΙV
                                  =
                                    43
naturalHarmonicPitch :: Part -> Str -> Int -> MidiPitch
naturalHarmonicPitch part str tone =
    fundamental + overtone
    where
        fundamental = openStringPitch part str
        overtone = scaleFromSteps [0,12,7,5,4,3,3,2,2,2] 'step' tone
```

We determine amount of pitch bend from the part, doubling and technique. Note that the cents function converts a frequency to cents, so by subtracting the reference pitch from the intonation, we get the amount of bending in cents. Then divide this by 100 to get the amount in semitones.

For harmonics, we add a compensation for the difference between just and twelve-tone equal temperament. Unfortunately this does not work for harmonic tremolos.

```
midiBend :: Cue -> MidiBend
midiBend (Cue part doubling dynamics technique) =
    midiBend' (intonation', cents') + just
    where
        intonation' = intonation doubling technique
        tuning' = partTuning part
        cents' = cents tuning' - cents 440
```

```
= midiBendJust (head . leftHand $ technique)
       just
midiBend' (Raised, c)
                           = getCent (c + raisedIntonation) / 100
midiBend' (Tuning, c)
                              getCent c / 100
midiBend' (Common, c)
midiBend' ( Individual, c ) = 0
midiBendJust :: LeftHand Pitch Str -> MidiBend
midiBendJust ( NaturalHarmonic x s ) = midiBendJust' x
                                    = 0
midiBendJust _
midiBendJust' 0 = 0
midiBendJust'1 = 0
midiBendJust' 2 = 0.0196
midiBendJust'3 = 0
midiBendJust' 4 = -0.1369
midiBendJust' 5 = 0.0196
midiBendJust' 6 = -0.3117
midiBendJust'7 = 0
midiBendJust' 8 = 0.0391
```

Left hand

The renderLeftHand function returns a score of duration one, possibly containing tremolos. This property is formalized by the use of a TremoloScore, i.e. a score containing either notes or tremolos.

Note: Glissandos are not supported yet.

```
renderLeftHand :: Part -> LeftHand Pitch Str -> TremoloScore Dur MidiNote
renderLeftHand part ( OpenString
                                        s)
                                                    renderLeftHandSingle (openStringPitch
renderLeftHand part (NaturalHarmonic
                                       xs)
                                                    renderLeftHandSingle (naturalHarmonic
renderLeftHand part ( NaturalHarmonicTrem x y s ) = renderLeftHandTrem (naturalHarmonicPi
renderLeftHand part ( NaturalHarmonicGliss x y s ) = renderLeftHandGliss
renderLeftHand part ( QuarterStoppedString s )
                                                 = renderLeftHandSingle (openStringPitch
                                                 = renderLeftHandSingle x
renderLeftHand part (StoppedString
                                      xs)
renderLeftHand part ( StoppedStringTrem
                                      x y s ) = renderLeftHandTrem x y
```

Right hand

```
renderRightHand :: Part -> Technique -> TremoloScore Dur MidiNote
renderRightHand part ( Pizz articulation leftHand ) = renderLeftHand part leftHand
renderRightHand part ( Single articulation leftHand ) = renderLeftHand part leftHand
renderRightHand part ( Phrase phrasing leftHand ) = renderLeftHands part leftHand
renderRightHand part ( Jete phrasing leftHand ) = renderLeftHands part (zip bounceDur
renderLeftHands :: Part -> [(Dur, LeftHand Pitch Str)] -> TremoloScore Dur MidiNote
renderLeftHands part = stretchTo 1 . concatSeq . map leftHands
where
leftHands (d, x) = stretch d $ renderLeftHand part x
```

Cues

This section needs some cleanup...

```
setMidiChannel :: MidiChannel -> TremoloScore Dur MidiNote -> TremoloScore Dur MidiNote
setMidiChannel c = fmapE f g
   where f = (\((MidiNote _ i p b n) -> MidiNote c i p b n))
        g = fmap (\((MidiNote _ i p b n) -> MidiNote c i p b n))

setMidiInstrument :: MidiInstrument -> TremoloScore Dur MidiNote -> TremoloScore Dur MidiNote
setMidiInstrument i = fmapE f g
   where f = (\((MidiNote c _ p b n) -> MidiNote c i p b n))
        g = fmap (\((MidiNote c _ p b n) -> MidiNote c i p b n))
```

setMidiBend :: MidiBend -> TremoloScore Dur MidiNote -> TremoloScore Dur MidiNote

```
setMidiBend b = fmapE f g
   where f = (\((MidiNote c i p _ n) -> MidiNote c i p b n)
        g = fmap (\((MidiNote c i p _ n) -> MidiNote c i p b n))

setMidiDynamic :: Dynamics -> TremoloScore Dur MidiNote -> TremoloScore Dur MidiNote
setMidiDynamic (Dynamics n) = tmapE f g
   where f = (\t (MidiNote c i p b _) -> MidiNote c i p b (round $ n t * 63 + 63))
        g = (\t x -> tmap (\t (MidiNote c i p b _) -> MidiNote c i p b (round $ n t * 63 + 63) + 63)

Some constants used for the rendering of jeté strokes.

bounceDur :: [Dur]
bounceDur = [ (2 ** (-0.9 * x)) / 6 | x <- [0, 0.1..1.2] ]</pre>
```

Render each cue to a score of MidiNote elements. Each generated score has a duration of one, so this function can be used with >>= to render a score of cues to Midi (see below.)

This instance makes it possible to use the play function on scores of cues:

```
instance Render (Score Dur Cue) Midi where
  render = render
```

bounceVel = [abs (1 - x) | x < [0, 0.08..]]

bounceVel :: [Double]

- . restAfter 5
- . renderTremoloEvents
- . (>>= renderCue)

High-level constructors

Allthough the *cues* defined in the previous chapters is a flexible representation for an orchestral piece, they are somewhat cubersome to construct. This is easily solved by adding some higher-level constructors.

The constructors all create *standard cues* with the following definitions:

These can be overriden using the methods of the type classes Temporal, Timed, Delayed, PartFunctor, PitchFunctor and LevelFunctor respectively.

Open Strings

```
openString :: Str -> Score Dur Cue
openString x = standardCue
    $ Single standardArticulation
    $ OpenString x
openStringPizz :: Str -> Score Dur Cue
openStringPizz x = standardCue
     $ Pizz standardArticulation
     $ OpenString x
openStringJete :: [Str] -> Score Dur Cue
openStringJete xs = standardCue
     $ Jete standardPhrasing
     $ map OpenString xs
openStrings :: [(Dur, Str)] -> Score Dur Cue
openStrings xs = standardCue
     $ Phrase standardPhrasing
     map ((d,x) \rightarrow (d, OpenString x)) xs
```

Natural harmonics

```
naturalHarmonic :: Str -> Pitch -> Score Dur Cue
naturalHarmonic s x = standardCue
     $ Single standardArticulation
     $ NaturalHarmonic x s
naturalHarmonicPizz :: Str -> Pitch -> Score Dur Cue
naturalHarmonicPizz s x = standardCue
     $ Pizz standardArticulation
     $ NaturalHarmonic x s
naturalHarmonicJete :: Str -> [Pitch] -> Score Dur Cue
naturalHarmonicJete s xs = standardCue
     $ Jete standardPhrasing
     $ map (\x -> NaturalHarmonic x s) xs
naturalHarmonics :: Str -> [(Dur, Pitch)] -> Score Dur Cue
naturalHarmonics s xs = standardCue
     $ Phrase standardPhrasing
     map ((d,x) \rightarrow (d, Natural Harmonic x s)) xs
Quarter stopped strings
quarterStoppedString :: Str -> Score Dur Cue
quarterStoppedString x = standardCue
     $ Single standardArticulation
     $ QuarterStoppedString x
quarterStoppedStrings :: [(Dur, Str)] -> Score Dur Cue
quarterStoppedStrings xs = standardCue
     $ Phrase standardPhrasing
     map ((d,x) \rightarrow (d, QuarterStoppedString x)) xs
Stopped strings
stoppedString :: Pitch -> Score Dur Cue
```

```
stoppedString x = standardCue
     $ Single standardArticulation
     $ StoppedString x I
stoppedStringPizz :: Pitch -> Score Dur Cue
stoppedStringPizz x = standardCue
     $ Pizz standardArticulation
     $ StoppedString x I
stoppedStringJete :: [Pitch] -> Score Dur Cue
stoppedStringJete xs = standardCue
     $ Jete standardPhrasing
     $ map (\x -> StoppedString x I) xs
stoppedStrings :: [(Dur, Pitch)] -> Score Dur Cue
stoppedStrings xs = standardCue
     $ Phrase standardPhrasing
     map ((d,x) \rightarrow (d, StoppedString x I)) xs
Tremolo
stoppedStringTrem :: Pitch -> Pitch -> Score Dur Cue
stoppedStringTrem x y = standardCue
     $ Single standardArticulation
     $ StoppedStringTrem x y I
naturalHarmonicTrem :: Str -> Pitch -> Pitch -> Score Dur Cue
naturalHarmonicTrem s x y = standardCue
     $ Single standardArticulation
```

\$ NaturalHarmonicTrem x y s

Final composition

In this chapter we will assemble the final piece.

Pitches

The pitch material is based on a 15-tone symmetric scale. The lower half is mixolydian and the upper half is aeolian (i.e. the inverse of mixolydian).

We will represent melodies in a relative fashion, using 0 to represent a reference pitch. This simplifies inversion and similar techniques. We use A3 as the reference pitch (corresponding to step 0). The tonality function applies the major-minor scale at the reference pitch, so pitch operations applied *before* this function is diatonic, while operations applied *after* it is chromatic.

```
minScale = scaleFromSteps [0, 2, 1, 2, 2, 1, 2, 2]
majMinScale = Scale $ getScale lower ++ getScale upper
    where
        lower = retrograde . invert $ minScale
        upper = Scale . tail . getScale $ minScale

tonality :: PitchFunctor f => f -> f

tonality = mapPitch $ offset . scale . tonic
    where
        tonic = (+ 7)
        scale = (majMinScale 'step')
        offset = (+ 57)
```

The tonalSeq function generates a binary musical sequence, in which the second operand is transposed the given amount of steps. The tonalConcat function is the same on higher arities.

The fifthUp, fifthDown etc are handy shortcuts for transposition.

```
tonalSeq :: (Time t, PitchFunctor a) => Pitch -> Score t a -> Score t a
tonalConcat :: (Time t, PitchFunctor a) => Pitch -> [Score t a] -> Score t a

tonalSeq  p x y = x >>> mapPitch (+ p) y
tonalConcat p = List.foldr (tonalSeq p) instant
```

```
duodecDown, octaveDown, fifthDown :: PitchFunctor a => a -> a
fifthUp, octaveUp, duodecUp :: PitchFunctor a => a -> a
duodecDown = mapPitch (+ (-19))
octaveDown = mapPitch (+ (-12))
fifthDown = mapPitch (+ (-7))
fifthUp = mapPitch (+ 7)
octaveUp = mapPitch (+ 12)
duodecUp = mapPitch (+ 19)
```

Melody

Melodic patterns that may work well in the symmetric scale.

```
type Pattern = [(Dur, Pitch)]
pattern :: Int -> Pattern
pattern = (patterns !!)
-- Play using
       play . tonality . patternMelody $ pattern 0
patterns =
    [
       zip [ 3, 3 ]
            [0,1],
        zip [ 1, 1, 1, 1, 3, 3 ]
            [ 0, 1, 1, 2, 0, 1 ],
        zip [ 1, 1, 1, 2, 1, 3, 3 ]
            [0, 1, 1, 2, 3, 0, 1],
        zip [] [],
        zip [] [],
        -- 5
        zip [ 1, 1, 1, 1, 3, 3 ]
            [0, 2, 1, 2, 0, -1],
```

```
zip [ 1, 1, 1, 1, 4 ]
            [0,2,1,2,3]
    ]
patternMelody :: Pattern -> Score Dur Cue
patternMelody x = stretch (scaling x / 2) . stoppedStrings $ x
        scaling = sum . map fst
patternSequence :: Pitch -> [Pattern] -> Score Dur Cue
patternSequence p = tonalConcat p . map patternMelody
Harmony
secondChord :: [Int] -> [Str] -> [Int] -> Score Dur Cue
secondChord xs ss ps = instant
    ||| (setDynamics p . setPart (Cello (xs !! 0)) $ naturalHarmonic (ss !! 0) (ps !! 0))
    ||| (setDynamics p . setPart (Viola (xs !! 0)) $ naturalHarmonic (ss !! 1) (ps !! 1))
    ||| (setDynamics p . setPart (Violin (xs !! 0)) $ naturalHarmonic (ss !! 2) (ps !! 2))
    ||| (setDynamics p . setPart (Violin (xs !! 0)) $ naturalHarmonic (ss !! 3) (ps !! 3))
secondChordTrem :: [Int] -> [Str] -> [Int] -> Score Dur Cue
secondChordTrem xs ss ps = instant
    ||| (setDynamics p . setPart (Cello (xs !! 0)) $ naturalHarmonicTrem (ss !! 0) 0 (ps !!
    ||| (setDynamics p . setPart (Viola (xs !! 0)) $ naturalHarmonicTrem (ss !! 1) 0 (ps !!
    ||| (setDynamics p . setPart (Violin (xs !! 0)) $ naturalHarmonicTrem (ss !! 2) 0 (ps !!
    ||| (setDynamics p . setPart (Violin (xs !! 0)) $ naturalHarmonicTrem (ss !! 3) 0 (ps !!
scs = concatSeq $ do
    ss <- return [IV,III,II,I]
    ps <- List.permutations [1,2,3,4]
    -- xs <- List.permutations [2,1,2,1]
    -- return $ secondChord xs ss ps
    return \ secondChord [1,1,1,1] ss ps ||| secondChord [2,2,2,2] ss ps
```

```
-- g, a, d, e
-- scs = concatSeq $ do
       ss <- return [IV, III, II, I]
       xs <- List.permutations [2,1,2,1]
       ps <- List.permutations [1,2,2,3]
       return $ secondChord xs ss ps
-- g, a, d, e
-- scs = concatSeq $ do
      xs <- return [1,1,1,1]
       ss <- return [IV,III,II,I]
      ps <- List.permutations [1,1,1,2]
      return $ secondChord xs ss ps
ch = instant
     ||| (setDynamics p . setPart DoubleBass $ naturalHarmonic I 4)
    ||| (setDynamics p . setPart (Cello 2)
                                             $ naturalHarmonic IV 2)
    ||| (setDynamics p . setPart (Viola 2)
                                             $ naturalHarmonic III 1)
    ||| (setDynamics p . setPart (Violin 2)
                                             $ naturalHarmonic II 3)
    ||| (setDynamics p . setPart (Violin 2)
                                             $ naturalHarmonic IV 1)
a = instant
    ||| (setDynamics ppp . setPart DoubleBass
                                               $ naturalHarmonic IV 4)
    ||| (setDynamics ppp . setPart (Cello 1)
                                               $ naturalHarmonic IV 3)
    ||| (setDynamics ppp . setPart (Viola 1)
                                               $ naturalHarmonic III 2)
    ||| (setDynamics ppp . setPart (Violin 1)
                                               $ naturalHarmonic II 1)
```

\$ naturalHarmonic II 1)

||| (setDynamics ppp . setPart (Violin 2)

```
b = instant
   ||| (setDynamics ppp . setPart (Cello 2)
                                  $ naturalHarmonic IV 3)
                                  $ naturalHarmonic III 2)
   ||| (setDynamics ppp . setPart (Viola 2)
   ||| (setDynamics ppp . setPart (Violin 2)
                                  $ naturalHarmonic II 1)
   ||| (setDynamics ppp . setPart (Violin 1)
                                  $ naturalHarmonic II 1)
d = instant
   ||| (setDynamics pp . setPart DoubleBass $ naturalHarmonic I 3)
   mm = instant
   | | | (setDynamics pp . delay 0 . stretch 2 . mapPitch (+ 7) . tonality . setPart (Cello
nn = instant
   ||| (setDynamics pp . delay 0 . stretch 2 . mapPitch (+ 7) . tonality . setPart (Cello
m = instant
   ||| (setDynamics pp . delay 0.0 . stretch 2.1 . mapPitch (+ 0) . tonality . setPart (Cel
   ||| (setDynamics pp . delay 1.1 . stretch 2.2 . mapPitch (+ 0) . tonality . invert . set
n = instant
   ||| (setDynamics pp . delay 5 . stretch 5 . mapPitch (+ 7) . tonality . setPart (Cello
   ||| (setDynamics pp . delay 0.0 . stretch 4 . mapPitch (+ 0) . tonality . setPart (Cello
Sections
```

```
introHarm :: Int -> Score Dur Cue
introHarm sect = stretch 1 $ instant
   >>> stretch 3 a >>> stretch 2.2 g >>> stretch 3.4 a >>> introHarm sect
   where a = setPart (Cello sect) . setDynamics ppp $ naturalHarmonic IV 1
         g = setPart (Viola sect) . setDynamics ppp $ naturalHarmonic II 1
```

```
introHarmTrem :: Int -> Score Dur Cue
introHarmTrem sect = stretch 2 $ instant
   >>> stretch 3 a >>> stretch 2.4 g
   where a = setPart (Cello sect) . setDynamics ppp $ naturalHarmonicTrem IV 0 1
         g = setPart (Viola sect) . setDynamics ppp $ naturalHarmonicTrem II 0 1
introHarmVln :: Int -> Score Dur Cue
introHarmVln sect = stretch 1 $ instant
   >>> stretch 3 d >>> stretch 2.2 d2 >>> stretch 3.4 a >>> introHarm sect
   where d = setPart (Violin sect) . setDynamics ppp $ naturalHarmonic I 2
         d2 = setPart (Violin sect) . setDynamics ppp $ naturalHarmonic II 1
         a = setPart (Violin sect) . setDynamics ppp $ naturalHarmonic III 1
intro2 = instant
    ||| (before 30 $ introHarm 1)
    ||| (delay 15 . before 30 $ introHarm 2)
    ||| (delay 25 . stretch 5 $ db)
    | | | (delay 35 . before 35 $ introHarm 1)
    ||| (delay 50 . before 35 $ introHarm 2)
    ||| (delay 60 . stretch 5 $ db2)
    ||| (delay 80 . before 15 $ introHarmTrem 1)
    ||| (delay 90 . before 30 $ introHarm 2)
    ||| (delay 100 . stretch 5 $ db)
    ||| (delay 110 . before 30 $ introHarm 1)
    ||| (delay 125 . before 15 $ introHarmTrem 2)
    ||| (delay 75 . before 25 $ introHarmVln 1)
    ||| (delay 95 . before 30 $ introHarmVln 1)
   where
       db = setPart DoubleBass . setDynamics ppp . stretch 4 $ naturalHarmonic III 4
       db2 = setPart DoubleBass . setDynamics ppp . stretch 4  $ naturalHarmonic IV 4
```

```
-- TODO redo completely
intro = instant
    ||| (before 40 . stretch 4 . loopOverlayAll $ [a, b])
    ||| rest 5 >>> mm >>> rest 5 >>> nn
-- TODO expand
middle = instant
    | | | stretch 10 d
    | | (setPart (Cello 1) . setDynamics p . octaveDown . tonality . patternMelody) (patter
middle2 = compress 1.1 . reverse $ instant
    | | (setDynamics mf . {-delay 0.3 . -}stretch 2.1 . octaveUp . tonality . setPart (Violi
    | | | (setDynamics mf . {-delay 0.2 . -}stretch 2.2 . octaveUp . tonality . setPart (Violi
    ||| (setDynamics mf . {-delay 0.1 . -}stretch 2.5 . fifthUp . tonality . setPart (Violi
    ||| (setDynamics mf . {-delay 0.4 . -}stretch 2.9 . fifthUp . tonality . setPart (Violi
    ||| (setDynamics mf . {-delay 0.6 . -}stretch 3.5 . id
                                                                  . tonality . setPart (Violi
    ||| (setDynamics mf . {-delay 0.5 . -}stretch 4.1 . id
                                                                   . tonality . setPart (Viola
middle2b = middle2 >>> (before 40 . stretch 0.6 . reverse $ middle2)
end = compress 1.1 $ instant
    ||| (setDynamics f . delay 0.3 . stretch 2.1 . duodecUp . tonality . setPart (Violin 1)
    ||| (setDynamics f . delay 0.2 . stretch 2.2 . duodecUp . tonality . setPart (Violin 2)
    | | (setDynamics f . delay 0.1 . stretch 2.5 . octaveUp . tonality . setPart (Violin 3)
    ||| (setDynamics f . delay 0.4 . stretch 2.9 . octaveUp . tonality . setPart (Violin 4)
    ||| (setDynamics f . delay 0.6 . stretch 3.5 . fifthUp . tonality . setPart (Violin 2) $
    \c | \c | \c | (setDynamics f . delay 0.5 . stretch 4.1 . fifthUp . tonality . setPart (Viola 1) $
    ||| (setDynamics mf . concatSeq \mbox{map} (\mbox{x} -> stretch 20 . setPart (Cello 1) \mbox{stoppedSt}
    ||| (setDynamics mf . concatSeq $ map (\x -> stretch 30 . setPart (Cello 1)
                                                                                   $ stoppedSt
```

||| (setDynamics mf . stretch 80 . setPart DoubleBass \$ openString IV)