

Give an array, print the Next Smaller Element (NSE) for every element. The NSE for an element x is the first smaller element on the right side x in the array. For elements for which no smaller element exists (on the right side) then we will return NSE as -1 .

Input: $[4, 8, 5, 2, 25]$
Output: $[2, 5, 2, -1, -1]$

Understanding the problem

We have an array & for each element in the array we need to find the NSE.

What is NSE??

The NSE for an element x in the array is the first element that is smaller than x & appears to its right in the array.

If no such element exists, we return -1 .

Code

```
def next_smaller_element(arr):
    n = len(arr)
    result = [-1] * n
    stack = []

    for i in range(n-1, -1, -1):
        while stack and stack[-1] >= arr[i]:
            stack.pop()
```

```
        if stack:
            result[i] = stack[-1]
```

```
        stack.append(arr[i])
```

```
    return result
```

~~arr~~ # Inputting.

arr = $[4, 8, 5, 2, 25]$

print(next_smaller_element(arr))

Execution with stack

① $n = \text{len}(arr) = 5$

$result = [-1, -1, -1, -1, -1]$

→ Initial result why?

② If an element does not have a smaller element to its right its NSE should be -1

③ Ensure correct output length

stack = []

Initially stack is empty because to avoid unnecessary comparisons. stack helps us store only relevant elements.

if stack is not empty?!

if we initialized stack w/ some values, we would have to clear it first, which adds extra complexity.

for i in range(n-1, -1, -1):

traversing from right to left?

we need to find the NSE on the right instead of storing all elements. we keep only the useful ones on the stack.

we process elements from right to left, so that the stack always contains elements to the right of $arr[i]$.

Before adding $arr[i]$ to the stack, we remove elements greater than or equal to it because they will never be useful for NSE.

remaining elements on the right every time

Ex:

At 4 we'd have to scan [8, 5, 2, 25] to find '2'

while stack and stack[-1] >=

arr[i]:

stack.pop()

Remove useless elements from stack.

stack[-1] → then check the top element of the stack.

stack[-1] >= arr[i] → if the top element is greater than or equal to $arr[i]$, it can not be the NSE for $arr[i]$.

or any future element so we remove (pop) it.

we keep removing elements until

stack becomes empty → no smaller element found

stack top is smaller than $arr[i]$ → this element is the NSE

what happens if we traverse left to right?

we would need to scan all

Example : [4, 8, 5, 2, 25]

traversal direction : Right to Left

Step	arr[i]	Stack Before	Action taken	Stack After	NSE
1	25	[]	No NSE push 25	[25]	-1
2	2	[25]	2 < 25 → pop push 2	[2]	-1
3	5	[2]	5 > 2 → NSE for 2 is 5 push 5	[2, 5]	2
4	8	[2, 5]	8 > 5 → NSE for 8 is 5 push 8	[2, 5, 8]	5
5	4	[2, 5, 8]	4 < 8 → pop 8 4 < 5 → pop 5 NSE for 4 is 2 push 4	[2, 4]	2

if stack :

result[i] = stack[-1] # set NSE as the top of the stack
stack.append(arr[i]) # push the current element onto the stack

result = [-1, -1, -1, -1, -1]

Stack = []

① result[4] = stack[-1]

i = 4 Stack is empty no elem

→ push 25 on to stack

result = [-1, -1, -1, -1, -1]

stack = [25]

② i = 3 arr[3] = 2

result[3] = stack[-1]

while cond 25

DOMS

if stack is empty no pop

stack is now empty

so result[3] remain -1

push 2 on to stack

stack [2]

result [-1, -1, -1, -1, -1]

$$q = 2$$

$$\text{stack} = [2, 5]$$

$$\text{res} = [-1, -1, 2, -1, -1]$$

$$q = 1$$

$$\text{stack} = [2, 5, 8]$$

$$\text{res} = [-1, 5, 2, -1, -1]$$

$$q = 0$$

$$\text{stack} = [2, 4]$$

$$\text{res} = [2, 5, 2, -1, -1]$$