1. transform_homography()

- a. Given the src coordinates and homography matrix, matrix multiply h_matrix with each coordinate (appended with 1) transpose.
- b. Scale the transformed coordinates back down to form [x, y, 1]

2. warp image()

- a. Given the dst, src and homography matrix, construct a matrix of coordinate points in dst.
- b. Transform each coordinate point in dst back to src image coordinates using transform_homography using inv(homography).
- c. Remap the src image over the dst image.

3. compute_affine_rectification()

- a. Given 2 pairs of parallel line, find the vanishing point of each pair and cross these 2 vanishing point to get the vanishing line at infinity.
- b. Parameterize this vanishing line and construct Hp.
- c. Calculate the new size of transformed image and warp the src image onto this new size.

4. compute_metric_rectification_step2()

- a. Given 2 pairs of parallel lines, construct the constraint for each pair of parallel line and stack them to form a 2x3 matrix.
- b. Use svd to get the null vector (last row of Vh) and contruct S from the null vector.
- c. Using Cholesky decomposition to get the matrix K and scale it down by its determinant.
- d. Convert K to a 3x3 matrix in form [[K.Transpose, 0], [0, 1]]
- e. Calculate the new size of transformed image and warp the src image onto this new size.

5. compute_metric_rectification_one_step()

- a. Given 5 pairs of orthogonal lines, construct the constraint for each pair and stack them to form a 5x6 matrix.
- b. Use svd to get the null vector (last row of Vh) and construct the conic in form of 3x3 matrix [[a, b/2, d/2], [b/2, c, e/2], [d/2, e/2, f]].
- c. Use svd again to get the $D = \operatorname{sqrt}(\Sigma)$ and Homography matrix = UD
- d. Calculate a similarity/translation matrix to scale/translate the warped image back into view window.
- e. Warp the src image into the dst using H = (Hs*H)



Figure 1 Affinely Rectified Image



Figure 2 Final Rectified Image 1



Figure 3 Final Rectified Image 2

- 6. compute_homography_error()
 - a. Given the src(x), dst(x') and homography matrix, calculate the estimated dst(Hx) and src(inv(H)x') coordinates using the homography matrix.
 - b. Calculate the distance error using formula, $d(x,x') = ||x inv(H)x'||^2 + ||x' Hx||^2$

7. compute_homography_ransac()

- a. Given 2 sets of corresponding points from 2 images, randomly choose 4 pairs of corresponding points.
- b. Compute the homography matrix using these 4 pairs of points.
- c. Count number of inliers according to distance error below threshold
- d. If number of inliers > current max inliers, save the homography matrix and inliers mask.
- e. Repeat for the specified number of tries to find max inliers, homography and mask
- f. Recalculate homography with the inliners.