

Fundamentels of Robotics

Assignment 6 - Calibration. Innopolis University, Fall 2020

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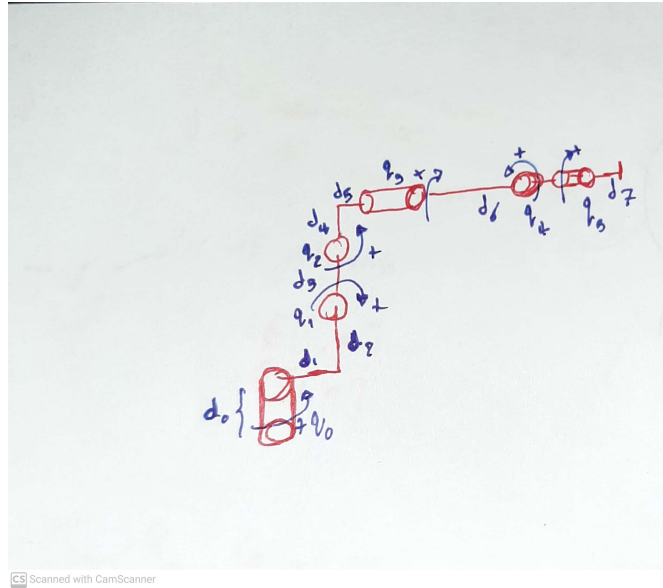
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Section 1: Reducible Model Identification Jacobian

The robot is a manipulator from Fanuc (R-2000i C/165F) This robot has 6 joints and is 6 DoF manipulator, moreover, it has a spherical wrists.

The model of the robot in zero configuration is as following:



Robot model in zero configuration

d_0	364 mm
d_1	312 mm
d_2	324 mm
d_3	1075 mm
d_4	255 mm
d_5	155.5 mm
d_6	1124.5 mm
d_7	215 mm

Note: I am using zero-indexing such that:

The reducible Kinematic Model is as following:

The convention of the notation are from [2, 1]

$$T = [T_x \ T_y \ T_z \ R_x \ R_y \ R_z]_b^T R_z(q_0) T_x(d_1 + Px_0) T_y(Py_0) R_x(\phi_{x0}) R_y(q_1 + \Delta q_1) T_x(Px_1) R_x(\phi_{x1}) R_z(\phi_{z1}) R_y(q_2 + \Delta q_2) T_x(d_5 + Px_3) T_z(d_4 + Pz_2) R_z(\phi_{z2}) R_x(q_3 + \Delta q_3) T_y(Py_3) T_z(Pz_3) R_z(\phi_{z3}) R_y(q_4 + \Delta q_4) T_z(Pz_4) R_z(\phi_{z4}) R_x(q_5) [T_x \ T_y \ T_z]_t$$

$$\pi = [Px_0, Py_0, \phi_{x0}, \Delta q_1, Px_1, \phi_{x1}, \phi_{z1}, \Delta q_2, Px_2, Pz_2, \phi_{z2}, \Delta q_3, Py_3, Pz_3, \phi_{z3}, \Delta q_4, Pz_4, \phi_{z4}]^T$$

Picture for the draft solution with full steps is in the appendix.

For calculating identification jacobian, I have used Numerical derivative method from Assignment 3 ([1], pages 58-61). It is written in the code in details.

Section2: Calibration Algorithm

The algorithm is an iterative algorithm that start with the nominal π_0 and improving the results by solving optimization problems. It is separated into 4 parts:

- (a) Estimate T_{base} T_{tool} based on knowing π q for each configuration in the experiment. A draft for the solution is in the following figure.
- (b) Estimate $\Delta\pi$ based on knowing T_{base} T_{tool}
Picture for the draft solution is in the appendix, but for better and illustrative understanding check the code.
- (c) Update the old values $\pi_{s+1} = \pi_s + \alpha\Delta\pi$
- (d) Termination criteria from the lecture slides: $\sum_{i=1}^m \sum_{j=1}^n ((J_{\pi_i}^{j(p)} \cdot \Delta\pi - \Delta P_i^j)^T (J_{\pi_i}^{j(p)} \cdot \Delta\pi - \Delta P_i^j))$ if is less than epsilon then terminate. Moreover, I have added a criteria that related to number of iterations with limits to a maximum number of iterations

The full details for the first two steps in ([1], pages 71, 72)

The full algorithm from the lecture slides: TODO: picture from the lecture for the flow

Section 3: Results

I have run the code for multiple iterations with some modifications with the initial π_0 and with different step size, I have received the following results (This could be improved by letting the code runs for more iterations

- (a) π :
 (-555.794)
 (3309.881)
 (0.296)
 (-0.344)
 (4737.156)

(0.276)
 (0.541)
 (0.328)
 (-1526.099)
 (3661.048)
 (-0.501)
 (-0.185)
 (-113.33)
 (45.404)
 (0.105)
 (-0.007)
 (-195.059)
 (-0.188))

T_{base} :
 ((1. -0.511 1.248 -899.966)
 (0.511 1. -0.259 -1240.865)
 (-1.248 0.259 1. -273.891)
 (0. 0. 0. 1.))

T_{tool} :

(((1. 0. 0. -3192.595)
 (0. 1. 0. 1529.686)
 (0. 0. 1. -2240.37)
 (0. 0. 0. 1.))

(((1. 0. 0. -3208.42)
 (0. 1. 0. 1581.136)
 (0. 0. 1. -2234.376)
 (0. 0. 0. 1.))

(((1. 0. 0. -3217.408)
 (0. 1. 0. 1532.212)
 (0. 0. 1. -2238.681)
 (0. 0. 0. 1.)))

RMS Error: 7231.12555725946

Max Distance error (mm): 9094.900265365977

RMS Error for x-coordinate: 76.53313656933175

Max error for x-coordinate (mm): 8994.553268508553

RMS Error for y-coordinate: 46.630787166701175

Max error for y-coordinate (mm): 4680.645947228523

RMS Error for z-coordinate: 41.99144598156676

Max error for z-coordinate (mm): 4913.890037857653

Moreover, I wanted to try a learning based approach by extend this assignment to use CMA-ES as I have seen an implementation for it for system identification for a tensegrity robot and wanted to discover the results and the implementation for this method it in this assignment but did not have time

References

- [1] WU, Y. *Optimal pose selection for the identification of geometric and elastostatic parameters of machining robots*. PhD thesis, 2014.
- [2] WU, Y., KLIMCHIK, A., CARO, S., FURET, B., AND PASHKEVICH, A. Geometric calibration of industrial robots using enhanced partial pose measurements and design of experiments. *Robotics and Computer-Integrated Manufacturing* 35 (2015), 151–168.

Section 4: Appendix

[illegible]

Steps for reducible Model for the robot

Step 1

$n=3 \rightarrow$ tool number of references
 $m=24 \rightarrow$ number of configurations experiments
 $i \rightarrow$ experiment number
 $j \rightarrow$ ref. point number

$T_i^j = T_{base} \cdot T_{rot}(q_i/\pi) \cdot T_{tool}^j$
 loc. of ref. points
 $i \in [1, m]$
 $j \in [1, n]$
 manipulator geometry

$P_i^j = P_{base} + R_{base} \cdot R_{rot}(q_i/\pi) + R_{base} \cdot R_{rot}(q_i/\pi) \cdot P_{tool}^j \rightarrow 3mn \text{ scalar equations}$

$R_{base} = [{}^0\omega_{base}] + I$
 ${}^0\omega_{base} \rightarrow$ derivations in the base orientation angles $\rightarrow ?$
 $[{}^0\omega_{base}] = \begin{bmatrix} \dot{\theta}_1 & \dot{\theta}_2 & \dot{\theta}_3 \\ \dot{\theta}_4 & 0 & -\dot{\theta}_5 \\ \dot{\theta}_6 & \dot{\theta}_7 & 0 \end{bmatrix}$

$u_{tool}^j = R_{base} P_{tool}^j \rightarrow R_{base} P_{tool}^j = R_{base}^{-1} u_{tool}^j$
 $P_i^j = P_{base} + R_{rot}^j \cdot P_{tool}^j \Rightarrow P_i^j = P_{base} + [I \quad R_{rot}^j]^T \begin{bmatrix} P_{base} \\ u_{tool}^j \end{bmatrix}$

from robot to the ref point
 apply linear least square using Gauss dot

$$A_i^j = \begin{bmatrix} R_{rot}^j \\ I \end{bmatrix} \begin{bmatrix} P_{base} \\ u_{tool}^j \end{bmatrix}$$

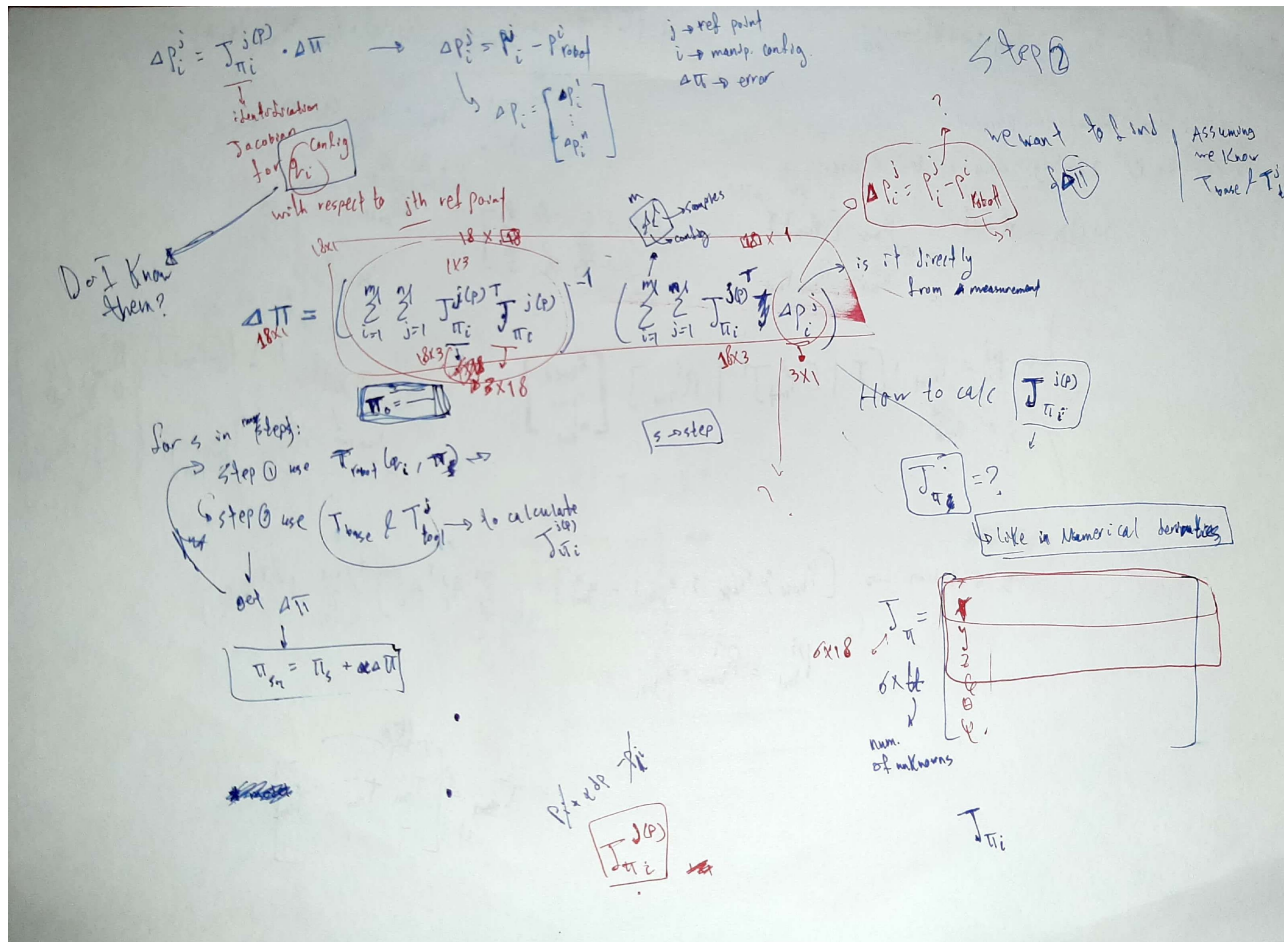
$$A_i^j = \begin{bmatrix} R_{rot}^j \\ I \end{bmatrix} \begin{bmatrix} P_{base} \\ u_{tool}^j \end{bmatrix}$$

$$A_i^j = \begin{bmatrix} R_{rot}^j \\ I \end{bmatrix} \begin{bmatrix} P_{base} \\ u_{tool}^j \end{bmatrix}$$

get u_{tool}^j
 get P_{tool}^j
 get R_{base}
 find P_{base}

Assumptions:
 1. All joints are revolute
 2. All joints are prismatic
 3. All joints are revolute

Calibration Algorithm step1 draft



Calibration Algorithm step2 draft