

Q.1. The average temperature ( $t$ ) of  $x$  number of days is 40 degrees. The temperature of one more day is added, which is 45 degrees. The new average temperature is 41 degrees. What is  $x$ ?

$$\text{Average} = \sum (t_i)/x$$

Premises:

$$1) t_{x+1} = 45^\circ$$

$$2) \sum_{i=1}^x t_i/x = 40^\circ$$

$$3) \sum_{i=1}^{x+1} t_i/(x+1) = 41^\circ$$

Formula: [1]

$$\sum_{i=1}^{x+1} t_i/(x+1) = t_{x+1}/(x+1) + x/(x+1) \sum_{i=1}^x t_i/x$$

[1]

$$\begin{aligned} \sum_{i=1}^{x+1} t_i/(x+1) &= (t_1 + t_2 + \dots + t_i + t_{i+1})/(x+1) = \\ &= (x/x) * (t_1 + t_2 + \dots + t_i + t_{i+1})/(x+1) = \\ &= x/(x+1) * (t_1 + t_2 + \dots + t_i + t_{i+1})/x = \\ &= (\sum_{i=1}^x t_i + t_{x+1})/x * x/(x+1) = \\ &= [x/(x+1)] * (\sum_{i=1}^x t_i/x + t_{x+1}/x) = \\ &= t_{x+1}/(x+1) + x/(x+1) \sum_{i=1}^x t_i/x \end{aligned}$$

Calculation using formula 1:

$$\begin{aligned} \sum_{i=1}^{x+1} t_i/(x+1) &= t_{x+1}/(x+1) + x/(x+1) \sum_{i=1}^x t_i/x \\ 41^\circ &= t_{x+1}/(x+1) + x/(x+1) * 40^\circ \\ 41^\circ &= 45^\circ/(x+1) + x/(x+1) * 40^\circ \\ 41^\circ(x+1) &= 45^\circ + 40^\circ x \\ 41x + 41 &= 45 + 40x \end{aligned}$$

$$x = 4$$