

Reputational Bargaining in the Shadow of the Law

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Bargaining in the Shadow of the Law

- ▶ Two parties (e.g. a union and a firm, or partners of a company) negotiate to resolve a conflict.
- ▶ Each party is
 - ▶ **unjustified (no evidence supporting a claim)**, or
 - ▶ **justified (verifiable evidence supporting a claim)**
- ▶ Two parties can settle the conflict on their own.
- ▶ Or they can let the court resolve their conflict when they get the chance.
 - ▶ A justified party goes to a third party (e.g., court, arbitrator) whenever there is a chance.
 - ▶ An unjustified party may go to the court **strategically**.
 - ▶ Opponent can avoid the court cost by agreeing.

Reputational Bargaining (Abreu and Gul, 2000)

- ▶ Two players negotiate to divide a unit pie.
- ▶ Each player is
 - ▶ rational (flexible and strategic), or
 - ▶ persistent (inflexible and behavioral)
- ▶ Time is continuous.
- ▶ Players persist or concede.

Reputational Bargaining in the Shadow of the Law

- ▶ Two players negotiate to divide a unit pie.
- ▶ Each player is
 - ▶ rational (flexible and strategic), or
 - ▶ persistent (inflexible and behavioral)
- ▶ Time is continuous.
- ▶ Players persist or concede or threaten to go to the court (ultimatum).

Results

1. Testable implication

How likely a player sends an ultimatum depends on own reputation and opponent's reputation, and is *not* monotonic in time.

2. New economic forces

Having the ultimatum may or may not benefit the challenger.

- ▶ Negative effect “no news is bad news”: harder to build reputation.
- ▶ Positive effect “no news is good news”: easier to build reputation.

3. Comparisons with Abreu and Gul (2000)

Players' limit payoffs depend on discount rates and the arrival rates of challenge opportunities.

Players' reputations **do not necessarily build up** when both sides can send ultimatums (vs reputations always build up in Abreu and Gul (2000)).

Reputational Bargaining (Abreu and Gul, 2000)

- ▶ Players 1 and 2 negotiate to divide a unit pie.
- ▶ Time is continuous. Player i 's discount rate is r_i .
- ▶ With probability z_i player $i = 1, 2$ persistently demands a_i .
- ▶ Assume difference $D \equiv a_1 + a_2 - 1 > 0$.
- ▶ At each instant, each player can persist or concede.

Equilibrium: War of Attrition

1. Players' reputations (probabilities of being a persistent type) increase over time and reach 1 at the same time.
2. Each player mixes between persisting and conceding at every moment, and concedes at a constant rate

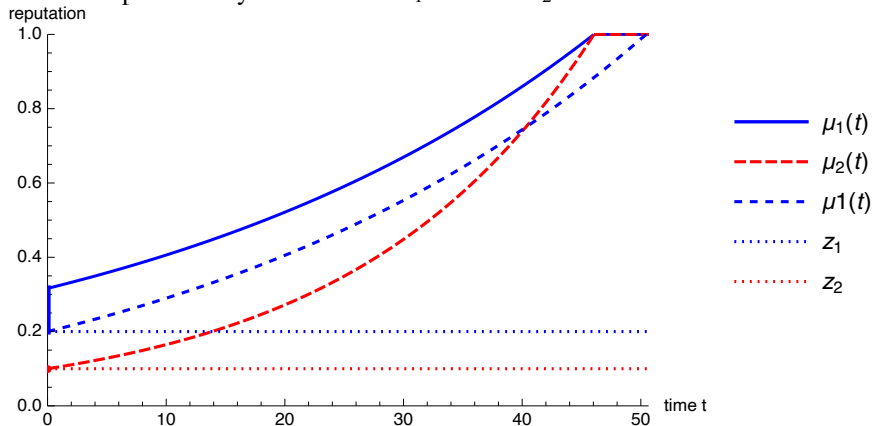
$$\lambda_j = \frac{r_i(1 - a_j)}{D}$$

to make opponent indifferent between persisting and conceding.

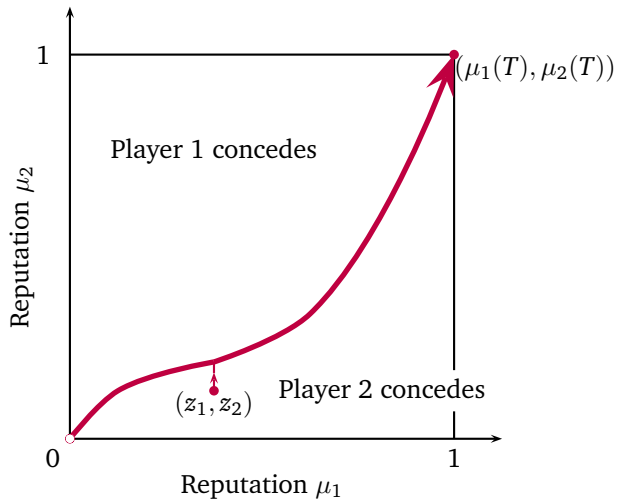
3. At most one player concedes with a positive probability at time 0.

Reputation Dynamics

Reputation Dynamics when $a_1=0.8$ and $a_2=0.6$



Reputation Coevolution



Reputational Bargaining

- ▶ Players 1 and 2 negotiate to divide a unit pie.
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- ▶ With probability z_i player $i = 1, 2$ persistently demands a_i .
- ▶ Assume $D \equiv a_1 + a_2 - 1 > 0$.
- ▶ At each instant, each player can persist or concede.

Reputational Bargaining with One-Sided Challenge

- ▶ In addition, player 1 can pay cost c_1 to challenge:
 - ▶ A justified player 1 challenges with Poisson rate γ_1 .
 - ▶ An unjustified player 1 can (strategically) challenge any time.
- ▶ A justified player 2 always sees the challenge.
- ▶ An unjustified player 2 can choose.
 - ▶ If 2 yields to the challenge, 1 gets a_1 and 2 gets $1 - a_1$.
 - ▶ If 2 pays cost c_2 to see the challenge, a court determines outcome:
 - ▶ An unjustified player loses to a justified player.
 - ▶ An unjustified challenger wins with prob w against an unjustified opponent.

Challenging is like bluffing: it can be beneficial (if the opponent concedes) or harmful (if the opponent calls).

Incentives to Challenge and See the Challenge

- If player 1's reputation is ν_1 , player 2 is indifferent between responding and yielding when

$$(1 - \nu_1)(1 - w)D - c_2 = 0.$$

$$\nu_1 = 1 - \frac{c_2}{(1 - w)D} \equiv \nu_1^*.$$

- An unjustified player 1 does not challenge if

$$\mu_2 > 1 - \frac{c_1}{D} \equiv \mu_2^*$$

Player 1's highest gain from challenging is

$$(1 - \mu_2)D - c_1.$$

Mutual Indifference in Unique Equilibrium

- ▶ Players concede at Abreu-Gul rates.
- ▶ When for $\mu_2 \leq \mu_2^*$, player 2 responds with probability

$$s_2(\mu_2) = \frac{1}{1-w} \left[1 - \frac{c_1}{D} \frac{1}{1-\mu_2} \right].$$

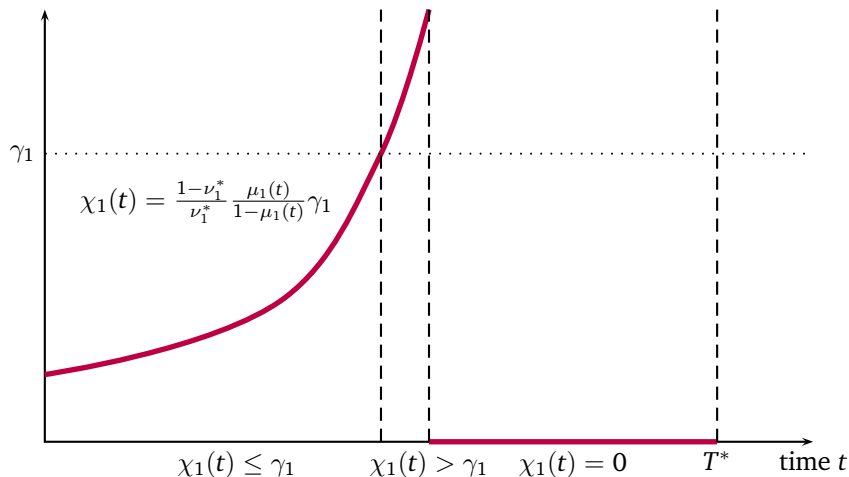
to make 1 indifferent between challenging and conceding.

- ▶ When $\mu_2 < \mu_2^*$, player 1 challenges with rate χ_1 :

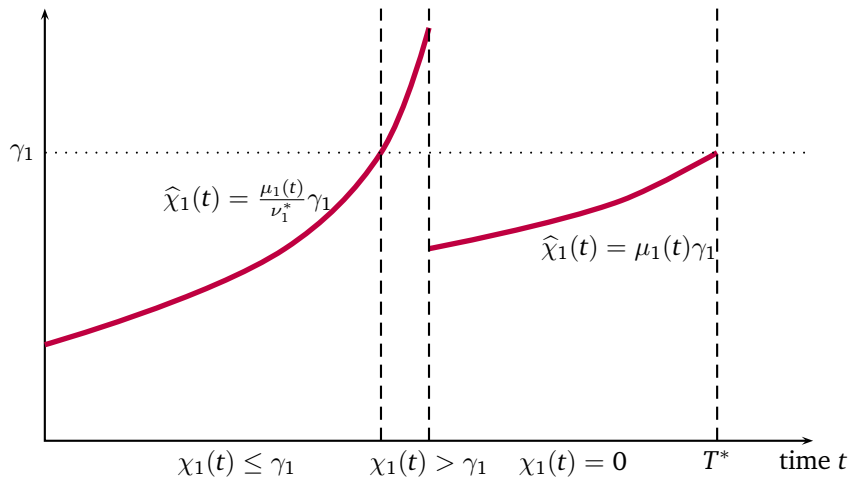
$$\frac{\mu_1 \gamma_1}{\mu_1 \gamma_1 + (1 - \mu_1) \chi_1} = \nu_1^* \Rightarrow \chi_1 = \frac{1 - \nu_1^*}{\nu_1^*} \frac{\mu_1}{1 - \mu_1} \gamma_1$$

to make 2 indifferent between responding and yielding to the challenge.

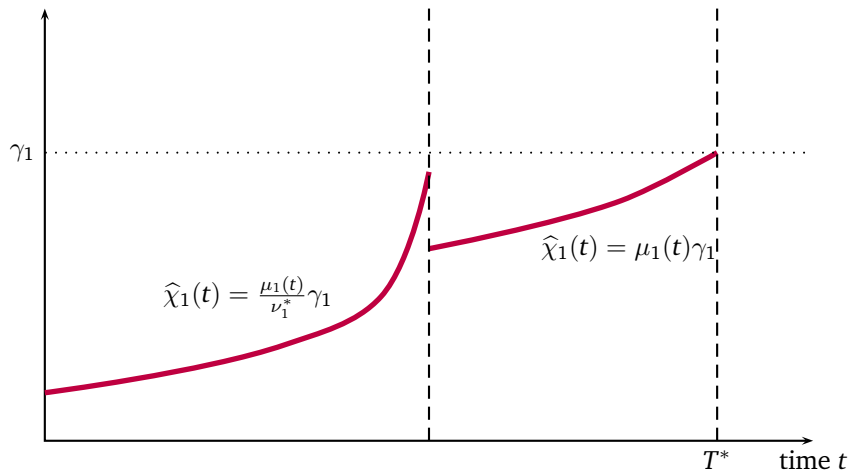
An Unjustified Player's Equilibrium Challenge Rate



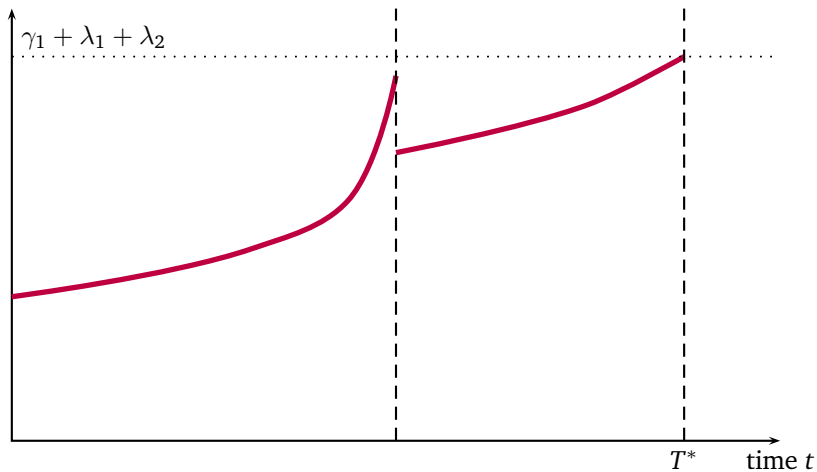
Overall Challenge Rate



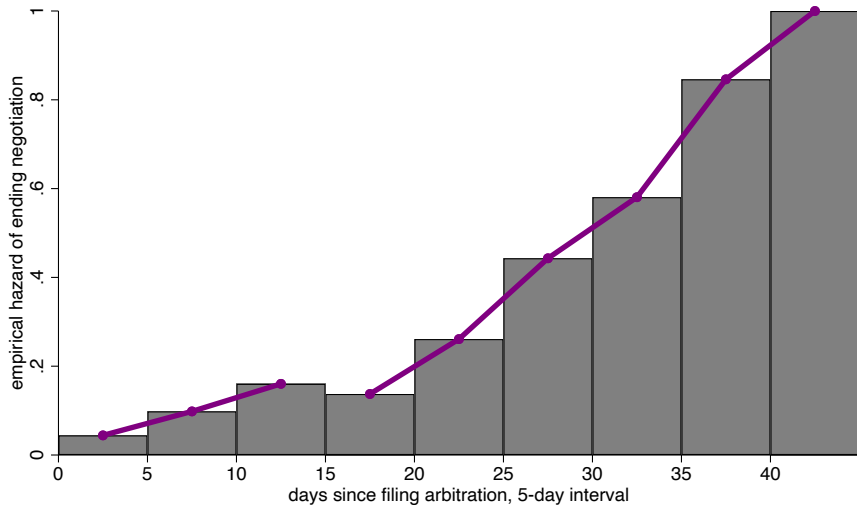
Overall Challenge Rate, Case 2



Predicted Hazard Rate of Ending the Game



MLB Salary Arbitration, 2011-2020



Reputation Dynamics

2's reputation follows

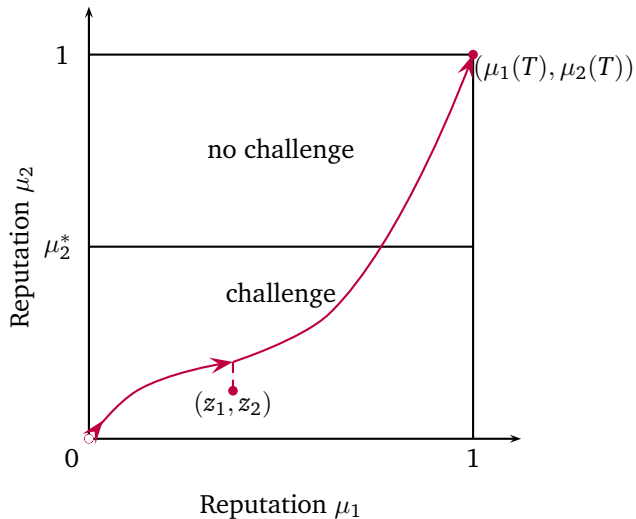
$$\mu_2'(t) = \lambda_2 \mu_2(t).$$

1's reputation follows Bernoulli in the no-challenging phase ($\mu_2 > \mu_2^*$):

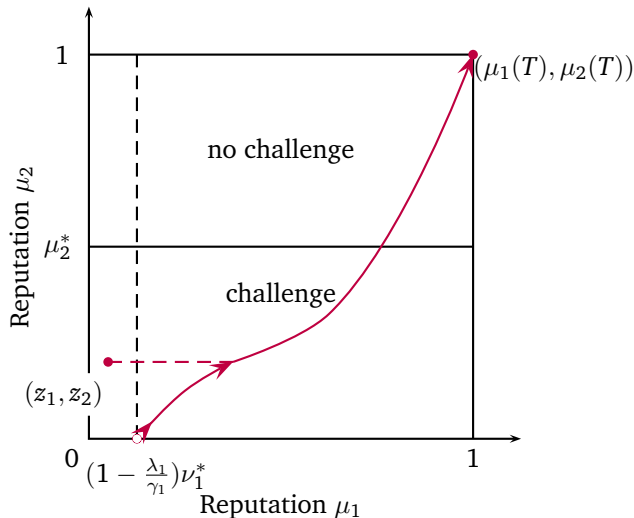
$$\mu_1'(t) = \lambda_1 \mu_1(t) - \gamma_1 (1 - \mu_1(t)) \mu_1(t) < \lambda_1 \mu_1(t).$$

1's reputation follows Bernoulli in the challenging phase ($\mu_2 < \mu_2^*$):

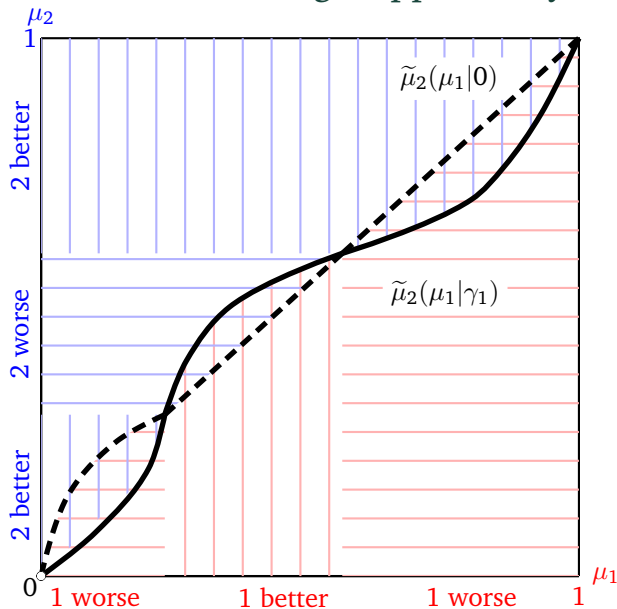
$$\mu_1'(t) = \lambda_1 \mu_1(t) - \gamma_1 (1 - \mu_1(t)) \mu_1(t) + \left(\frac{\gamma_1}{\nu_1^*} - \gamma_1 \right) \mu_1^2(t) \begin{cases} \leq \lambda_1 \mu_1(t) & \text{if } \mu_1(t) \leq \nu_1^* \\ > \lambda_1 \mu_1(t) & \text{if } \mu_1(t) > \nu_1^* \end{cases}$$

Reputation Coevolution: $\gamma_1 \leq \lambda_1$ 

Reputation Coevolution: $\gamma_1 > \lambda_1$



Who Benefits from Challenge Opportunity?



Multiple Types

Suppose players can choose their initial demands a_i and a_j from finite sets A_i and A_j , respectively.

Unique Equilibrium

There exists a unique sequential equilibrium.

Limit Payoffs

“Sufficiently rich” sets and small probabilities of persistence:

- ▶ Agreements are efficient: limit payoffs add up to 1.
- ▶ Player 1's limit payoff in Abreu and Gul (2000) is Rubinstein (1982) payoff

$$\frac{r_2}{r_1 + r_2}.$$

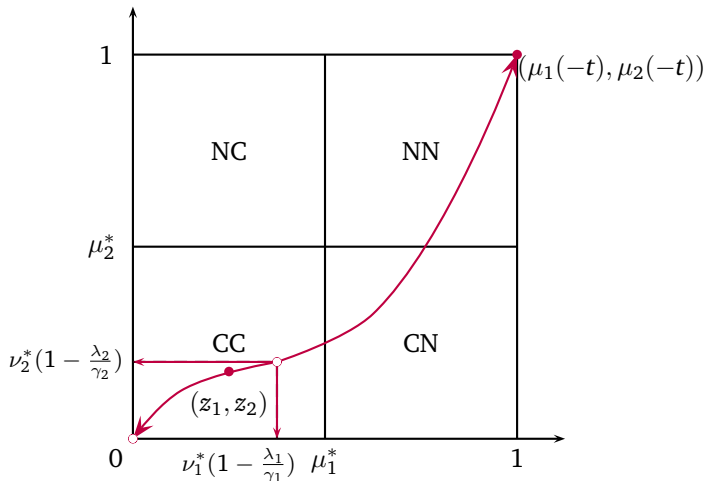
- ▶ Player 1's limit payoff in bargaining with one-sided challenge is

$$\frac{r_2}{\max\{r_1, \gamma_1\} + r_2}.$$

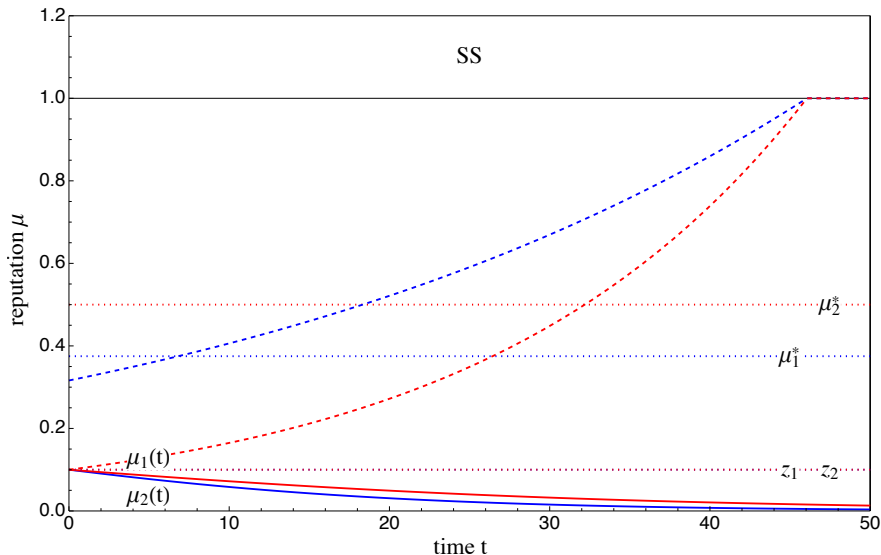
Bargaining with Two-Sided Challenges

- ▶ Player 1 and player 2 bargain to divide a unit pie.
- ▶ With probability z_i player i persistently/irrationally demands a_i .
- ▶ Assume $d \equiv a_1 + a_2 - 1 > 0$.
- ▶ Time is continuous. Player i 's discount rate is r_i .
- ▶ At each instant, each player can persist or concede, **or**
 - ▶ A justified player $i = 1, 2$ challenges with Poisson rate γ_i .
 - ▶ An unjustified player $i = 1, 2$ can challenge any time.
- ▶ If player i pays cost c_i to challenge, player $j \neq i$ has to respond.
 - ▶ A justified player j always sees the challenge.
 - ▶ If player j yields to the challenge, player i gets a_i and player j gets $1 - a_j$.
 - ▶ If player j pays cost c_j to see the challenge, a court determines outcome:
 - ▶ An unjustified player loses to a justified player.
 - ▶ An unjustified challenger wins with probability w against an unjustified player.

Reputation Not Building Up



Reputation Not Building Up



Conclusion

- ▶ The paper builds a model of reputational bargaining with an opportunity to challenge the opponent.
- ▶ A player increases the challenge rate initially, and then does not challenge at all.
- ▶ The challenge opportunity may or may not benefit the challenger.
- ▶ Limit payoffs may depend on the arrival rate of challenge opportunities.
- ▶ The paper incorporates the continuous-time bargaining model of Abreu and Gul (2000) as a special case, and provides an economic interpretation and application of “irrationality”/“persistence”.

THANK YOU!

References I

Abreu, Dilip and Faruk Gul, “Bargaining and Reputation,” *Econometrica*, 2000, 68 (1), 85–117.

Rubinstein, Ariel, “Perfect Equilibrium in a Bargaining Model,” *Econometrica*, January 1982, 50 (1), 97–108.