

# Reputational Bargaining in the Shadow of the Law

Mehmet Ekmekci<sup>1</sup>   Hanzhe Zhang<sup>2</sup>

<sup>1</sup>Boston College

<sup>2</sup>Michigan State University

Friday, May 8, 2020

Canadian Economic Theory Conference

# Bargaining in the Shadow of Law

- ▶ Two parties (e.g. a union and a firm, or partners of a company) negotiate to resolve a conflict.
- ▶ Each party is
  - ▶ **unjustified (no evidence supporting a claim)**, or
  - ▶ **justified (verifiable evidence supporting a claim)**
- ▶ Two parties can settle the conflict on their own.
- ▶ Or they can let the court resolve their conflict when they get the chance.
  - ▶ A justified party goes to a third party (e.g., court, arbitrator) whenever there is a chance.
  - ▶ An unjustified party may go to the court **strategically**.
  - ▶ Opponent can avoid the court cost by agreeing.

# Reputational Bargaining (Abreu and Gul, 2000)

- ▶ Two players negotiate to divide a unit pie.
- ▶ Each player is
  - ▶ rational (flexible and strategic), or
  - ▶ persistent (inflexible and behavioral)
- ▶ Time is continuous.
- ▶ Players persist or concede.

# Reputational Bargaining in the Shadow of the Law

- ▶ Two players negotiate to divide a unit pie.
- ▶ Each player is
  - ▶ rational (flexible and strategic), or
  - ▶ persistent (inflexible and behavioral)
- ▶ Time is continuous.
- ▶ Players persist or concede or threaten to go to the court (ultimatum).

# Results

## 1. Testable implication

How likely a player sends an ultimatum depends on own reputation and opponent's reputation, and is *not* monotonic in time.

## 2. New economic forces

Having the ultimatum may or may not benefit the challenger.

- ▶ Negative effect “no news is bad news”: harder to build reputation.
- ▶ Positive effect “no news is good news”: easier to build reputation.

## 3. Comparisons with Abreu and Gul (2000)

Players' limit payoffs depend on discount rates and the arrival rates of challenge opportunities.

Players' reputations **do not necessarily build up** when both sides can send ultimatums (vs reputations always build up in Abreu and Gul (2000)).

# Reputational Bargaining (Abreu and Gul, 2000)

- ▶ Players 1 and 2 negotiate to divide a unit pie.
- ▶ Time is continuous. Player  $i$ 's discount rate is  $r_i$ .
- ▶ With probability  $z_i$  player  $i = 1, 2$  persistently demands  $a_i$ .
- ▶ Assume difference  $D \equiv a_1 + a_2 - 1 > 0$ .
- ▶ At each instant, each player can persist or concede.

## Equilibrium: War of Attrition

1. Players' reputations (probabilities of being a persistent type) increase over time and reach 1 at the same time.
2. Each player mixes between persisting and conceding at every moment, and concedes at a constant rate

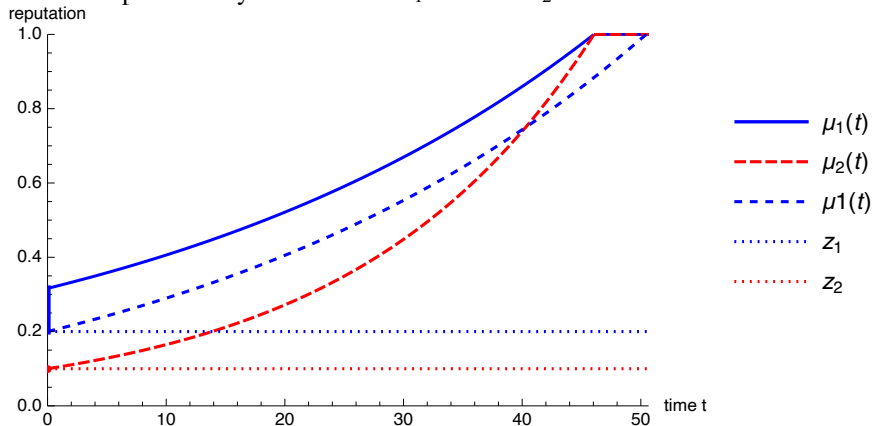
$$\lambda_j = \frac{r_i(1 - a_j)}{D}$$

to make opponent indifferent between persisting and conceding.

3. At most one player concedes with a positive probability at time 0.

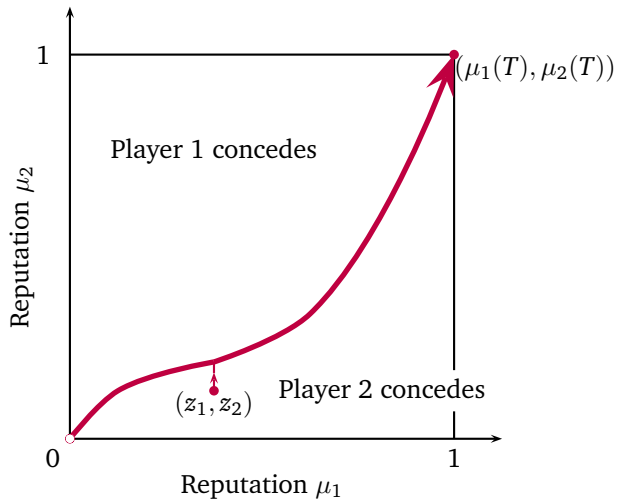
# Reputation Dynamics

Reputation Dynamics when  $a_1=0.8$  and  $a_2=0.6$





# Reputation Coevolution



# Reputational Bargaining

- ▶ Players 1 and 2 negotiate to divide a unit pie.
- ▶ Time is continuous. Player  $i$ 's discount rate is  $r_i$ .
- ▶ With probability  $z_i$  player  $i = 1, 2$  persistently demands  $a_i$ .
- ▶ Assume  $D \equiv a_1 + a_2 - 1 > 0$ .
- ▶ At each instant, each player can persist or concede.

# Reputational Bargaining with One-Sided Challenge

- ▶ In addition, player 1 can pay cost  $c_1$  to challenge:
  - ▶ A justified player 1 challenges with Poisson rate  $\gamma_1$ .
  - ▶ An unjustified player 1 can (strategically) challenge any time.
- ▶ A justified player 2 always sees the challenge.
- ▶ An unjustified player 2 can choose.
  - ▶ If 2 yields to the challenge, 1 gets  $a_1$  and 2 gets  $1 - a_1$ .
  - ▶ If 2 pays cost  $c_2$  to see the challenge, a court determines outcome:
    - ▶ An unjustified player loses to a justified player.
    - ▶ An unjustified challenger wins with prob  $w$  against an unjustified opponent.

**Challenging is like bluffing:** it can be beneficial (if the opponent concedes) or harmful (if the opponent calls).

# Incentives to Challenge and See the Challenge

- If player 1's reputation is  $\nu_1$ , player 2 is indifferent between responding and yielding when

$$(1 - \nu_1)(1 - w)D - c_2 = 0.$$

$$\nu_1 = 1 - \frac{c_2}{(1 - w)D} \equiv \nu_1^*.$$

- An unjustified player 1 does not challenge if

$$\mu_2 > 1 - \frac{c_1}{D} \equiv \mu_2^*$$

Player 1's highest gain from challenging is

$$(1 - \mu_2)D - c_1.$$

# Mutual Indifference in Unique Equilibrium

- ▶ Players concede at Abreu-Gul rates.
- ▶ When for  $\mu_2 \leq \mu_2^*$ , player 2 responds with probability

$$s_2(\mu_2) = \frac{1}{1-w} \left[ 1 - \frac{c_1}{D} \frac{1}{1-\mu_2} \right].$$

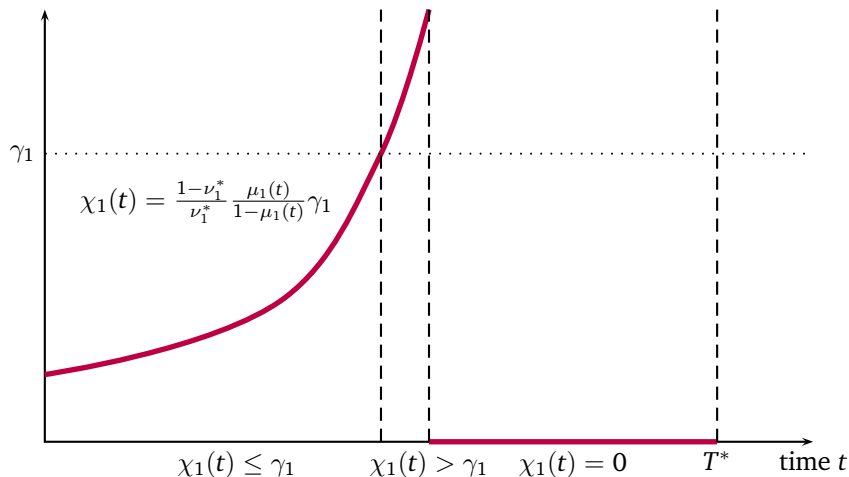
to make 1 indifferent between challenging and conceding.

- ▶ When  $\mu_2 < \mu_2^*$ , player 1 challenges with rate  $\chi_1$ :

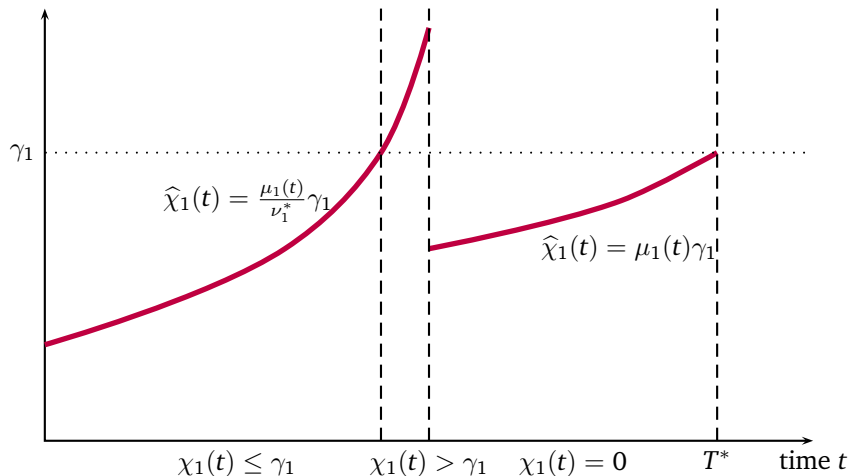
$$\frac{\mu_1 \gamma_1}{\mu_1 \gamma_1 + (1 - \mu_1) \chi_1} = \nu_1^* \Rightarrow \chi_1 = \frac{1 - \nu_1^*}{\nu_1^*} \frac{\mu_1}{1 - \mu_1} \gamma_1$$

to make 2 indifferent between responding and yielding to the challenge.

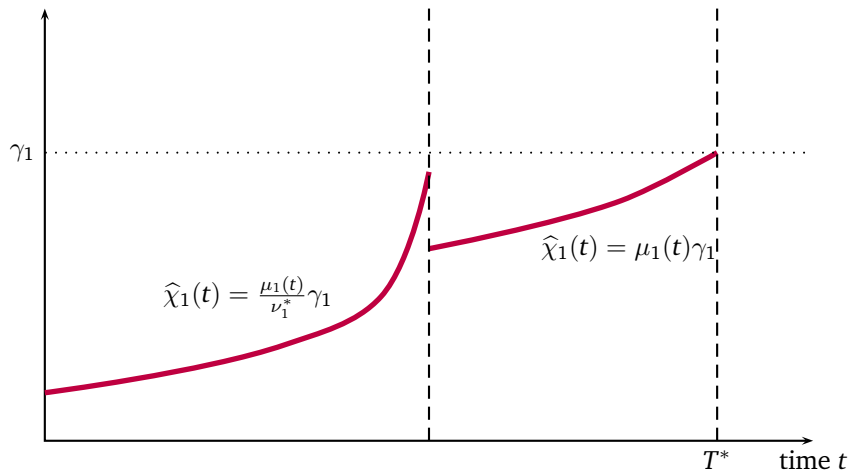
# An Unjustified Player's Equilibrium Challenge Rate



## Overall Challenge Rate

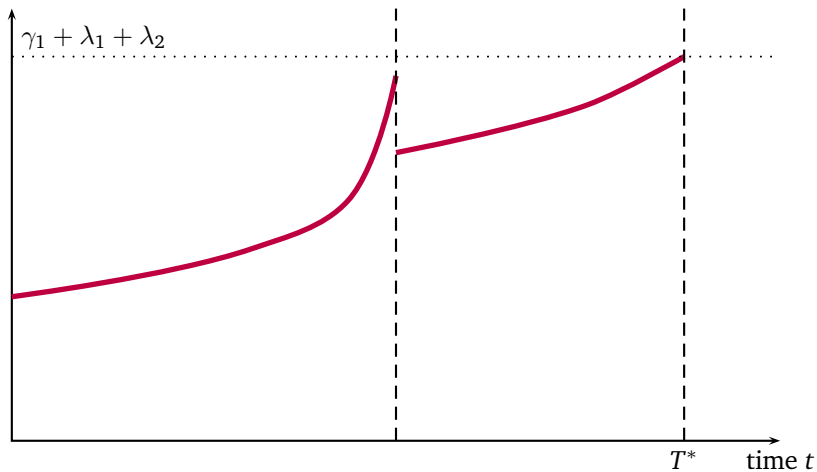


## Overall Challenge Rate, Case 2

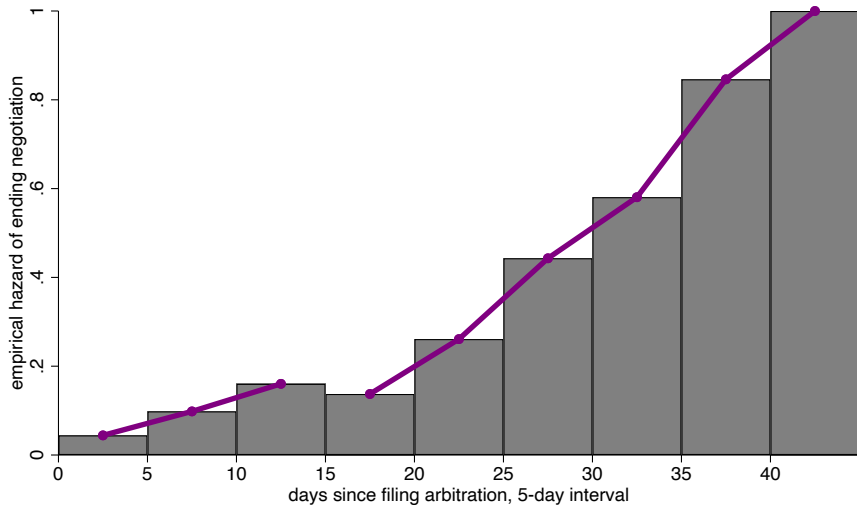




# Predicted Hazard Rate of Ending the Game



# MLB Salary Arbitration, 2011-2020



# Reputation Dynamics

2's reputation follows

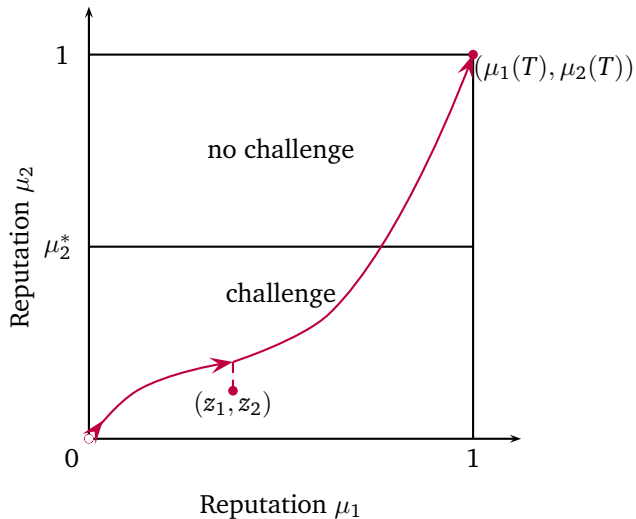
$$\mu_2'(t) = \lambda_2 \mu_2(t).$$

1's reputation follows Bernoulli in the no-challenging phase ( $\mu_2 > \mu_2^*$ ):

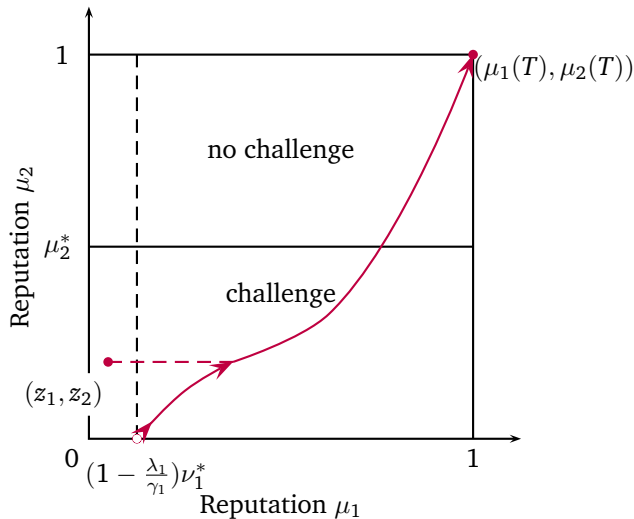
$$\mu_1'(t) = \lambda_1 \mu_1(t) - \gamma_1 (1 - \mu_1(t)) \mu_1(t) < \lambda_1 \mu_1(t).$$

1's reputation follows Bernoulli in the challenging phase ( $\mu_2 < \mu_2^*$ ):

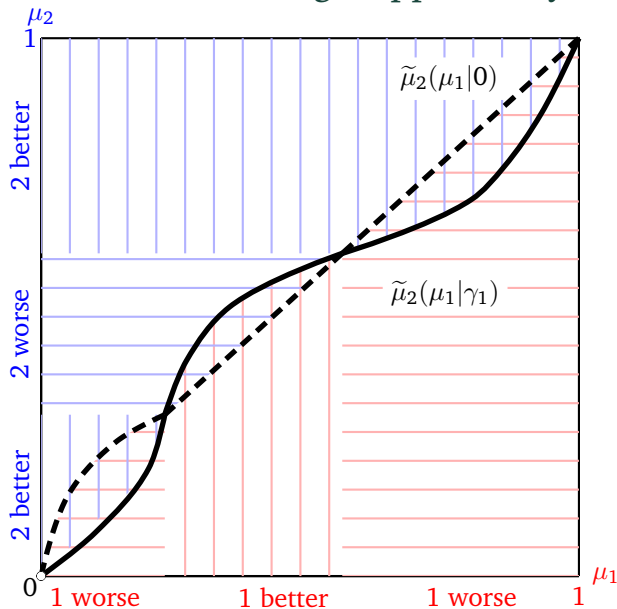
$$\mu_1'(t) = \lambda_1 \mu_1(t) - \gamma_1 (1 - \mu_1(t)) \mu_1(t) + \left( \frac{\gamma_1}{\nu_1^*} - \gamma_1 \right) \mu_1^2(t) \begin{cases} \leq \lambda_1 \mu_1(t) & \text{if } \mu_1(t) \leq \nu_1^* \\ > \lambda_1 \mu_1(t) & \text{if } \mu_1(t) > \nu_1^* \end{cases}$$

Reputation Coevolution:  $\gamma_1 \leq \lambda_1$ 

# Reputation Coevolution: $\gamma_1 > \lambda_1$



## Who Benefits from Challenge Opportunity?



## Multiple Types

Suppose players can choose their initial demands  $a_i$  and  $a_j$  from finite sets  $A_i$  and  $A_j$ , respectively.

### Unique Equilibrium

There exists a unique sequential equilibrium.

# Limit Payoffs

“Sufficiently rich” sets and small probabilities of persistence:

- ▶ Agreements are efficient: limit payoffs add up to 1.
- ▶ Player 1's limit payoff in Abreu and Gul (2000) is Rubinstein (1982) payoff

$$\frac{r_2}{r_1 + r_2}.$$

- ▶ Player 1's limit payoff in bargaining with one-sided challenge is

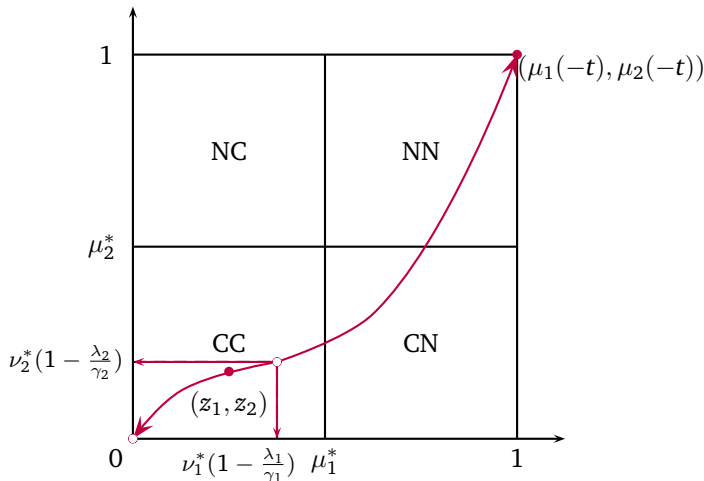
$$\frac{r_2}{\max\{r_1, \gamma_1\} + r_2}.$$



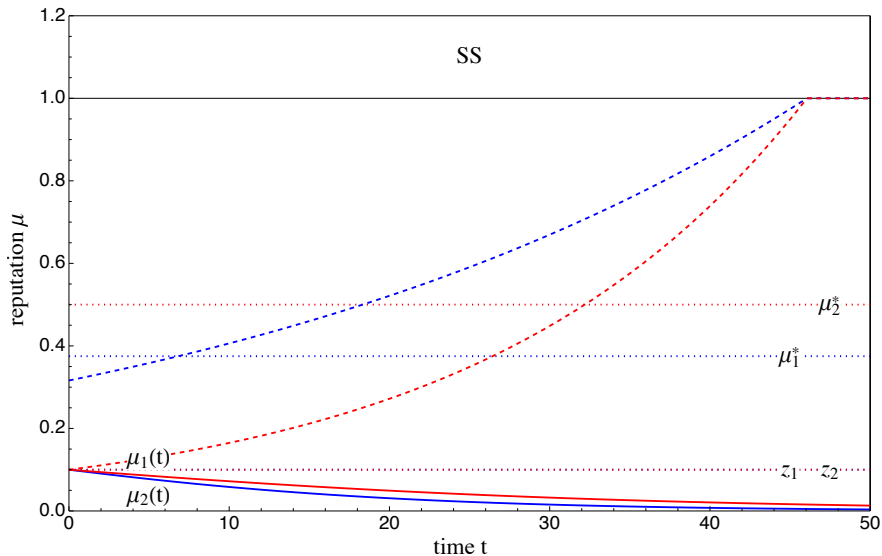
# Bargaining with Two-Sided Challenges

- ▶ Player 1 and player 2 bargain to divide a unit pie.
- ▶ With probability  $z_i$  player  $i$  persistently/irrationally demands  $a_i$ .
- ▶ Assume  $d \equiv a_1 + a_2 - 1 > 0$ .
- ▶ Time is continuous. Player  $i$ 's discount rate is  $r_i$ .
- ▶ At each instant, each player can persist or concede, **or**
  - ▶ A justified player  $i = 1, 2$  challenges with Poisson rate  $\gamma_i$ .
  - ▶ An unjustified player  $i = 1, 2$  can challenge any time.
- ▶ If player  $i$  pays cost  $c_i$  to challenge, player  $j \neq i$  has to respond.
  - ▶ A justified player  $j$  always sees the challenge.
  - ▶ If player  $j$  yields to the challenge, player  $i$  gets  $a_i$  and player  $j$  gets  $1 - a_j$ .
  - ▶ If player  $j$  pays cost  $c_j$  to see the challenge, a court determines outcome:
    - ▶ An unjustified player loses to a justified player.
    - ▶ An unjustified challenger wins with probability  $w$  against an unjustified player.

# Reputation Not Building Up



# Reputation Not Building Up



# Conclusion

- ▶ The paper builds a model of reputational bargaining with an opportunity to challenge the opponent.
- ▶ A player increases the challenge rate initially, and then does not challenge at all.
- ▶ The challenge opportunity may or may not benefit the challenger.
- ▶ Limit payoffs may depend on the arrival rate of challenge opportunities.
- ▶ The paper incorporates the continuous-time bargaining model of Abreu and Gul (2000) as a special case, and provides an economic interpretation and application of “irrationality”/“persistence”.

**THANK YOU!**

# References I

**Abreu, Dilip and Faruk Gul**, “Bargaining and Reputation,” *Econometrica*, 2000, 68 (1), 85–117.

**Rubinstein, Ariel**, “Perfect Equilibrium in a Bargaining Model,” *Econometrica*, January 1982, 50 (1), 97–108.