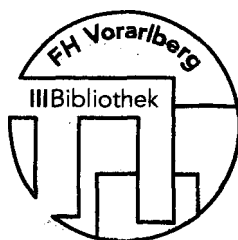


The Econometrics of Financial Markets

John Y. Campbell

Andrew W. Lo

A. Craig MacKinlay



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