Lab 2: Higher-Order Functions, Lambda Expressions **lab02.zip (lab02.zip)**

Due by 11:59pm on Wednesday, September 6.

Starter Files

Download lab02.zip (lab02.zip). Inside the archive, you will find starter files for the questions in this lab, along with a copy of the Ok (ok) autograder.

Topics

Consult this section if you need a refresher on the material for this lab. It's okay to skip directly to the questions and refer back here should you get stuck.

Short Circuiting

Higher-Order Functions

Lambda Expressions

Environment Diagrams

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Required Questions

Getting Started Videos

What Would Python Display?

Important: For all WWPD questions, type Function if you believe the answer is <function...>, Error if it errors, and Nothing if nothing is displayed.

Q1: WWPD: The Truth Will Prevail

Use Ok to test your knowledge with the following "What Would Python Display?" questions:

python3 ok -q short-circuit -u

```
>>> True and 13
-----
>>> False or 0
-----
>>> not 10
-----
>>> not None
-----
```

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```
>>> True and 1 / 0
-----
>>> True or 1 / 0
-----
>>> -1 and 1 > 0
-----
>>> -1 or 5
-----
>>> (1 + 1) and 1
-----
>>> print(3) or ""
```

```
>>> def f(x):
... if x == 0:
... return "I am zero!"
... elif x > 0:
... return "Positive!"
... else:
... return ""
>>> 0 or f(1)
-----
>>> f(0) or f(-1)
-----
>>> f(0) and f(-1)
```

Q2: WWPD: Higher Order Functions

Use Ok to test your knowledge with the following "What Would Python Display?" questions:

```
questions:

python3 ok -q hof-wwpd -u
```

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```
>>> def cake():
... print('beets')
     def pie():
          print('sweets')
. . .
          return 'cake'
     return pie
>>> chocolate = cake()
>>> chocolate
>>> chocolate()
>>> more_chocolate, more_cake = chocolate(), cake
>>> more_chocolate
>>> def snake(x, y):
... if cake == more_cake:
           return chocolate
... else:
           return x + y
>>> snake(10, 20)
>>> snake(10, 20)()
>>> cake = 'cake'
>>> snake(10, 20)
```

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Q3: WWPD: Lambda the Free

Use Ok to test your knowledge with the following "What Would Python Display?"

```
questions:
                                                                                     Qρ
 python3 ok -q lambda -u
As a reminder, the following two lines of code will not display anything in the Python
interpreter when executed:
 >>> x = None
 >>> x
```

```
>>> lambda x: x \# A lambda expression with one parameter x
>>> a = lambda x: x # Assigning the lambda function to the name a
>>> a(5)
>>> (lambda: 3)() # Using a lambda expression as an operator in a call exp.
>>> b =  lambda x, y: lambda: x + y # Lambdas can return other lambdas!
>>> c = b(88, 43)
>>> c
>>> c()
>>> d = lambda f: f(4) # They can have functions as arguments as well.
>>> def square(x):
        return x * x
>>> d(square)
```

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Coding Practice

Q4: Composite Identity Function

Write a function that takes in two single-argument functions, f and g, and returns another **function** that has a single parameter x. The returned function should return True if f(g(x)) is equal to g(f(x)). You can assume the output of g(x) is a valid input for f and vice versa. Try to use the composer function defined below for more HOF practice, or a lambda expression for more lambda practice.

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```
def composer(f, g):
    """Return the composition function which given x, computes f(g(x)).
   >>> add_one = lambda x: x + 1
                                       # adds one to x
   >>> square = lambda x: x**2
                                       # squares x [returns x^2]
   \Rightarrow a1 = composer(square, add_one) # (x + 1) ** 2
   >>> a1(4)
   25
   >>> a2 = composer(mul_three, a1)
                                      \# ((x + 1) ** 2) * 3
   >>> a2(4)
   75
   >>> a2(5)
   108
   11 11 11
   return lambda x: f(g(x))
def composite_identity(f, g):
   Return a function with one parameter x that returns True if f(g(x)) is
   equal to g(f(x)). You can assume the result of g(x) is a valid input for f
   and vice versa.
   >>> add_one = lambda x: x + 1
                                      # adds one to x
   >>> square = lambda x: x**2
                                      # squares x [returns x^2]
   >>> b1 = composite_identity(square, add_one)
   >>> b1(0)
                                       # (0 + 1) ** 2 == 0 ** 2 + 1
   True
                                       # (4 + 1) ** 2 != 4 ** 2 + 1
   >>> b1(4)
   False
    11 11 11
   "*** YOUR CODE HERE ***"
```

Use Ok to test your code:

```
python3 ok -q composite_identity
```

Q5: Count van Count

Consider the following implementations of count_fives and count_primes:

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```
def sum_digits(y):
    """Sum all the digits of y."""
    # implementation from Lab 1 Q6
def count_fives(n):
    """Return the number of values i from 1 up to and including n
    where sum_digits(n * i) is 5.
    >>> count_fives(10)
        # 50 (10 * 5)
    >>> count_fives(50)
      # 50 (50 * 1), 500 (50 * 10), 1400 (50 * 28), 2300 (50 * 46)
    11 11 11
    i = 1
    count = 0
    while i <= n:
        if sum_digits(n * i) == 5:
            count += 1
        i += 1
    return count
def is_prime(n):
    """Returns True if n is a prime number, False otherwise."""
    # implementation from Discussion 1 Q6
def count_primes(n):
    """Return the number of prime numbers up to and including n.
    >>> count_primes(6)
    3 # 2, 3, 5
    >>> count_primes(13)
        # 2, 3, 5, 7, 11, 13
    11 11 11
    i = 1
    count = 0
    while i <= n:
        if is_prime(i):
            count += 1
        i += 1
    return count
```

The implementations look quite similar! Generalize this logic by writing a function count_cond, which takes in a two-argument predicate function condition(n, i). count_cond returns a one-argument function that takes in n, which counts all the numbers from 1 to n that satisfy condition when called.

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Note: When we say condition is a predicate function, we mean that it is a function that will return True or False based on some specified condition in its body.

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```
def sum_digits(y):
   total = 0
   while y > 0:
        total, y = total + y % 10, y // 10
    return total
def is_prime(n):
    if n == 1:
        return False
   k = 2
   while k < n:</pre>
        if n % k == 0:
            return False
       k += 1
    return True
def count_cond(condition):
    """Returns a function with one parameter N that counts all the numbers from
    1 to N that satisfy the two-argument predicate function Condition, where
    the first argument for Condition is N and the second argument is the
    number from 1 to N.
   >>> count_fives = count_cond(lambda n, i: sum_digits(n * i) == 5)
   >>> count_fives(10) # 50 (10 * 5)
   1
   >>> count_fives(50) # 50 (50 * 1), 500 (50 * 10), 1400 (50 * 28), 2300 (50 * 46)
    4
   >>> is_i_prime = lambda n, i: is_prime(i) # need to pass 2-argument function into cour
   >>> count_primes = count_cond(is_i_prime)
   >>> count_primes(2)
                          # 2
   >>> count_primes(3) # 2, 3
   2
   >>> count_primes(4)
                        # 2, 3
   >>> count_primes(5)  # 2, 3, 5
   >>> count_primes(20)  # 2, 3, 5, 7, 11, 13, 17, 19
    11 11 11
    "*** YOUR CODE HERE ***"
```

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Use Ok to test your code:

python3 ok -q count_cond

Check Your Score Locally

You can locally check your score on each question of this assignment by running

python3 ok --score

This does NOT submit the assignment! When you are satisfied with your score, submit the assignment to Gradescope to receive credit for it.

Submit

Make sure to submit this assignment by uploading any files you've edited **to the appropriate Gradescope assignment.** For a refresher on how to do this, refer to Lab 00 (https://cs61a.org/lab/lab00/#submit-with-gradescope).

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Environment Diagram Practice

There is no Gradescope submission for this component.

However, we still encourage you to do this problem on paper to develop familiarity with Environment Diagrams, which might appear in an alternate form on the exam. To check your work, you can try putting the code into PythonTutor.

Q6: HOF Diagram Practice

Draw the environment diagram that results from executing the code below.

```
def f(x):
    n = 8
    return x + 1

def g(x):
    n = 9
    def h():
        return x + 1
    return h

def f(f, x):
    return f(x + n)

f = f(g, n)
g = (lambda y: y())(f)
```

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Optional Questions

These questions are optional, but you must complete them in order to be checked off before the end of the lab period. They are also useful practice!

Q7: Multiple

Write a function that takes in two numbers and returns the smallest number that is a multiple of both.

```
def multiple(a, b):
    """Return the smallest number n that is a multiple of both a and b.

>>> multiple(3, 4)
    12
    >>> multiple(14, 21)
    42
    """
    "*** YOUR CODE HERE ***"
```

Use Ok to test your code:

```
python3 ok -q multiple
```

Q8: I Heard You Liked Functions...

Define a function cycle that takes in three functions f1, f2, and f3, as arguments. cycle will return another function g that should take in an integer argument g and return another function g. That final function g should take in an argument g and cycle through applying g and g argument g and g argument g and g argument g argument g and g argument g argument g and g argument g argument g argument g and g argument g ar

```
n = 0, return x
n = 1, apply f1 to x, or return f1(x)
n = 2, apply f1 to x and then f2 to the result of that, or return f2(f1(x))
```

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- n = 3, apply f1 to x, f2 to the result of applying f1, and then f3 to the result of applying f2, or f3(f2(f1(x)))
- n = 4, start the cycle again applying f1, then f2, then f3, then f1 again, or f1(f3(f2(f1(x))))
- And so forth.

Hint: most of the work goes inside the most nested function.

```
def cycle(f1, f2, f3):
    """Returns a function that is itself a higher-order function.
   >>> def add1(x):
           return x + 1
   >>> def times2(x):
           return x * 2
   >>> def add3(x):
          return x + 3
   >>> my_cycle = cycle(add1, times2, add3)
   >>> identity = my_cycle(0)
   >>> identity(5)
   >>> add_one_then_double = my_cycle(2)
   >>> add_one_then_double(1)
   >>> do_all_functions = my_cycle(3)
   >>> do_all_functions(2)
   >>> do_more_than_a_cycle = my_cycle(4)
   >>> do_more_than_a_cycle(2)
   10
   >>> do_two_cycles = my_cycle(6)
   >>> do_two_cycles(1)
   19
    .....
    "*** YOUR CODE HERE ***"
```

Use Ok to test your code:

```
python3 ok -q cycle
```

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