

CS224d-Lec ture2

CS224d Deep Learning for Natural Language Processing

Lecture 2: Word Vectors

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How do we represent the meaning of a word?

Definition: **Meaning** (Webster dictionary)

- the idea that is represented by a word, phrase, etc.
- the idea that a person wants to express by using words, signs, etc.
- the idea that is expressed in a work of writing, art, etc.

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texonomy How to represent meaning in a computer? Common answer: Use a taxonomy like WordNet that has hypernyms (is-a) relationships from nltk.corpus import wordnet as wn panda = wn.synset('panda.n.01') hyper = lambda s: s.hypernyms() synonym sets (good): list(panda.closure(hyper)) [Synset('procyonid.n.01'), S: (adj) full, good Synset('carnivore.n.01'), S: (adj) estimable, good, honorable, respectable Synset('placental.n.01'). S: (adj) beneficial, good Synset('mammal.n.01'), S: (adj) good, just, upright S: (adj) adept, expert, good, practiced, Synset('vertebrate.n.01'), Synset('chordate.n.01'), proficient, skillful Synset('animal.n.01'), S: (adj) dear, good, near Synset('organism.n.01'), S: (adj) good, right, ripe Synset('living_thing.n.01'), Synset('whole.n.02'), S: (adv) well, good Synset('object.n.01'), S: (adv) thoroughly, soundly, good Synset('physical_entity.n.01'), S: (n) good, goodness Synset('entity.n.01')] S: (n) commodity, trade good, good Richard Socher 3/31/16

Problems with this discrete representation

Great as resource but missing nuances, e.g. synonyms: adept, expert, good, practiced, proficient, skillful?

now words mility

- Missing new words (impossible to keep up to date): wicked, badass, nifty, crack, ace, wizard, genius, ninjia
- Subjective

Requires human labor to create and adapt

Hard to compute accurate word similarity →

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hotexist for languages.

Problems with this discrete representation

The vast majority of rule-based and statistical NLP work regards words as atomic symbols: hotel, conference, walk

In vector space terms, this is a vector with one 1 and a lot of zeroes

[000000000010000]

We call this a "one-hot" representation. Its problem:

motel [000000000010000] AND hotel [000000010000000] = 0

Dimensionality: 20K (speech) - 50K (PTB) - 500K (big vocab) - 13M (Google 1T)

Distributional similarity based representations

You can get a lot of value by representing a word by means of its neighbors

"You shall know a word by the company it keeps"

(J. R. Firth 1957: 11)

One of the most successful ideas of modern statistical NLP

government debt problems turning into banking crises as has happened in saying that Europe needs unified banking regulation to replace the hodgepodge

HOW

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How to make neighbors represent words?

Answer: With a cooccurrence matrix X

- · 2 options: full document vs windows
- Word document cooccurrence matrix will give general topics (all sports terms will have similar entries) leading to "Latent Semantic Analysis"
- Instead: Window around each word → captures both syntactic (POS) and semantic information

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Window based cooccurence matrix

- (Window length 1 (more common: 5 10)
- Symmetric (irrelevant whether left or right context)
- Example corpus:
 - I like deep learning.
 - I like NLP.
 - I enjoy flying.

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instead of taking
the entire of dic
as continot
as just take

Window based cooccurence matrix

- Example corpus:
 - I like deep learning.
 - I like NLP.
 - I enjoy flying.



counts	1	like	enjoy	deep	learning	NLP	flying	
Ĭ	0	2	1_	0	0	0	0	0
like	2	0	0	1	0	1	0	0
enjoy	1	0	0	0	0	0	1	0
deep	0	1	0	0	1	0	0	0
learning	0	0	0	1	0	0	0	1
NLP	0	1	0	0	0	0	0	1
flying	0	0	1	0	0	0	0	1
	0	0	0	0	1	1	1	0

Problems with simple cooccurrence vectors

Increase in size with vocabulary

Very high dimensional: require a lot of storage

Subsequent classification models have sparsity issues

sparsity

→ Models are less robust

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Solution: Low dimensional vectors

 Idea: store "most" of the important information in a fixed, small number of dimensions: a dense vector

• Usually around 25 – 1000 dimensions

2 dimensions

The translature has higher from the pharmachine translature.

· How to reduce the dimensionality?

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Method 1: Dimensionality Reduction on X

Singular Value Decomposition of cooccurrence matrix X.

 \hat{X} is the best rank k approximation to X, in terms of least squares.

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Simple SVD word vectors in Python

Corpus

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I like deep learning. I like NLP. I enjoy flying.

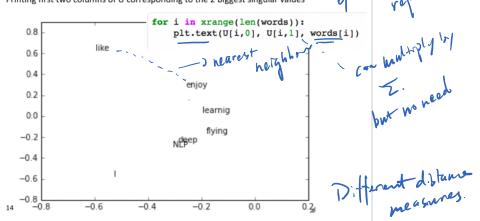
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apture the (agust variation)

Simple SVD word vectors in Python

Corpus: I like deep learning. I like NLP. I enjoy flying. Printing first two columns of U corresponding to the 2 biggest singular values



Word meaning is defined in terms of vectors

 In all subsequent models, including deep learning models, a word is represented as a dense vector

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Hacks to X

function words too often

- Problem: <u>function words</u> (the, he, has) are too frequent → syntax has too much impact. Some fixes:
 - min(X,t), with t~100
 - Ignore them all

closer words
re counted more
en set

TRAM MY GUN?

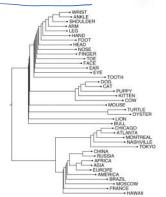
- Ramped windows that count closer words more
- Use Pearson correlations instead of counts, then set negative values to 0
- +++

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Interesting semantic patters emerge in the vectors



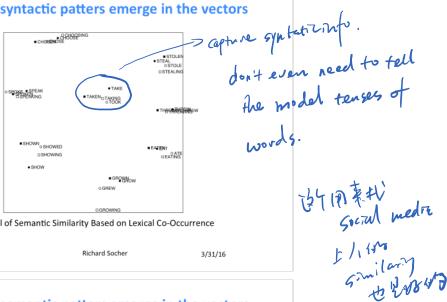
An Improved Model of Semantic Similarity Based on Lexical Co-Occurrence Rohde et al. 2005

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Interesting syntactic patters emerge in the vectors



An Improved Model of Semantic Similarity Based on Lexical Co-Occurrence Rohde et al. 2005

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Interesting semantic patters emerge in the vectors



An Improved Model of Semantic Similarity Based on Lexical Co-Occurrence Rohde et al. 2005

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Problems with SVD

Computational cost scales quadratically for n x m matrix:

 $O(mn^2)$ flops (when n<m)

→ Bad for millions of words or documents

Hard to incorporate new words or documents Different learning regime than other DL models

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DL: bok at a sperifu grample, lown from it -, pro-se to hert one

Idea: Directly learn low-dimensional word vectors

Old idea. Relevant for this lecture & deep learning:

Idea: Directly learn low-dimensional word vectors

- Old idea. Relevant for this lecture & deep learning:
 - Learning representations by back-propagating errors. (Rumelhart et al., 1986)
 - A neural probabilistic language model (Bengio et al., 2003)



- NLP (almost) from Scratch (Collobert & Weston, 2008)
- A recent, even simpler and faster model: word2vec (Mikolov et al. 2013) → intro now

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Main Idea of word2vec

- Instead of capturing cooccurrence counts directly,
- Predict surrounding words of every word
- Both are quite similar, see "Glove: Global Vectors for Word Representation" by Pennington et al. (2014) and Levy and Goldberg (2014) ... more later
- Faster and can easily incorporate a new sentence/ document or add a word to the vocabulary

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Details of Word2Vec

- Predict surrounding words in a window of length m of every word.
- Objective function: Maximize the log probability of any context word given the current center word:

Where θ represents all variables we optimize

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Details of Word2Vec 6. How does that grows a revolut?

Predict surrounding words in a window of length m of every

hext one

Details of Word2Vec

Predict surrounding words in a window of length m of every

word to be implemented on python For
$$p(w_{t+j}|w_t)$$
 the simplest first formulation is
$$p(o|c) = \frac{\exp\left(u_o^T v_c\right)}{\sum_{w=1}^W \exp\left(u_w^T v_c\right)}$$

- where o is the outside (or output) word id, c is the center word id, u and v are "center" and "outside" vectors of o and c
- Every word has two vectors!

This is essentially "dynamic" logistic regression

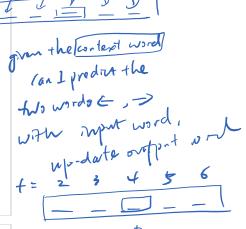
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tangent line

slope=f(x)



Cost/Objective functions

We will optimize (maximize or minimize) our objective/cost functions

For now: minimize → gradient descent

Refresher with trivial example: (from Wikipedia) Find a local minimum of the function $f(x)=x^4-3x^3+2$, with derivative $f'(x)=4x^3-9x^2$.

hile abs(x_new - x_old) > precision:

3 P(0/C) 3 log (2xp (U's Va))

3 7 No: V = No;

Derivations of gradient

- Whiteboard (see video if you're not in class;)
- The basic Lego piece
- Useful basics: $\frac{\partial \mathbf{x}^T \mathbf{a}}{\partial \mathbf{x}} = \frac{\partial \mathbf{a}^T \mathbf{x}}{\partial \mathbf{x}} = \mathbf{a}$
- If in doubt: write out with indices
- Chain rule! If y = f(u) and u = g(x), i.e. y=f(g(x)), then:

$$\frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}$$

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Chain Rule

Chain rule! If y = f(u) and u = g(x), i.e. y=f(g(x)), then:

Zw exp(NJVo) X & L Zx exp(uw) Chain rule! If y = f(u) and u = g(x), i.e. y=f(g(x)), then:

$$\frac{dy}{dx} = \frac{dy}{du}\frac{du}{dx} = \frac{df(u)}{du}\frac{dg(x)}{dx}$$

Simple example: $\frac{dy}{dx} = \frac{d}{dx}5(x^3+7)^4$

$$y = f(u) = 5u^{4}$$

$$u = g(x) = x^{3} + 7$$

$$\frac{dy}{du} = 20u^{3}$$

$$\frac{du}{dx} = 3x^{2}$$

$$\frac{dy}{dx} = 20(x^3 + 7)3x^2$$

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Interactive Whiteboard Session!

$$J(\theta) = \frac{1}{T} \sum_{t=1}^{T} \sum_{-m \le j \le m, j \ne 0} \log p(w_{t+j}|w_t)$$

Let's derive gradient together For one example window and one example outside word:

$$\log p(o|c) = \log \frac{\exp \left(u_o^T v_c\right)}{\sum_{w=1}^{W} \exp \left(u_w^T v_c\right)}$$

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Approximations: PSet 1

- With large vocabularies this objective function is not scalable and would train too slowly! \rightarrow Why?
- Idea: approximate the normalization or
- Define negative prediction that only samples a few words that do not appear in the context
- Similar to focusing on mostly positive correlations

You will derive and implement this in Pset 1!

The water a former hat after and model.

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Linear Relationships in word2vec

These representations are very good at encoding dimensions of similarity!

Analogies testing dimensions of similarity can be solved quite well just by doing vector subtraction in the embedding space

X du [Zx exp(uive)] 3= Zw ove exp(univy = \frac{\interp(u\text{TVc).uw}}{\text{uw}} sigle hunber. Joy pro(c) = No - Zw=1 =xp(u,vc)

= xp(u,vc)

= xp(u,vc) = No - Zm=1 b (x(c) nx Where do we got u. v? Sturt from small # 's 6ther than soft max, What are the other Advot setment - directly

get the word ventor.

Linear Relationships in word2vec

These representations are very good at encoding dimensions of similarity!

- Analogies testing dimensions of similarity can be solved quite well just by doing vector subtraction in the embedding space Syntactically
 - $X_{apple} X_{apples} \approx X_{car} X_{cars} \approx X_{family} X_{families}$
 - · Similarly for verb and adjective morphological forms Semantically (Semeval 2012 task 2)
 - $X_{shirt} X_{clothing} \approx X_{chair} X_{furniture}$
 - $X_{king} X_{man} \approx X_{queen} X_{woman}$

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Darameters matter

get the word voitor:

Count based vs direct prediction

LSA, HAL (Lund & Burgess), COALS (Rohde et al), Hellinger-PCA (Lebret & Collobert)

- · Fast training
- · Efficient usage of statistics
- · Primarily used to capture word similarity
- · Disproportionate importance given to large counts
- NNLM, HLBL, RNN, Skipgram/CBOW, (Bengio et al; Collobert & Weston; Huang et al; Mnih & Hinton; Mikolov et al; Mnih & Kavukcuoglu)
- Scales with corpus size
- Inefficient usage of statistics
- Generate improved performance on other tasks
- Can capture complex patterns beyond word similarity

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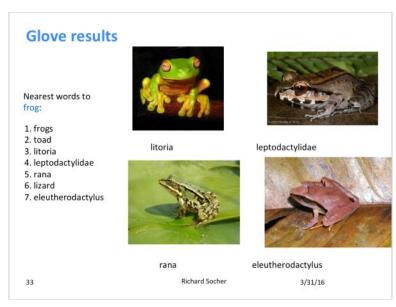
Combining the best of both worlds $J(\theta) = \frac{1}{2} \sum_{i,j=1}^W f(P_{ij}) (u_i^T v_j - \underline{\log P_{ij}})^2$

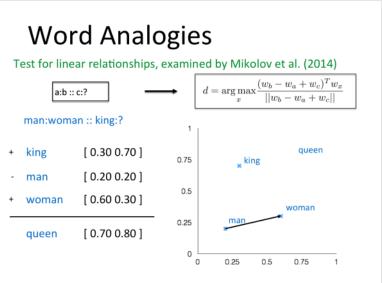
- Fast training
- Scalable to huge corpora
- Good performance even with small corpus, and small vectors

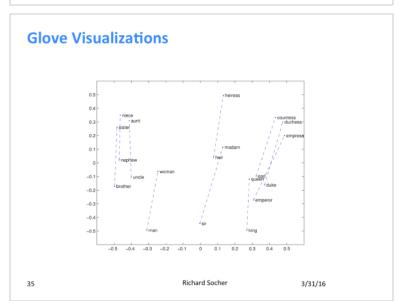
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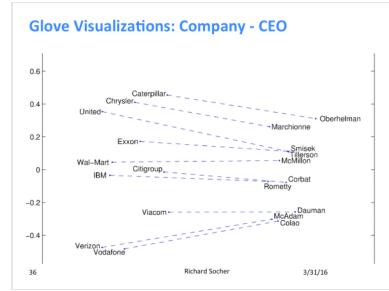
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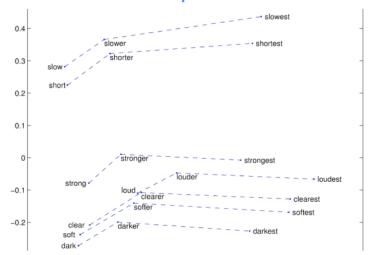


Onestion:
Identify one CEO.

Land the

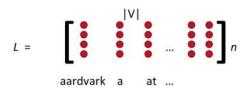
rest?





Word embedding matrix

• Initialize most word vectors of future models with our "pretrained" embedding matrix $\ L \in \mathbb{R}^{n \times |V|}$

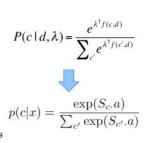


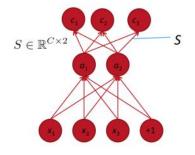
- Also called a look-up table
 - · Conceptually you get a word's vector by left multiplying a one-hot vector e (of length |V|) by L: x = Le

Advantages of low dimensional word vectors

What is the major benefit of deep learned word vectors?

Ability to also propagate **any** information into them via neural networks (next lecture).





Advantages of low dimensional word vectors

- Word vectors will form the basis for all subsequent lectures.
- All our semantic representations will be vectors!
- Next lecture:
 - Some more details about word vectors
 - Predict labels for words in context for solving lots of different tasks

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