

# Assignment 2 Dataflow Analysis

Due Date: **Mar. 8<sup>th</sup>**, Total Marks: 100 pts

CSCD70 Compiler Optimizations  
Department of Computer Science  
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## ABSTRACT

In class, we discussed interesting dataflow analyses such as Reaching Definitions, Liveness, and Available Expressions. Although these analyses are different in certain ways, for example they compute different program properties and analyze the program in different directions (i.e., forward, backward), they share some common properties such as iterative algorithms, transfer functions, and meet operators. These commonalities make it worthwhile to write a generic framework that can be parameterized appropriately for solving a specific dataflow analysis. In this assignment, you will implement such an iterative dataflow analysis framework in LLVM, and use it to implement forward and backward dataflow analyses. Although the analyses that we are about to implement in this assignment are available in some form in LLVM, they are not of the iterative flavor, and the objective of this assignment is to create a generic framework for solving iterative dataflow analysis problems.

## 1 POLICY

### 1.1 Collaboration

You will work in groups of **two** for the assignments in this course. Please turn in a single submission per group.

### 1.2 Submission

Please submit all your files to MarkUs/GitHub Classroom. Make sure that your submission includes the followings:

writeup.pdf

```
include/dfa/Framework.h
include/dfa/MeetOp.h
lib/AvailExpr.cpp
lib/Liveness.cpp
lib/LCM/*
CMakeLists.txt
test/...
```

- A report named writeup.pdf that describes the implementation of your passes, and has answers to the theoretical questions.
- Well-commented source code for your framework and passes (*Available Expressions*, *Liveness*, and *LCM*), together with a build file CMakeLists.txt (please write your CMakeLists.txt in such a way that all passes can be built, integrated, and tested using the command `cmake .. && make && make test`).
- A subfolder named test that contains all the microbenchmarks used for verification of your code.

## 2 PROBLEM STATEMENT

### 2.1 Iterative Framework

A well written iterative dataflow analysis framework significantly reduces the burden of implementing new dataflow passes, the developer only writes pass specific details such as the meet operator, transfer function, analysis direction etc. Specifically, *the framework should solve any unidirectional dataflow analysis as long the analysis supplies the following:*

- (1) Domain
- (2) Direction (Forward/Backward)
- (3) Meet Operation
- (4) Transfer Function

### 2.2 Dataflow Analysis [40 pts]

**2.2.1 Available Expressions [20 pts].** Upon convergence, your Available Expressions pass should report all the binary expressions that are *available* at each program point. For this assignment, *we are only concerned with expressions represented using an instance of BinaryOperator*. Analyzing comparison instructions and unary instructions such as negation is not required.

We will consider two expressions *equal* if the instructions that calculate these expressions share the same opcode, left-hand-side and right-hand-side operand. In addition to this, the expression  $x \oplus y$  is equal to expression  $y \oplus x$  under the condition that the operator  $\oplus$  is *commutative*.

**2.2.2 Liveness [20 pts].** Upon convergence, your *Liveness* pass should report all variables that are *live* at each program point. For this assignment, we will only track the liveness of *instruction-defined values* and *function arguments*. That is, when determining which values are used by an instruction, you will use code like this:

```
Instruction *Inst = ...
```

```
for (auto Iter = Inst->op_begin();
     Iter != Inst->op_end(); ++Iter) {
    Value *V = *Iter;

    if (isa<Instruction>(V) || isa<Argument>(V)) {
        ...
    }
}
```

The fact that there are  $\phi$  instructions has ramifications on how your passes are implemented. Think carefully about what this means to your implementation and *briefly explain this in your writeup*.

### 2.3 Lazy Code Motion [40 pts]

Now that you have completed an example on the forward and backward analysis, consider the Lazy Code Motion (LCM) problem that we described in class, which consists of two forward and two backward dataflow analyses. Your job in this subsection is to leverage the framework to determine the *earliest placement* in LCM. This hence requires the *anticipated* and *will-be-available expressions* analysis, both of which you will have to inherit from the framework.

The implementation of LCM is somewhat similar to that of the passes in the previous subsections: Similar to the case of Available Expressions, the domain of analysis in LCM is restricted to expressions represented using an instance of BinaryOperator; and similar to the case of Liveness, the presence of  $\phi$  instructions has ramifications on your passes. Again, think carefully what this means and *briefly explain this in your writeup*.

The provided benchmark file LCM.11 is directly copied from the problem statement in Question 3.2 (therefore, it is recommended that you complete Question 3.2 first before approaching this problem). Check your program outputs with your answer in Question 3.2 after the completion of both parts. Do they corroborate each other?

## 3 THEORETICAL QUESTIONS

### 3.1 Loop Invariant Code Motion [10 pts]

Suppose that you are optimizing the code in Figure 1.

- (1) List the *loop invariant instructions*.
- (2) Indicate if each loop invariant instruction can be moved to the loop preheader, and give a brief justification.

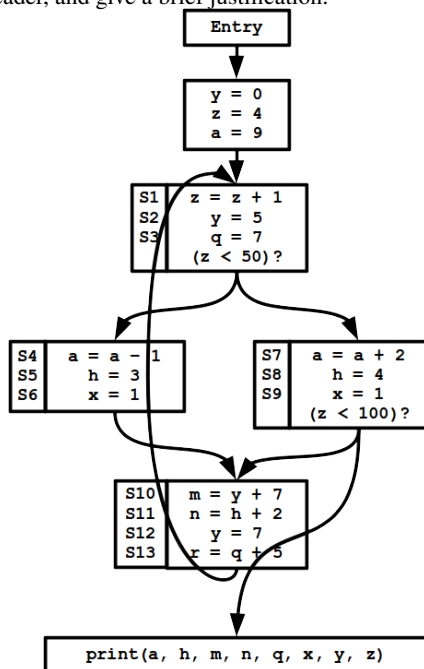


Figure 1: CFG for Analysis

### 3.2 Lazy Code Motion [10 pts]

Suppose that you are optimizing the code in Listing 1.

```

int foo(a, b, c) {
    if (a > 5) {
        g = b + c;
    } else {
        while (b < 5) {
            b = b + 1;
            d = b + c;
        }
    }
    e = b + c;
    return e;
}
  
```

Listing 1: Source Code for Analysis

- (1) Summarize what is *Lazy Code Motion*?
- (2) Build the CFG for this code and break the critical edges. Using the algorithm described in class, provide *anticipated expressions* for each basic block.
- (3) Provide *will-be-available expressions* for each basic block, and indicate the *earliest placement* for each expression, if applicable.
- (4) Provide *postponable expressions* and *used expressions* for each basic block, and indicate the *latest placement* for each expression, if applicable.
- (5) Complete the final pass of lazy code motion by inserting and replacing expressions. Provide the finalized CFG, and label each basic block with its instruction(s). Answer why it should have better performance compared with the raw CFG.

## 4 FAQ

Given below is the questions asked during previous offering of the class. If you do not think they fully answer your question, please open a new thread on [Piazza](#).

**Q:** In class, we always dealt with the DFA by basic blocks (i.e., the transfer function operates on an entire basic block). But it seems from the starter code that we are doing transfer function on each instruction. How does this work?

**A:** Remember that we mentioned from class that the transfer function of the entire basic blocks is just the composite of the transfer function of all the instructions within that basic block, i.e.,

$$f_{bb} = f_{i_n} \circ f_{i_{n-1}} \circ \dots \circ f_{i_1}^1, i_{1\dots, n-1, n} \in bb$$

You can prove that the above equation is mathematically correct, but hopefully it makes sense by intuition.

**Q:** How does the domain work? What is the relationship between domain and the instruction-domain mapping? Specifically, suppose that we have  $N$  expressions in our program text, then for available expressions we just have a bitvector of length  $N$ ? If that is the case, then how do we know which bit in the bit vector is associated with a particular expression?

**A:** Your understanding is right. Suppose that you have  $N$  domain elements, then your bitvector length should be  $N$  as well. The reason

<sup>1</sup>The order of composition depends on the direction of DFA.

## Assignment 2 Dataflow Analysis

is because there shall be a one-to-one correspondence between the domain elements and the bitvector indices.

As an example, let us suppose that we have three expressions in our program text, namely  $\{a + b, a - b, a \times b\}$ . When we say that the output of instruction  $i$  is  $\{001\}$ , that '1' can be  $a + b$ ,  $a - b$ , or  $a \times b$ . What really matters is that *the mapping between bitvector indices and domain elements must be consistent throughout the*

*entire analysis*, and that is the reason why we have domain, which plays the role of the metadata that describes the bitvectors.

**Q: Do we have to include every expression in our Lazy Code Motion analysis?**

**A:** No. You do not have to. However, if you decide to not include any expression(s), explain why they cannot be optimized using Lazy Code Motion.