Instruction of integer_converter.r (R)

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1. Introduction

The R file *integer_converter.r* provides some extra functions for integers, particularly for the calculation of integers with large number of digits. With *integer_converter.r*, it is good for study of integers, research of cryptography and simulation. Because it is not designed to speed up the computation, but to sustain as many functions as possible in dealing with integers with large number of digits, it is not appropriate to be installed directly into the applications related to cryptography or something else, which require calculation speed for integers with large number of digits.

- Current version 0.1.1, June 6, 2022. The script of R is also provided; some more functions are added.
- Version 0.1.0, June 1, 2022. This is the initial script of Python.

2. Integer Format

In *integer_converter.r*, the format of integers, which can be used for all the following functions, is a *numeric & vector*, where the first element is -1 or 0 or 1 (1 represents positive integer, -1 represents negative integer, 0 represents zero) and the following elements of type *numeric* are the digits of the integer. Alongside with the integer of type *numeric & vector*, a radix of type *numeric*, which is greater than or equal to 2, is also required.

For example, 123456 with radix 1000 is

-123456 with radix 2 is

where the higher index of the element in the *numeric & vector*, the element is with the higher power of radix.

Zero is

```
a = c(0, 0)
print(a)
#------
```

3. Check Function, Conversion Functions, Comparison Functions

3.1. integer_check

```
integer_check = function(x, radix)
```

The function to check whether *x* of type *numeric & vector* is a valid format of an integer with *radix*, like

If these exists one digit in *x* which is greater than or equal to the radix, then, the integer is invalid, like

If x is not zero, and the highest digit is 0, then, the integer is invalid, like

If the radix is less than or equal to 1, then, the integer is invalid, like

3.2. integer_num_2_vec

```
integer_num_2_vec = function(x, radix, check = TRUE)
```

The function to convert *x* of type *numeric* to the integer of type *numeric* & *vector* with *radix*, like

where the argument *check* is whether to scan the validity of other arguments.

3.3. integer_vec_2_num

```
integer_vec_2_num = function(x, radix, check = TRUE)
```

The function to convert *x* of type *numeric* & *vector* with *radix* to the variable of *numeric*, like

where the argument *check* is whether to scan the validity of other arguments.

3.4. Integer_vec_change_radix

```
integer_vec_change_radix = function(x, origin_radix, new_radix,
    check = TRUE)
```

The function to convert *x* of type *numeric & vector* with *origin_radix* to the integer with *new_radix*, like

3.5. integer_less_vec_vec

```
integer_less_vec_vec = function(x, y, radix, check = TRUE)
```

The function to check whether *x* of type *numeric & vector* with *radix* is less than *y* of type *numeric & vector* with *radix*, like

```
rad = 1000
a = 1234
b = integer num 2 vec(a, rad)
c = 5678
d = integer num 2 vec(c, rad)
e1 = integer_less_vec_vec(x = b, y = d,
                          radix = rad)
e2 = integer less vec vec(x = b, y = b,
                          radix = rad)
e3 = integer less vec vec(x = d, y = b,
                         radix = rad)
> print(e1)
TRUE
> print(e2)
FALSE
> print(e3)
FALSE
```

where the argument *check* is whether to scan the validity of other arguments.

3.6. integer_lesseq_vec_vec

```
integer_lesseq_vec_vec = function(x, y, radix, check = TRUE)
```

The function to check whether *x* of type *numeric* & *vector* with *radix* is less than or equal to *y* of type *numeric* & *vector* with *radix*, like

```
rad = 1000
a = 1234
b = integer num 2 vec(a, rad)
c = 5678
d = integer num 2 vec(c, rad)
e1 = integer lesseq vec vec(x = b, y = d,
                         radix = rad)
e2 = integer lesseq vec vec(x = b, y = b,
                         radix = rad)
e3 = integer lesseq vec vec(x = d, y = b,
                    radix = rad)
#-----
> print(e1)
TRUE
> print(e2)
TRUE
> print(e3)
FALSE
```

3.7. integer_more_vec_vec

```
integer_more_vec_vec = function(x, y, radix, check = TRUE)
```

The function to check whether *x* of type *numeric* & *vector* with *radix* is more than *y* of type *numeric* & *vector* with *radix*, like

```
rad = 1000
a = 1234
b = integer num 2 vec(a, rad)
c = 5678
d = integer num 2 vec(c, rad)
e1 = integer more vec vec(x = b, y = d,
                          radix = rad)
e2 = integer_more_vec_vec(x = b, y = b,
                          radix = rad)
e3 = integer_more_vec_vec(x = d, y = b,
                         radix = rad)
> print(e1)
FALSE
> print(e2)
FALSE
> print(e3)
TRUE
```

where the argument *check* is whether to scan the validity of other arguments.

3.8. integer_moreeq_vec_vec

```
integer_moreeq_vec_vec = function(x, y, radix, check = TRUE)
```

The function to check whether *x* of type *numeric & vector* with *radix* is more than or equal to *y* of type *numeric & vector* with *radix*, like

```
rad = 1000
a = 1234
b = integer num 2 vec(a, rad)
c = 5678
d = integer num 2 vec(c, rad)
e1 = integer_moreeq_vec_vec(x = b, y = d,
                          radix = rad)
e2 = integer_moreeq_vec_vec(x = b, y = b,
                          radix = rad)
e3 = integer moreeq vec vec(x = d, y = b,
                          radix = rad)
#-----
> print(e1)
FALSE
> print(e2)
TRUE
> print(e3)
TRUE
```

where the argument *check* is whether to scan the validity of other arguments.

3.9. integer_eq_vec_vec

```
integer_eq_vec_vec = function(x, y, radix, check = TRUE)
```

The function to check whether *x* of type *numeric & vector* with *radix* is equal to *y* of type *numeric & vector* with *radix*, like

```
rad = 1000
a = 1234
b = integer num 2 vec(a, rad)
c = 5678
d = integer num 2 vec(c, rad)
e1 = integer eq vec vec(x = b, y = d,
                       radix = rad)
e2 = integer eq vec vec(x = b, y = b,
                       radix = rad)
e3 = integer_eq_vec_vec(x = d, y = b,
                   radix = rad)
> print(e1)
FALSE
> print(e2)
TRUE
> print(e3)
FALSE
```

3.10. integer_noteq_vec_vec

```
integer_noteq_vec_vec = function(x, y, radix, check = TRUE)
```

The function to check whether *x* of type *numeric* & *vector* with *radix* is not equal to *y* of type *numeric* & *vector* with *radix*, like

```
rad = 1000
a = 1234
b = integer num 2 vec(a, rad)
c = 5678
d = integer num 2 vec(c, rad)
e1 = integer noteq vec vec(x = b, y = d,
                         radix = rad)
e2 = integer noteq vec vec(x = b, y = b,
                         radix = rad)
e3 = integer_noteq_vec_vec(x = d, y = b,
                        radix = rad)
#-----
> print(e1)
TRUE
> print(e2)
FALSE
> print(e3)
TRUE
```

where the argument *check* is whether to scan the validity of other arguments.

3.11. integer_is_even

```
integer_is_even = function(x, radix, check = TRUE)
```

The function to check whether *x* of type *numeric & vector* with *radix* is an even integer, like

where the argument *check* is whether to scan the validity of other arguments.

4. Basic Operation Functions

4.1. integer_inverse

```
integer_inverse = function(x, radix, check = TRUE)
```

The function to return the inverse value of x of type numeric & vector with radix, like

where the argument *check* is whether to scan the validity of other arguments.

4.2. integer_absolute

like

```
integer_absolute = function(x, radix, check = TRUE)
```

The function to return the absolute value of *x* of type *numeric & vector* with *radix*,

where the argument *check* is whether to scan the validity of other arguments.

4.3. integer_plus

```
integer_plus = function(x, y, radix, check = TRUE)
```

The function to calculate the sum (x+y) of x and y of type *numeric* & *vector* with *radix*, like

4.4. integer_minus

```
integer_minus = function(x, y, radix, check = TRUE)
```

The function to calculate the difference (x-y) of x and y of type numeric & vector with radix, like

where the argument *check* is whether to scan the validity of other arguments.

4.5. integer_multiply

```
integer_multiply = function(x, y, radix, check = TRUE)
```

The function to calculate the product $(x \times y)$ of x and y of type *numeric* & *vector* with *radix*, like

4.6. integer_modulo

```
integer_modulo = function(x, y, radix, check = TRUE)
```

The function to calculate the modulo of x and y of type numeric & vector with radix, like

where the argument *check* is whether to scan the validity of other arguments, and the output is the *list*, in which *quo* is the quotient and *rem* is the remainder.

4.7. integer_power

```
integer_power = function(x, y, radix, check = TRUE)
```

The function to calculate the power of base *x* and exponent *y* of type *numeric* & *vector* with *radix*, like

where the argument *check* is whether to scan the validity of other arguments, and y should be a non-negative integer.

```
Specially, 0^0 = 1.
```

4.8. integer_factorial

```
integer_factorial = function(x, radix, check = TRUE)
```

The function to calculate the factorial of x of type numeric & vector with radix, like

where the argument *check* is whether to scan the validity of other arguments.

4.9. integer_permute

```
integer_permute = function(m, n, radix, check = TRUE)
```

The function to calculate (m permute n), where m and n are of type numeric & vector with radix, like

4.10. integer_choose

```
integer_choose = function(m, n, radix, check = TRUE)
```

The function to calculate (m choose n), where m and n are of type numeric & vector with radix, like

where the argument *check* is whether to scan the validity of other arguments.

4.11. integer_mod_inverse

```
integer_mod_inverse = function(x, m, radix, check = TRUE)
```

The function to calculate the modular inverse integer of x modulo m, where m and n are of type *numeric* & *vector* with *radix*, like

In the above example, it is

$$(15 \times 3) \mod 22 = 1$$

4.12. integer_crt

```
integer_crt = function(r, m, radix, check = TRUE)
```

The function to calculate the number of the Chinese remainder theorem, where r is the *list* of remainders, m is the *list* of divisors. For example,

```
rad = 1000
r1 = 3
r1 = integer num 2 vec(r1, rad)
r2 = 4
r2 = integer num 2 vec(r2, rad)
r3 = integer_num_2_vec(r3, rad)
r list = list(r1, r2, r3)
a = 35
a = integer num 2 vec(a, rad)
b = integer num 2 vec(b, rad)
c = 17
c = integer_num_2_vec(c, rad)
m list = list(a, b, c)
d = integer_crt(r = r_list, m = m_list,
                radix = rad)
print(d)
1 378 11
```

where the argument *check* is whether to scan the validity of other arguments.

In the above example, it is

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 $\begin{cases} 11378 \ mod \ 35 = 3 \\ 11378 \ mod \ 22 = 4 \\ 11378 \ mod \ 17 = 5 \end{cases}$

5. Prime-Related, Composite-Related Functions

5.1. integer_is_prime

```
integer_is_prime = function(x, radix, check = TRUE)
```

The function to check whether *x* of type *numeric & vector* with *radix* is a prime or composite, like

or

where the argument *check* is whether to scan the validity of other arguments.

If *x* is -1 or 0 or 1, it will return *NULL*.

5.2. integer_factorization

```
integer_factorization = function(x, radix, check = TRUE)
```

The function to calculate the prime factors of x of type numeric & vector with radix, like

```
rad = 1000
a = -4641920
a = integer num 2 vec(a, rad)
b = integer factorization(x = a, radix = rad)
#-----
$prime
$prime[[1]]
1 2
$prime[[2]]
1 5
$prime[[3]]
1 253
$power
$power[[1]]
1 7
$power[[2]]
1 1
$power[[3]]
1 1
```

where the argument *check* is whether to scan the validity of other arguments, and the output is the *list*, in which *prime* is of the prime factors and *power* is of the corresponding power of the prime factors.

In the above example, it is

$$-4641914 = -2^7 \times 5^1 \times 7253^1$$

5.3. integer_Euler_phi

```
integer_Euler_phi = function(x, radix, check = TRUE)
```

The function to calculate the Euler's ϕ of x of type numeric & vector with radix, like

In the above example, it is

$$\phi(3^2 \times 7 = 63) = [3^{2-1} \times (3-1)] \times [7^{1-1} \times (7-1)] = 36$$

5.4. integer_gcd

```
integer_gcd = function(x, y, radix, check = TRUE)
```

The function to calculate the greatest common divisor of *x* and *y* of type *numeric* & *vector* with *radix*, like

where the argument *check* is whether to scan the validity of other arguments.

5.5. integer_is_relatively_primes

```
integer_is_relatively_primes = function(x, y, radix, check = TRUE)
```

The function to calculate check whether *x* and *y* of type *numeric & vector* with *radix* are relatively primes, like

5.6. integer_lcm

```
integer_lcm = function(x, y, radix, check = TRUE)
```

The function to calculate the least common multiple of x and y of type *numeric* & *vector* with radix, like

where the argument *check* is whether to scan the validity of other arguments.

6. Functions of Arithmetic-Modulo Sequence

6.1. integer_am_seq_complete_root_condition

```
integer_am_seq_complete_root_condition = function(c, a, m, radix)
```

The function to check whether the integers c, a, m can construct an arithmetic-modulo sequence (AM sequence) with shift term a

$$(a_1, a_2, ..., a_n, ...)$$

where $a_n = c(n + a) \mod m$, and c is the complete root.

For example,

```
rad = 1000
c0 = 3
c0 = integer num 2 vec(c0, rad)
a0 = 10
a0 = integer num 2 vec(a0, rad)
m0 = 25
m0 = integer_num_2_vec(m0, rad)
condition = integer am seq complete root condition(c = c0,
                                                     m = m0,
                                                     radix = rad)
print(condition)
$encode
$encode$type
"am_seq"
$encode$c
1 3
$encode$a
1 10
$encode$m
1 25
$decode
$decode$type
"am seq"
$decode$c
1 17
$decode$a
1 20
$decode$m
1 25
```

where the output is the *list*, in which *encode* is of the parameters of AM sequence conversion and *decode* is of the parameters for the inverse conversion.

6.2. integer_am_seq_convert

```
integer_am_seq_convert = function(x, am_seq_list, radix)
```

The function to convert from x to a_x in the arithmetic-modulo sequence (AM sequence) with shift term a

$$(a_1, a_2, ..., a_n, ...)$$

where $a_n = c(n + a) \mod m$, and c is the complete root.

For example, if the argument of *am_seq_list* is the *encode* from *integer_am_seq_complete_root_condition*, then,

```
rad = 1000
c0 = 3
c0 = integer num 2 vec(c0, rad)
a0 = 10
a0 = integer num 2 vec(a0, rad)
m0 = 25
m0 = integer num 2 vec(m0, rad)
condition = integer am seq complete root condition(c0,
                                                    m0,
                                                    rad)
encode condition = condition[["encode"]]
decode condition = condition[["decode"]]
n = 5
n = integer_num_2_vec(n, rad)
an = integer_am_seq_convert(x = n,
                            am_seq_list = encode_condition,
                            radix = rad)
print(an)
1 20
```

and if *n* is 20 and argument of *am_seq_list* is the *decode* from *integer_am_seq_complete_root_condition*, then,

```
rad = 1000
c0 = 3
c0 = integer_num_2_vec(c0, rad)
a0 = 10
a0 = integer num 2 vec(a0, rad)
m0 = 25
m0 = integer_num_2_vec(m0, rad)
condition = integer_am_seq_complete_root_condition(c0,
                                                 m0,
                                                 rad)
encode_condition = condition[["encode"]]
decode_condition = condition[["decode"]]
n = 20
n = integer num 2 vec(n, rad)
an = integer am seq convert(x = n,
                          am_seq_list = decode_condition,
                          radix = rad)
print(an)
#-----
```

7. Functions of Type-1 Geometric-Modulo Sequence

7.1. integer_t1gm_seq_primitive_root_condition

```
integer_tlgm_seq_primitive_root_condition = function(c, a, p,
p_power, radix, double = FALSE)
```

The function to check whether the integers c, a, m can construct a type-1 geometric-modulo sequence (T1GM sequence) with coefficient c

$$(g_1, g_2, ..., g_n, ...)$$

where $g_n = ca^n \mod m$, and

$$m = egin{cases} p^{ ext{p_power}}, & ext{if double is False} \ 2p^{ ext{p_power}}, & ext{if double is True'} \end{cases} p ext{ is a prime}$$

and *a* is the primitive root.

For example,

```
rad = 1000
c0 = 1
c0 = integer num 2 vec(c0, rad)
a0 = 2
a0 = integer num 2 vec(a0, rad)
p0 = 11
p0 = integer num 2 vec(p0, rad)
p power0 = 3
p power0 = integer num 2 vec(p power0, rad)
condition = integer t1gm seq primitive root condition(c = c0,
                                                           a = a0,
                                                           p = p0,
                                                          p_power =
p power0,
                                                           radix = rad,
                                                           double =
FALSE)
print(condition)
"t1gm_seq_primitive_root"
$с
1 1
$a
1 2
$m
1 331 1
$m prime
$m prime[[1]]
1 \overline{1}1
$m power
$m_power[[1]]
$phi m
1 210
$phi phi m
1 \ 44\overline{0}
```

which reveals 2 is the primitive root of the T1GM sequence modulo $11^3 = 1331$.

7.2. integer_t1gm_seq_convert

```
integer_tlgm_seq_convert = function(x, tlpm_seq_pr_list, radix)
```

The function to convert from x to g_x in the type-1 geometric-modulo sequence (T1GM sequence) with coefficient c

$$(g_1, g_2, ..., g_n, ...)$$

where $g_n = ca^n \mod m$, and

$$m = \begin{cases} p^{p_{\text{-power}}}, & \text{if double is False} \\ 2p^{p_{\text{-power}}}, & \text{if double is True} \end{cases}$$
 p is a prime

and *a* is the primitive root.

For example,

```
rad = 1000
c0 = 1
c0 = integer num 2 vec(c0, rad)
a0 = integer num 2 vec(a0, rad)
p0 = 23
p0 = integer_num_2_vec(p0, rad)
p power0 = 1
p_power0 = integer_num_2_vec(p_power0, rad)
condition = integer t1gm seq primitive root condition(c0,
                                                        р0,
                                                       p power0,
                                                        rad)
n = 12
n = integer_num_2_vec(n, rad)
gn = integer_t1gm_seq_convert(x = n,
                              t1pm seq pr list = condition,
                               radix = rad)
print(gn)
```

where 5 is a primitive root of T1GM sequence modulo 23, and

$$5^{12} \mod 23 = 18$$

7.3. integer_t1gm_seq_index

```
integer_tlgm_seq_index = function(x, tlpm_seq_pr_list, radix)
```

The function to find the index of x in the type-1 geometric-modulo sequence (T1GM sequence) with coefficient c

$$(g_1, g_2, ..., g_n, ...)$$

where $g_n = ca^n \mod m$, and

$$m = egin{cases} p^{ ext{p-power}}, & ext{if double is False} \ 2p^{ ext{p-power}}, & ext{if double is True'} \end{cases} p ext{ is a prime}$$

and *a* is the primitive root.

For example,

```
rad = 1000
c0 = 1
c0 = integer_num_2_vec(c0, rad)
a0 = 5
a0 = integer_num_2_vec(a0, rad)
p0 = 23
p0 = integer_num_2_vec(p0, rad)
p_power0 = 1
p_power0 = integer_num_2_vec(p_power0, rad)
condition = integer t1gm seq primitive root condition(c0,
                                                            р0,
                                                            p_power0,
                                                            rad)
g = 18
g = integer_num_2_vec(g, rad)
n = integer_t1gm_seq_index(x = g,
                              t1pm_seq_pr_list = condition,
                              radix = rad
print(n)
1 12
```

8. Functions of Power-Modulo Sequence

8.1. integer_pm_seq_complete_root_condition

```
integer_pm_seq_complete_root_condition = function(c, b, p_list,
radix, inverse = TRUE)
```

The function to check whether the integers c, b, m can construct a power-modulo sequence (T1GM sequence) with coefficient c

$$(p_1, p_2, ..., p_n, ...)$$

where $p_n = cn^b \mod m$, and

$$m = \prod q_i$$
 , where q_i are the primes from p_vec

and b is the complete root.

For example,

```
rad = 1000
c0 = 1
c0 = integer num 2 vec(c0, rad)
b0 = 5
b0 = integer num 2 vec(b0, rad)
p0 = 37
p0 = integer num 2 vec(p0, rad)
p1 = 23
p1 = integer num 2 vec(p1, rad)
p list = list(p0, p1)
condition = integer_pm_seq_complete_root_condition(c = c0,
                                                      b = b0,
                                                      p list =
p list,
                                                      radix = rad,
                                                      inverse = TRUE)
print(condition)
"pm seq complete root"
$c
1 1
$b
1 5
$m
1 851
$m prime
$m_prime[[1]]
1 23
$m_prime[[2]]
\frac{1}{37}
$phi m
1 792
$phi_phi_m
1 240
$mod inverse c
1 1
$mod inverse b
1 \ 317
```

8.2. integer_pm_seq_convert

```
integer_pm_seq_convert = function(x, pm_seq_cr_list, radix)
```

The function to convert from x to p_x in the power-modulo sequence (PM sequence) with coefficient c

$$(p_1, p_2, \ldots, p_n, \ldots)$$

where $p_n = cn^b \mod m$, and

$$m = \prod q_i$$
, where q_i are the primes from p_vec

and b is the complete root.

For example,

```
rad = 1000
c0 = 1
c0 = integer_num_2_vec(c0, rad)
b0 = integer num 2 vec(b0, rad)
p0 = 37
p0 = integer num 2 vec(p0, rad)
p1 = 23
p1 = integer num 2 vec(p1, rad)
p list = list(p0, p1)
condition = integer pm seq complete root condition(c = c0,
                                                    b = b0,
                                                    p list =
p list,
                                                    radix = rad,
                                                     inverse = TRUE)
n = 18
n = integer num 2 vec(n, rad)
pn = integer_pm_seq_convert(x = n,
                            pm seq cr list = condition,
                            radix = rad)
print(pn)
1 348
```

where 5 is a complete root of PM sequence modulo $23 \times 37 = 851$, and

$$18^5 \mod 851 = 345$$

8.3. integer_pm_seq_index

```
integer_pm_seq_index = function(x, pm_seq_cr_list, radix)
```

The function to find the index of x in the power-modulo sequence (PM sequence) with coefficient c

$$(p_1, p_2, ..., p_n, ...)$$

where $p_n = cn^b \mod m$, and

$$m = \prod q_i$$
 , where q_i are the primes from p_vec

and b is the complete root.

For example,

```
rad = 1000
c0 = 1
c0 = integer_num_2_vec(c0, rad)
b0 = integer_num_2_vec(b0, rad)
p0 = 37
p0 = integer_num_2_vec(p0, rad)
p1 = 23
p1 = integer num 2 vec(p1, rad)
p list = list(p0, p1)
condition = integer pm seq complete root condition(c = c0,
                                                    b = b0,
                                                    p list =
p list,
                                                    radix = rad,
                                                    inverse = TRUE)
p = 348
p = integer num 2 vec(p, rad)
n = integer pm seq index(x = p,
                         pm seq cr list = condition,
                         radix = rad)
print(n)
1 18
```