

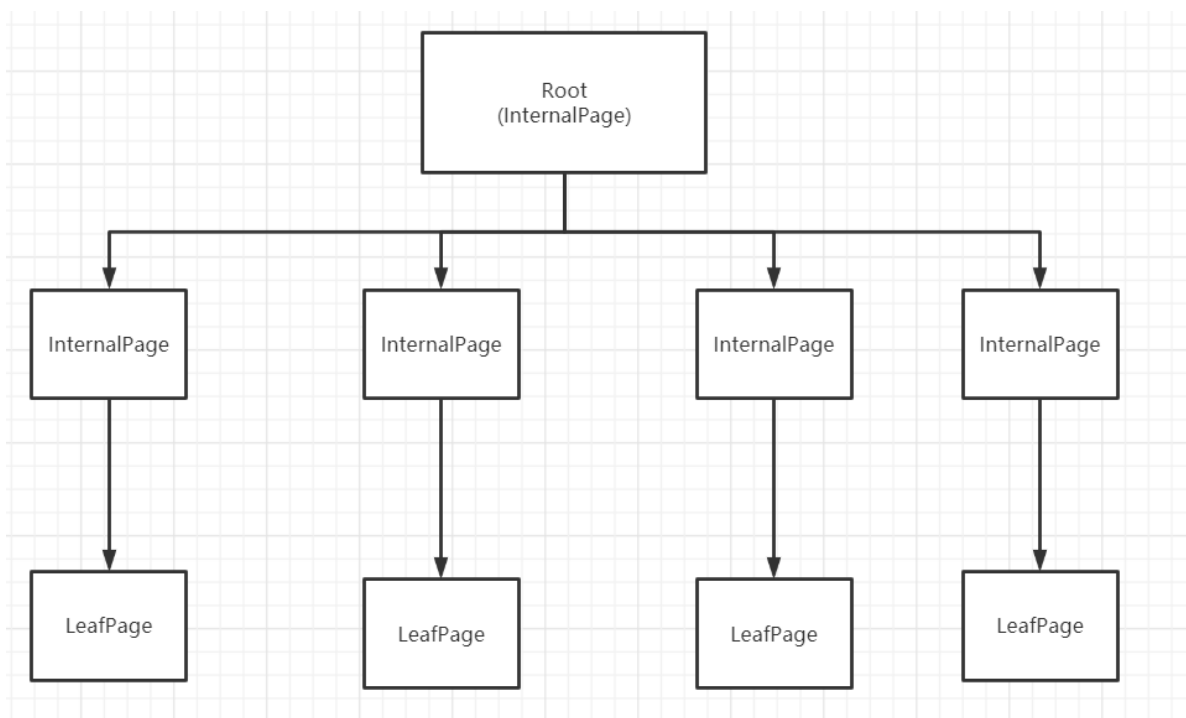
INDEX MANAGER

1. 实验概述

Index Manager 负责数据表索引的实现和管理，包括：索引的创建和删除，索引键的等值查找，索引键的范围查找（返回对应的迭代器），以及插入和删除键值等操作，并对外提供相应的接口。

由于通过堆表遍历来进行查找记录效率过于低下，因此本实验实现了一个基于磁盘的B+树动态索引结构。

2. 实验总体框架



可以看到需要实现的B+树的结构，由于内部节点和叶节点的结构不同，因此在实现B+树需要分别实现 `BPlusTreePage` 和 `BPlusInternalPage`，最后根据B+树的操作分别调用数据页中提供的接口函数。

2. B+树数据页

2.1 BPlusTreePage

由于 `LeafPage` 和 `InternalPage` 均是继承自 `BplusTreePage`，因此需要先实现 `BPlusTreePage`

- 数据结构

- 1 • `page_type_`: 标记数据页是中间结点还是叶子结点;
- 2 • `lsn_`: 数据页的日志序列号，目前不会用到，如果之后感兴趣做Crash Recovery相关的内容需要用到;
- 3 • `size_`: 当前结点中存储Key-Value键值对的数量;
- 4 • `max_size_`: 当前结点最多能够容纳Key-Value键值对的数量;
- 5 • `parent_page_id_`: 父结点对应数据页的`page_id`;
- 6 • `page_id_`: 当前结点对应数据页的`page_id`。

2.2 BPlusTreeLeafPage

- 数据结构

```
1  /*
2  * Leaf page format (keys are stored in order):
3  * -----
4  * | HEADER | KEY(1) + RID(1) | KEY(2) + RID(2) | ... | KEY(n) + RID(n)
5  * -----
6  *
7  * Header format (size in byte, 24 bytes in total):
8  * -----
9  * | PageType (4) | CurrentSize (4) | MaxSize (4) | ParentPageId (4) |
10 * -----
11 *
12 * | PageId (4) | NextPageId (4)
13 * -----
14 */
```

- 函数

下面我将对关键函数进行详细说明

Insert相关函数

- `BPlusTreeLeafPage::int Insert(const KeyType &key, const valueType &value, const KeyComparator &comparator);`

设计思路:

1. 在相应的LeafPage插入记录, 更新LeafPage的 `Size`
2. 插入完成后, 返回 `Size`, 方便上层判断是否需要分裂。

代码:

```
1  INDEX_TEMPLATE_ARGUMENTS
2  int B_PLUS_TREE_LEAF_PAGE_TYPE::Insert(const KeyType &key, const
3  valueType &value, const KeyComparator &comparator) {
4      int index = -1;
5      if (this->GetSize() + 1 <= this->GetMaxSize()) {
6          for (int i = 0; i < this->GetSize(); i++) {
7              // Find the Position which the key will insert into.
8              if (comparator(key, this->array_[i].first) < 0) {
9                  index = i;
10                 break;
11             }
12         }
13         // NewKey &value should insert into end of the NewNode
14         if (index == -1) {
15             index = this->GetSize();
16         }
17     }
18     return index;
19 }
```

```

15     if (this->GetSize() < this->GetMaxSize()) this->array_[index]
    = {key, value};
16
17     this->IncreaseSize(1);
18     /*     for (int i = 0; i < this->GetSize(); i++) {
19         std::cout << this->array_[i].first << endl;
20     }*/
21     return this->GetSize();
22 }
23 // NewKey& Value should insert into middle of the NewNode
24 else {
25     // Copy From the End to First
26     for (int i = this->GetSize(); i > index; i--) {
27         this->array_[i] = this->array_[i - 1];
28     }
29     // Insert the NewKey&Value into Right Position
30     if (this->GetSize() < this->GetMaxSize()) this->array_[index]
    = {key, value};
31     this->IncreaseSize(1);
32     return this->GetSize();
33 }
34 } else {
35     return this->GetSize()+1;
36 }
37
38 }

```

- o `void MoveHalfTo(BPlusTreeLeafPage *recipient, BufferPoolManager *bufferpoolManager);`

设计思路:

在上述 Insert 操作之后, 节点个数大于临界值, 需要进行 split

- 将此页一半的Key移动到接收页中
- 更新相邻节点的页号

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_LEAF_PAGE_TYPE::MoveHalfTo(BPlusTreeLeafPage
    *recipient, BufferPoolManager* bufferpoolManager) {
3
4      int DeleteSize = (this->GetMinSize());
5      recipient->CopyNFrom(&this->array_[(this->GetSize()-this-
    >GetMinSize())], DeleteSize); // Recipient Increase Size Here
6      if (this->GetNextPageId() != INVALID_PAGE_ID) {
7          recipient->SetNextPageId(this->GetNextPageId());
8      }
9      this->SetNextPageId(recipient->GetPageId());
10
11     //Decrease Size
12     this->IncreasesSize(-recipient->GetSize());
13
14
15 }

```

- `void CopyNFrom(MappingType *items, int size);`

设计思路:

此函数是在MoveHalfTo函数的子函数，主要完成，复制的功能。

- 将items[0]--items[size]的Element复制到此页中

代码:

```
1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_LEAF_PAGE_TYPE::CopyNFrom(MappingType *items, int
   size) {
3
4
5      // Copy Entries into This Page
6      for (int i = 0; i < size; i++) {
7
8          this->array_[i].first = items[i].first;
9          this->array_[i].second = items[i].second;
10
11     }
12     // Increment the Size
13     this->IncreasesSize(size);
14
15 }
```

Remove相关函数

- `int RemoveAndDeleteRecord(const KeyType &key, const KeyComparator &comparator);`

设计思路:

- 首先在LeafPage进行查找相应的想要删除的 key
- 如果存在，进行删除，不存在，返回
- 返回值说明：返回 Size 以方便上层，进行判断，是否需要从兄弟节点 Merge 或者 Redistribute。

代码:

```
1  INDEX_TEMPLATE_ARGUMENTS
2  int B_PLUS_TREE_LEAF_PAGE_TYPE::RemoveAndDeleteRecord(const KeyType
   &key, const KeyComparator &comparator) {
3      bool state = false;
4
5      for (int i = 0; i < this->GetSize(); i++) {
6          if (comparator(key, this->array_[i].first) == 0) {
7              state = true;
8              int index = i;
9              for (int i = index + 1; i < this->GetSize(); i++) {
10                 this->array_[i - 1].first = this->array_[i].first;
11                 this->array_[i - 1].second = this->array_[i].second;
12             }
13         }
14     }
15 }
```

```

13         this->IncreaseSize(-1);
14         break;
15     }
16 }
17
18 if (state == false) {
19     return this->GetSize();
20 }
21 return this->GetSize();
22 }

```

- `void MoveAllTo(BPlusTreeLeafPage *recipient);`

设计思路:

上述 RemoveAndDelete 函数可能出现 Merge, 此函数就是用来 Merge 功能的函数

- 将所有的 key, Value 全部复制到接受页中

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_LEAF_PAGE_TYPE::MoveAllTo(BPlusTreeLeafPage *recipient
3  ) {
4      //Copy the Instance into the recipient Page
5      for (int i = 0; i < this->GetSize(); i++) {
6          recipient->CopyLastFrom(this->array_[i]); // Add Size Here
7      }
8      this->IncreaseSize(-this->GetSize()); //
9      //Decrease Size of this Page
10     //Set the Next Page id.
11     recipient->SetNextPageId(this->GetNextPageId());
12 }

```

- `void MoveFirstToEndOf(BPlusTreeLeafPage *recipient);`

设计思路:

上述 RemoveAndDelete 函数可能出现 Redistribute, 此函数就是用来 Redistribute 功能的函数

- 将此页的 第一个 key & value 复制到 recipient

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_LEAF_PAGE_TYPE::MoveFirstToEndOf(BPlusTreeLeafPage
   *recipient) {
3      recipient->CopyLastFrom(this->array_[0]); //Add Size Here
4      //Remove the First Key
5      for (int i = 0; i < this->GetSize()-1; i++) {
6          this->array_[i] = this->array_[i + 1];
7      }
8      this->IncreasesSize(-1);
9  }
10

```

- `void MoveLastToFrontOf(BPlusTreeLeafPage *recipient);`

设计思路:

上述 `RemoveAndDelete` 函数可能出现 `Redistribute` , 此函数就是用来 `Redistribute` 功能的函数

- 将此页的 末尾的 `key & value` 复制到 `recipient`

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_LEAF_PAGE_TYPE::MoveLastToFrontOf(BPlusTreeLeafPage
   *recipient) {
3
4      recipient->CopyFirstFrom(this->array_[this->GetSize() - 1]);
5      this->IncreasesSize(-1);
6  }
7

```

2.3 BPlusTreeInternalPage

- 数据结构

```

1  /*
2   * Internal page format (keys are stored in increasing order):
3   * -----
4   * | HEADER | KEY(1)+PAGE_ID(1) | KEY(2)+PAGE_ID(2) | ... |
   KEY(n)+PAGE_ID(n) |
5   * -----
6   */

```

- 函数说明

Insert相关函数

- `void PopulateNewRoot(const ValueType &old_value, const KeyType &new_key, const ValueType &new_value);`

设计思路:

此函数应用在如果Insert一直进行分裂, 并且一直分裂到根节点, 需要产生新的Root。

- 将新产生的键值对插入RootNode

代码:

```
1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_INTERNAL_PAGE_TYPE::PopulateNewRoot(const
   valueType &old_value, const KeyType &new_key,
3                                     const
   valueType &new_value)
4  {
5
6      //old_value means old root-page id
7      this->array_[0].second = old_value;
8      SetkeyAt(1, new_key);
9      this->array_[1].second = new_value;
10     //Increase Size by two
11     this->Increasesize(2);
12
13 }
```

- `int InsertNodeAfter(const ValueType &old_value, const KeyType &new_key, const ValueType &new_value);`

设计思路:

- 将键值对插入到 oldvalue 之后。
- 返回Size, 来判断是否需要进行 split

代码:

```
1  INDEX_TEMPLATE_ARGUMENTS
2  int B_PLUS_TREE_INTERNAL_PAGE_TYPE::InsertNodeAfter(const ValueType
   &old_value, const KeyType &new_key,
3                                     const ValueType
   &new_value) {
4      //Get Index of the old_value
5      int index = valueIndex(old_value);
6      //If the index do not overflow
7      if (index + 1 < this->GetMaxSize()) {
8          for (int i = this->GetSize(); i > index+1; i--) {
9              if (i - 1 > 0) {
10                 this->array_[i] = this->array_[i - 1];
11             } else {
12                 this->array_[i].second = this->array_[i - 1].second;
13             }
14         }
15         this->SetkeyAt(index + 1, new_key);
```

```

16     array_[index + 1].second = new_value;
17     this->IncreasesSize(1);
18 } else {
19     throw "B_PLUS_TREE_INTERNAL_PAGE_TYPE::InsertNodeAfter-
OverFlow" ;
20     return this->GetSize() + 1;
21 }
22
23 return this->GetSize();
24 }

```

- `void MoveHalfTo(BPlusTreeInternalPage *recipient, BufferPoolManager *buffer_pool_manager);`

设计思路:

- 将一半的键值对复制到接受页

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void
   B_PLUS_TREE_INTERNAL_PAGE_TYPE::MoveHalfTo(BPlusTreeInternalPage
*recipient,
3                                     BufferPoolManager
*buffer_pool_manager) {
4
5      // Copy into the recipient Page
6      recipient->CopyNFrom(&this->array_[this->GetSize()-this-
>GetMinSize()],this->GetMinSize(),buffer_pool_manager);
7      // Remove From the Current Page
8      this->IncreasesSize(-recipient->GetSize());
9
10     //buffer_pool_manager->UnpinPage(this->GetPageId(),true);
11
12
13 }

```

Remove 相关函数

- `void Remove(int index);`

设计思路:

- 将index对应的键值对进行删除
- 更新Size

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_INTERNAL_PAGE_TYPE::Remove(int index) {
3
4      //Delete the first Child
5      if (index == 0&&this->GetSize()>=2) {
6          //Remove from the first value

```



```

7         for (int i = 0; i < this->GetSize(); i++) {
8             if (i == 0) {
9                 this->array_[i].second = this->array_[i + 1].second;
10            } else {
11                this->array_[i] = this->array_[i + 1];
12            }
13        }
14        this->IncreasesSize(-1);
15    }
16
17    if (this->GetSize() == 0) {
18        std::cerr << "Can not Remove" << endl;
19    } else {
20        //Move Forward the array_
21        if (this->GetSize() == 2) {
22            // it means it only has one child and one pair key& value
23            // it delete the last element, so we need to delete the
last pair,
24            // it does not need to remove
25
26            this->IncreasesSize(-1);
27            return;
28        } else {
29            for (int i = index + 1; i < this->GetSize(); i++) {
30                this->array_[i - 1].first = this->array_[i].first;
31                this->array_[i - 1].second = this->array_[i].second;
32            }
33        }
34
35    }
36
37    }
38    this->IncreasesSize(-1);
39 }

```

- `void MoveAllTo(BPlusTreeInternalPage *recipient, const KeyType &middle_key, BufferPoolManager *buffer_pool_manager);`

设计思路:

- 将此页的所有key&Value和Middle_key全部复制到接受页中

代码:

```

1 INDEX_TEMPLATE_ARGUMENTS
2 void B_PLUS_TREE_INTERNAL_PAGE_TYPE::MoveAllTo(BPlusTreeInternalPage
  *recipient, const KeyType &middle_key,
3                                     BufferPoolManager
  *buffer_pool_manager) {
4     MappingType NewPair = {middle_key, this->array_[0].second};
5     for (int i = 0; i < this->GetSize(); i++) {
6         if (i != 0)
7             recipient->CopyLastFrom(this->array_[i], buffer_pool_manager);
8         else
9             recipient->CopyLastFrom(NewPair, buffer_pool_manager);
10    }
11    //Remove the Key from this Page
12    this->IncreasesSize(-this->GetSize());
13 }

```

- `void MoveFirstToEndOf(BPlusTreeInternalPage *recipient, const KeyType &middle_key, BufferPoolManager *buffer_pool_manager);`

设计思路:

上述 `RemoveAndDelete` 函数可能出现 `Redistribute`, 此函数就是用来 `Redistribute` 功能的函数

- 将此页的 第一个 `key & value` 复制到 `recipient`

代码:

```

1 INDEX_TEMPLATE_ARGUMENTS
2 void B_PLUS_TREE_INTERNAL_PAGE_TYPE::MoveFirstToEndOf(BPlusTreeInternalPage
  *recipient, const KeyType &middle_key,
3                                     BufferPoolManager
  *buffer_pool_manager) {
4     MappingType NewPair = {middle_key, this->array_[0].second};
5     recipient->CopyLastFrom(NewPair, buffer_pool_manager); //Add Size Here
6     //Remove the First Key
7     // If we need to Update the Middle_key in the Parent node
8     // We just Get from the Index ==0
9     for (int i = 0; i < this->GetSize()-1; i++) {
10        this->array_[i] = this->array_[i + 1];
11    }
12    this->IncreasesSize(-1);
13
14
15 }

```

- `void MoveLastToFrontOf(BPlusTreeInternalPage *recipient, const KeyType &middle_key, BufferPoolManager *buffer_pool_manager);`

设计思路:

上述 `RemoveAndDelete` 函数可能出现 `Redistribute`, 此函数就是用来 `Redistribute` 功能的函数

- 将此页的 末尾的 `key & value` 复制到 `recipient`

代码:

```
1  INDEX_TEMPLATE_ARGUMENTS
2  void
   B_PLUS_TREE_INTERNAL_PAGE_TYPE::MoveLastToFrontOf(BPlusTreeInternalPage
   *recipient, const KeyType &middle_key,
3                                     BufferPoolManager
   *buffer_pool_manager) {
4
5     MappingType NewPair = {middle_key, this->array_[this-
   >GetSize()-1].second};
6     recipient->CopyFirstFrom(NewPair, buffer_pool_manager); //AddSize Here
7     //If we need to update the Parent's middle_key just get from the
   index==GetSize
8     this->IncreaseSize(-1);
9
10 }
```

- `void ResetParent(const page_id_t &old_node, const page_id_t &new_node, BufferPoolManager *buffer_pool_manager);`

设计思路:

将此页的 末尾的 `key & value` 复制到 `recipient`

代码:

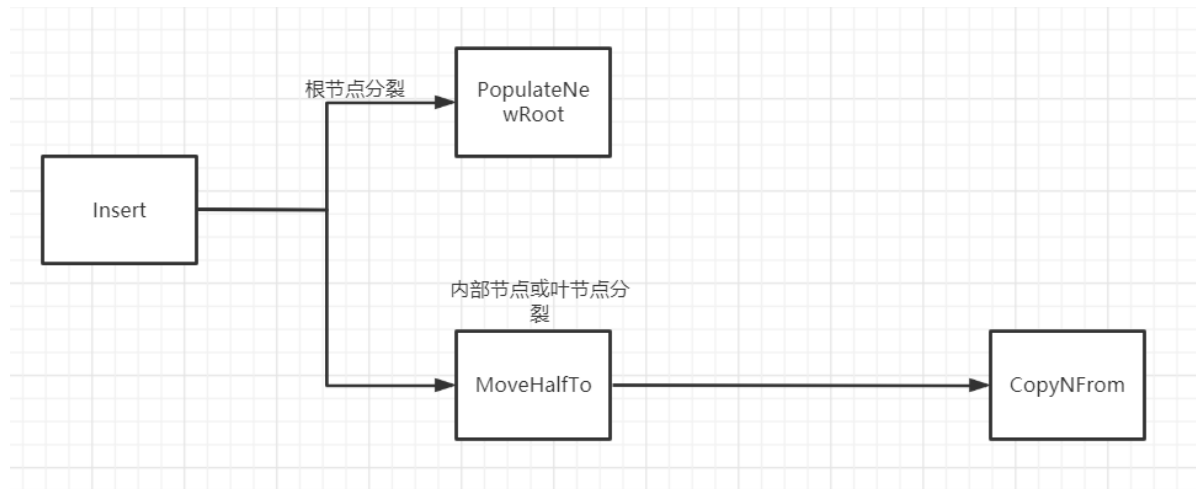
```
1  INDEX_TEMPLATE_ARGUMENTS
2  void B_PLUS_TREE_INTERNAL_PAGE_TYPE::ResetParent(const page_id_t &old_node,
   const page_id_t &new_node, BufferPoolManager* buffer_pool_manager_) {
3     // Read the old_page and new_page
4     BPlusTreePage *old_page = reinterpret_cast<BPlusTreePage *>
   (buffer_pool_manager_->FetchPage(old_node));
5     BPlusTreePage *new_page = reinterpret_cast<BPlusTreePage *>
   (buffer_pool_manager_->FetchPage(new_node));
6     old_page->SetParentPageId(this->GetPageId());
7     new_page->SetParentPageId(this->GetPageId());
8     buffer_pool_manager_->UnpinPage(old_node, true);
9     buffer_pool_manager_->UnpinPage(new_node, true);
10 }
```

3. B+树索引

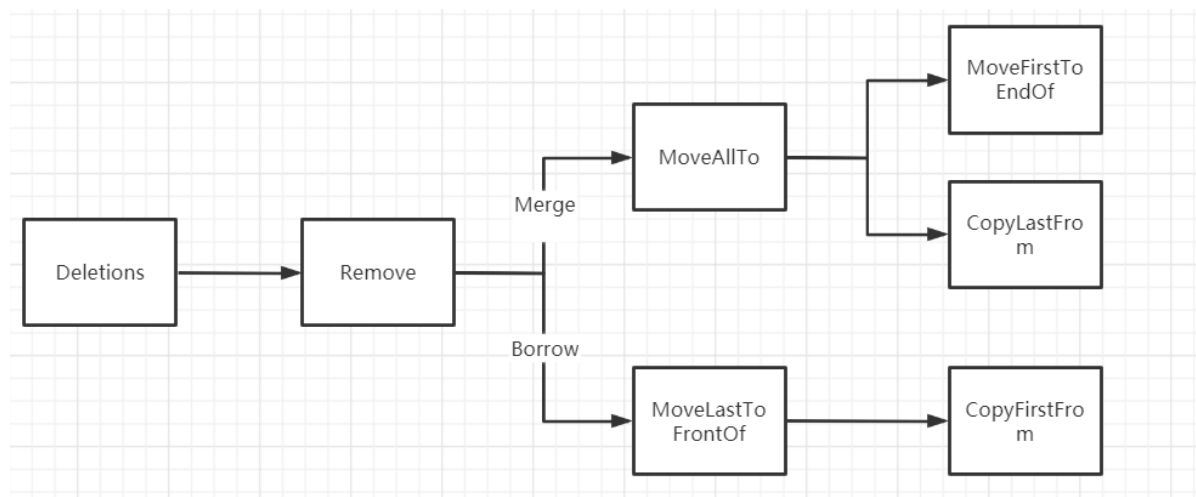
3.1 总体框架

由于B+树索引主要就是 `Insert` 和 `Remove` 两个操作，下面图片将说明这两个操作和上述两个数据页中的函数之间的关系。

1.Insert



2.Remove



3.2 函数说明

- `Insert`

伪代码:

```
1  step1:若为空树，创建一个叶子结点，然后将记录插入其中，此时这个叶子结点也是根结点，插入操作结束。
2
3  step2:
4      针对叶子类型结点：根据key值找到叶子结点，
5      if(插入后节点的个数<=n-1)
6          插入结束
7      else
8          //split
9          divide into (1,2 .....n/2) and ((n/2)+1,.....n-1)
10         将(n/2)+1节点推到父节点
11         当前节点指向父节点
12         //Insert Into Parent
13         //索引类型节点
```

```

14     while(当前的个数>=n-1)
15         //split
16         分成(m-1)/2,m-(m-1)/2两组
17         将当前节点指向父节点

```

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  bool BPLUSTREE_TYPE::Insert(const KeyType &key, const ValueType &value,
Transaction *transaction) {
3      bool state = false;
4      //Empty Tree
5      if (this->IsEmpty()) {
6          //std::cout << "Insert::StartNewTree" << endl;
7          this->StartNewTree(key, value);
8          state = true;
9      } else {
10         //std::cout << "Insert::InsertIntoLeaf" << endl;
11         state=InsertIntoLeaf(key, value, transaction);
12     }
13     return state;
14 }

```

Split相关函数

- INDEX_TEMPLATE_ARGUMENTS
template<typename N>
N *BPLUSTREE_TYPE::Split(N *node)

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  template<typename N>
3  N *BPLUSTREE_TYPE::Split(N *node) {
4      page_id_t NewId = INVALID_PAGE_ID;
5      auto *page = buffer_pool_manager->NewPage(NewId);
6      if (page != nullptr) {
7          N *NewNode = reinterpret_cast<N *>(page->GetData());
8          //Init
9          NewNode->Init(NewId, INVALID_PAGE_ID,node->GetMaxSize());
10
11
12         node->MoveHalfTo(NewNode,buffer_pool_manager_);
13
14         //Set the sibling point to the Same Parent
15         NewNode->SetParentPageId(node->GetParentPageId());
16         buffer_pool_manager->UnpinPage(NewId, true);
17
18         return NewNode;
19     } else {
20         buffer_pool_manager->UnpinPage(NewId, false);
21         std::cerr << "BPLUSTREE_TYPE::InsertIntoParent---Can not Allocate
Memory AnyMore" << endl;
22         return nullptr;
23     }

```

25

InsertIntoParent相关函数

- INDEX_TEMPLATE_ARGUMENTS void

```
BPLUSTREE_TYPE::InsertIntoParent(BPlusTreePage *old_node, const KeyType
&key, BPlusTreePage *new_node, Transaction *transaction)
```

代码：

```

1 INDEX_TEMPLATE_ARGUMENTS
2 void BPLUSTREE_TYPE::InsertIntoParent(BPlusTreePage *old_node,
3   const KeyType &key, BPlusTreePage *new_node,
4   Transaction *transaction) {
5     KeyType NewKey = key;
6     while (1) {
7       //old_node is root
8       if (old_node->GetPageId() == this->root_page_id_) {
9         page_id_t NewId = INVALID_PAGE_ID;
10        auto *page = buffer_pool_manager->NewPage(NewId);
11        if (page != nullptr) {
12          auto *node = reinterpret_cast<InternalPage *>(page->
13            >GetData());
14          node->Init(NewId, INVALID_PAGE_ID, this->
15            >internal_max_size_);
16          //Generate the New Root
17          node->PopulateNewRoot(old_node->GetPageId(), NewKey,
18            new_node->GetPageId());
19          //Reset Parent
20          node->ResetParent(old_node->GetPageId(), new_node->
21            >GetPageId(), buffer_pool_manager_);
22
23          //Update the New Root
24          this->root_page_id_ = NewId;
25          this->UpdateRootPageId(false);
26          buffer_pool_manager->UnpinPage(NewId, true);
27          //std::cout << "BPLUSTREE_TYPE::InsertIntoParent-----286"
28          << endl;
29          break;
30        }
31      }
32      else {
33        buffer_pool_manager->UnpinPage(NewId, false);
34        std::cerr << "BPLUSTREE_TYPE::InsertIntoParent---Can not
35          Allocate Memory AnyMore" << endl;
36      }
37    }
38  }
39  else
40  {
41    //Percolate Up
42    //Get Parent Page From the BufferPoolManager
43    page_id_t Id = old_node->GetParentPageId();
44    auto *page = buffer_pool_manager->FetchPage(Id);
45    if (page != nullptr)
46    {

```

```

38         auto * ParentNode = reinterpret_cast<InternalPage *>
(page->GetData());
39         //Insert NewKey into the Parent Node
40         /*for (int i = 0; i < ParentNode->GetSize(); i++) cout
<< ParentNode->array_[i].first << " ";
41         cout << endl;*/
42         int size = ParentNode->InsertNodeAfter(old_node->
GetPageId(), NewKey, new_node->GetPageId());
43         /*for (int i = 0; i < ParentNode->GetSize(); i++) cout
<< ParentNode->array_[i].first << " ";
44         cout << endl;*/
45         // if the Parent Node is not OverFlow
46         if (size < this->internal_max_size_) {
47             buffer_pool_manager->UnpinPage(Id, true);
48             //std::cout << "BPLUSTREE_TYPE::InsertIntoParent-----
-311" << endl;
49             break;
50         }
51         else {
52             //If the Parent Node is Full
53             KeyType middle_key = ParentNode->KeyAt(ParentNode->
GetSize()-ParentNode->GetMinSize());
54             InternalPage *Sibling = this->Split(ParentNode);
55             old_node = ParentNode;
56             NewKey = middle_key;
57             new_node = Sibling;
58             buffer_pool_manager->UnpinPage(Id, true);
59             //std::cout << "BPLUSTREE_TYPE::InsertIntoParent-----
-321" << endl;
60             continue;
61         }
62     }
63     else
64     {
65         buffer_pool_manager->UnpinPage(Id, false);
66         //std::cerr << "BPLUSTREE_TYPE::InsertIntoParent---2Can
not Allocate Memory AnyMore" << endl;
67     }
68 }
69 }
70
71 }

```

- Remove

伪代码:

```

1
2  step1:删除叶子结点中对应的key。删除后若结点的key的个数大于等于Math.ceil(m-1)/2 -
1, 删除操作结束, 否则执行第2步。
3
4  step2:
5      if(兄弟结点key有富余 (大于Math.ceil(m-1)/2 - 1)),
6          向兄弟结点借一个记录

```

```

7      同时用借到的key替换父结（指当前结点和兄弟结点共同的父结点）点中的key，删除
      结束。
8      else
9          if(兄弟结点中没有富余的key)
10         则当前结点和兄弟结点合并成一个新的叶子结点，并删除父结点中的key
11         （父结点中的这个key两边的孩子指针就变成了一个指针，正好指向这个新的叶子结
      点）
12         将当前结点指向父结点（必为索引结点）
13     else
14         while(索引结点的key的个数<Math.ceil(m-1)/2 - 1)
15             if(兄弟结点有富余)
16                 父结点key下移，兄弟结点key上移
17                 break
18             else
19                 当前结点和兄弟结点及父结点下移key合并成一个新的结点。
20                 将当前结点指向父结点

```

相关函数:

- INDEX_TEMPLATE_ARGUMENTS

```
void BPLUSTREE_TYPE::Remove(const KeyType &key, Transaction *transaction)
```

代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  void BPLUSTREE_TYPE::Remove(const KeyType &key, Transaction
   *transaction) {
3      if (this->IsEmpty()) return;
4      auto page = FindLeafPage(key, false);
5      auto node = reinterpret_cast<BPlusTreePage*> (page->GetData());
6      page_id_t FirstLeafId = page->GetPageId();
7
8
9
10     if (node->IsRootPage()) {
11         LeafPage* Root = reinterpret_cast<LeafPage *> (node);
12         int size=Root->RemoveAndDeleteRecord(key, comparator_);
13         if (size == 0) {
14             if (this->AdjustRoot(node)) {
15                 buffer_pool_manager_->UnpinPage(node->GetPageId(),true);
16
17                 bool state=buffer_pool_manager_->DeletePage(node->
   >GetPageId());
18                 if (state == false) {
19                     throw "fuck";
20                 }
21             }
22         }
23
24     else {
25         auto Leaf = reinterpret_cast<LeafPage *>(page->GetData());
26         int size = Leaf->RemoveAndDeleteRecord(key, comparator_);
27         //After the Deletetion the Leaf size >= MinSize
28         if (size >= (Leaf->GetMinSize())) {
29             buffer_pool_manager_->UnpinPage(FirstLeafId, true);

```



```

30
31     return;
32 }
33
34 else {
35     //After the Deletion the Leaf size < MinSize
36     //Merge or Borrow
37     ///
38
39     if (this->CoalesceOrRedistribute(&Leaf, transaction) ==
false) {
40         buffer_pool_manager_->UnpinPage(FirstLeafId, true);
41
42         return;
43     }
44     else {
45         // We need to Adjust Percolate Up
46
47         auto ParentPage = buffer_pool_manager_->FetchPage(Leaf-
>GetParentPageId());
48         page_id_t ParentId = ParentPage->GetPageId();
49         InternalPage *node = reinterpret_cast<InternalPage*>
(ParentPage->GetData());
50         buffer_pool_manager_->UnpinPage(Leaf->GetPageId(),
true);
51         bool state=buffer_pool_manager_->DeletePage(Leaf-
>GetPageId());
52         if (state == false) {
53             throw "fuck";
54         }
55         InternalPage *Parent = nullptr;
56
57
58
59
60         while (1) {
61             if (this->CoalesceOrRedistribute(&node, transaction)
== false) {
62                 buffer_pool_manager_->UnpinPage(FirstLeafId, true);
63                 buffer_pool_manager_->UnpinPage(ParentId,true);
64
65                 break;
66             }
67             else {
68
69                 Parent = reinterpret_cast<InternalPage *>
(buffer_pool_manager_->FetchPage(node->GetParentPageId())-
>GetData());
70                 buffer_pool_manager_->UnpinPage(ParentId, true);
71                 buffer_pool_manager_->UnpinPage(node->GetPageId(),
true);
72                 bool state = buffer_pool_manager_->DeletePage(node-
>GetPageId());
73                 ParentId = Parent->GetPageId();
74                 if (state == false) {

```

```

75         throw "fuck";
76     }
77     node = Parent;
78 }
79 }
80 }
81
82 }
83 }
84     buffer_pool_manager_>UnpinPage(node->GetPageId(), true);
85
86
87
88 }

```

- INDEX_TEMPLATE_ARGUMENTS

```
template<typename N>
```

```
bool BPLUSTREE_TYPE::CoalesceOrRedistribute(N **node, Transaction
*transaction)
```

- 代码:

```

1  INDEX_TEMPLATE_ARGUMENTS
2  template<typename N>
3  bool BPLUSTREE_TYPE::CoalesceOrRedistribute(N **node, Transaction
   *transaction)
4  {
5
6      bool state = false;
7      if (this->IsEmpty() == true) return false;
8      InternalPage *ParentNode = nullptr;
9      // Root Page
10     if ((* node)->IsRootPage()) {
11         if (( * node)->GetSize() == 1) {
12             state=this->AdjustRoot(*node);
13             if (state) {
14
15                 page_id_t PageId = (*node)->GetPageId();
16                 buffer_pool_manager_>UnpinPage(PageId, true);
17
18                 bool state=buffer_pool_manager_>DeletePage(PageId);
19                 if (state == false) {
20                     throw "fuck";
21                 }
22             }
23         }
24         return false;
25     }
26
27     //Get the Parent Page
28     page_id_t ParentPageId = (*node)->GetParentPageId();
29     auto Page=buffer_pool_manager_>FetchPage(ParentPageId);

```

```

30     ParentNode = reinterpret_cast<InternalPage *>(Page-
>GetData());
31     //Get the child node index in the ParentNode
32     int index = ParentNode->ValueIndex((*node)->GetPageId());
33
34     //If the Node is LeafNode
35     if (( * node)->IsLeafPage()) {
36         // If the Node is the right Most Element
37         if (index == ParentNode->GetSize() - 1) {
38             // node is last child of the Parent Node
39             int siblingIndex = index - 1;
40             page_id_t Sibling_Page_Id = ParentNode-
>ValueAt(SiblingIndex);
41             // Merge or Borrow from the Left Page
42             auto SiblingPage = buffer_pool_manager_-
>FetchPage(Sibling_Page_Id);
43             LeafPage *SiblingNode = reinterpret_cast<LeafPage *>
(SiblingPage->GetData());
44             LeafPage *Node = reinterpret_cast<LeafPage *>(*node);
45             //case 1----Borrow From the Sibling Node ----Test---Not
Check
46             if (SiblingNode->GetSize() + Node->GetSize() > Node-
>GetMaxSize()) {
47                 // Move the Sibling Last Pair into the This Node
48                 this->Redistribute(SiblingNode, Node, 1);
49                 int index = ParentNode->ValueIndex(Node->GetPageId());
50                 ParentNode->SetKeyAt(index, Node->KeyAt(0));
51                 state = false;
52             }
53             //case 2---- Merge with the Sibling Node ----Test---OK
54             else {
55                 state = this->Coalesce(&SiblingNode, &Node,
&ParentNode, index, transaction,true);
56             }
57             buffer_pool_manager_->UnpinPage(Sibling_Page_Id, true);
58         }
59         // if the node is not right most Node
60         else {
61             page_id_t Sibling_Page_Id = ParentNode->ValueAt(index +
1);
62             auto SiblingPage = buffer_pool_manager_-
>FetchPage(Sibling_Page_Id);
63             LeafPage *SiblingNode = reinterpret_cast<LeafPage *>
(SiblingPage->GetData());
64             LeafPage *Node = reinterpret_cast<LeafPage *>(*node);
65             //case 1--- Borrow From the Sibling Node----- Test----
Not Check
66             if (SiblingNode->GetSize() + Node->GetSize() > Node-
>GetMaxSize()) {
67                 // Move the Redistribute First Pair into the End of this
node
68                 this->Redistribute(SiblingNode, Node, 0);
69                 // Adjust the Key in the Parent Node
70                 int index = ParentNode->ValueIndex(SiblingNode-
>GetPageId());

```

```

71         ParentNode->SetKeyAt(index, SiblingNode->KeyAt(0));
72         state = false;
73     }
74     // case 2----Merge with the Sibling Node -----Test---Ok
75     else {
76         state = this->Coalesce(&Node, &SiblingNode,
77 &ParentNode, index + 1, transaction, false);
78         *node = (reinterpret_cast<N*> (SiblingNode));
79     }
80     buffer_pool_manager->UnpinPage(Sibling_Page_Id, true);
81 }
82 buffer_pool_manager->UnpinPage(ParentPageId, true);
83
84
85 } else {
86     // If the node is Internal Node
87     // node is >= MinSize
88     if (( * node)->GetSize() >= (*node)->GetMinSize()) {
89         buffer_pool_manager->UnpinPage(ParentPageId, true);
90
91         return false;
92     }
93     // If the Node is the right Most Element
94     if (index == ParentNode->GetSize() - 1) {
95         // node is last child of the Parent Node
96         int SiblingIndex = index - 1;
97         page_id_t Sibling_Page_Id = ParentNode-
98 >ValueAt(SiblingIndex);
99         // Merge or Borrow from the Left Page
100         auto SiblingPage = buffer_pool_manager_-
101 >FetchPage(Sibling_Page_Id);
102
103         InternalPage *SiblingNode = reinterpret_cast<InternalPage
104 *>(SiblingPage->GetData());
105         InternalPage *Node = reinterpret_cast<InternalPage *>
106 (*node);
107
108         // case 1----Borrow From the Sibling Node ---- Test Not
109 Check
110         if (SiblingNode->GetSize() + Node->GetSize() > Node-
111 >GetMaxSize()) {
112             // Move the Sibling Last Pair into the This Node
113             this->Redistribute(SiblingNode, Node, 1);
114             int index = ParentNode->ValueIndex(Node->GetPageId());
115             ParentNode->SetKeyAt(index, Node->KeyAt(SiblingNode-
116 >GetSize()));
117             state = false;
118         }
119         // case 2---- Merge with the Sibling Node -----Test Not
120 Check
121         else {
122             state = this->Coalesce(&SiblingNode, &Node, &ParentNode,
123 index, transaction, true);

```

```

116     }
117     buffer_pool_manager_>UnpinPage(Sibbling_Page_Id, true);
118 }
119 // if the node is not right most Node
120 else
121 {
122     page_id_t Sibbling_Page_Id = ParentNode->ValueAt(index +
123 1);
124     auto SibblingPage = buffer_pool_manager_
125 >FetchPage(Sibbling_Page_Id);
126     InternalPage *SibblingNode = reinterpret_cast<InternalPage
127 *>(SibblingPage->GetData());
128     InternalPage *Node = reinterpret_cast<InternalPage *>
129 (*node);
130     // case 1--- Borrow From the Sibbling Node----- Test-Not
131 Check
132     if (SibblingNode->GetSize() + Node->GetSize() > Node-
133 >GetMaxSize()) {
134         // Move the Redistribute First Pair into the End of this
135 node
136         this->Redistribute(SibblingNode, Node, 0);
137         // Adjust the Key in the Parent Node
138         int index = ParentNode->ValueIndex(SibblingNode-
139 >GetPageId());
140         ParentNode->SetKeyAt(index, SibblingNode->KeyAt(0));
141         state = false;
142     }
143     // case 2----Merge With the sibbling Node -----Test-Not
144 Check
145     else {
146         state = this->Coalesce(&Node, &SibblingNode, &ParentNode,
147 index + 1, transaction, false);
148         *node = (reinterpret_cast<N *>(SibblingNode));
149     }
150     //
151     buffer_pool_manager_>UnpinPage(Sibbling_Page_Id, true);
152 }
153
154     buffer_pool_manager_>UnpinPage(ParentPageId, true);
155
156 }
157
158     return state;
159 }

```

3.3 测试结果

- 测试BplusTree的 Insert 和 Remove

```
cjx@LAPTOP-V8K17SA0:/mnt/c/Users/25347/Desktop/Minisql-6.6/build$ ./test/b_plus_tree_test
[=====] Running 1 test from 1 test suite.
[-----] Global test environment set-up.
[-----] 1 test from BPlusTreeInsertTests
[ RUN      ] BPlusTreeInsertTests.SampleTest
[ OK       ] BPlusTreeInsertTests.SampleTest (28 ms)
[-----] 1 test from BPlusTreeInsertTests (28 ms total)

[-----] Global test environment tear-down
[=====] 1 test from 1 test suite ran. (31 ms total)
[ PASSED  ] 1 test.
```

4.BPlusTreeIndexIterator

- 成员定义

为了方便索引查询，提供迭代器，方便上层进行调用。

```
1 private:
2     // add your own private member variables here
3     BufferPoolManager *bufferPoolManager;
4     page_id_t CurrPageId;
5     int CurrLocation;
6     // if we Read the Tuple from the Leaf Page , We need to Copy the
7     Item
8     MappingType *Item = nullptr;
```

- 基本操作

- `const MappingType &operator*();`

实现逻辑:

取出叶节点的键值对

代码:

```
1 INDEX_TEMPLATE_ARGUMENTS const MappingType
2 &INDEXITERATOR_TYPE::operator*() {
3     auto page = bufferPoolManager->FetchPage(this->CurrPageId);
4     auto node = reinterpret_cast<LeafPage *>(page);
5     // Free the preview Item
6     if (this->Item != nullptr) delete this->Item;
7     this->Item = new MappingType;
8     MappingType *Pair = new (this->Item) MappingType(node-
9 >GetItem(this->CurrLocation));
10    bufferPoolManager->UnpinPage(this->CurrPageId, false);
11    return *Pair;
12 }
```

- `IndexIterator &operator++();`

实现逻辑:

完成 ++ 的Overload

```
1
2 INDEX_TEMPLATE_ARGUMENTS INDEXITERATOR_TYPE
  &INDEXITERATOR_TYPE::operator++() {
3     auto page = bufferPoolManager->FetchPage(this->CurrPageId);
4     auto node = reinterpret_cast<LeafPage *>(page);
5     int Capacity = node->GetSize();
6     // just Point to Next Pair in this Page
7     if (this->CurrLocation + 1 < Capacity) {
8         bufferPoolManager->UnpinPage(this->CurrPageId, false);
9         CurrLocation++;
10    } else {
11        page_id_t NextPage = node->GetNextPageId();
12
13        bufferPoolManager->UnpinPage(this->CurrPageId, false);
14        // It means NextPage is the Last Page
15        if (NextPage == INVALID_PAGE_ID) {
16            this->CurrPageId = INVALID_PAGE_ID;
17            this->CurrLocation = 0;
18        } else {
19            // Update Next Page
20            this->CurrPageId = NextPage;
21            // Update Next Position
22            this->CurrLocation = 0;
23        }
24    }
25    return *this;
26 }
27 }
```

- `bool operator==(const IndexIterator &itr) const;`

实现逻辑:

判断当前的迭代器，是否和待比较的迭代器相等

代码:

```
1 INDEX_TEMPLATE_ARGUMENTS
2 bool INDEXITERATOR_TYPE::operator==(const IndexIterator &itr) const {
3     if (this->CurrLocation == itr.CurrLocation && this->CurrPageId ==
4         itr.CurrPageId) {
5         return true;
6     } else
7         return false;
8 }
```

- o `bool operator!=(const IndexIterator &itr) const;`

实现逻辑:

判断当前的迭代器, 是否和待比较的迭代器不相等

代码:

```
1 INDEX_TEMPLATE_ARGUMENTS
2 bool INDEXITERATOR_TYPE::operator!=(const IndexIterator &itr) const {
3
4     return !(*this == itr);
5
6 }
```

- 测试BplusTree的 `Iterator`

```
cjx@LAPTOP-V8K17SA0:/mnt/c/Users/25347/Desktop/Minisql-6.6/build$ ./test/b_plus_tree_index_test
[=====] Running 2 tests from 1 test suite.
[-----] Global test environment set-up.
[-----] 2 tests from BPlusTreeTests
[ RUN     ] BPlusTreeTests.BPlusTreeIndexGenericKeyTest
[       OK ] BPlusTreeTests.BPlusTreeIndexGenericKeyTest (9 ms)
[ RUN     ] BPlusTreeTests.BPlusTreeIndexSimpleTest
[       OK ] BPlusTreeTests.BPlusTreeIndexSimpleTest (652 ms)
[-----] 2 tests from BPlusTreeTests (662 ms total)

[-----] Global test environment tear-down
[=====] 2 tests from 1 test suite ran. (664 ms total)
[ PASSED ] 2 tests.
```

3.5 总体测试

- 测试BPlusTreeIndex的 `BPlusTree` 和 `Iterator`

```
[100%] build target b_plus_tree_index_test
cjx@LAPTOP-V8K17SA0:/mnt/c/Users/25347/Desktop/Minisql-6.6/build$ ./test/b_plus_tree_index_test
[=====] Running 2 tests from 1 test suite.
[-----] Global test environment set-up.
[-----] 2 tests from BPlusTreeTests
[ RUN     ] BPlusTreeTests.BPlusTreeIndexGenericKeyTest
[       OK ] BPlusTreeTests.BPlusTreeIndexGenericKeyTest (8 ms)
[ RUN     ] BPlusTreeTests.BPlusTreeIndexSimpleTest
[       OK ] BPlusTreeTests.BPlusTreeIndexSimpleTest (696 ms)
[-----] 2 tests from BPlusTreeTests (706 ms total)

[-----] Global test environment tear-down
[=====] 2 tests from 1 test suite ran. (707 ms total)
[ PASSED ] 2 tests.
cjx@LAPTOP-V8K17SA0:/mnt/c/Users/25347/Desktop/Minisql-6.6/build$
```

5. 模块相关代码

- `src/include/storage/page/b_plus_tree_page.h`
- `src/page/b_plus_tree_page.cpp`
- `src/include/storage/page/b_plus_tree_internal_page.h`
- `src/storage/page/b_plus_tree_internal_page.cpp`
- `src/include/storage/page/b_plus_tree_leaf_page.h`
- `src/storage/page/b_plus_tree_leaf_page.cpp`
- `src/include/storage/index/b_plus_tree.h`
- `src/storage/index/b_plus_tree.cpp`
- `src/include/storage/index/index_iterator.h`
- `src/storage/index/index_iterator.cpp`

