FT

May 10, 2020

```
[3]: import pandas as pd
     import numpy as np
     from sklearn.model_selection import train_test_split
     from sklearn.preprocessing import StandardScaler
     from sklearn.preprocessing import MinMaxScaler
     from sklearn.linear_model import LogisticRegression
     from sklearn.svm import SVC
     from sklearn.tree import DecisionTreeClassifier
     from sklearn.ensemble import RandomForestClassifier
     from sklearn.neighbors import KNeighborsClassifier
     from sklearn.metrics import accuracy_score
     from sklearn.metrics import f1_score
     from sklearn.metrics import precision_score
     from sklearn.metrics import recall_score
     import matplotlib.pyplot as plt
     from sklearn.metrics import confusion_matrix
[4]: data = pd.read_csv('clean.csv')
    data
[5]:
[5]:
                    blueWardsPlaced blueWardsDestroyed blueFirstBlood
           blueWins
                  0
                                   28
                                                         2
                                                                          1
     0
     1
                  0
                                   12
                                                         1
                                                                          0
     2
                                                         0
                  0
                                   15
                                                                          0
     3
                  0
                                   43
                                                         1
                                                                          0
     4
                  0
                                   75
                                                         4
                                                                          0
     9874
                                   17
                                                         2
                  1
                                                                          1
     9875
                  1
                                   54
                                                         0
                                                                          0
     9876
                  0
                                   23
                                                         1
                                                                          0
     9877
                  0
                                   14
                                                         4
                                                                          1
     9878
                  1
                                                         0
                                   18
           blueKills
                      blueDeaths blueAssists
                                                blueDragons
                                                              blueHeralds \
     0
                                            11
                                                           0
     1
                   5
                                5
                                             5
                                                           0
                                                                        0
```

2	7	11		4	1	0	
3	4	5		5	0	1	
4	6	6		6	0	0	
 9874	 7	 4	•••	 5	 1	0	
9875	6	4		8	1	0	
9876	6	7		5	0	0	
9877	2	3		3	1	0	
9878	6	6		5	0	0	
3010	O	O		J	V	O	
	blueTowersD	estroyed	redWard	lsDestroyed	redAssists	redDragons	\
0		0		6	8	0	
1		0		1	2	1	
2		0		3	14	0	
3		0		2	10	0	
4		0		2	7	1	
		•••		•••	•••	•••	
9874		0		3	7	0	
9875		0		21	3	0	
9876		0		0	11	1	
9877		0		4	1	0	
9878		0		2	4	1	
	redHeralds	redTowersDe	estroyed	redTotalG	_		
0	0		0		567	6.8	
1	1		1		620	6.8	
2	0		0		285	6.8	
3	0		0	16	478	7.0	
4	0		0	17	404	7.0	
•••	•••		•••	•••	•••		
9874	0		0		246	6.8	
9875	0		0		456	7.0	
9876	0		0		319	7.4	
9877	0		0		298	7.2	
9878	0		0	15	339	6.8	
	m	omionas	1Ta+-1M±	done17:17 - 1	modT-+-77	n m]	
^	redTotalExp		llotalMin	ionsKilled	rediotalju	ngleMinionsK	
0		17047		197			55
1		17438		240			52
2		17254		203			28
3		17961		235			47
4		18313		225			67
						•••	2.4
9874		16498		229			34
9875		18367		206			56
9876		19909		261			60
9877		18314		247			40

[9879 rows x 26 columns]

```
[6]: X = data.iloc[:, 1:]
      y = data['blueWins']
 [7]: print(X.shape)
      print(y.shape)
      print('Class labels:', np.unique(y))
     (9879, 25)
     (9879.)
     Class labels: [0 1]
 [8]: X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.3,_
       →random_state=42, stratify=y)
 [9]: print('Labels counts in y:', np.bincount(y))
      print('Labels counts in y_train:', np.bincount(y_train))
      print('Labels counts in y_test:', np.bincount(y_test))
     Labels counts in y: [4949 4930]
     Labels counts in y_train: [3464 3451]
     Labels counts in y_test: [1485 1479]
[10]: # StandardScaler estimated the parameters, (sample mean) and (standard_
      \rightarrow deviation),
      # for each feature dimension from the training data.
      # By calling the transform method,
      # we then standardized the training data using those estimated parameters, a
      # we used the same scaling parameters to standardize the test dataset
      # so that both the values in the training and test dataset are comparable to \Box
      \rightarrow each other.
      sc = StandardScaler()
      sc.fit(X_train)
      X_train_std = sc.transform(X_train)
      X_test_std = sc.transform(X_test)
[11]: mms = MinMaxScaler()
      X_train_norm = mms.fit_transform(X_train)
      X_test_norm = mms.transform(X_test)
```

Decision trees and random forests are two of the very few machine learning algorithms where we don't need to worry about feature scaling

```
[12]: # Although normalization via min-max scaling is a commonly used technique that
      \rightarrow is useful when
      # we need values in a bounded interval,
      # standardization can be more practical for many machine learning algorithms,
      # especially for optimization algorithms such as gradient descent.
      # The reason is that many linear models,
      # such as the logistic regression and SVM
      # initialize the weights to 0 or small random values close to 0.
      # Using standardization,
      # we center the feature columns at mean 0 with standard deviation 1
      # so that the feature columns have the same parameters
      # as a standard normal distribution (zero mean and unit variance),
      # which makes it easier to learn the weights.
      # Furthermore, standardization maintains useful information about outliers
      \# and makes the algorithm less sensitive to them in contrast to min-max_{\sqcup}
       \hookrightarrow scaling,
      # which scales the data to a limited range of values.
```

0.1 LogisticRegression

```
[13]: | lr = LogisticRegression(random_state=42)
      lr.fit(X_train, y_train)
      lr_y_pred = lr.predict(X_test)
      print('Logistic Regression')
      print('accuracy score:', round(accuracy_score(y_test, lr_y_pred),2))
      print('precision score:', round(precision_score(y_test, lr_y_pred), 2))
      print('recall score:', round(recall_score(y_test, lr_y_pred),2))
      print('f1 score:', round(f1_score(y_test, lr_y_pred), 2))
     Logistic Regression
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.72
     f1 score: 0.72
[14]: | lr_std = LogisticRegression(random_state=42)
      lr_std.fit(X_train_std, y_train)
      lr_y_pred_std = lr_std.predict(X_test_std)
      print('Logistic Regression')
      print('accuracy score:', round(accuracy score(y_test, lr_y_pred_std),2))
      print('precision score:', round(precision_score(y_test, lr_y_pred_std), 2))
      print('recall score:', round(recall_score(y_test, lr_y_pred_std),2))
      print('f1 score:', round(f1_score(y_test, lr_y_pred_std), 2))
```

Logistic Regression

accuracy score: 0.72 precision score: 0.72 recall score: 0.73 f1 score: 0.73 [15]: lr_norm = LogisticRegression(random_state=42) lr_norm.fit(X_train_norm, y_train) lr_y_pred_norm = lr_norm.predict(X_test_norm) print('Logistic Regression') print('accuracy score:', round(accuracy_score(y_test, lr_y_pred_norm),2)) print('precision score:', round(precision_score(y_test, lr_y_pred_norm), 2)) print('recall score:', round(recall_score(y test, lr_y pred_norm),2)) print('f1 score:', round(f1_score(y_test, lr_y_pred_norm), 2)) Logistic Regression accuracy score: 0.73 precision score: 0.72 recall score: 0.74 f1 score: 0.73 [16]: # L1 regularization, which can help us to avoid overfitting by reducing the \rightarrow complexity of a model # L1 regularization usually yields sparse feature vectors and most feature →weights will be zero. # Sparsity can be useful in practice if we have a high-dimensional dataset with # many features that are irrelevant, # especially in cases where we have more irrelevant dimensions than training_ \rightarrow examples. # In this sense, L1 regularization can be understood as a technique for feature. \rightarrow selection. # since the L1 penalty is the sum of the absolute weight coefficients # (remember that the L2 term is quadratic), C = [10, 1, .1, .001]for c in C: clf = LogisticRegression(penalty='l1', C=c, solver='liblinear') clf.fit(X_train_std, y_train) clf_y_pred = clf.predict(X_test_std) print('C:', c) print('Coefficient of each feature:', clf.coef_) print('Training accuracy:', round(clf.score(X_train_std, y_train),2)) print('Test accuracy:', round(clf.score(X_test_std, y_test), 2))

```
print('')
C: 10
Coefficient of each feature: [[-0.05060588 0.00624146 0.03989941 -0.17830676
0.11966111 -0.03650483
  0.18081067 - 0.01065741 - 0.05512811 \ 0.88840429 \ 0.02824817 \ 0.2118192
             0.01624977 -0.02844106 0.02199978 0.0731246 -0.14969972
                      -0.77401722 0.02089828 -0.38941623 0.12879156
 -0.02453345 0.065656
  0.07948544]]
Training accuracy: 0.74
Test accuracy: 0.72
C: 1
Coefficient of each feature: [[-0.04932012 0.00558484 0.03947949 -0.15476994
0.09431558 -0.03240532
  0.17937524 -0.0090911 -0.04933969 0.8604793
                                              0.02807441 0.20837399
 -0.09665317 0.02017021 -0.02783993 0.02095591 0.06931171 -0.14794594
 -0.02353184 0.05939556 -0.74560102 0.01303072 -0.37672691 0.11784165
  0.07209325]]
Training accuracy: 0.74
Test accuracy: 0.72
C: 0.1
Coefficient of each feature: [[-0.0372447 0.
                                                   0.03727023 0.
0.
          0.
  0.17077836 0.
                       0.04708822 -0.0208155
                                   -0.0150288
 -0.01453174  0.01803723  -0.59260289  0.
                                             -0.33721523 0.05461194
  0.02716905]]
Training accuracy: 0.74
Test accuracy: 0.72
C: 0.001
Coefficient of each feature: [[ 0. 0.
                                                   0.
                                                              0.
0.
          0.
                                   0.19857233 0.
                        0.
                                                         0.
  0.
             0.
  0.
             0.
                        0.
                                   0.
                                              0.
                                                         0.
                       -0.18872236 0.
  0.
             0.
                                              0.
                                                         0.
  0.
           11
Training accuracy: 0.72
```

Test accuracy: 0.72

0.2 SVM

```
[17]: svm = SVC(random state=42)
      svm.fit(X_train, y_train)
      svm_y_pred = svm.predict(X_test)
      print('SVM')
      print('accuracy score:', round(accuracy_score(y_test, svm_y_pred),2))
      print('precision score:', round(precision_score(y_test, svm_y_pred),2))
      print('recall score:', round(recall_score(y_test, svm_y_pred),2))
      print('f1 score:', round(f1_score(y_test, svm_y_pred),2))
     SVM
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.73
     f1 score: 0.72
[18]: svm std = SVC(random state=42)
      svm_std.fit(X_train_std, y_train)
      svm_y_pred_std = svm_std.predict(X_test_std)
      print('SVM')
      print('accuracy score:', round(accuracy_score(y_test, svm_y_pred_std),2))
      print('precision score:', round(precision_score(y_test, svm_y_pred_std),2))
      print('recall score:', round(recall_score(y_test, svm_y_pred_std),2))
      print('f1 score:', round(f1_score(y_test, svm_y_pred_std),2))
     SVM
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.73
     f1 score: 0.72
[19]: svm norm = SVC(random state=42)
      svm_norm.fit(X_train_norm, y_train)
      svm_y_pred_norm = svm_norm.predict(X_test_norm)
      print('SVM')
      print('accuracy score:', round(accuracy_score(y_test, svm_y_pred_norm),2))
      print('precision score:', round(precision_score(y_test, svm_y_pred_norm),2))
      print('recall score:', round(recall_score(y_test, svm_y_pred_norm),2))
      print('f1 score:', round(f1_score(y_test, svm_y_pred_norm),2))
     SVM
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.73
```

```
f1 score: 0.73
[20]: svm lin = SVC(random state=42, kernel='linear')
      svm_lin.fit(X_train, y_train)
      svm_y_pred_lin = svm_lin.predict(X_test)
      print('SVM')
      print('accuracy score:', round(accuracy_score(y_test, svm_y_pred_lin),2))
      print('precision score:', round(precision_score(y_test, svm_y_pred_lin),2))
      print('recall score:', round(recall_score(y_test, svm_y_pred_lin),2))
      print('f1 score:', round(f1_score(y_test, svm_y_pred_lin),2))
     SVM
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.72
     f1 score: 0.72
[21]: svm_lin_std = SVC(random_state=42, kernel='linear')
      svm_lin_std.fit(X_train_std, y_train)
      svm_y_pred_lin_std = svm_lin_std.predict(X_test_std)
      print('SVM')
      print('accuracy score:', round(accuracy_score(y_test, svm_y_pred_lin_std),2))
      print('precision score:', round(precision_score(y_test, svm_y_pred_lin_std),2))
      print('recall score:', round(recall_score(y_test, svm_y_pred_lin_std),2))
      print('f1 score:', round(f1_score(y_test, svm_y_pred_lin_std),2))
     SVM
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.73
     f1 score: 0.72
     0.3 DecisionTreeClassifier
[22]: tree = DecisionTreeClassifier(criterion='gini',max_depth=4,random_state=1)
      tree.fit(X_train, y_train)
      tree_y_pred = tree.predict(X_test)
```

```
8
```

print('accuracy score:', round(accuracy_score(y_test, tree_y_pred),2))
print('precision score:', round(precision_score(y_test, tree_y_pred),2))

print('recall score:', round(recall_score(y_test, tree_y_pred),2))

print('f1 score:', round(f1_score(y_test, tree_y_pred),2))

print('Tree')

```
Tree
     accuracy score: 0.71
     precision score: 0.69
     recall score: 0.75
     f1 score: 0.72
[23]: tree_norm = DecisionTreeClassifier(criterion='gini', max_depth=4, random_state=1)
      tree_norm.fit(X_train_norm, y_train)
      tree_y_pred_norm = tree_norm.predict(X_test_norm)
      print('Tree')
      print('accuracy score:', round(accuracy_score(y_test, tree_y_pred_norm),2))
      print('precision score:', round(precision_score(y_test, tree_y_pred_norm),2))
      print('recall score:', round(recall_score(y_test, tree_y_pred_norm),2))
      print('f1 score:', round(f1_score(y_test, tree_y_pred_norm),2))
     Tree
     accuracy score: 0.71
     precision score: 0.69
     recall score: 0.75
     f1 score: 0.72
     0.4 RandomForestClassifier
[24]: forest = RandomForestClassifier(random_state=42)
      forest.fit(X_train, y_train)
      forest_y_pred = forest.predict(X_test)
      print('Tree')
      print('accuracy score:', round(accuracy_score(y_test, forest_y_pred),2))
      print('precision score:', round(precision_score(y_test, forest_y_pred),2))
      print('recall score:', round(recall_score(y_test, forest_y_pred),2))
      print('f1 score:', round(f1_score(y_test, forest_y_pred),2))
     Tree
     accuracy score: 0.72
     precision score: 0.72
     recall score: 0.72
     f1 score: 0.72
[26]: forest_norm = RandomForestClassifier(random_state=42)
```

forest_norm.fit(X_train_norm, y_train)

```
forest_y_pred_norm = forest_norm.predict(X_test_norm)

print('Tree')
print('accuracy score:', round(accuracy_score(y_test, forest_y_pred_norm),2))
print('precision score:', round(precision_score(y_test, forest_y_pred_norm),2))
print('recall score:', round(recall_score(y_test, forest_y_pred_norm),2))
print('f1 score:', round(f1_score(y_test, forest_y_pred_norm),2))
```

Tree

accuracy score: 0.72 precision score: 0.72 recall score: 0.72 f1 score: 0.72

0.5 KNeighborsClassifier

```
[27]: knn = KNeighborsClassifier()
knn.fit(X_train, y_train)
knn_y_pred = knn.predict(X_test)

print('Tree')
print('accuracy score:', round(accuracy_score(y_test, knn_y_pred),2))
print('precision score:', round(precision_score(y_test, knn_y_pred),2))
print('recall score:', round(recall_score(y_test, knn_y_pred),2))
print('f1 score:', round(f1_score(y_test, knn_y_pred),2))
```

Tree

accuracy score: 0.69 precision score: 0.68 recall score: 0.7 f1 score: 0.69

```
[28]: knn_std = KNeighborsClassifier()
knn_std.fit(X_train_std, y_train)
knn_y_pred_std = knn_std.predict(X_test_std)

print('Tree')
print('accuracy score:', round(accuracy_score(y_test, knn_y_pred_std),2))
print('precision score:', round(precision_score(y_test, knn_y_pred_std),2))
print('recall score:', round(recall_score(y_test, knn_y_pred_std),2))
print('f1 score:', round(f1_score(y_test, knn_y_pred_std),2))
```

Tree

accuracy score: 0.68 precision score: 0.68

recall score: 0.69 f1 score: 0.69

```
[29]: knn_norm = KNeighborsClassifier()
knn_norm.fit(X_train_norm, y_train)
knn_y_pred_norm = knn_norm.predict(X_test_norm)

print('Tree')
print('accuracy score:', round(accuracy_score(y_test, knn_y_pred_norm),2))
print('precision score:', round(precision_score(y_test, knn_y_pred_norm),2))
print('recall score:', round(recall_score(y_test, knn_y_pred_norm),2))
print('f1 score:', round(f1_score(y_test, knn_y_pred_norm),2))
```

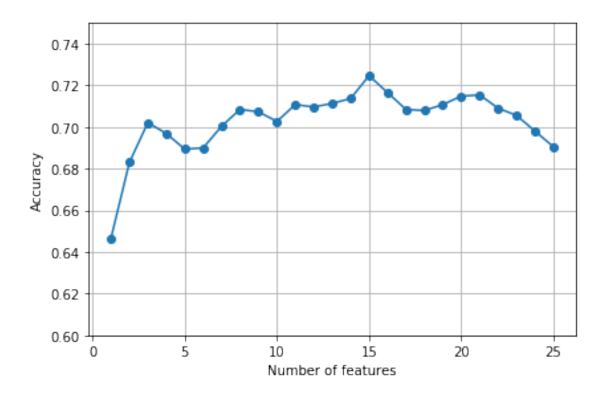
Tree accuracy score: 0.69 precision score: 0.68 recall score: 0.69

f1 score: 0.69

0.6 Sequential feature selection algorithms

```
[30]: # reduce the complexity of the model and avoid overfitting is
      # dimensionality reduction via feature selection,
      # which is especially useful for unregularized models.
      from sklearn.base import clone
      from itertools import combinations
      class SBS():
          def __init__(self, estimator, k_features,
                       scoring=accuracy_score,
                       test_size=0.25, random_state=1):
              self.scoring = scoring
              self.estimator = clone(estimator)
              self.k features = k features
              self.test_size = test_size
              self.random_state = random_state
          def fit(self, X, y):
              X_train, X_test, y_train, y_test = \
                  train_test_split(X, y, test_size=self.test_size,
                                   random_state=self.random_state)
              dim = X_train.shape[1]
              self.indices_ = tuple(range(dim))
              self.subsets_ = [self.indices_]
```

```
score = self._calc_score(X_train, y_train,
                                       X_test, y_test, self.indices_)
              self.scores_ = [score]
              while dim > self.k_features:
                  scores = []
                  subsets = []
                  for p in combinations(self.indices_, r=dim - 1):
                      score = self._calc_score(X_train, y_train,
                                                X_test, y_test, p)
                      scores.append(score)
                      subsets.append(p)
                  best = np.argmax(scores)
                  self.indices_ = subsets[best]
                  self.subsets_.append(self.indices_)
                  \dim -= 1
                  self.scores_.append(scores[best])
              self.k_score_ = self.scores_[-1]
              return self
          def transform(self, X):
              return X[:, self.indices_]
          def _calc_score(self, X_train, y_train, X_test, y_test, indices):
              self.estimator.fit(X_train[:, indices], y_train)
              y_pred = self.estimator.predict(X_test[:, indices])
              score = self.scoring(y_test, y_pred)
              return score
[31]: knn_eve = KNeighborsClassifier(n_neighbors=5)
      sbs = SBS(knn_eve, k_features=1)
      sbs.fit(X_train_std, y_train)
[31]: <__main__.SBS at 0x1a19453290>
[32]: k_feat = [len(k) for k in sbs.subsets_]
      plt.plot(k_feat, sbs.scores_, marker='o')
      plt.ylim([0.6, 0.75])
      plt.ylabel('Accuracy')
      plt.xlabel('Number of features')
      plt.grid()
      plt.tight_layout()
      plt.show()
```



```
[33]: for i in range(25):
          if len(sbs.subsets_[i])==15:
              print(i)
     10
[35]: k15 = list(sbs.subsets_[10])
      print(data.columns[1:][k15])
     Index(['blueWardsDestroyed', 'blueKills', 'blueDragons', 'blueTotalGold',
            'blueAvgLevel', 'blueTotalMinionsKilled',
            'blueTotalJungleMinionsKilled', 'redWardsDestroyed', 'redDragons',
            'redHeralds', 'redTotalGold', 'redAvgLevel', 'redTotalExperience',
            'redTotalMinionsKilled', 'redTotalJungleMinionsKilled'],
           dtype='object')
[36]: knn_eve.fit(X_train_std, y_train)
      knn_y_pred_eve = knn_eve.predict(X_test_std)
      print('Training accuracy:', round(knn_eve.score(X_train_std, y_train),4))
      print('Test accuracy:', round(knn_eve.score(X_test_std, y_test),4))
```

Training accuracy: 0.7864

Test accuracy: 0.6845

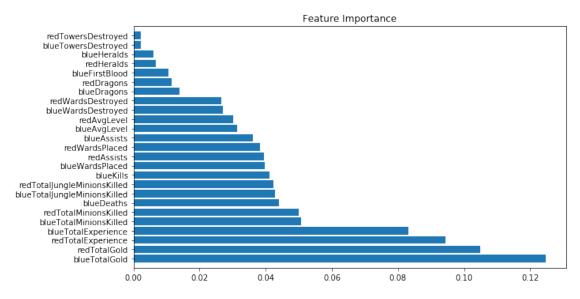
```
[38]: # This may indicate that those features do not provide less
# discriminatory information than the original dataset.

# While we did not increase the performance of the KNN model
# by reducing the number of features, we shrank the size of the dataset,
# which can be useful in real-world applications that
# may involve expensive data collection steps.
# Also, by substantially reducing the number of features,
# we obtain simpler models, which are easier to interpret.
```

0.7 Assessing feature importance with random forests

```
plt.ylim([-1, X_train.shape[1]])
plt.tight_layout()
plt.show()
```

1)	blueTotalGold	0.124592
2)	redTotalGold	0.104914
3)	redTotalExperience	0.094390
4)	blueTotalExperience	0.083116
5)	${\tt blueTotalMinionsKilled}$	0.050728
6)	${\tt redTotalMinionsKilled}$	0.049979
7)	blueDeaths	0.043987
8)	$\verb blueTotalJungleMinionsKilled $	0.042882
9)	${\tt redTotalJungleMinionsKilled}$	0.042260
10)	blueKills	0.041046
11)	blueWardsPlaced	0.039726
12)	redAssists	0.039429
13)	redWardsPlaced	0.038255
14)	blueAssists	0.036247
15)	blueAvgLevel	0.031270
16)	${\tt redAvgLevel}$	0.030150
17)	blueWardsDestroyed	0.027127
18)	${\tt redWardsDestroyed}$	0.026610
19)	blueDragons	0.013918
20)	redDragons	0.011518
21)	blueFirstBlood	0.010665
22)	redHeralds	0.006716
23)	blueHeralds	0.006108
24)	blueTowersDestroyed	0.002250
25)	${\tt redTowersDestroyed}$	0.002115



```
[40]: # However, as far as interpretability is concerned,
# the random forest technique comes with an important gotcha that is worth

→ mentioning.

# If two or more features are highly correlated,
# one feature may be ranked very highly
# while the information on the other feature(s) may not be fully captured.
# On the other hand, we don't need to be concerned about this problem
# if we are merely interested in the predictive performance of a model
# rather than the interpretation of feature importance values.
```

0.8 SelectFromModel

```
[41]: from sklearn.feature_selection import SelectFromModel

sfm = SelectFromModel(forest, threshold=0.05, prefit=True)

X_selected = sfm.transform(X_train)

print('Number of features that meet this threshold', 'criterion:', X_selected.

→shape[1])

for f in range(X_selected.shape[1]):

print("%2d) %-*s %f" % (f + 1, 30, feat_labels[indices[f]], 
→importances[indices[f]]))
```

Number of features that meet this threshold criterion: 5

1) blueTotalGold 0.124592

2) redTotalGold 0.104914

3) redTotalExperience 0.094390

4) blueTotalExperience 0.083116

5) blueTotalMinionsKilled 0.050728

0.9 PCA

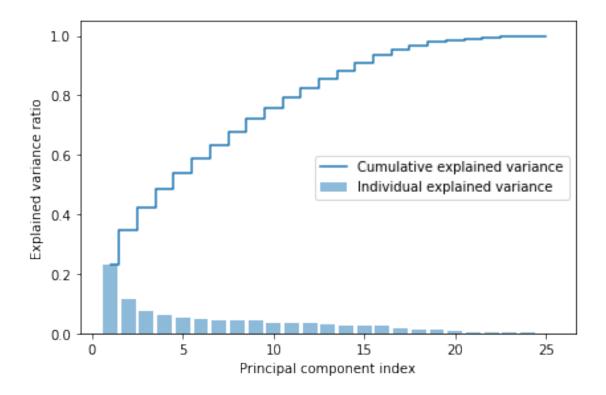
```
[43]: cov_mat = np.cov(X_train_std.T)
eigen_vals, eigen_vecs = np.linalg.eig(cov_mat)
```

```
print('\nEigenvalues \n%s' % eigen_vals)
```

Eigenvalues [5.81609522 2.89709742 1.89016027 1.56619826 1.30911826 1.23793264

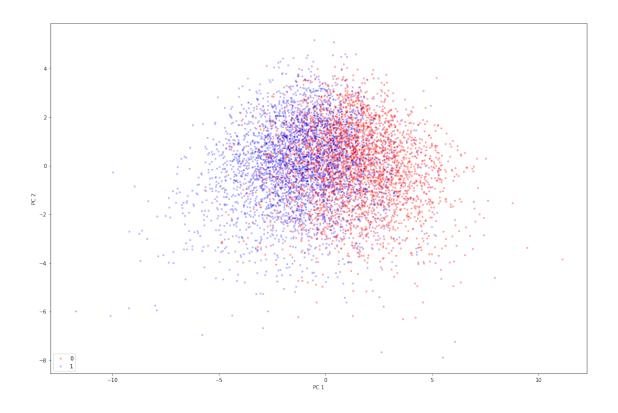
1.13363867 1.11122491 1.06351397 0.03122298 0.0354456 0.06619959 0.07900005 0.14179771 0.19159083 0.28952091 0.41070525 0.33723218 0.92448807 0.87085092 0.82103946 0.77150876 0.64507624 0.68739618

0.67556148]



```
[45]: # we can see that the first two principal components
      # combined explain almost 80 percent of the variance in the dataset:
[46]: # Make a list of (eigenvalue, eigenvector) tuples
      eigen_pairs = [(np.abs(eigen_vals[i]), eigen_vecs[:, i]) for i in_
       →range(len(eigen_vals))]
      # Sort the (eigenvalue, eigenvector) tuples from high to low
      eigen_pairs.sort(key=lambda k: k[0], reverse=True)
[47]: | w = np.hstack((eigen_pairs[0][1][:, np.newaxis], eigen_pairs[1][1][:, np.
       →newaxis]))
      print('Matrix W:\n', w)
     Matrix W:
      [[-1.13468999e-02 -2.13953627e-02]
      [-3.67680038e-02 3.56627170e-02]
      [-1.55730629e-01 -1.13297138e-02]
      [-2.66089102e-01 -3.63651709e-01]
      [ 2.60006765e-01 -3.69908044e-01]
      [-2.22710896e-01 -3.44841259e-01]
      [-1.36278292e-01 2.05069484e-02]
      [-7.80041555e-02 2.82881320e-02]
```

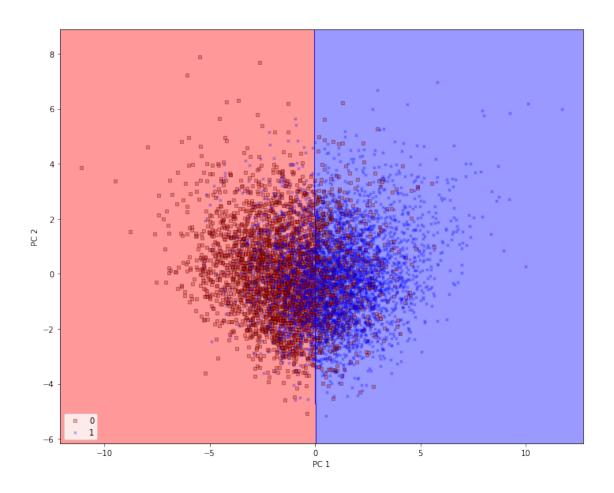
```
[-1.19929082e-01 -9.41213413e-02]
      [-3.26936406e-01 -2.37421962e-01]
      [-2.90911407e-01 1.34852869e-01]
      [-3.11130112e-01 1.44273360e-01]
      [-1.84446492e-01 2.95599904e-01]
      [-8.75919443e-02 2.35924062e-01]
      [ 1.10184018e-02 1.71758524e-02]
      [ 4.67433821e-02 4.08922278e-02]
      [ 2.13326358e-01 -3.53736839e-01]
      [ 1.40535774e-01 3.81648395e-02]
      [ 8.30441690e-02 -3.29115056e-04]
      [ 1.12625689e-01 -8.07592051e-02]
      [ 3.22585043e-01 -2.44076820e-01]
      [ 2.91392399e-01 1.22992487e-01]
      [ 3.11624525e-01 1.34427832e-01]
      [ 1.86937919e-01 2.90519477e-01]
      [ 9.50644772e-02 2.22294830e-01]]
[48]: X_train_std[0].dot(w)
[48]: array([-1.74742023, 4.13319886])
[49]: X_train_pca = X_train_std.dot(w)
[50]: colors = ['r', 'b']
      markers = [ 'o', 'x']
     plt.figure(figsize=(15,10))
      for 1, c, m in zip(np.unique(y_train), colors, markers):
              plt.scatter(X_train_pca[y_train==1, 0], X_train_pca[y_train==1, 1],__
      ⇔c=c, label=1, marker=m,
                          s= 7, alpha=0.3)
      plt.xlabel('PC 1')
      plt.ylabel('PC 2')
      plt.legend(loc='lower left')
     plt.tight_layout()
     plt.show()
```



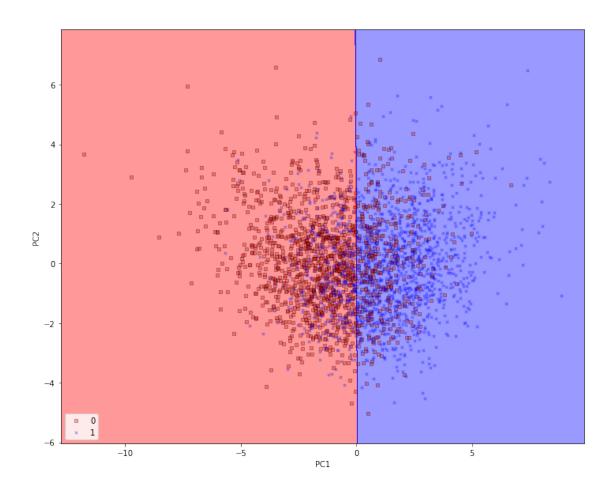
```
[51]: from matplotlib.colors import ListedColormap
      def plot_decision_regions(X, y, classifier, resolution=0.02):
          # setup marker generator and color map
          markers = ('s', 'x', 'o', '^', 'v')
          colors = ('red', 'blue', 'lightgreen', 'gray', 'cyan')
          cmap = ListedColormap(colors[:len(np.unique(y))])
          # plot the decision surface
          x1_{min}, x1_{max} = X[:, 0].min() - 1, X[:, 0].max() + 1
          x2_{min}, x2_{max} = X[:, 1].min() - 1, X[:, 1].max() + 1
          xx1, xx2 = np.meshgrid(np.arange(x1_min, x1_max, resolution),
                                 np.arange(x2_min, x2_max, resolution))
          Z = classifier.predict(np.array([xx1.ravel(), xx2.ravel()]).T)
          Z = Z.reshape(xx1.shape)
          plt.contourf(xx1, xx2, Z, alpha=0.4, cmap=cmap)
          plt.xlim(xx1.min(), xx1.max())
          plt.ylim(xx2.min(), xx2.max())
          # plot examples by class
          for idx, cl in enumerate(np.unique(y)):
              plt.scatter(x=X[y == cl, 0],
                          y=X[y == c1, 1],
```

```
alpha=0.3,
color=cmap(idx),
edgecolor='black',
marker=markers[idx],
label=cl, s= 10)
```

```
[52]: from sklearn.linear_model import LogisticRegression
      from sklearn.decomposition import PCA
      # initializing the PCA transformer and
      # logistic regression estimator:
      pca = PCA(n_components=2)
      lr = LogisticRegression(random_state=42)
      # dimensionality reduction:
      X_train_pca = pca.fit_transform(X_train_std)
      X_test_pca = pca.transform(X_test_std)
      # fitting the logistic regression model on the reduced dataset:
      lr.fit(X_train_pca, y_train)
      plt.figure(figsize=(10,8))
      plot_decision_regions(X_train_pca, y_train, classifier=lr)
      plt.xlabel('PC 1')
      plt.ylabel('PC 2')
      plt.legend(loc='lower left')
      plt.tight_layout()
      plt.show()
```



```
[53]: plt.figure(figsize=(10,8))
    plot_decision_regions(X_test_pca, y_test, classifier=lr)
    plt.xlabel('PC1')
    plt.ylabel('PC2')
    plt.legend(loc='lower left')
    plt.tight_layout()
    plt.show()
```



1 Classification LDA

```
[55]: np.set_printoptions(precision=4)

mean_vecs = []
for label in range(0,2):
    mean_vecs.append(np.mean(X_train_std[y_train==label], axis=0))
    print('MV %s: %s\n' %(label, mean_vecs[label-1]))
```

Within-class scatter matrix: 25x25

 $S_W += class_scatter$

for row in X_train_std[y_train == label]:

row, mv = row.reshape(d, 1), mv.reshape(d, 1)
class_scatter += (row - mv).dot((row - mv).T)

```
[57]: print('Class label distribution: %s'
% np.bincount(y_train))
```

print('Within-class scatter matrix: %sx%s' % (S_W.shape[0], S_W.shape[1]))

Class label distribution: [3464 3451]

Scaled within-class scatter matrix: 25x25

```
[59]: mean_overall = np.mean(X_train_std, axis=0)

d = 25 # number of features

S_B = np.zeros((d, d))
```

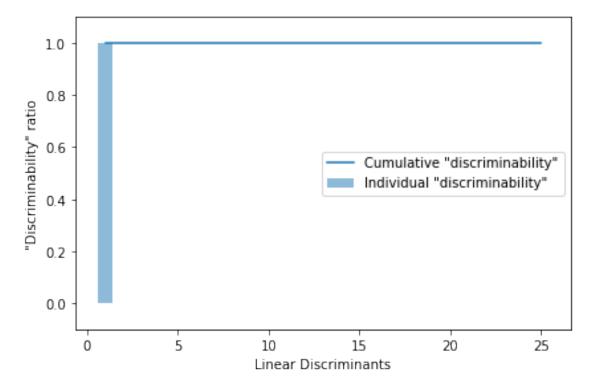
```
for i, mean_vec in enumerate(mean_vecs):
    n = X_train_std[y_train == i + 1, :].shape[0]
    mean_vec = mean_vec.reshape(d, 1) # make column vector
    mean_overall = mean_overall.reshape(d, 1)
    S_B += n * (mean_vec - mean_overall).dot(
        (mean_vec - mean_overall).T)
print('Between-class scatter matrix: %sx%s' % (S_B.shape[0], S_B.shape[1]))
```

Between-class scatter matrix: 25x25

Eigenvalues in descending order:

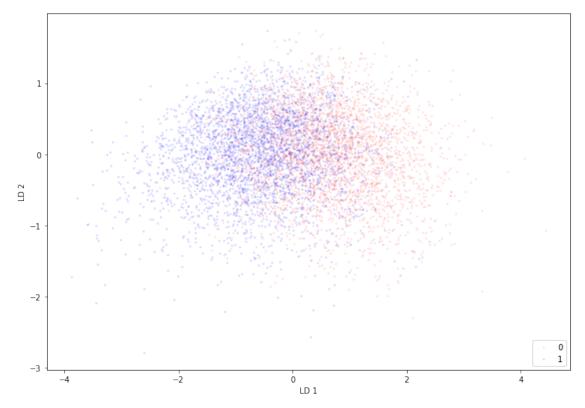
```
672.4503168121524
9.773443222512302e-13
9.720237790933486e-13
7.437879509763636e-13
7.437879509763636e-13
5.876707830719263e-13
3.4214650020990603e-13
2.693515866762188e-13
2.279678377514385e-13
2.279678377514385e-13
2.1104344161168111e-13
1.6116228879927517e-13
1.6116228879927517e-13
1.4323466211558735e-13
8.185342750146758e-14
8.185342750146758e-14
6.997601494862712e-14
5.168741241038838e-14
5.168741241038838e-14
1.91988475947768e-14
1.91988475947768e-14
1.6781183663007214e-14
3.5744835862024005e-15
```

9.174558044701644e-16 0.0



```
[63]: w = np.hstack((eigen_pairs[0][1][:, np.newaxis].real, eigen_pairs[1][1][:, np.
      →newaxis].real))
      print('Matrix W:\n', w)
     Matrix W:
      [[ 0.0369  0.0061]
      [-0.0104 0.0294]
      [-0.0403 0.0191]
      [ 0.1355 -0.0401]
      [-0.0767 0.6833]
      [ 0.0286  0.0199]
      [-0.1388 0.0448]
      [-0.0019 0.0031]
      [ 0.0969 0.06 ]
      [-0.6738 0.2987]
      [-0.0167 0.0047]
      [-0.1518 0.1423]
      [0.0888 - 0.0586]
      [-0.0103 -0.0208]
      [0.0171 - 0.0154]
      [-0.0147 0.0024]
      [-0.0552 -0.0014]
      [ 0.1229 -0.0166]
      [ 0.0219  0.002 ]
      [-0.0692 0.1289]
      [ 0.5786 -0.3068]
      [-0.037 -0.3064]
      [ 0.2905  0.4526]
      [-0.0978 -0.0031]
      [-0.0627 -0.0285]]
[64]: X_train_lda = X_train_std.dot(w)
      colors = ['r', 'b']
      markers = ['x', 'o']
      plt.figure(figsize=(10,7))
      for l, c, m in zip(np.unique(y_train), colors, markers):
           plt.scatter(X_train_lda[y_train==1, 0], X_train_lda[y_train==1, 1] * (-1),
          c=c, label=1, marker=m, s=3, alpha=0.1)
      plt.xlabel('LD 1')
      plt.ylabel('LD 2')
```

```
plt.legend(loc='lower right')
plt.tight_layout()
plt.show()
```



```
If 'classlabel' the prediction is based on
  the argmax of class labels. Else if
  'probability', the argmax of the sum of
  probabilities is used to predict the class label
  (recommended for calibrated classifiers).
weights : array-like, shape = [n_classifiers]
  Optional, default: None
  If a list of `int` or `float` values are
  provided, the classifiers are weighted by
  importance; Uses uniform weights if `weights=None`.
def __init__(self, classifiers,
             vote='classlabel', weights=None):
    self.classifiers = classifiers
    self.named_classifiers = {key: value for
                              key, value in
                              _name_estimators(classifiers)}
    self.vote = vote
    self.weights = weights
def fit(self, X, y):
    """ Fit classifiers.
    Parameters
    X : {array-like, sparse matrix},
        shape = [n_examples, n_features]
        Matrix of training examples.
    y : array-like, shape = [n_examples]
        Vector of target class labels.
    Returns
    self : object
    if self.vote not in ('probability', 'classlabel'):
        raise ValueError("vote must be 'probability'"
                         "or 'classlabel'; got (vote=%r)"
                         % self.vote)
    if self.weights and len(self.weights) != len(self.classifiers):
        raise ValueError("Number of classifiers and weights"
                         "must be equal; got %d weights,"
```

```
"%d classifiers"
                         % (len(self.weights),
                         len(self.classifiers)))
    # Use LabelEncoder to ensure class labels start
    # with 0, which is important for np.arqmax
    # call in self.predict
    self.lablenc_ = LabelEncoder()
    self.lablenc_.fit(y)
    self.classes_ = self.lablenc_.classes_
    self.classifiers_ = []
    for clf in self.classifiers:
        fitted_clf = clone(clf).fit(X,
                           self.lablenc_.transform(y))
        self.classifiers_.append(fitted_clf)
    return self
def predict(self, X):
    """ Predict class labels for X.
    Parameters
    X : {array-like, sparse matrix},
        Shape = [n_examples, n_features]
        Matrix of training examples.
    Returns
    maj_vote : array-like, shape = [n_examples]
        Predicted class labels.
    if self.vote == 'probability':
        maj_vote = np.argmax(self.predict_proba(X), axis=1)
    else: # 'classlabel' vote
        # Collect results from clf.predict calls
        predictions = np.asarray([clf.predict(X)
                                  for clf in
                                  self.classifiers ]).T
        maj_vote = np.apply_along_axis(lambda x: np.argmax(
                                       np.bincount(x,
                                       weights=self.weights)),
                                       axis=1,
                                       arr=predictions)
    maj_vote = self.lablenc_.inverse_transform(maj_vote)
    return maj_vote
```

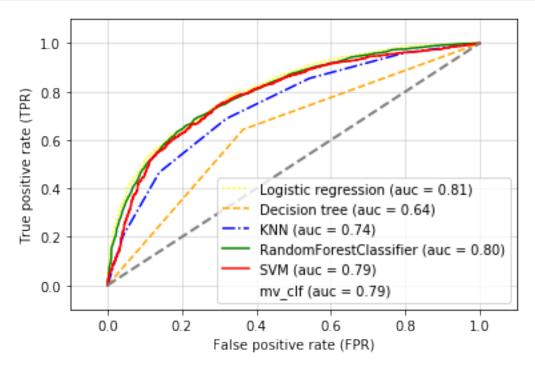
```
def predict_proba(self, X):
              """ Predict class probabilities for X.
              Parameters
              X : {array-like, sparse matrix},
                  shape = [n_examples, n_features]
                  Training vectors, where
                  n_examples is the number of examples and
                  n_features is the number of features.
              Returns
              avg_proba : array-like,
                  shape = [n_examples, n_classes]
                  Weighted average probability for
                  each class per example.
              probas = np.asarray([clf.predict_proba(X)
                                   for clf in self.classifiers ])
              avg_proba = np.average(probas, axis=0,
                                     weights=self.weights)
              return avg_proba
          def get_params(self, deep=True):
              """ Get classifier parameter names for GridSearch"""
              if not deep:
                  return super(MajorityVoteClassifier,
                                 self).get_params(deep=False)
              else:
                  out = self.named_classifiers.copy()
                  for name, step in self.named_classifiers.items():
                      for key, value in step.get_params(
                              deep=True).items():
                          out['%s__%s' % (name, key)] = value
                  return out
[67]: from sklearn.model_selection import cross_val_score
      from sklearn.pipeline import Pipeline
```

```
[67]: from sklearn.model_selection import cross_val_score
    from sklearn.pipeline import Pipeline

clf1 = LogisticRegression(random_state=42)
    clf2 = DecisionTreeClassifier(random_state=42)
    clf3 = KNeighborsClassifier()
    clf4 = RandomForestClassifier(random_state=42)
    clf5 = SVC(random_state=42, probability = True)
```

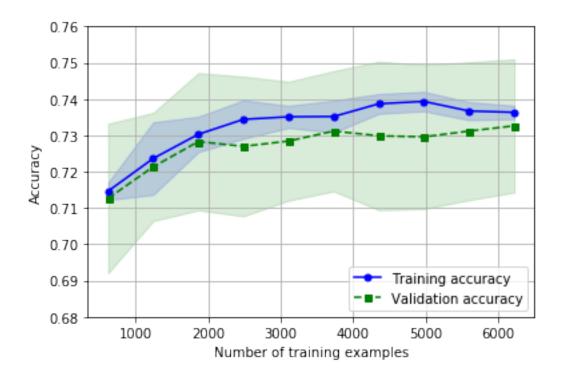
```
pipe1 = Pipeline([['sc', StandardScaler()], ['clf', clf1]])
     pipe3 = Pipeline([['sc', StandardScaler()], ['clf', clf3]])
     pipe5 = Pipeline([['sc', StandardScaler()], ['clf', clf5]])
     mv_clf = MajorityVoteClassifier(classifiers=[pipe1, clf2, pipe3, clf4, pipe5])
     clf_labels = ['Logistic regression', 'Decision tree', 'KNN', |
      print('10-fold cross validation:\n')
     for clf, label in zip([pipe1, clf2, pipe3, clf4, pipe5, mv_clf], clf_labels):
         scores = cross_val_score(estimator=clf, X=X_train, y=y_train, cv=10,_
      ⇔scoring='roc_auc')
         print("ROC AUC: %0.2f (+/- %0.2f) [%s]"
               % (scores.mean(), scores.std(), label))
     10-fold cross validation:
     ROC AUC: 0.81 (+/- 0.02) [Logistic regression]
     ROC AUC: 0.63 (+/-0.03) [Decision tree]
     ROC AUC: 0.74 (+/- 0.01) [KNN]
     ROC AUC: 0.79 (+/- 0.02) [RandomForestClassifier]
     ROC AUC: 0.79 (+/- 0.02) [SVM]
     ROC AUC: 0.78 (+/-0.02) [mv_clf]
[68]: from sklearn.metrics import roc curve
     from sklearn.metrics import auc
     colors = ['yellow', 'orange', 'b', 'green', 'r', 'black']
     all_clf = [pipe1, clf2, pipe3, clf4, pipe5, mv_clf]
     linestyles = [':', '--', '-.', '-', 'solid', '']
     for clf, label, clr, ls \
         in zip(all clf, clf labels, colors, linestyles):
         # assuming the label of the positive class is 1
         y_pred = clf.fit(X_train, y_train).predict_proba(X_test)[:, 1]
         fpr, tpr, thresholds = roc_curve(y_true=y_test, y_score=y_pred)
         roc_auc = auc(x=fpr, y=tpr)
         plt.plot(fpr, tpr, color=clr, linestyle=ls, label='%s (auc = %0.2f)' %L
      →(label, roc_auc))
     plt.legend(loc='lower right')
     plt.plot([0, 1], [0, 1], linestyle='--', color='gray', linewidth=2)
     plt.xlim([-0.1, 1.1])
     plt.ylim([-0.1, 1.1])
     plt.grid(alpha=0.5)
```

```
plt.xlabel('False positive rate (FPR)')
plt.ylabel('True positive rate (TPR)')
plt.show()
```



```
print(knn_cv.best_params_)
      print(knn_cv.best_score_)
     {'n_neighbors': 23}
     0.7117871811816668
[73]: from sklearn.pipeline import make_pipeline
      pipe_lr = make_pipeline(StandardScaler(), PCA(n_components=2),
                              LogisticRegression(random state=42, solver='lbfgs'))
      pipe_lr.fit(X_train, y_train)
      y_pred = pipe_lr.predict(X_test)
      print('Test Accuracy: %.3f' % pipe_lr.score(X_test, y_test))
     Test Accuracy: 0.726
 []: pipe svc = make pipeline(StandardScaler(), SVC(random state=42))
      param range = [0.0001, 0.001, 0.01, 0.1, 1.0, 10.0, 100.0, 1000.0]
      param_grid = [{'svc_C': param_range, 'svc_kernel': ['linear']},
                    {'svc_C': param range, 'svc_gamma': param range, 'svc_kernel': __
       →['rbf']}]
      gs = GridSearchCV(estimator=pipe svc, param grid=param grid,,,
      ⇒scoring='accuracy',cv=10,refit=True,n_jobs=-1)
      gs = gs.fit(X_train, y_train)
      print(gs.best_score_)
      print(gs.best_params_)
     /opt/anaconda3/lib/python3.7/site-
     packages/joblib/externals/loky/process executor.py:706: UserWarning: A worker
     stopped while some jobs were given to the executor. This can be caused by a too
     short worker timeout or by a memory leak.
       "timeout or by a memory leak.", UserWarning
[74]: from sklearn.model_selection import StratifiedKFold
      kfold = StratifiedKFold(n_splits=10).split(X_train, y_train)
      scores = []
      for k, (train, test) in enumerate(kfold):
          pipe_lr.fit(X_train[train], y_train[train])
          score = pipe_lr.score(X_train[test], y_train[test])
          scores.append(score)
```

```
print('Fold: %2d, Class dist.: %s, Acc: %.3f' % (k+1, np.
       ⇒bincount(y_train[train]), score))
     Fold: 1, Class dist.: [3118 3105], Acc: 0.712
     Fold: 2, Class dist.: [3117 3106], Acc: 0.702
     Fold: 3, Class dist.: [3117 3106], Acc: 0.753
     Fold: 4, Class dist.: [3117 3106], Acc: 0.734
     Fold: 5, Class dist.: [3117 3106], Acc: 0.714
     Fold: 6, Class dist.: [3118 3106], Acc: 0.747
     Fold: 7, Class dist.: [3118 3106], Acc: 0.742
     Fold: 8, Class dist.: [3118 3106], Acc: 0.744
     Fold: 9, Class dist.: [3118 3106], Acc: 0.731
     Fold: 10, Class dist.: [3118 3106], Acc: 0.715
[84]: from sklearn.model_selection import learning_curve
      pipe_lr = make_pipeline(StandardScaler(), LogisticRegression(random_state= 42))
      train_sizes, train_scores, test_scores =__
      →learning_curve(estimator=pipe_lr,X=X_train,
                                          y=y_train, train_sizes=np.linspace(0.1, 1.
      \rightarrow 0, 10), cv=10, n jobs=1)
      train_mean = np.mean(train_scores, axis=1)
      train_std = np.std(train_scores, axis=1)
      test_mean = np.mean(test_scores, axis=1)
      test_std = np.std(test_scores, axis=1)
      plt.plot(train_sizes, train_mean, color='blue', marker='o', markersize=5,u
      →label='Training accuracy')
      plt.fill_between(train_sizes,train_mean + train_std, train_mean -_
       →train_std,alpha=0.15, color='blue')
      plt.plot(train_sizes, test_mean,color='green', linestyle='--', marker='s',u
       →markersize=5,label='Validation accuracy')
      plt.fill_between(train_sizes, test_mean + test_std, test_mean - test_std,__
      ⇒alpha=0.15, color='green')
      plt.grid()
      plt.xlabel('Number of training examples')
      plt.ylabel('Accuracy')
      plt.legend(loc='lower right')
      plt.ylim([0.68, 0.76])
      plt.show()
```

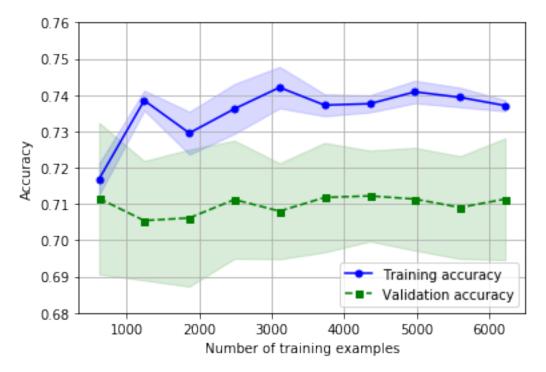


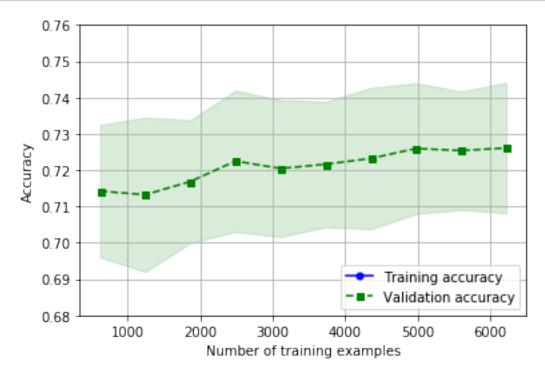
```
[85]: pipe knn = make_pipeline(StandardScaler(), KNeighborsClassifier(n_neighbors=23))
      train_sizes, train_scores, test_scores =_
       →learning_curve(estimator=pipe_knn,X=X_train,
                                           y=y_train, train_sizes=np.linspace(0.1, 1.
      \rightarrow 0, 10), cv=10, n_jobs=1)
      train mean = np.mean(train scores, axis=1)
      train_std = np.std(train_scores, axis=1)
      test_mean = np.mean(test_scores, axis=1)
      test_std = np.std(test_scores, axis=1)
      plt.plot(train_sizes, train_mean, color='blue', marker='o', markersize=5,__
       →label='Training accuracy')
      plt.fill_between(train_sizes,train_mean + train_std, train_mean -_

→train_std,alpha=0.15, color='blue')
      plt.plot(train_sizes, test_mean,color='green', linestyle='--', marker='s',u
       →markersize=5,label='Validation accuracy')
      plt.fill_between(train_sizes, test_mean + test_std, test_mean - test_std,__
       →alpha=0.15, color='green')
```

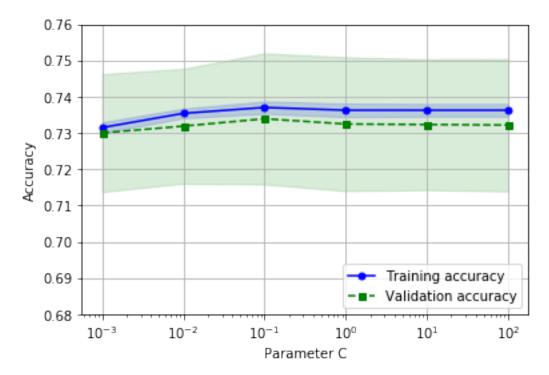
```
plt.grid()

plt.xlabel('Number of training examples')
plt.ylabel('Accuracy')
plt.legend(loc='lower right')
plt.ylim([0.68, 0.76])
plt.show()
```





```
train_mean = np.mean(train_scores, axis=1)
train_std = np.std(train_scores, axis=1)
test_mean = np.mean(test_scores, axis=1)
test_std = np.std(test_scores, axis=1)
plt.plot(param_range, train_mean, color='blue', marker='o', markersize=5, u
→label='Training accuracy')
plt.fill_between(param_range, train_mean + train_std,train_mean - train_std,__
⇒alpha=0.15, color='blue')
plt.plot(param_range, test_mean, color='green', linestyle='--', marker='s', u
→markersize=5,label='Validation accuracy')
plt.fill_between(param_range, test_mean + test_std, test_mean - test_std,__
⇒alpha=0.15, color='green')
plt.grid()
plt.xscale('log')
plt.legend(loc='lower right')
plt.xlabel('Parameter C')
plt.ylabel('Accuracy')
plt.ylim([0.68, 0.76])
plt.show()
```



[]:[