

PHY 5410: Homework Week 11

18.2 Investigate the scattering from the δ -shell potential of Problem 17.2

$$v(r) = -\lambda \frac{\hbar^2}{2m} \delta(r - a) \quad ,$$

using the notation introduced there.

- (a) Calculate the scattering phases $\delta_l(k)$.
- (b) Give the scattering cross section for s -waves.
- (c) Determine the condition for the maxima of the s -wave scattering cross section.
- (d) From here on, assume $g \gg \pi$. Determine the maxima for $ka \ll g$.

18.4 Calculate the total cross section for s -wave scattering on a completely impenetrable sphere, i.e., for

$$v(r) = \begin{cases} \infty, & r < a \\ 0, & r > a \end{cases} .$$

18.5 Calculate the phase shift δ_0 from s -wave scattering states for an attractive and for a repulsive square-well potential.