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CS 440

1. $(\sim \text{stench}(m) \vee \text{Adjacent}(x, f(x))) \wedge (\sim \text{stench}(m) \vee \text{At}(\text{wumpus}, f(x)))$
2.
 - a. $\forall x, \text{Likes}(x, \text{Apples}) \rightarrow \text{Plays}(x, \text{Chess})$
 - b. $\forall x, \text{Likes}(x, \text{Oranges}) \rightarrow \text{Plays}(x, \text{Go})$
 - c. $\forall x, (\text{Likes}(x, \text{Oranges}) \vee \text{Likes}(x, \text{Apples})) \rightarrow \sim (\text{Likes}(x, \text{Oranges}) \wedge \text{Likes}(x, \text{Apples}))$
 - d. $\text{Likes}(\text{John}, \text{Apples})$
 - e. $\forall x, y, \text{Marry}(y) \wedge \text{John}(x) \wedge \text{Likes}(x, F) \rightarrow \sim \text{Likes}(y, F)$
3. \exists, \forall
 - a. C1: $\sim \text{Likes}(x, \text{Apples}) \vee \text{Plays}(x, \text{Chess})$
 - b. C2: $\sim \text{Likes}(x, \text{Oranges}) \vee \text{Plays}(x, \text{Go})$
 - c. C3: $(\sim \text{Likes}(x, \text{Oranges}) \wedge \text{Likes}(x, \text{Apples})) \vee (\sim \text{Likes}(x, \text{Apples}) \wedge \text{Likes}(x, \text{Oranges}))$
 - d. C4: $\text{Likes}(\text{John}, \text{Apples})$
 - e. C5: $(\sim \text{Likes}(f(x), F)) \vee \text{Likes}(x, F)$
- 4.

C6: $\sim \text{Plays}(\text{Mary}, \text{Go})$

C7: $\text{Plays}(\text{Mary}, \text{Go})$

$\sim (\text{Likes}(\text{Mary}, \text{Oranges}))$ C2

$\text{Likes}(\text{Mary}, \text{Apples})$ C3

$\text{Likes}(\text{John}, \text{Apples})$ C4

$\sim \text{Likes}(\text{Mary}, \text{Apples})$ C5

Contradiction: $\text{Likes}(\text{Mary}, \text{Apples}) \wedge \sim \text{Likes}(\text{Mary}, \text{Apples})$

Therefore, C6 is wrong, and $\text{Plays}(\text{Mary}, \text{Go})$ is true.

Conclusion: Based on the proof, the query $\text{Plays}(\text{Mary}, \text{Go})$ is true.