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CS 440

HW 10

1.

- a. $P(\text{BuyJersey} = \text{yes}) = 7/11 = 0.63$, $P(\text{BuyJersey} = \text{No}) = 1 - P(\text{BuyJersey}) = 1 - 0.63 = 0.37$
- b. $P(\text{Weather} = \text{clear}) = 4/11$, $P(\text{Weather} = \text{cloudy}) = 3/11$, $P(\text{Weather} = \text{rainy}) = 4/11$
 $P(\text{Weather} = \text{clear} \mid \text{BuyJersey} = \text{yes}) = 3/7$
 $P(\text{Weather} = \text{clear} \mid \text{BuyJersey} = \text{no}) = 1/4$
 $P(\text{Weather} = \text{cloudy} \mid \text{BuyJersey} = \text{yes}) = 2/7$
 $P(\text{Weather} = \text{cloudy} \mid \text{BuyJersey} = \text{No}) = 1/4$
 $P(\text{Weather} = \text{rainy} \mid \text{BuyJersey} = \text{Yes}) = 2/7$
 $P(\text{Weather} = \text{rainy} \mid \text{Buyjersey} = \text{No}) = 2/4$
- c. $P(\text{Uniform} = \text{Crimson} \mid \text{BuyJersey} = \text{Yes}) = 6/7$
 $P(\text{Uniform} = \text{Crimson} \mid \text{BuyJersey} = \text{No}) = 0/4$
 $P(\text{Unifrom} = \text{Gray} \mid \text{BuyJersey} = \text{Yes}) = 1/7$
 $P(\text{Unifrom} = \text{Gray} \mid \text{BuyJersey} = \text{No}) = 4/4$
- d. $P(\text{Win} = \text{yes} \mid \text{BuyJersey} = \text{Yes}) = 4/7$
 $P(\text{Win} = \text{Yes} \mid \text{BuyJersey} = \text{No}) = 3/4$
 $P(\text{Win} = \text{No} \mid \text{BuyJersey} = \text{Yes}) = 3/7$
 $P(\text{Win} = \text{No} \mid \text{BuyJersey} = \text{No}) = 3/4$
- e. $P(\text{BuyJersey} = \text{yes} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes}) = 0 = 1/2$
 $P(\text{BuyJersey} = \text{no} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes}) = 0 = 1/2$
- f. Since both $P(\text{BuyJersey} = \text{yes} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes})$ and $P(\text{BuyJersey} = \text{no} \mid \text{Weather} = \text{cloudy}, \text{Uniform} = \text{gray}, \text{Win} = \text{yes})$ is 50%, both $\text{BuyJersey} = \text{yes}$ and $\text{BuyJersey} = \text{no}$ class are possible to be chosen.

2.

a.

Weather	Uniform	Win	BuyJersey
0	0	1	1
0	0	0	1
0	1	1	1
0	1	0	0
1	0	1	1
1	0	0	1
1	1	0	0
2	0	1	1
2	0	0	1
2	1	1	0
2	1	0	0

- b. New instance: $\langle \text{Weather} = 1, \text{Uniform} = 1, \text{Win} = 1 \rangle$

Perceptron: $X_0W_0 + X_1W_1 + X_2W_2 + X_3W_3 = 1 + 1 + 1 + 1 = 4 \geq 0$. It would identify the new instance as YES.

c. J

Instance	Correct	W_0	W_1	W_2	W_3
0	NAN	1	1	1	1
1	True	1	1	1	1
2	True	1	1	1	1
3	True	1	1	1	1
4	False	$1-0.5=0.5$	$1+0 = 1$	$1-0.5=0.5$	1
5	True	0.5	1	0.5	1
6	True	0.5	1	0.5	1
7	False	$0.5-0.5=0$	$1-0.5=0.5$	$0.5-0.5=0$	1
8	True	0	0.5	0	1
9	True	0	0.5	0	1
10	False	-0.5	-0.5	-0.5	0.5
11	True	-0.5	-0.5	-0.5	0.5

d. New perceptron: $-0.5*1-0.5*1-0.5*1-0.5*1-0.5*1 < 0$
 New perceptron would identify this new instance as No