

L11: 6D Pose Estimation (Cont')

Hao Su

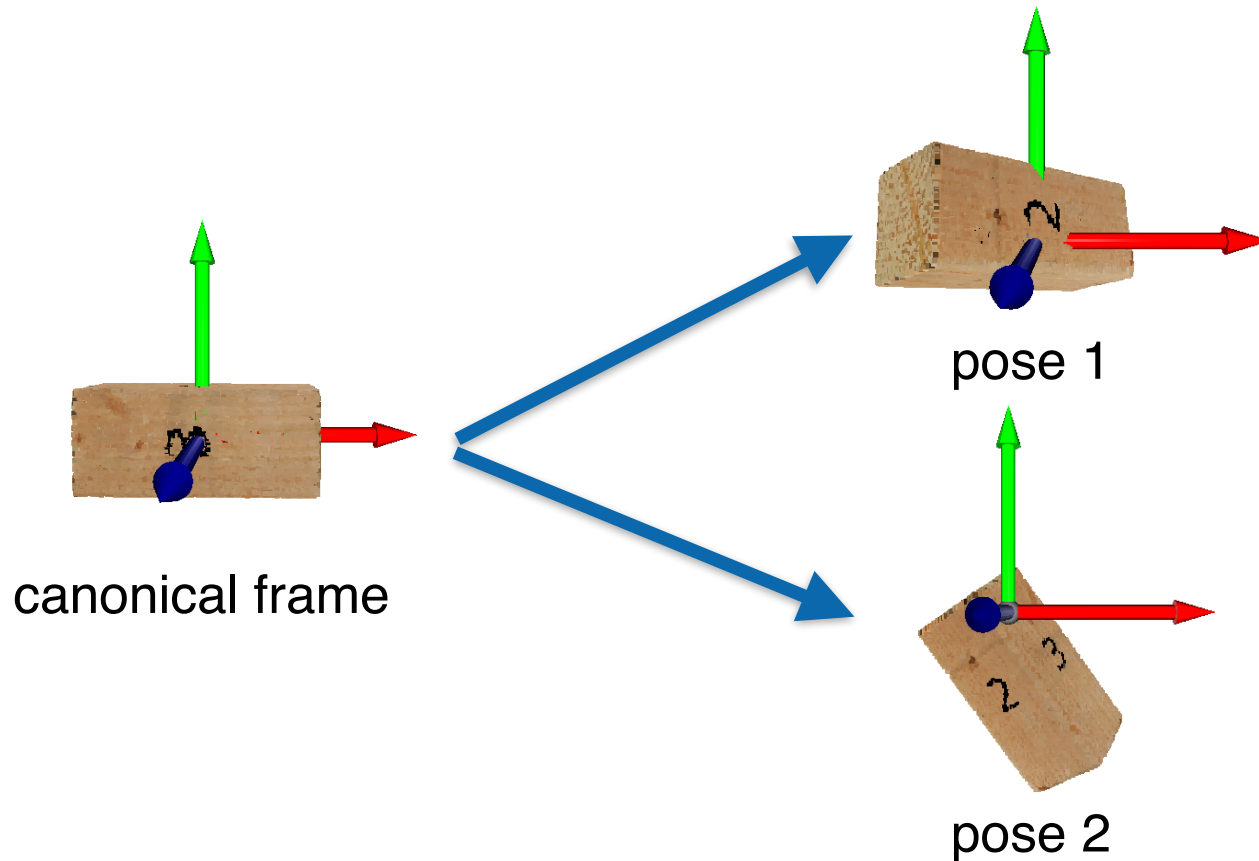
Ack: Minghua Liu and Jiayuan Gu for helping to prepare slides

We are talking about object pose



Figure from <https://paperswithcode.com/task/6d-pose-estimation>

6D Pose Estimation



recognize the 3D location and orientation
of an object relative to a canonical frame

Review

Agenda

- Introduction
- Rigid transformation estimation
 - Closed-form solution given correspondences
 - Iterative closet point (ICP)
- Learning-based approaches
 - Direct approaches
 - Indirect approaches

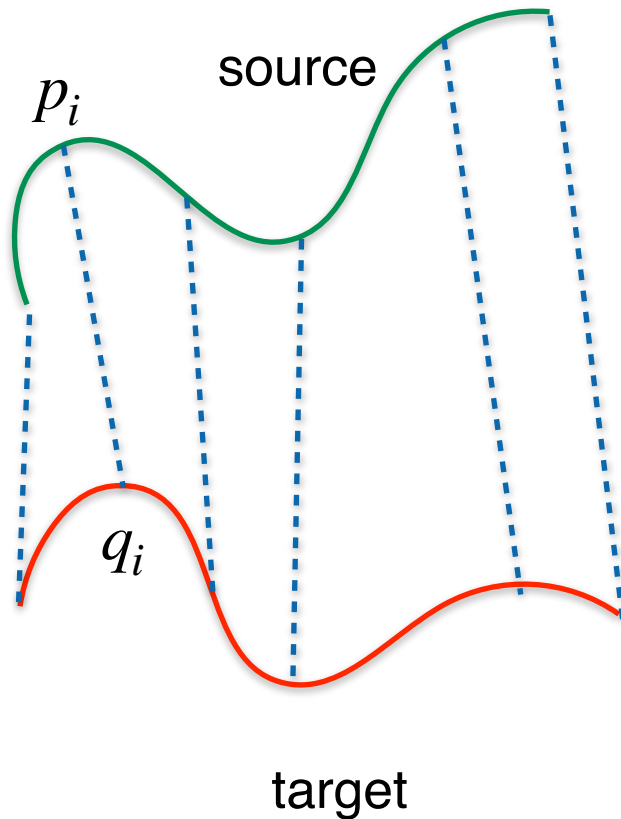
Review

Rigid Transformation Estimation

Review

Correspondence

Rigid transformation $T(p) = Rp + t$



$$q_1 = T(p_1) = Rp_1 + t$$

$$q_2 = T(p_2) = Rp_2 + t$$

\vdots

$$q_n = T(p_n) = Rp_n + t$$

3n equations from
n pairs of points

Review

Umeyama's Algorithm

- Known: $P = \{p_i\}$, $Q = \{q_i\}$
- Objective: $\min_{R,t} \sum_{i=1}^n \|Rp_i + t - q_i\|^2$
- Solution
 - $\sum_{i=1}^n (q_i - \bar{q})(p_i - \bar{p})^T = U\Sigma V^T$ (SVD)
 - $R = UV^T$ (flip the sign of the last column of V if $\det(R) = -1$)
 - $t = \frac{\sum_{i=1}^n q_i}{n} - \frac{\sum_{i=1}^n Rp_i}{n} := \bar{q} - R\bar{p}$

Review

Direct Approaches

Review

Direct Approaches

- Input: cropped image/point cloud/depth map of a single object
- Output: (R, t)



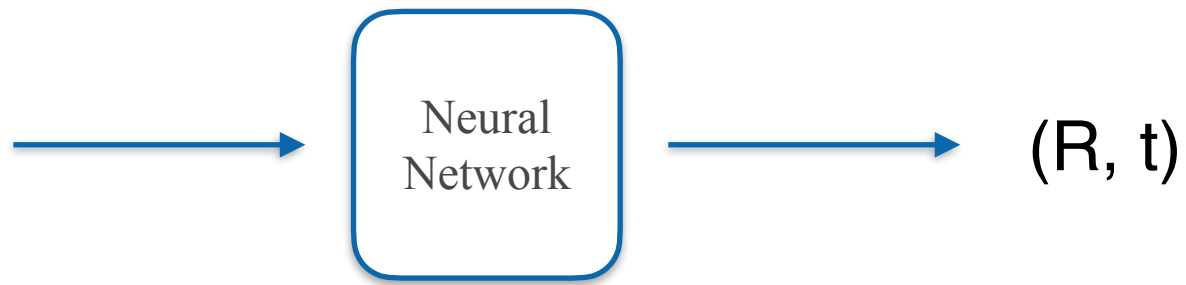
Image



Depth map



Point cloud



Review

Indirect Approaches

Indirect Approaches

- Input: cropped image/point cloud/depth map of a single object
- Output: corresponding pairs $\{(p_i, q_i)\}$
 - points in canonical frame $\{p_i\}$
 - points in camera frame $\{q_i\}$
 - estimate (R, t) by solving

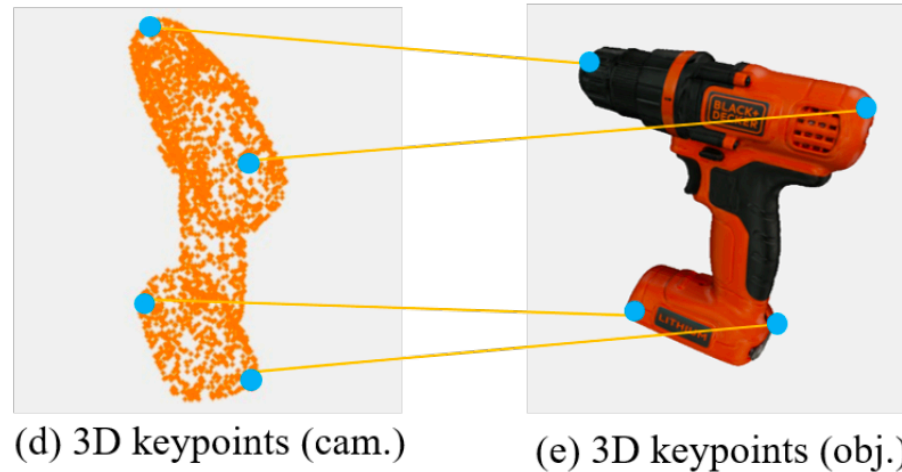
$$\min_{R, t} \sum_{i=1}^n \|Rp_i + t - q_i\|^2$$

Two Categories of Indirect Approaches

- If points in the **canonical frame** are known, predict their corresponding locations in the **camera frame**
- If points in the **camera frame** are known, predict their corresponding locations in the **canonical frame**

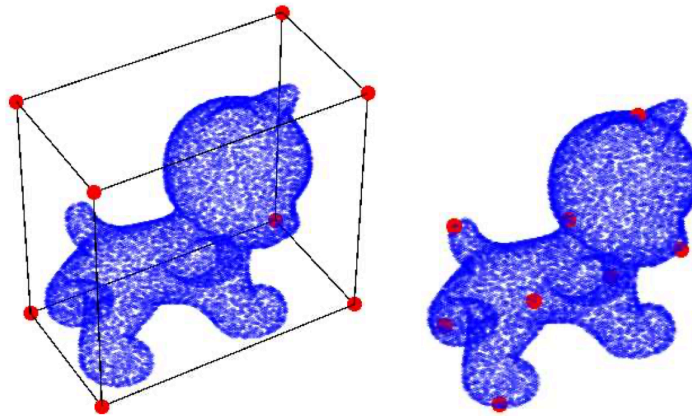
Given Points in the **Canonical Frame**, Predict Corresponding Location in the **Camera Frame**

- Recall: Three correspondences are enough
- Which points in the canonical frame should be given?
 - Choice by PVN3D: keypoints in the canonical frame

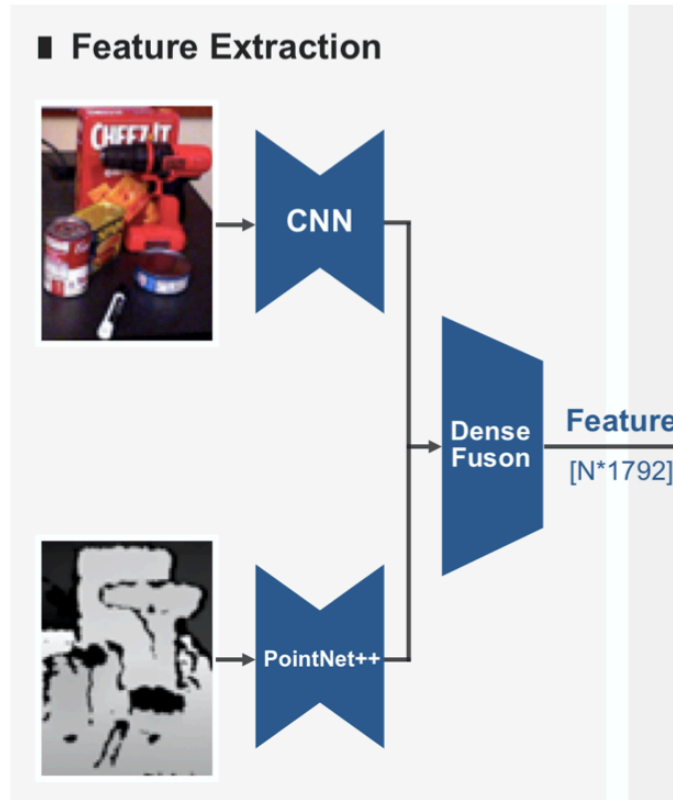


Keypoint Selection

- Option1: bounding box vertices
- Option 2: farthest point sampling (FPS) over CAD object model

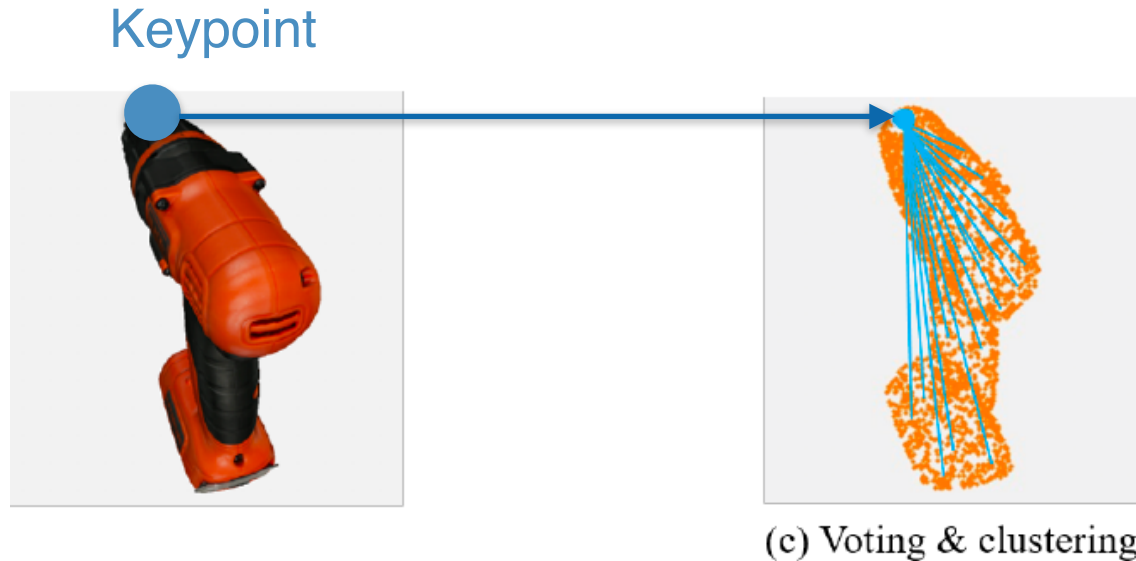


Example: PVN3D



Get point-wise features
by fusing color and geometry features

Example: PVN3D

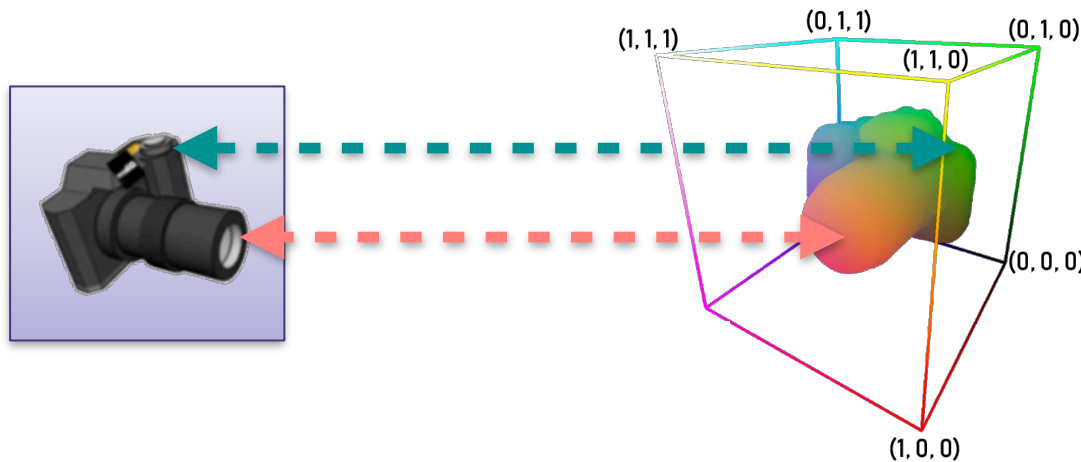


For each keypoint:

- **Voting**: for each point in the camera frame, predict its offset to the keypoint (in the camera frame)
- **Clustering**: find one location according to all the candidates

Given Points in the **Camera Frame**, Predict Corresponding Location in the **Canonical Frame**

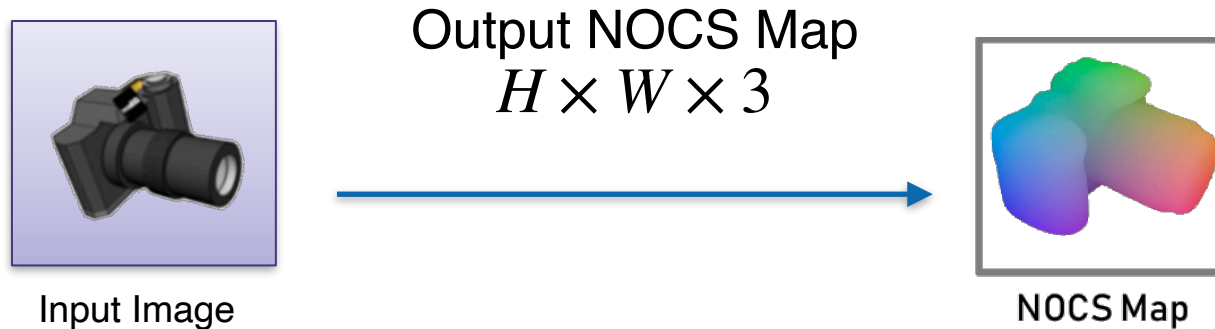
- Which points in the camera frame should be given?
 - Choice by NOCS: every point in the camera frame



3D point in the camera frame
(2D visible pixel with depth)

3D point in the (normalized)
canonical frame

Example: NOCS



Note: the object is normalized to have unit diagonal of bounding box in the canonical space, so the canonical space is called “Normalized Object Canonical Space” (NOCS)

Example: NOCS for Symmetric Objects

- Given equivalent GT rotations
 $\mathcal{R} = \{R_{GT}^1, R_{GT}^2, \dots, R_{GT}^n\}$ (finite symmetry order n),
we can generate n equivalent NOCS maps
- Similar to shape-agnostic loss in direct approaches,
we can use *Min of N* loss

Umeyama's Algorithm with Unknown Scale

- However, the target points in the canonical space of NOCS are normalized, and thus we also need to predict the scale factor
- Similarity transformation estimation (rigid transformation + uniform scale factor)
- Closed-form solution
 - Umeyama algorithm: <http://web.stanford.edu/class/cs273/refs/umeyama.pdf>
 - Similar to the counterpart without scale

Tips for Homework 2

- For learning-based approaches
 - Start with direct approaches
 - Crop the point cloud of each object from GT depth map given GT segmentation mask
 - Train a neural network, e.g. PointNet, with shape-agnostic loss
 - Improve the results considering symmetry