



Figure 1. An illustration of the proposed graph pooling layer with  $k = 2$ .  $\times$  and  $\odot$  denote matrix multiplication and element-wise product, respectively. We consider a graph with 4 nodes, and each node has 5 features. By processing this graph, we obtain the adjacency matrix  $A^\ell \in \mathbb{R}^{4 \times 4}$  and the input feature matrix  $X^\ell \in \mathbb{R}^{4 \times 5}$  of layer  $\ell$ . In the projection stage,  $p \in \mathbb{R}^5$  is a trainable projection vector. By matrix multiplication and sigmoid( $\cdot$ ), we obtain  $y$  that are scores estimating scalar projection values of each node to the projection vector. By using  $k = 2$ , we select two nodes with the highest scores and record their indices in the top-k-node selection stage. We use the indices to extract the corresponding nodes to form a new graph, resulting in the pooled feature map  $\tilde{X}^\ell$  and new corresponding adjacency matrix  $A^{\ell+1}$ . At the gate stage, we perform element-wise multiplication between  $\tilde{X}^\ell$  and the selected node scores vector  $\tilde{y}$ , resulting in  $X^{\ell+1}$ . This graph pooling layer outputs  $A^{\ell+1}$  and  $X^{\ell+1}$ .