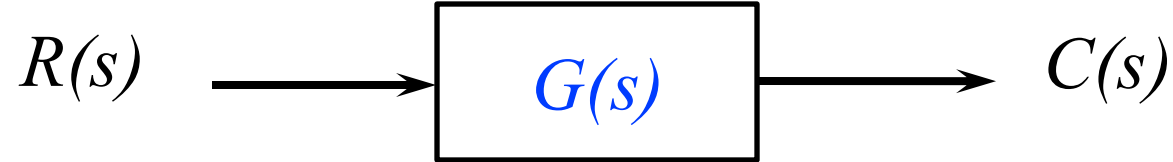


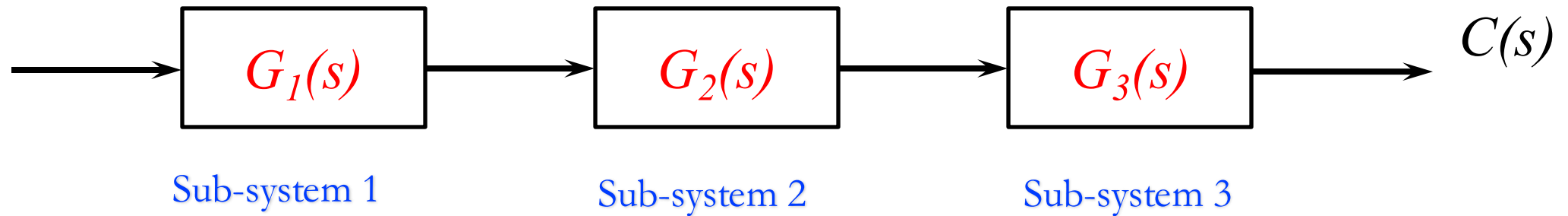
# Mechatronic Modeling and Design with Applications in Robotics

## Graphical Models

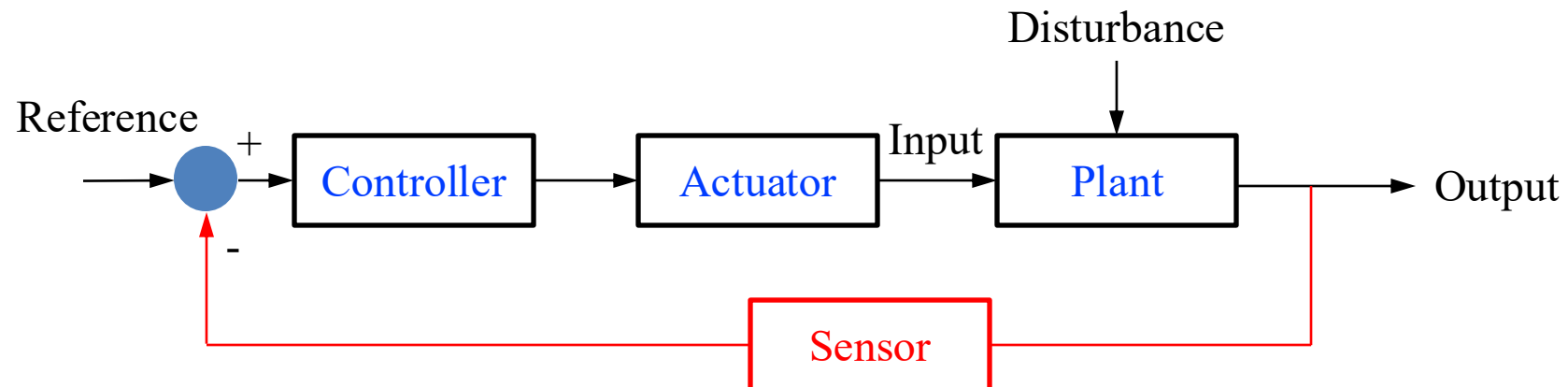


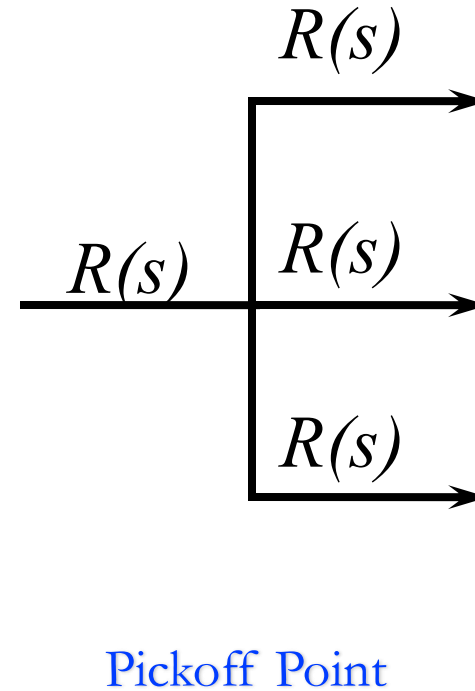
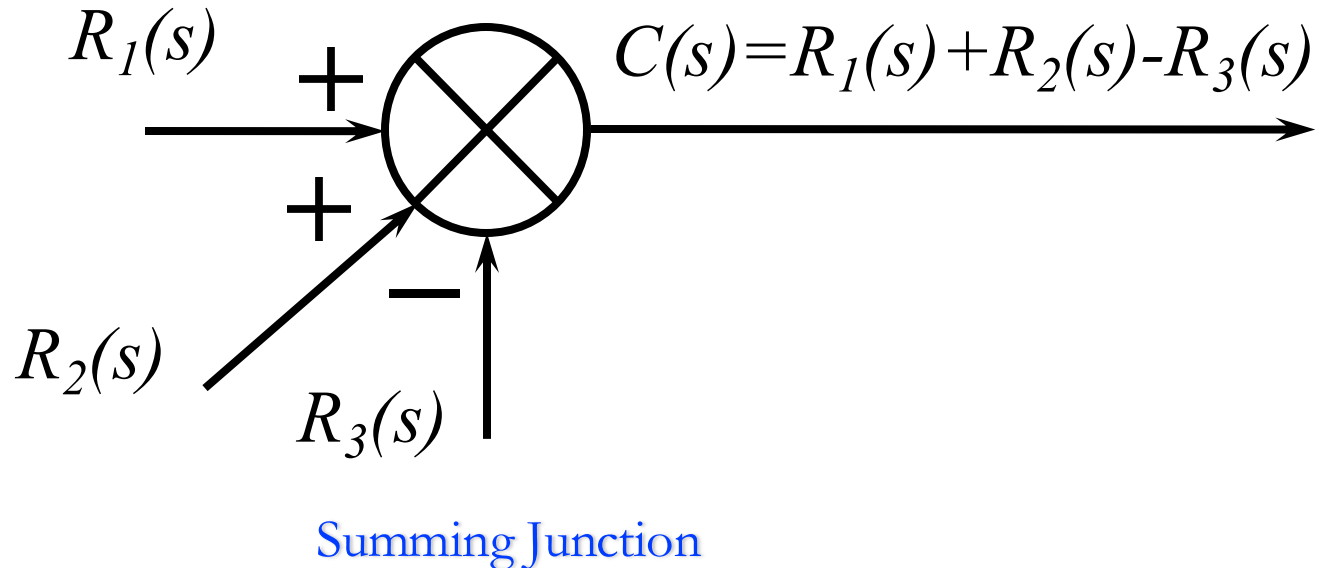
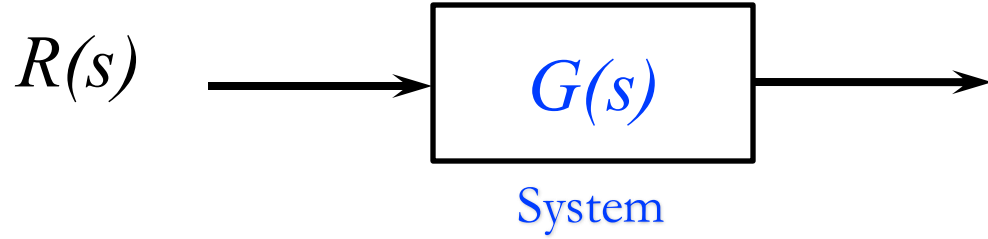
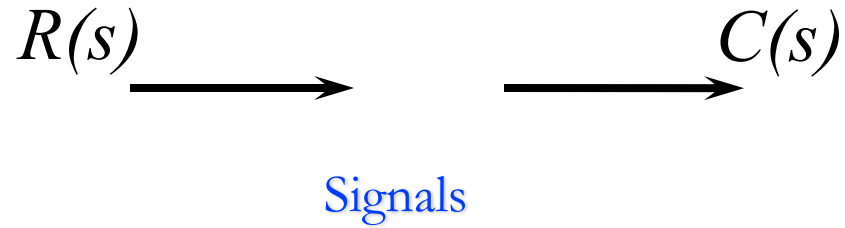


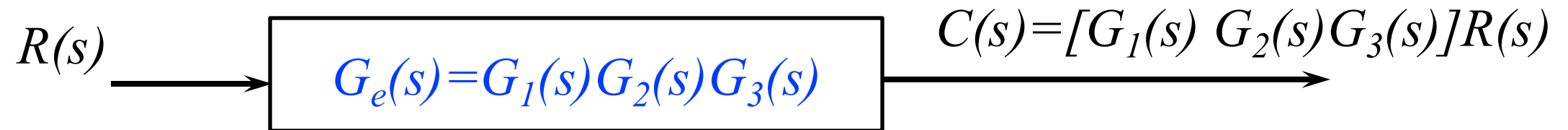
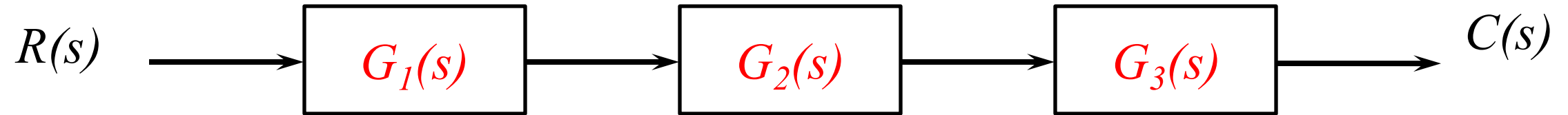
Systems usually are composed of multiple subsystems:

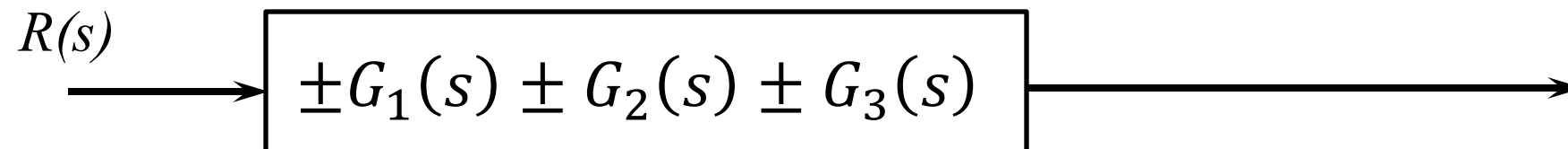
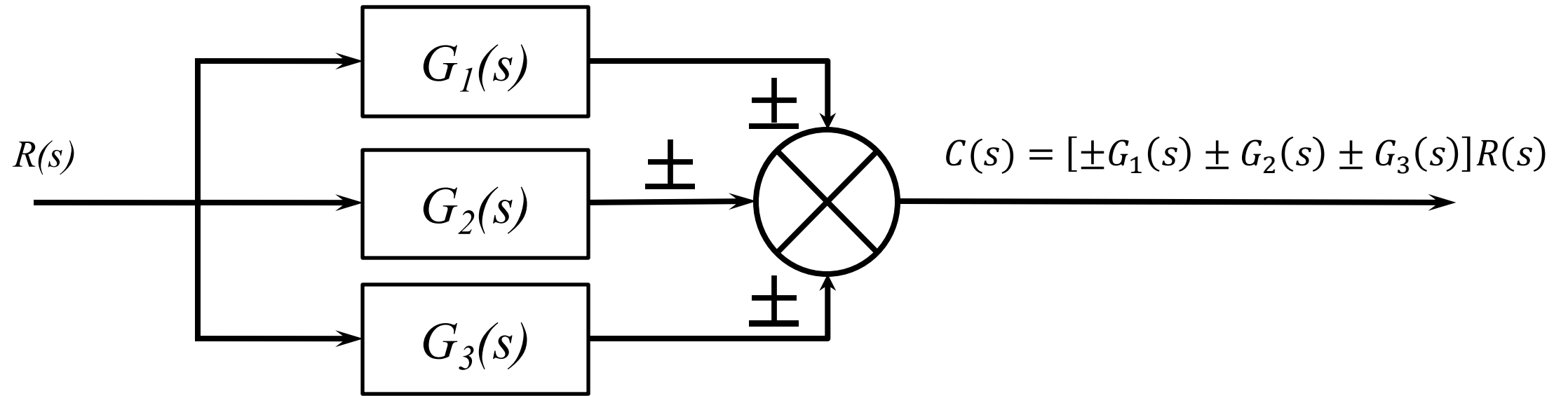


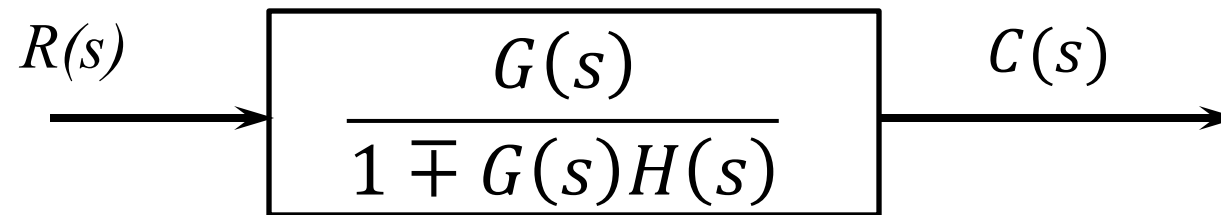
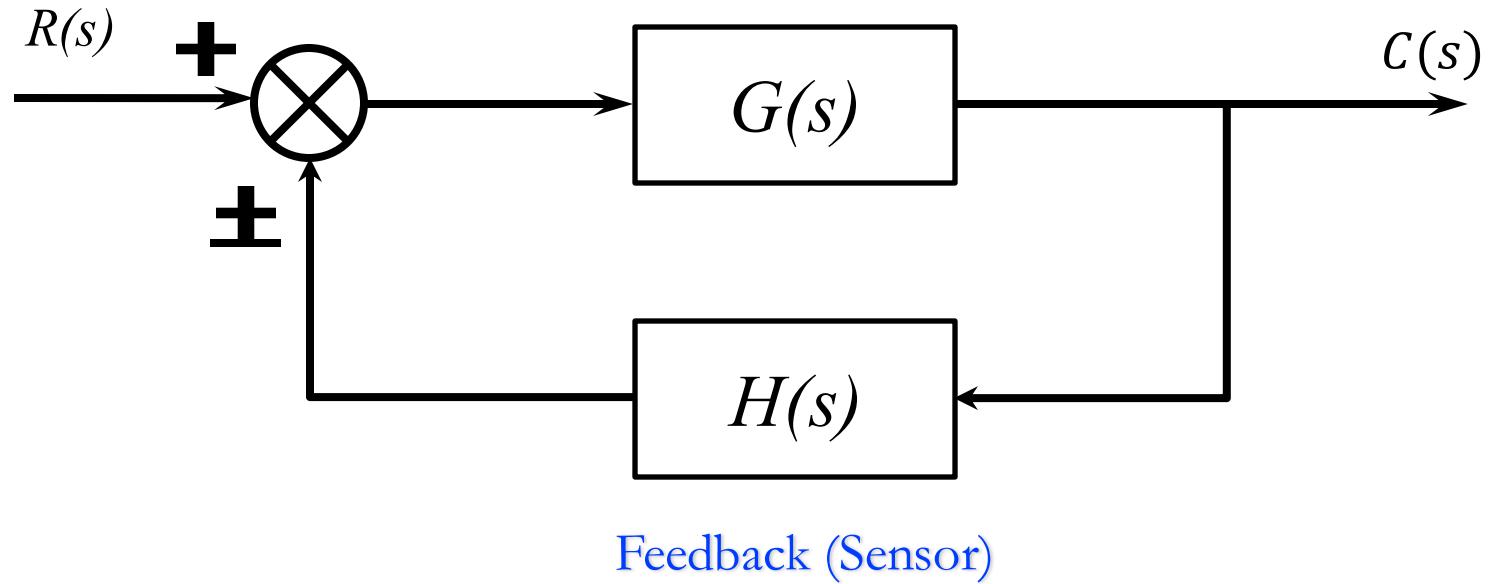
More complex control block diagram (e.g., Feedback)

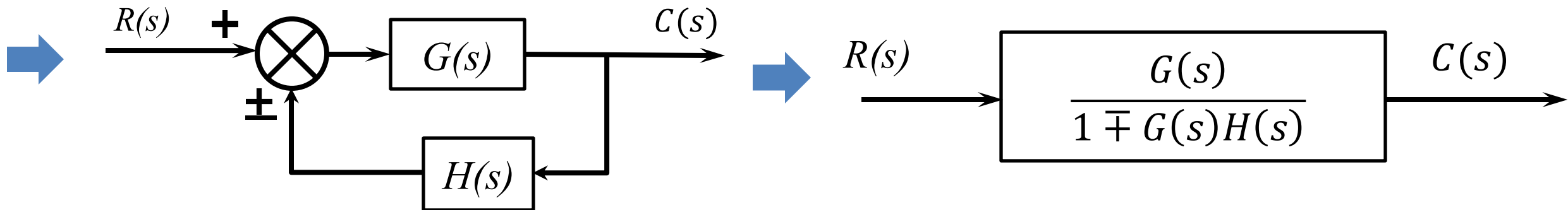
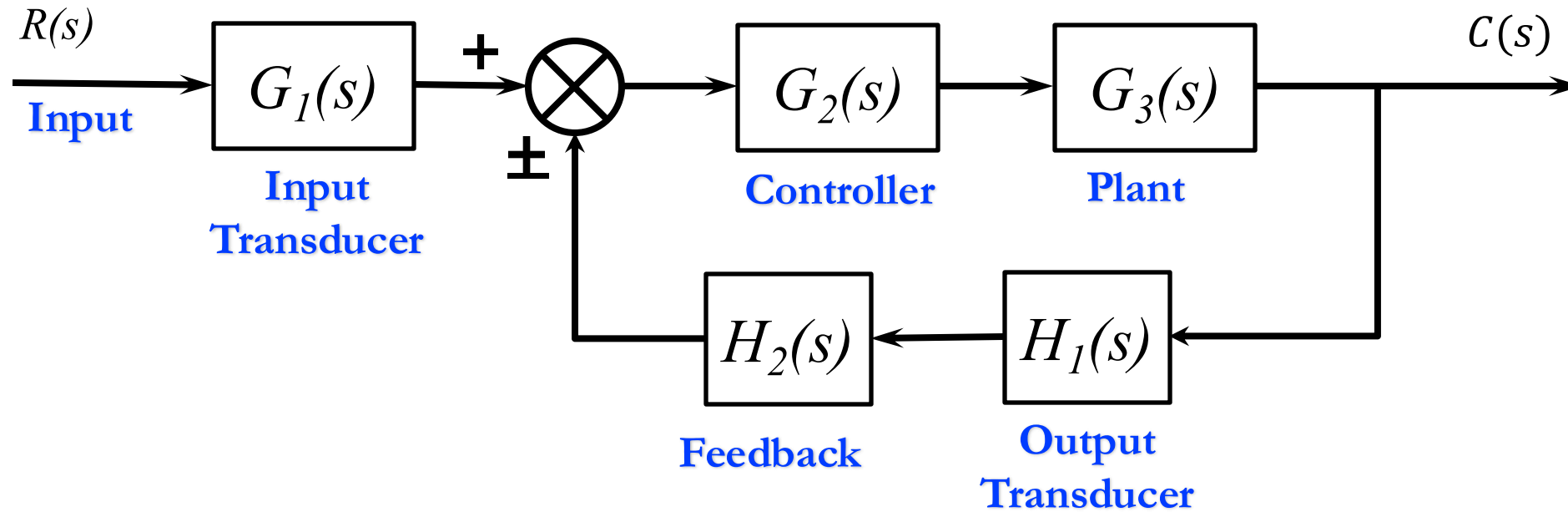






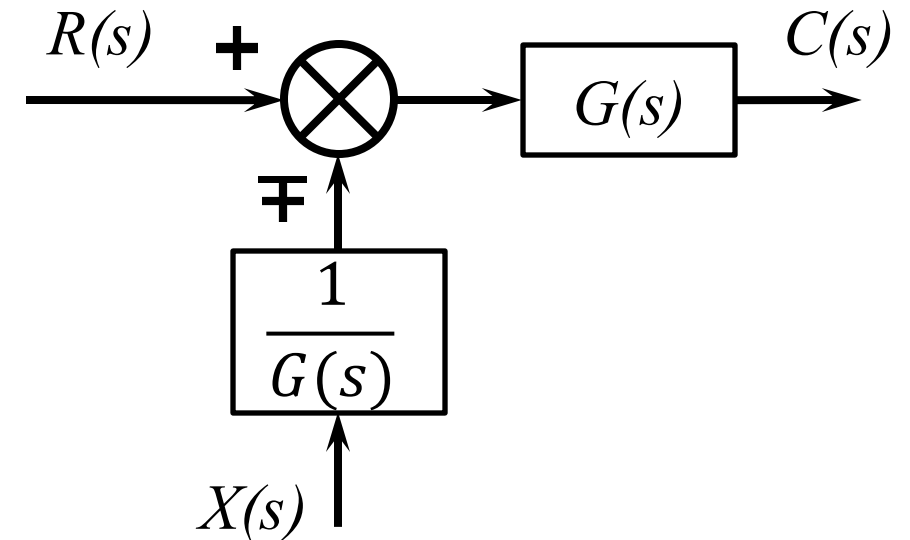
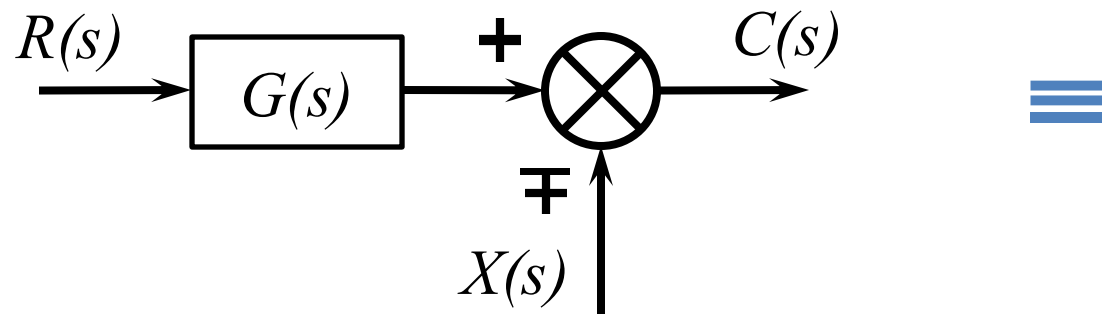
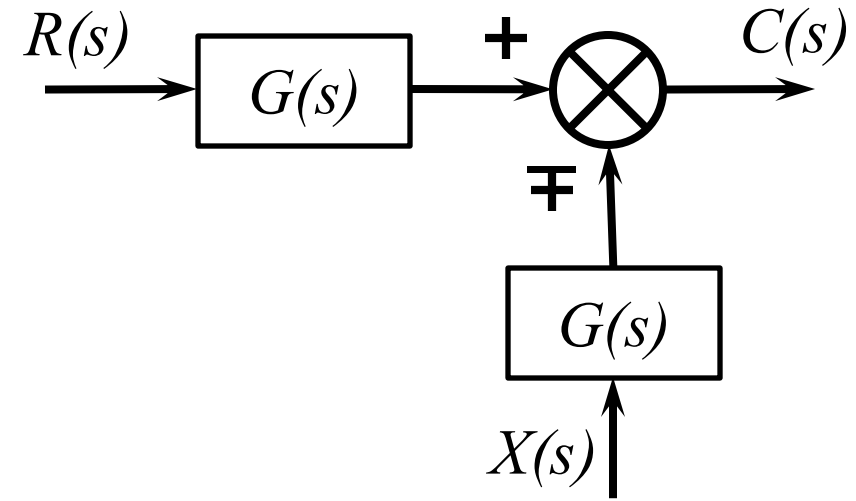
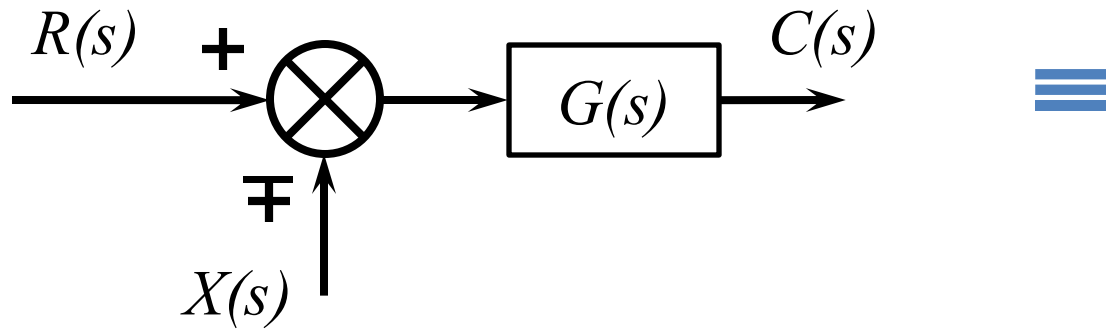


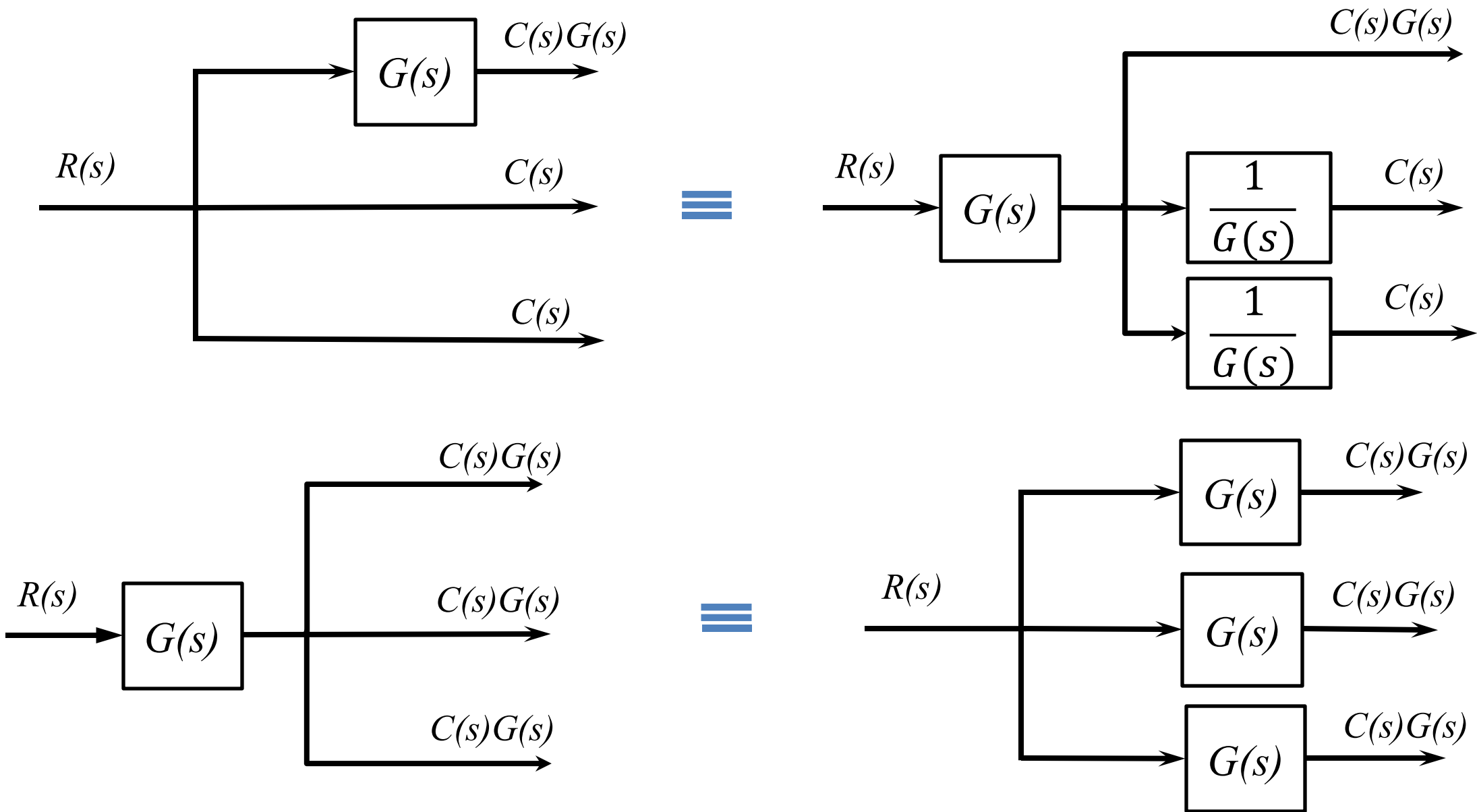


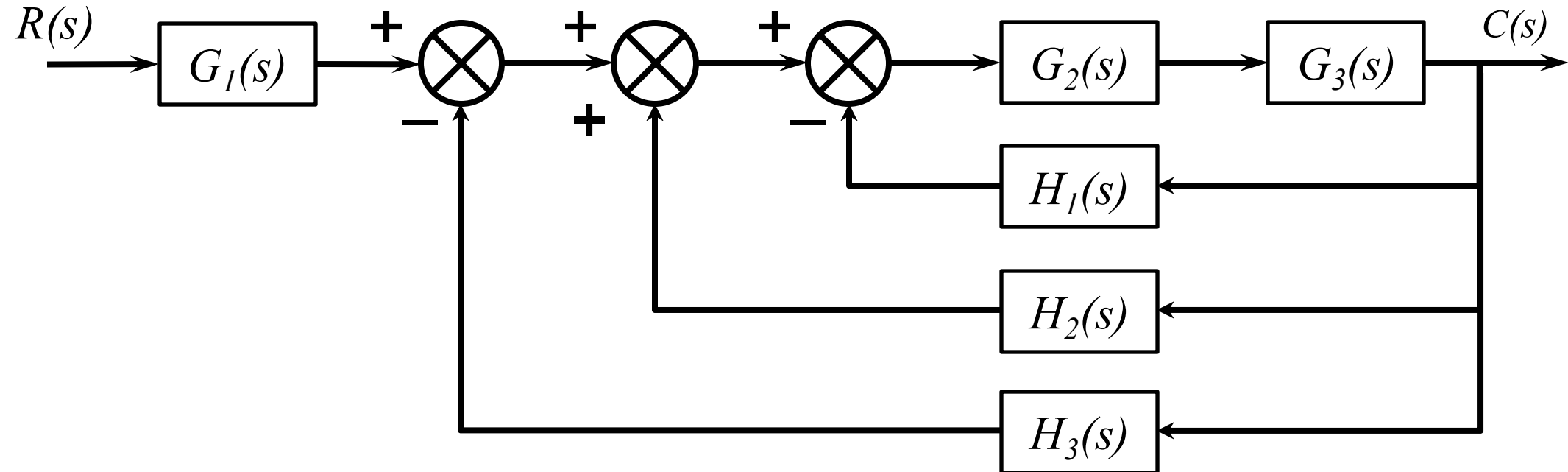




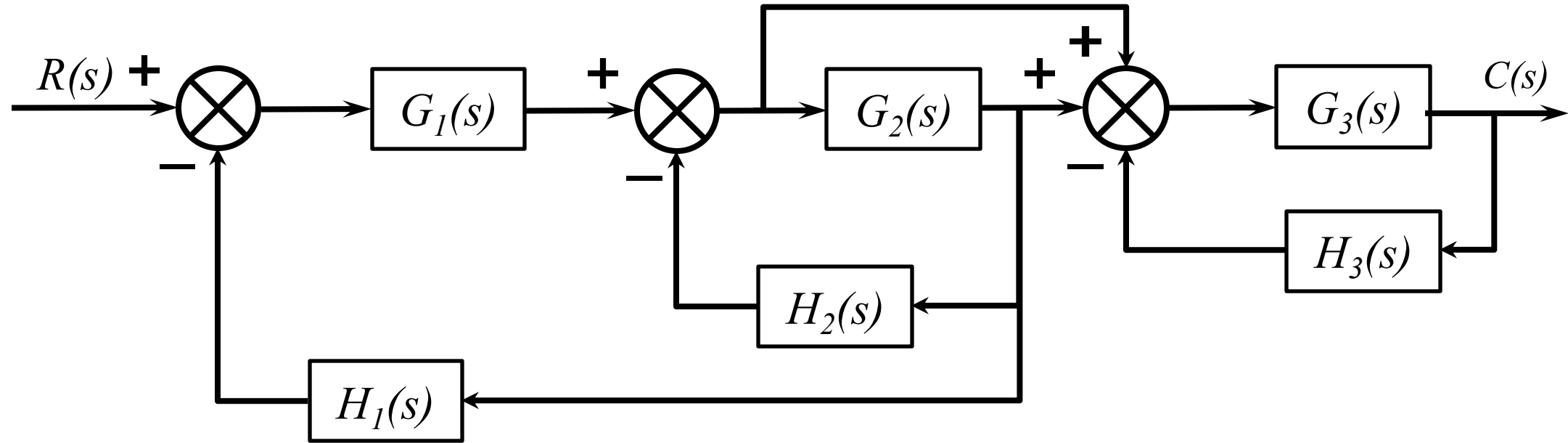
# Moving a Summing Junction















A system is represented by a line with an arrow showing the direction of signal flow through the system.



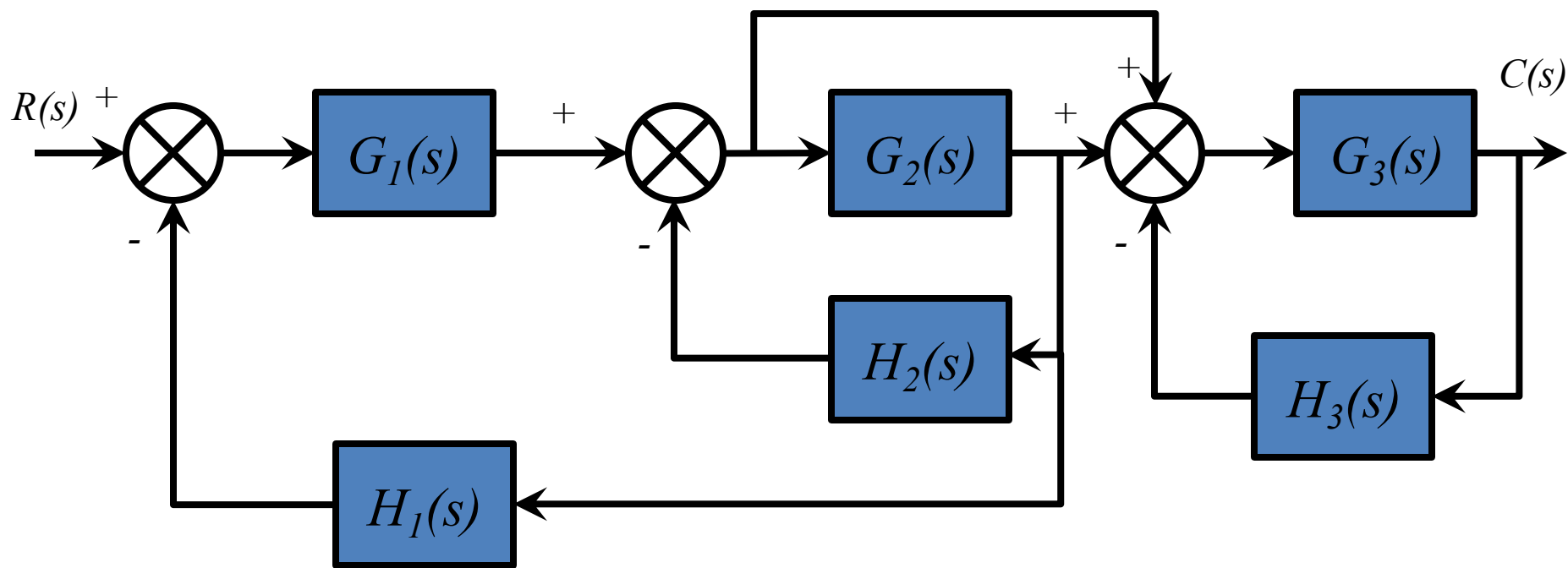
A signal-flow graph consists only **branches** and **nodes**:

**Branches:** represent **systems**

**Nodes:** represent **signals**







## **Loop Gain:**

The product of branch gains found by traversing a path that starts at a node and ends at the same node, following the direction of the signal flow, without passing through any other node more than once.

## **Forward-path Gain:**

The product of gains found by traversing a path from the input node to the output node of the signal-flow graph in the direction of signal flow.

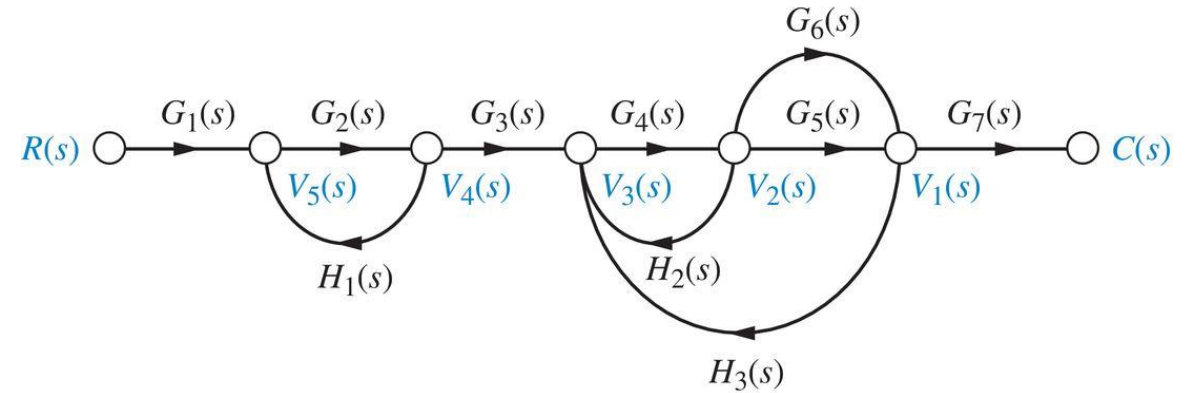
## **Non-touching Loops:**

Loops that do not have any nodes in common.

## **Non-Touching-Loop Gain:**

The product of loop gains from non-touching loops taken two, three four, or more at a time

Loop Gain:



Forward-path Gain:

Non-touching Loops:

Non-Touching-Loop Gain:

$$G(s) = \frac{C(s)}{R(s)} = \frac{\sum_k T_k \Delta_k}{\Delta}$$

$k$  = number of forward paths

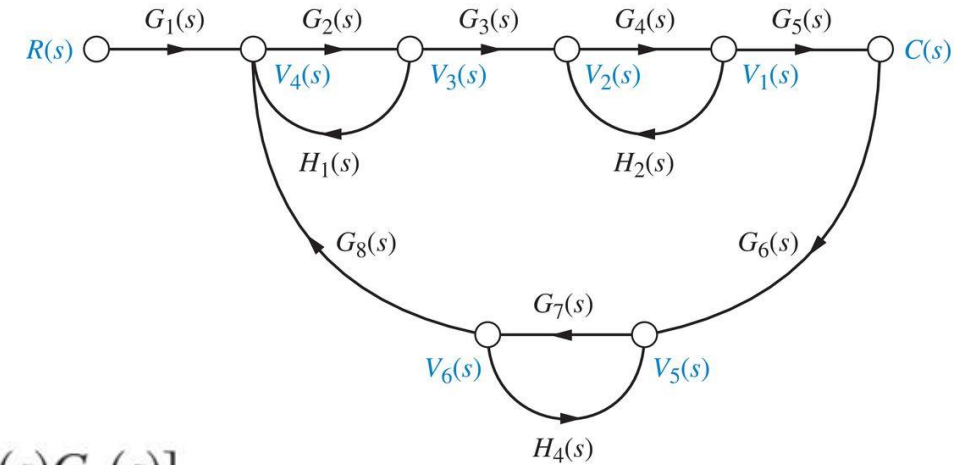
$T_k$  = the  $k$ th forward-path gain

$\Delta$  =  $1 - \sum$  loop gains +  $\sum$  non-touching loop gains  
taken two at a time  $- \sum$  non-touching loop gains  
taken three at a time +  $\sum$  non-touching loop gains  
taken four at a time ...

$\Delta_k$  =  $\Delta - \sum$  loop gain terms in  $\Delta$  that touch the  $k$ th forward path. In other words,  
 $\Delta_k$  is formed by eliminating from  $\Delta$  those loop gains that touch the  $k$ th forward  
path.

Find the transfer function,  $C(s)/R(s)$  for the signal-flow-graph:

$$G(s) = \frac{T_1 \Delta_1}{\Delta} = \frac{[G_1(s)G_2(s)G_3(s)G_4(s)G_5(s)][1 - G_7(s)H_4(s)]}{\Delta}$$



$$\begin{aligned} \Delta = & 1 - [G_2(s)H_1(s) + G_4(s)H_2(s) + G_7(s)H_4(s) \\ & + G_2(s)G_3(s)G_4(s)G_5(s)G_6(s)G_7(s)G_8(s)] \\ & + [G_2(s)H_1(s)G_4(s)H_2(s) + G_2(s)H_1(s)G_7(s)H_4(s) \\ & + G_4(s)H_2(s)G_7(s)H_4(s)] \\ & - [G_2(s)H_1(s)G_4(s)H_2(s)G_7(s)H_4(s)] \end{aligned}$$

Consider the following state and output equations:

$$\begin{cases} \dot{x}_1 = 2x_1 - 5x_2 + 3x_3 + 2r \\ \dot{x}_2 = -6x_1 - 2x_2 + 2x_3 + 5r \\ \dot{x}_3 = x_1 - 3x_2 - 4x_3 + 7r \\ y = -4x_1 + 6x_2 + 9x_3 \end{cases}$$

where  $r$  is the input,  $y$  is the output,  $x_1$ ,  $x_2$  and  $x_3$  are the state variables, please draw its signal-flow graph.

