Chapter 1

Demo problem: Large-amplitude shear deformation of a 3D elastic solid

Detailed documentation to be written. Here's the already fairly well documented driver code...

```
//LIC// This file forms part of oomph-lib, the object-oriented,
//LIC// multi-physics finite-element library, available
//LIC// at http://www.oomph-lib.org.
//LIC//
           Version 1.0; svn revision $LastChangedRevision$
//T.TC//
//LIC// $LastChangedDate$
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//LIC//
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//LIC// The authors may be contacted at oomph-lib@maths.man.ac.uk.
// Driver for elastic deformation of a cuboidal domain
// The deformation is a simple shear in the x-z plane driven by
// motion of the top boundary, for exact solution see Green & Zerna
// Generic oomph-lib headers
#include "generic.h"
// Solid mechanics
#include "solid.h"
#include "meshes/simple_cubic_mesh.template.h"
using namespace std;
using namespace oomph;
/// Simple cubic mesh upgraded to become a solid mesh
```

```
template<class ELEMENT>
class ElasticCubicMesh : public virtual SimpleCubicMesh<ELEMENT>,
                     public virtual SolidMesh
public:
 /// \short Constructor:
ElasticCubicMesh(const unsigned &nx, const unsigned &ny, const unsigned &nz,
               const double &a, const double &b, const double &c,
TimeStepper* time_stepper_pt=&Mesh::Default_TimeStepper) :
  SimpleCubicMesh<ELEMENT>(nx,ny,nz,-a,a,-b,b,-c,c,time_stepper_pt)
  //Assign the initial lagrangian coordinates
  set_lagrangian_nodal_coordinates();
 /// Empty Destructor
virtual ~ElasticCubicMesh() { }
} ;
/// Global variables
namespace Global_Physical_Variables
 /// Pointer to strain energy function
StrainEnergyFunction* Strain_energy_function_pt;
 /// Pointer to constitutive law
ConstitutiveLaw* Constitutive law pt;
 /// Elastic modulus
double E=1.0;
 /// Poisson's ratio
double Nu=0.3;
 /// "Mooney Rivlin" coefficient for generalised Mooney Rivlin law
double C1=1.3;
 /// Body force
double Gravity=0.0;
 /// Body force vector: Vertically downwards with magnitude Gravity
 void body_force(const Vector<double>& xi,
              const double& t,
              Vector<double>& b)
 b[0]=0.0;
 b[1]=-Gravity;
/// Boundary-driven elastic deformation of fish-shaped domain.
template<class ELEMENT>
class SimpleShearProblem : public Problem
double Shear;
void set_incompressible(ELEMENT *el_pt,const bool &incompressible);
public:
 /// Constructor:
```

```
SimpleShearProblem(const bool &incompressible);
 /// Run simulation.
void run(const std::string &dirname);
 /// Access function for the mesh
ElasticCubicMesh<ELEMENT>* mesh_pt()
  {return dynamic_cast<ElasticCubicMesh<ELEMENT>*>(Problem::mesh_pt());}
/// Doc the solution
void doc_solution(DocInfo& doc_info);
 /// Update function (empty)
void actions_after_newton_solve() {}
 /// \short Update before solve: We're dealing with a static problem so
 /// the nodal positions before the next solve merely serve as
 /// initial conditions. For meshes that are very strongly refined
 /// near the boundary, the update of the displacement boundary
 /// conditions (which only moves the SolidNodes *on* the boundary),
 /// can lead to strongly distorted meshes. This can cause the
 /// Newton method to fail \operatorname{\dashrightarrow} the overall method is actually more robust
 /// if we use the nodal positions as determined by the <code>Domain/MacroElement-</code>
 /// based mesh update as initial guesses.
 void actions_before_newton_solve()
   apply_boundary_conditions();
   bool update_all_solid_nodes=true;
   mesh_pt()->node_update(update_all_solid_nodes);
 ///Shear the top
 void apply_boundary_conditions()
   unsigned ibound = 5;
   unsigned num_nod=mesh_pt()->nboundary_node(ibound);
   for (unsigned inod=0;inod<num_nod;inod++)</pre>
     SolidNode *solid_nod_pt = static_cast<SolidNode*>(
    mesh_pt()->boundary_node_pt(ibound,inod));
     solid nod pt->x(0) = solid nod pt->xi(0) + Shear*
     solid_nod_pt->xi(2);
};
/// Constructor:
template<class ELEMENT>
SimpleShearProblem<ELEMENT>::SimpleShearProblem(const bool &
     incompressible)
: Shear (0.0)
{
double a = 1.0, b = 1.0, c = 1.0;
unsigned nx = 5, ny = 5, nz = 5;
 // Build mesh
Problem::mesh_pt()=new ElasticCubicMesh<ELEMENT>(nx,ny,nz,a,b,c);
 //Loop over all boundaries
 for (unsigned b=0;b<6;b++)</pre>
   //Loop over nodes in the boundary
   unsigned n_node = mesh_pt()->nboundary_node(b);
   for (unsigned n=0;n<n_node;n++)</pre>
     //Pin all nodes in the y and z directions to keep the motion in plane
     for (unsigned i=1;i<3;i++)</pre>
       mesh_pt()->boundary_node_pt(b,n)->pin_position(i);
     //On the top and bottom pin the positions in \boldsymbol{\boldsymbol{x}}
     if((b==0) | (b==5))
       mesh_pt()->boundary_node_pt(b,n)->pin_position(0);
      }
    }
 //Loop over the elements in the mesh to set parameters/function pointers
 unsigned n_element =mesh_pt()->nelement();
 for(unsigned i=0;i<n_element;i++)</pre>
   //Cast to a solid element
```

```
ELEMENT *el_pt = dynamic_cast<ELEMENT*>(mesh_pt()->element_pt(i));
   // Set the constitutive law
   el_pt->constitutive_law_pt() =
   Global_Physical_Variables::Constitutive_law_pt;
   set_incompressible(el_pt,incompressible);
   // Set the body force
   //el_pt->body_force_fct_pt()=Global_Physical_Variables::body_force;
// Pin the redundant solid pressures (if any)
 //PVDEquationsBase<2>::pin_redundant_nodal_solid_pressures(
 // mesh_pt()->element_pt());
 //Attach the boundary conditions to the mesh
cout << assign_eqn_numbers() << std::endl;
/// Doc the solution
template<class ELEMENT>
void SimpleShearProblem<ELEMENT>::doc_solution(DocInfo& doc_info)
ofstream some_file;
char filename[100];
 // Number of plot points
unsigned npts = 5;
// Output shape of deformed body
sprintf(filename,"%s/soln%i.dat",doc_info.directory().c_str(),
         doc_info.number());
some_file.open(filename);
mesh_pt()->output(some_file,npts);
some_file.close();
sprintf(filename,"%s/stress%i.dat", doc_info.directory().c_str(),
         doc info.number());
some_file.open(filename);
//Output the appropriate stress at the centre of each element Vector < double > s(3,0.0);
Vector<double> x(3);
DenseMatrix<double> sigma(3,3);
 unsigned n_element = mesh_pt() ->nelement();
 for (unsigned e=0;e<n_element;e++)</pre>
   ELEMENT* el_pt = dynamic_cast<ELEMENT*>(mesh_pt()->element_pt(e));
   el_pt->interpolated_x(s,x);
   el_pt->get_stress(s, sigma);
   //Output
   for (unsigned i=0;i<3;i++)</pre>
     some_file << x[i] << " ";
   for (unsigned i=0;i<3;i++)</pre>
     for(unsigned j=0; j<3; j++)</pre>
       some_file << sigma(i,j) << " ";</pre>
   some_file << std::endl;
 some_file.close();
}
/// Run the problem
template<class ELEMENT>
void SimpleShearProblem<ELEMENT>::run(const std::string &dirname)
 // Output
DocInfo doc_info;
// Set output directory
doc_info.set_directory(dirname);
```

```
// Step number
doc_info.number()=0;
// Initial parameter values
 // Gravity:
Global_Physical_Variables::Gravity=0.1;
 //Parameter incrementation
unsigned nstep=2;
 for (unsigned i=0;i<nstep;i++)</pre>
   //Solve the problem with Newton's method, allowing for up to 5
   //rounds of adaptation
   newton_solve();
   // Doc solution
   doc_solution(doc_info);
   doc_info.number()++;
   //Increase the shear
   Shear += 0.5;
}
template<>
void SimpleShearProblem<QPVDElement<3,3> >::set_incompressible(
QPVDElement<3,3> *el_pt, const bool &incompressible)
//Does nothing
template<>
void SimpleShearProblem<QPVDElementWithPressure<3> >
      ::set_incompressible(
QPVDElementWithPressure<3> *el_pt, const bool &incompressible)
{
if(incompressible) {el_pt->set_incompressible();}
else {el_pt->set_compressible();}
template<>
void SimpleShearProblem<QPVDElementWithContinuousPressure<3>
set_incompressible(
QPVDElementWithContinuousPressure<3> *el_pt, const bool &incompressible)
if(incompressible) {el_pt->set_incompressible();}
else {el_pt->set_compressible();}
/// Driver for simple elastic problem
int main()
 //Initialise physical parameters
Global_Physical_Variables::E = 2.1;
Global_Physical_Variables::Nu = 0.4;
Global_Physical_Variables::C1 = 1.3;
  for (unsigned i=0;i<2;i++)</pre>
// Define a strain energy function: Generalised Mooney Rivlin
Global_Physical_Variables::Strain_energy_function_pt =
 new GeneralisedMooneyRivlin(&Global_Physical_Variables::Nu,
                                &Global_Physical_Variables::C1,
                                &Global_Physical_Variables::E);
 // Define a constitutive law (based on strain energy function)
 Global_Physical_Variables::Constitutive_law_pt
  new IsotropicStrainEnergyFunctionConstitutiveLaw(
   Global_Physical_Variables::Strain_energy_function_pt
      ) ;
  //Set up the problem with pure displacement formulation
  SimpleShearProblem<QPVDElement<3,3> > problem(false);
 problem.run("RESLT");
 //Discontinuous pressure
```

```
{
//Set up the problem with pure displacement formulation
SimpleShearProblem
(false);
problem.run("RESLT_pres");
}

/*{
//Set up the problem with pure displacement formulation
SimpleShearProblem
(PRESLT_pres_incomp");
}*/

{
//Set up the problem with pure displacement formulation
SimpleShearProblem
(PRESLT_pres_incomp");
}*/

{
//Set up the problem with pure displacement formulation
SimpleShearProblem
(PVDElementWithContinuousPressure
> problem.run("RESLT_cont_pres");
}

/*{
//Set up the problem with pure displacement formulation
SimpleShearProblem
(PVDElementWithContinuousPressure
> problem.run("RESLT_cont_pres_incomp");
}*/

/*
}
```

1.1 PDF file

A pdf version of this document is available.