

3.1 5730

3.2 5730

3.3 0101 1110 1101 0100

The attraction is that each hex digit contains one of 16 different characters (0-9, A-E). Since with 4 binary bits you can represent 16 different patterns, in hex each digit requires exactly 4 binary bits.

And bytes are defined as 8 bits long, so two hex digits are all that are required to represent the contents of 1 byte.

3.4 4365

3412

753

→ 753₍₈₎

3.5 4365 → -365

-365

-3412

(-3777)

|||| ||| ||| || → 7777

3.6 185

$$\begin{array}{r} 185 \\ -122 \\ \hline 63 \end{array}$$

Neither up overflow nor down overflow.

3.7 $185 \rightarrow 10111001 \rightarrow -57$
"2's"

$$185 + 122 = -57 + 122 = 65$$

Neither up-overflow nor down-overflow.

3.8 $-57 - 122 = -179 < -128$

Overflow

3.13 62 X 12

Step	Action	Multiplicand	Product / Multiplier
0	Initial Vals	0110 0010	0 0000 0000 0000 / 0010
1	lsb=0	0110 0010	0 0000 0000 0000 / 0010
	Rshift	0110 0010	0 0000 0000 0000 / 0010
2	lsb=1	0110 0010	0 0110 0010 0000 / 0010
	Rshift	0110 0010	0 0011 0001 0000 / 0010
3	lsb=0	0110 0010	0 0011 0001 0000 / 0010
	Rshift	0110 0010	0 0001 1000 1000 0010
4	lsb=0	0110 0010	0 0001 1000 1000 0010
	Rshift	0110 0010	0 0000 1100 0100 0001
5	lsb=1	0110 0010	0 0110 1110 0100 0001
	Rshift	0110 0010	0 0011 0111 0010 0000
6	lsb=0	0110 0010	0 0011 0111 0010 0000
	Rshift	0110 0010	0 0001 1011 1001 0000
7	lsb=0	0110 0010	0 0001 1011 1001 0000
	Rshift	0110 0010	0 0000 1101 1100 1000
8	lsb=0	0110 0010	0 0000 1101 1100 1000
	Rshift	0110 0010	0 0000 0110 1110 0100

3.14

For hardware, it takes 1 cycle to do the add, 1 cycle to do the shift, and 1 cycle to decide if we are done. So the loop takes $(3 \times A)$ cycles, with each cycle being B time units long.

For a software implementation, it takes 1 cycle to decide what to add, 1 cycle to do the add, 1 cycle to do each shift, and 1 cycle to decide if we are done. So the loop takes $(5 \times A)$ cycles, with each cycle being B time units long.

$$(3 \times 8) \times 4tu = 96 \text{ time units for hardware.}$$

$$(5 \times 8) \times 4tu = 160 \text{ time units for software.}$$

$$3.27 \quad -1.5625 \times 10^{-1} = -0.15625 \times 10^0$$

$$= -0.00101 \times 2^0$$

$$= -1.01 \times 2^{-3}$$

$$\text{exponent: } -3 + 15 = 12$$

$$\text{fraction: } -0.0100000000$$

$$\text{answer: } 10110001000000$$

$$\text{exp} \in [-15, 16] \quad \text{accuracy: } 10 \text{ bits}$$

3.29

$$2.6125 \times 10^1 + 4.150390625 \times 10^{-1}$$

$$2.6125000000 \times 10^1$$

$$0.04150390625$$

$$\hline 2.65400390625$$

$$2.6125 \times 10^1 = 26.125 = 11010.001 = 1.1010001000 \times 2^4$$

$$4.150390625 \times 10^{-1} = 0.4150390625 = 0.0110101011 \\ = 1.10101011 \times 2^{-2}$$

$$1.1010001000000000 \times 2^4$$

$$0.00000110101011$$

$$\hline 1.10101011$$

$$= 11010.10001011$$

$$= 26.5400390625$$

$$= 2.65400390625 \times 10^1$$

3.30

$$-8.0546875 \times -1.79931640625 \times 10^{-1}$$

$$\rightarrow -100000000111$$

$$\rightarrow -1.0000000111 \times 2^3$$

$$-0.179931640625 \rightarrow -1.011000010 \times 2^{-3}$$

$$\text{exp: } -3+3=0 \quad 0+16=16 \quad (10000)$$

$$1.0000000111$$

$$\times 1.011000010$$

$$1.011001100001001110 \times 2^0$$

$$\text{answer: } 0100000111001100$$

$$1.011001100 = 1.44921875$$

$$\text{however: } -8.0546875 \times -1.79931640625$$

$$= 1.4492931365966796875$$

Some information was lost because the result did not fit into the available 10-bit field. Answer (only) off by 0.00007438659667985