Modern Data Mining, HW $4\,$

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1 Overview

Logistic regression is used for modeling categorical response variables. The simplest scenario is how to identify risk factors of heart disease? In this case the response takes a possible value of YES or NO. Logit link function is used to connect the probability of one being a heart disease with other potential risk factors such as blood pressure, cholestrol level, weight. Maximum likelihood function is used to estimate unknown parameters. Inference is made based on the properties of MLE. We use AIC to help nailing down a useful final model. Predictions in categorical response case is also termed as Classification problems. One immediately application of logistic regression is to provide a simple yet powerful classification boundaries. Various metrics/criteria are proposed to evaluate the quality of a classification rule such as False Positive, FDR or Mis-Classification Errors.

LASSO with logistic regression is a powerful tool to get dimension reduction.

1.1 Objectives

- Understand the model
 - logit function
 - * interpretation
 - Likelihood function
- Methods
 - Maximum likelihood estimators
 - * Z-intervals/tests
 - * Chi-squared likelihood ratio tests
- Metrics/criteria
 - Sensitivity/False Positive
 - True Positive Prediction/FDR
 - Misclassification Error/Weighted MCE
 - Residual deviance
 - Training/Testing errors
- LASSO
- R functions/Packages
 - glm(), Anova
 - pROC
 - cv.glmnet

1.2 R Markdown / Knitr tips

You should think of this R Markdown file as generating a polished report, one that you would be happy to show other people (or your boss). There shouldn't be any extraneous output; all graphs and code run should clearly have a reason to be run. That means that any output in the final file should have explanations.

A few tips:

- Keep each chunk to only output one thing! In R, if you're not doing an assignment (with the <- operator), it's probably going to print something.
- If you don't want to print the R code you wrote (but want to run it, and want to show the results), use a chunk declaration like this: {r, echo=F}. Notice this is set as a global option.
- If you don't want to show the results of the R code or the original code, use a chunk declaration like: {r, include=F}
- If you don't want to show the results, but show the original code, use a chunk declaration like: {r, results='hide'}.

- If you don't want to run the R code in a chunk at all use {r, eval = F}.
- We show a few examples of these options in the below example code.
- For more details about these R Markdown options, see the documentation.
- Delete the instructions and this R Markdown section, since they're not part of your overall report.

1.3 Review

Review the code and concepts covered in

- Module Logistic Regressions/Classification
- Module LASSO in Logistic Regression

1.4 This homework

We have two parts in this homework. Part I is guided portion of work, designed to get familiar with elements of logistic regressions/classification. Part II, we bring you projects. You have options to choose one topic among either Credit Risk via LendingClub or Diabetes and Health Management. Find details in the projects.

2 Part I: Framingham heart disease study

We will continue to use the Framingham Data (Framingham.dat) so that you are already familiar with the data and the variables. All the results are obtained through training data.

Liz is a patient with the following readings: AGE=50, GENDER=FEMALE, SBP=110, DBP=80, CHOL=180, FRW=105, CIG=0. We would be interested to predict Liz's outcome in heart disease.

To keep our answers consistent, use a subset of the data, and exclude anyone with a missing entry. For your convenience, we've loaded it here together with a brief summary about the data.

We note that this dataset contains 311 people diagnosed with heart disease and 1095 without heart disease.

```
0 1
1095 311
```

After a quick cleaning up here is a summary about the data:

Lastly we would like to show five observations randomly chosen.

```
HD AGE
               SEX SBP DBP CHOL FRW CIG
643
        61
              MALE 140
                         68
                             248 104
     1
11
     0
        45
              MALE 110
                         88
                             183
                                        0
576
     1
        58
              MALE 150
                         95
                             296 100
                                       15
560
     1
        59
              MALE 260 130
                             246 111
                                       20
702
        45 FEMALE 122
                         74
                             178
```

2.1 Identify risk factors

2.1.1 Understand the likelihood function

Conceptual questions to understand the building blocks of logistic regression. All the codes in this part should be hidden. We will use a small subset to run a logistic regression of HD vs. SBP.

- i. Take a random subsample of size 5 from hd_data_f which only includes HD and SBP. Also set set.seed(471). List the five observations neatly below. No code should be shown here.
- ii. Write down the likelihood function using the five observations above.
- iii. Find the MLE based on this subset using glm(). Report the estimated logit function of SBP and the probability of HD=1. Briefly explain how the MLE are obtained based on ii. above.

iv. Evaluate the probability of Liz having heart disease.

2.1.2 Identify important risk factors for Heart.Disease.

We focus on understanding the elements of basic inference method in this part. Let us start a fit with just one factor, SBP, and call it fit1. We then add one variable to this at a time from among the rest of the variables. For example

i. Which single variable would be the most important to add? Add it to your model, and call the new fit fit2.

We will pick up the variable either with highest |z| value, or smallest p value. Report the summary of your fit2 Note: One way to keep your output neat, we will suggest you using **xtable**. And here is the summary report looks like.

	Estimate	Std. Error	z value	$\Pr(> z)$
(Intercept)	-6.4863	0.7918	-8.19	0.0000
SBP	0.0143	0.0022	6.38	0.0000
AGE	0.0577	0.0142	4.06	0.0000

- ii. Is the residual deviance of fit2 always smaller than that of fit1? Why or why not?
- iii. Perform both the Wald test and the Likelihood ratio tests (Chi-Squared) to see if the added variable is significant at the .01 level. What are the p-values from each test? Are they the same?

2.1.3 Model building

Start with all variables. Our goal is to fit a well-fitting model, that is still small and easy to interpret (parsimonious).

- i. Use backward selection method. Only keep variables whose coefficients are significantly different from 0 at .05 level. Kick out the variable with the largest p-value first, and then re-fit the model to see if there are other variables you want to kick out.
- ii. Use AIC as the criterion for model selection. Find a model with small AIC through exhaustive search. Does exhaustive search guarantee that the p-values for all the remaining variables are less than .05? Is our final model here the same as the model from backwards elimination?
- iii. Use the model chosen from part ii. as the final model. Write a brief summary to describe important factors relating to Heart Diseases (i.e. the relationships between those variables in the model and heart disease). Give a definition of "important factors".
- iv. What is the probability that Liz will have heart disease, according to our final model?

2.2 Classification analysis

$2.2.1 \quad ROC/FDR$

- i. Display the ROC curve using fit1. Explain what ROC reports and how to use the graph. Specify the classifier such that the False Positive rate is less than .1 and the True Positive rate is as high as possible.
- ii. Overlay two ROC curves: one from fit1, the other from fit2. Does one curve always contain the other curve? Is the AUC of one curve always larger than the AUC of the other one? Why or why not?
- iii. Estimate the Positive Prediction Values and Negative Prediction Values for fit1 and fit2 using .5 as a threshold. Which model is more desirable if we prioritize the Positive Prediction values?
- iv. For fit1: overlay two curves, but put the threshold over the probability function as the x-axis and positive prediction values and the negative prediction values as the y-axis. Overlay the same plot for

fit2. Which model would you choose if the set of positive and negative prediction values are the concerns? If you can find an R package to do so, you may use it directly.

2.2.2 Cost function/ Bayes Rule

Bayes rules with risk ratio $\frac{a_{10}}{a_{01}} = 10$ or $\frac{a_{10}}{a_{01}} = 1$. Use your final model obtained from Part 1 to build a class of linear classifiers.

- i. Write down the linear boundary for the Bayes classifier if the risk ratio of $a_{10}/a_{01} = 10$.
- ii. What is your estimated weighted misclassification error for this given risk ratio?
- iii. How would you classify Liz under this classifier?
- iv. Bayes rule gives us the best rule if we can estimate the probability of HD-1 accurately. In practice we use logistic regression as our working model. How well does the Bayes rule work in practice? We hope to show in this example it works pretty well.

Now, draw two estimated curves where x = threshold, and y = misclassification errors, corresponding to the thresholding rule given in x-axis.

- v. Use weighted misclassification error, and set $a_{10}/a_{01} = 10$. How well does the Bayes rule classifier perform?
- vi. Use weighted misclassification error, and set $a_{10}/a_{01} = 1$. How well does the Bayes rule classifier perform?

3 Part II: Project

- 3.1 Project Option 1 Credit Risk via LendingClub
- 3.2 Project Opetion 2 Diabetes and Health Management