1 Fixed Functions in Graphic Pipeline

1.1 Rasterization

Addition Fomulars:

$$\cos(x+y) = \cos x \cos y - \sin x \sin y$$

$$\sin(x+y) = \sin x \cos y + \cos x \sin y$$

2D rotate matrix:

$$\begin{bmatrix} \cos \alpha & -\sin \alpha \\ \sin \alpha & \cos \alpha \end{bmatrix}$$

2D matrix to rotate a vector 90 degress counter-clockwise:

$$\left[\begin{array}{cc} 0 & 0 \\ -1 & 0 \end{array}\right]$$

To judge vector v1 is pointing to the right side of vector v0:

$$\left(\left[\begin{array}{cc} 0 & 0 \\ -1 & 0 \end{array} \right] \overrightarrow{v_0} \right) \cdot \overrightarrow{v_1} > 0$$

In OpenGL, default visiable triangles are counter-clockwise, thus left side of three edges form the triangle aera.

2 Linear Algebra

2.1 Cross Product

Cross product definition differs in right-hand coordinate system and left-hand coordinate system ensuring that:

From this, it can be inferred that:

$$\begin{bmatrix} a_1 \\ a_2 \\ a_3 \end{bmatrix} \times \begin{bmatrix} b_1 \\ b_2 \\ b_3 \end{bmatrix} = (a_1 \overrightarrow{x} + a_2 \overrightarrow{y} + a_3 \overrightarrow{z}) \times (a_1 \overrightarrow{x} + a_2 \overrightarrow{y} + a_3 \overrightarrow{z}) = \begin{vmatrix} \overrightarrow{x} & \overrightarrow{y} & \overrightarrow{z} \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix}$$