# User Manual for BACH

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Bach implements Bausch's algorithm to evaluate distribution function of chi-square weighted sum (1); one important application is to compute p-values of Bayes factors (2). There are two ways to run Bach: simple or in batch. Note in the following example, we use "./bach" as the program name; in the download there are "bach-mac" (bach for Mac OS X) and "bach-linux" (bach for Linux). You may either rename the executable or modify the command lines below.

## 1 Simple run

Denoted by  $\chi_1^2$  a chi-squared random variable (r.v.) with 1 degree of freedom (d.f). Let  $Y = X_1 + 0.8X_2 + 0.6X_3 + 0.4X_4$ , where  $X_i \sim \chi_1^2$  independently, and we want to compute P(Y > 10). The command line is:

./bach 1 0.8 0.6 0.4 10

A p-value will be printed to the screen:

0.00914343

Rules of input: Numbers are separated by space, the last number is the statistic and the numbers before are coefficients.

Suppose we also want to compute P(Y > 20). Of course we may repeat the above command line, substituting 10 with 20. But a more efficient way is to compute P(Y > 20) and P(Y > 10) simultaneously because we can reuse the distribution functions. The command line is:

./bach 1 0.8 0.6 0.4 10,20

Two p-values will be printed to the screen:

0.00914343 4.31004e-5

Rules of input: If we want to compute multiple p-values for the same coefficients, just append more test statistics in the end using ',' to delimit.

#### 2 Batch run

Suppose  $Z = 5X_5 + 0.2X_6$ , where  $X_i \sim \chi_1^2$ , and we want to compute P(Z > 34) in a batch with P(Y > 10) and P(Y > 20). We can create the following file (named "text.input"):

1 0.8 0.6 0.4 10,20

5 0.2 34

Each row in the input file is what you would type using command line save the "./bach". To run BACH in batch:

./bach -i test.input

Three p-values will then be printed on the screen:

0.00914343 4.31004e-5

0.00932733

Within each row, multiple p-values are delimited by a tab ('\t'); and rows in printout correspond to rows in the input file.

## 3 Output file

When '-o' argument is invoked for batch mode, an output file will be generated.

./bach -i test.input -o test.output

This command will produce a 'test.output' which reads

p-value	error-bound	coeff cients	statistic
0.00914343	3.02826e-15	$0.4\ 0.6\ 0.8\ 1$	10
4.31004 e - 05	5.37358e-11	$0.4\ 0.6\ 0.8\ 1$	20
0.00932733	3.55176e-08	$0.2\ 5$	34

The output file contains 4 columns: p-value; error bound, which is the upper error bound of the p-value; coefficients, which are coefficients of  $\chi_1^2$  used in computation; and statistic. Between field the delimit is the tab, and within the field of coefficient the delimit is the blank.

## 4 Options

- -i [string=]: the input filename. This is required for batch mode.
- -o [string=]: the output filename for the batch mode
- -c [int=6]: the precision of all output (number of significant digits, default is 6)
- -h: stop the program and print the HELP

There are additional options to control error bounds, some of which concern GMP library used in our implementation; one may send an email to inquire if on the off chance one is interested.

#### References

- [1] Johannes Bausch. On the efficient calculation of a linear combination of chi-square random variables with an application in counting string vacua. *Journal of Physics A: Mathematical and Theoretical*, 46(50):505202, 2013.
- [2] Quan Zhou and Yongtao Guan. On the null distribution of bayes factors in linear regressin. *submitted*, 2015.