



ACM/ICPC Template Manual

浙江工商大学

肥宅很快乐

December 12, 2019

Contents

0	头文件	1
1	字符串	2
1.1	KMP	2
2	动态规划	4
2.1	01Bag	4
2.2	BagProblem	4
2.3	FullBag	4
2.4	MultiBag	5
2.5	Maze01	6
3	数据结构	8
3.1	BTree	8
3.2	pbds-bbtree	10
3.3	树状数组	10
3.4	二维树状数组	12
3.5	线段树	12
3.6	二维线段树	15
3.7	树状数组求逆序对	17
3.8	ST	17
3.9	笛卡尔树	19
3.10	DancingLinks	19
3.11	静态主席树	21
3.12	动态主席树	22
3.13	伸展树 Splay	25
3.14	带权并查集	29
3.15	可持久化并查集	30
4	图论	32
4.1	Graph	32
4.2	Dijkstra	32
4.3	spfa	33
4.4	Dinic	34
4.5	hungry	35
4.6	MinSpanTree	36
4.7	MinCostMaxFlow	37
4.8	ISAP	40
4.9	树链剖分	42
4.10	倍增 LCA	43
4.11	Tarjan	44
4.12	支配树	45
4.13	Hopcroft-Karp	46
5	博弈	48
5.1	GameProblem	48
6	分治	49
6.1	IntegerFastPower	49
6.2	MatrixFastPower	49
6.3	三维 CDQ	50
6.4	树分治-点分治	50
6.5	DsuOnTree1	53
6.6	DsuOnTree2	58

7	数论	61
7.1	线性基	61
7.2	FWT	63
7.3	FFT	63
7.4	圆上整点	64
7.5	线性逆元	65
8	其他	66
8.1	BigInteger	66
8.2	FastIO	72
8.3	InputOutputSpeedUp	75
8.4	gcd	75
8.5	myItoa	76
8.6	Permutation	76
8.7	prime	76
8.8	Hash	77

0 头文件

```

1 // 巨菜的ACMer-Happy233
2
3 #include <bits/stdc++.h>
4
5 using namespace std;
6
7 //-----
8 typedef double db;
9 typedef long long ll;
10 typedef unsigned int ui;
11 typedef vector<int> vi;
12 typedef pair<int, int> pii;
13 typedef pair<ll, ll> pll;
14 #define fi first
15 #define se second
16 #define pw(x) (1ll << (x))
17 #define bt(x, k) (((x) >> k) & 1)
18 #define sz(x) ((int)(x).size())
19 #define all(x) (x).begin(),(x).end()
20 #define rep(i, l, r) for(int i=(l);i<(r);++i)
21 #define per(i, l, r) for(int i=(r)-1;i>=(l);--i)
22 #define mst(t, v, n) memset(t, v, sizeof(decltype(*(t))) * (n))
23 #define sf(x) scanf("%d", &(x))
24 #ifndef ACM_LOCAL
25 #define endl '\n'
26 #endif
27
28 int main() {
29 #ifdef ACM_LOCAL
30     freopen("./data/std.in", "r", stdin);
31     // freopen("./data/std.out", "w", stdout);
32 #else
33     ios_base::sync_with_stdio(false);
34     cin.tie(0);
35     cout.tie(0);
36 #endif
37
38 #ifdef ACM_LOCAL
39     auto start = clock();
40 #endif
41     int t = 1;
42     // cin >> t;
43     while (t--)
44         solve();
45 #ifdef ACM_LOCAL
46     auto end = clock();
47     cerr << "Run Time: " << double(end - start) / CLOCKS_PER_SEC << "s" << endl;
48 #endif
49     return 0;
50 }

```

1 字符串

1.1 KMP

```

1  template<class elemType>
2  inline void kmp_nxt(elemType &T, vector<int> &nxt) {
3      nxt[0] = -1;
4      for (int i = 1; i < T.size(); i++) {
5          int j = nxt[i - 1];
6          while (j >= 0 && T[i - 1] != T[j]) j = nxt[j];
7          if (j >= 0 && T[i - 1] == T[j]) nxt[i] = j + 1;
8          else nxt[i] = 0;
9      }
10 }
11
12 template<class elemType>
13 inline int kmp_count(elemType &S, elemType &T) {
14     vector<int> nxt(T.size());
15     kmp_nxt(T, nxt);
16     int index, count = 0;
17     for (index = 0; index < S.size(); ++index) {
18         int pos = 0;
19         int iter = index;
20         while (pos < T.size() && iter < S.size()) {
21             if (S[iter] == T[pos]) {
22                 ++iter;
23                 ++pos;
24             } else {
25                 if (pos == 0) ++iter;
26                 else pos = nxt[pos - 1] + 1;
27             }
28         }
29         if (pos == T.size() && (iter - index) == T.size()) ++count;
30     }
31     return count;
32 }
33
34 template<class elemType>
35 inline void kmp_next(elemType T[], int count, vector<int> &nxt) {
36     nxt[0] = -1;
37     for (int i = 1; i < count; i++) {
38         int j = nxt[i - 1];
39         while (j >= 0 && T[i - 1] != T[j]) j = nxt[j];
40         if (j >= 0 && T[i - 1] == T[j]) nxt[i] = j + 1;
41         else nxt[i] = 0;
42     }
43 }
44
45 template<class elemType>
46 inline int kmp_count(elemType S[], int c1, elemType T[], int c2) {
47     vector<int> nxt(c2);
48     kmp_nxt(T, c2, nxt);
49     int index, count = 0;
50     for (index = 0; index < c1; ++index) {
51         int pos = 0;
52         int iter = index;
53         while (pos < c2 && iter < c1) {
54             if (S[iter] == T[pos]) {
55                 ++iter;

```

```
56         ++pos;
57     }
58     else {
59         if (pos == 0) ++iter;
60         else pos = nxt[pos - 1] + 1;
61     }
62 }
63 if (pos == c2 && (iter - index) == c2) ++count;
64 }
65 return count;
66 }
```

2 动态规划

2.1 01Bag

```

1 void dp(int n, int m) {
2     // n=物品个数
3     for (int i = 0; i < n; i++) {
4         // m=背包最大容量
5         for (int j = m; j >= wei[i]; j--)
6             // wei=大小 val=价值
7             f[j] = max(f[j], f[j - wei[i]] + val[i]);
8     }
9 }

```

2.2 BagProblem

```

1 #define N 1000
2 // val=价值 wei=重量 num=数量
3 int val[N], wei[N], num[N], f[N];
4 // n=种类个数 m=背包最大值
5
6 // 01背包
7 void dp1(int n, int m) {
8     for (int i = 0; i < n; i++) {
9         for (int j = m; j >= wei[i]; j--)
10             f[j] = max(f[j], f[j - wei[i]] + val[i]);
11     }
12 }
13
14 // 完全背包
15 void dp2(int n, int m) {
16     //初始化看要求
17     for (int i = 0; i <= m; i++) {
18         f[i] = INF;
19     }
20     f[0] = 0;
21     //若要求恰好装满背包, 那在初始化时除了f[0]=0其它f[1..V]均=-∞
22     //若没要求背包装满, 只希望价格大, 初始化时应将f[0..V]=0
23     for (int i = 0; i < n; i++)
24         for (int j = wei[i]; j <= m; j++)
25             f[j] = max(f[j], f[j - wei[i]] + val[i]);
26 }
27
28 // 多重背包
29 void dp3(int n, int m) {
30     for (int i = 0; i < n; i++)
31         for (int k = 0; k < num[i]; k++)
32             for (int j = m; j >= wei[i]; j--)
33                 f[j] = max(f[j], f[j - wei[i]] + val[i]);
34 }

```

2.3 FullBag

```

1 /*
2 完全背包问题的特点是, 每种物品可以无限制的重复使用, 可以选择放或不放。
3 完全背包问题描述:
4 有N物品和一个容量为V的背包。第i件物品的重量是wei[i], 价值是val[i]。

```

```

5  */
6
7  #include <stdio>
8  #define INF 0x3fffffff
9  #define N 10047
10 int f[N],val[N],wei[N];
11 int min(int a,int b)
12 {
13     return x<y?x:y;
14 }
15 int main()
16 {
17     int t,i,j,k,E,F,m,n;
18     scanf("%d",&t);
19     while(t-->0)
20     {
21         scanf("%d%d",&E,&F);
22         int c = F-E;
23         for(i = 0 ; i <= c ; i++)
24             f[i]=INF;
25         scanf("%d",&n);
26         for(i = 0 ; i < n ; i++)
27         {
28             scanf("%d%d",&val[i],&wei[i]); //val[i]为面额, wei[i]为重量
29         }
30         f[0]=0; //因为此处假设的是小猪储钱罐 恰好装满 的情况
31         //注意初始化 (要求恰好装满背包, 那么在初始化时除了f[0]为0其它f[1..V]均设为-∞,
32         //这样就可以保证最终得到的f[N]是一种恰好装满背包的最优解。
33         //如果并没有要求必须把背包装满, 而是只希望价格尽量大, 初始化时应该将f[0..V]全部设为0)
34         for(i = 0 ; i < n ; i++)
35         {
36             for(j = wei[i] ; j <= c ; j++)
37             {
38                 f[j] = min(f[j],f[j-wei[i]]+val[i]); //此处求的是最坏的情况所以用min, 确定最少
39                 //的钱,当然最后就用max了, HEHE
40             }
41         }
42         if(f[c] == INF)
43             printf("This is impossible.\n");
44         else
45             printf("The minimum amount of money in the piggy-bank is %d.\n",f[c]);
46     }
47     return 0;
48 } //此代码为HDU1114;

```

2.4 MultiBag

```

1  //多重背包(MultiplePack): 有N种物品和一个容量为V的背包。
2  //第i种物品最多有n[i]件可用, 每件费用是c[i], 价值是w[i]。
3  //求解将哪些物品装入背包可使这些物品的费用总和不超过背包容量,
4  //且价值总和最大。
5  //HDU 2191
6
7  #include <stdio>
8  #include <cstring>
9  #define N 247
10 int max(int x,int y){

```



```

11     return x>y?x:y;
12 }
13 int main() {
14     int t,n,m,i,j,k;
15     int w[N],pri[N],num[N],f[N];
16     while(~scanf("%d",&t)){
17         while(t--){
18             memset(f,0,sizeof(f));
19             scanf("%d%d",&n,&m);//n为总金额, m为大米种类
20             for(i = 0 ; i < m ; i++){
21                 scanf("%d%d%d",&pri[i],&w[i],&num[i]);//num[i]为每种大米的袋数
22             }
23             for(i = 0 ; i < m ; i++){
24                 for(k = 0 ; k < num[i] ; k++){
25                     for(j = n ; j >= pri[i]; j--){
26                         f[j] = max(f[j],f[j-pri[i]]+w[i]);
27                     }
28                 }
29             }
30             printf("%d\n",f[n]);
31         }
32     }
33     return 0;
34 }

```

2.5 Maze01

```

1 struct Maze01 {
2     // 原始01矩阵 1-n 1-m
3     bool a[N][N];
4     // 以(i,j)向上最大高度的最大子矩阵的左右高
5     int l[N][N], r[N][N], h[N][N];
6     // 最大连续前缀1的左端位置, 如果(i,j)为0则ml=j+1
7     int ml[N][N];
8     // 矩阵大小
9     int n, m;
10
11     void prework() {
12         for (int i = 1; i <= m; i++) {
13             l[0][i] = 0;
14             r[0][i] = m;
15         }
16         for (int i = 1; i <= n; i++) {
17             int maxl = 1;
18             int maxr = m;
19             for (int j = 1; j <= m; j++) {
20                 if (a[i][j] == 0) {
21                     maxl = j + 1;
22                     h[i][j] = l[i][j] = 0;
23                 } else {
24                     h[i][j] = h[i - 1][j] + 1;
25                     l[i][j] = max(maxl, l[i - 1][j]);
26                 }
27                 ml[i - 1][j] = maxl;
28                 ml[i][j] = j + 1;
29             }
30             for (int j = m; j >= 1; --j) {
31                 if (a[i][j] == 0) {

```

```

32         maxr = j - 1;
33         r[i][j] = m;
34     } else {
35         r[i][j] = min(maxr, r[i - 1][j]);
36     }
37 }
38 }
39 }
40
41 // 单调栈
42 pii st[N];
43
44 int calc() {
45     prework();
46     int ans = 0;
47     for (int i = 1; i <= n; i++) {
48         int top = 0;
49         for (int j = 1; j <= m; j++) {
50             if (h[i][j] == 0) continue;
51             if (top == 0 || st[top] != make_pair(l[i][j], r[i][j])) {
52                 st[++top] = make_pair(l[i][j], r[i][j]);
53             }
54             while (top && st[top].second == j) {
55                 int pos = st[top--].first;
56                 if (pos < ml[i][j]) {
57                     // l[i][j]-r[i][j]为底, h[i][j]为高
58                     // 可以得到所有的唯一子矩阵, 不存在maze1完全属于maze2
59                     ans++;
60                 }
61             }
62         }
63     }
64     return ans;
65 }
66 } dp;

```

3 数据结构

3.1 BTree

```

1  template<class T>
2
3  struct TreeNode {
4      T value;
5      TreeNode *left;
6      TreeNode *right;
7  };
8
9  template<class T>
10 TreeNode<T> *createTree(const T *pre, const T *in, const int len) {
11     TreeNode<T> *t = NULL;
12     if (len > 0) {
13         t = new TreeNode<T>;
14         t->value = pre[0];
15         int index;
16         for (index = 0; index < len; index++) {
17             if (in[index] == pre[0]) {
18                 break;
19             }
20         }
21         if (index == len) {
22             index = -1;
23         }
24         t->left = createTree(pre + 1, in, index);
25         t->right = createTree(pre + index + 1, in + index + 1, len - index - 1);
26     }
27     return t;
28 }
29
30 template<class T>
31 int preOrder(TreeNode<T> *root, queue<T> &out) {
32     if (root) {
33         int count = 1;
34         out.push(root->value);
35         count += preOrder(root->left, out);
36         count += preOrder(root->right, out);
37         return count;
38     } else {
39         return 0;
40     }
41 }
42
43 template<class T>
44 int inOrder(TreeNode<T> *root, queue<T> &out) {
45     if (root) {
46         int count = 1;
47         count += inOrder(root->left, out);
48         out.push(root->value);
49         count += inOrder(root->right, out);
50         return count;
51     } else {
52         return 0;
53     }
54 }
55

```

```

56 template<class T>
57 void postOrder(TreeNode<T> *root, queue<T> &out) {
58     if (root) {
59         postOrder(root->left, out);
60         postOrder(root->right, out);
61         out.push(root->value);
62     } else {
63         return;
64     }
65 }
66
67 template<class T>
68 T *convertQueueToArray(queue<T> &out, int len) {
69     T *list = new T[len];
70     int now = 0;
71     while (!out.empty() && now < len) {
72         list[now] = out.front();
73         out.pop();
74         now++;
75     }
76     return list;
77 }
78
79 template<class T>
80 void destroyTree(TreeNode<T> *root) {
81     if (root) {
82         destroyTree(root->left);
83         destroyTree(root->right);
84         delete root;
85     } else return;
86 }
87
88 template<class T>
89 void insertIntoBSTree(TreeNode<T> *root, const T &value) {
90     if (!root) {
91         return;
92     }
93     if (value < root->value) {
94         if (root->left) {
95             insertIntoTree(root->left, value);
96         } else {
97             root->left = new TreeNode<T>;
98             root->left->value = value;
99             root->left->left = NULL;
100             root->left->right = NULL;
101         }
102     } else if (value > root->value) {
103         if (root->right) {
104             insertIntoTree(root->right, value);
105         } else {
106             root->right = new TreeNode<T>;
107             root->right->value = value;
108             root->right->left = NULL;
109             root->right->right = NULL;
110         }
111     }
112 }
113
114 template<class T>

```

```

115 TreeNode<T> *createBSTree(T *list, int len) {
116     if (len < 1) {
117         return NULL;
118     }
119     TreeNode<T> *root = new TreeNode<char>;
120     root->value = list[0];
121     root->left = NULL;
122     root->right = NULL;
123     for (int i = 1; i < len; i++) {
124         insertIntoBSTree(root, list[i]);
125     }
126     return root;
127 }

```

3.2 pbds-bbtree

```

1 // RBTREE 红黑树
2 #include <ext/pb_ds/tree_policy.hpp>
3 #include <ext/pb_ds/assoc_container.hpp>
4 // 红黑树
5 __gnu_pbds::tree<int, null_type, less<int>, rb_tree_tag,
6     tree_order_statistics_node_update> t;
7 // null_type无映射(低版本g++为null_mapped_type)
8 // 类似multiset
9 __gnu_pbds::tree<int, null_type, less_equal<int>, rb_tree_tag,
10     tree_order_statistics_node_update> t;
11 find_by_order(size_t order);
12 // 结点更新
13 tree_order_statistics_node_update
14 insert(p);
15 erase(it);
16 // 求k在树中是第几大:
17 order_of_key(p);
18 // 找到第order小的迭代器
19 find_by_order(order);
20 // 前驱
21 lower_bound(p);
22 // 后驱
23 upper_bound(p);
24 // 合并
25 a.join(b);
26 // 分割 key小于等于v的元素属于a, 其余的属于b
27 a.split(v, b);
28 // 优先队列
29 #include <ext/pb_ds/priority_queue.hpp>
30 #include <ext/pb_ds/assoc_container.hpp>
31 // 操作类似于stl的优先队列
32 typedef __gnu_pbds::priority_queue<node, greater<node>, __gnu_pbds::thin_heap_tag> heap;
33 ;
34 heap::point_iterator; // 指向元素的指针

```

3.3 树状数组

```

1 const int N = 1000005;
2 struct BITree {
3     int n;

```

```

4     ll c[N];
5
6     void init(int _n) {
7         n = _n + 1;
8         memset(c, 0, sizeof(ll) * n);
9     }
10
11    void change(int pos, ll v) {
12        for (int i = pos; i < n; i += i & (-i))
13            c[i] += v;
14    }
15
16    ll query(int x) {
17        ll ans = 0;
18        for (int i = x; i > 0; i -= i & (-i))
19            ans += c[i];
20        return ans;
21    }
22
23    void update(int l, int r, ll v) {
24        change(l, v);
25        change(r + 1, -v);
26    }
27 } tree;
28
29 // 区间更新区间查询
30 struct BITree {
31     int n;
32     ll c[N], d[N];
33
34     void init(int _n) {
35         n = _n + 1;
36         memset(c, 0, sizeof(ll) * n);
37         memset(d, 0, sizeof(ll) * n);
38     }
39
40     void change(int pos, ll v) {
41         for (int i = pos; i < n; i += i & (-i))
42             c[i] += v, d[i] += v * (pos - 1);
43     }
44
45     ll query(int x) {
46         ll ans = 0;
47         for (int i = x; i > 0; i -= i & (-i))
48             ans += x * c[i] - d[i];
49         return ans;
50     }
51
52     void update(int l, int r, ll v) {
53         change(l, v);
54         change(r + 1, -v);
55     }
56
57     ll sum(int l, int r) {
58         return query(r) - query(l - 1);
59     }
60 } tree;

```

3.4 二维树状数组

```

1  const int N = 2005;
2
3  inline int lowbit(const int &x) {
4      return x & -x;
5  }
6
7  struct TdBITree {
8      int n, m;
9      ll c[N][N];
10
11     void init(int n, int m) {
12         this->n = n;
13         this->m = m;
14         memset(c, 0, sizeof(c))
15     }
16
17     void init(int n, int m, ll v) {
18         this->n = n;
19         this->m = m;
20         rep(x, 1, N) {
21             rep(y, 1, N) {
22                 c[x][y] = (x * y + (x - lowbit(x)) * (y - lowbit(y)) - x * (y - lowbit(
23             y)) - (x - lowbit(x)) * y) * v;
24             }
25         }
26
27     void change(int x, int y, ll v) {
28         for (int i = x; i <= n; i += lowbit(i))
29             for (int j = y; j <= m; j += lowbit(j))
30                 c[i][j] += v;
31     }
32
33     ll query(int x, int y) {
34         ll ans = 0;
35         for (int i = x; i >= 1; i -= lowbit(i))
36             for (int j = y; j >= 1; j -= lowbit(j))
37                 ans += c[i][j];
38         return ans;
39     }
40
41     ll solve(int x1, int y1, int x2, int y2) {
42         return query(x2, y2) - query(x1 - 1, y2) - query(x2, y1 - 1) + query(x1 - 1, y1
43         - 1);
44     }
45 };

```

3.5 线段树

```

1  // hdu 6562
2  struct TreeNode {
3      int l, r;
4      int lson, rson;
5      ll sum;
6      ll len;
7      ll laz1, laz2, laz3;

```

```

8
9     inline void init(int a, int b, int ls, int rs) {
10         lson = ls;
11         rson = rs;
12         l = a, r = b;
13         sum = 0;
14         len = 1;
15         laz1 = laz2 = 0;
16         laz3 = 1;
17     }
18
19     inline int mid() {
20         return (l + r) >> 1;
21     }
22
23     inline int width() {
24         return r - l + 1;
25     }
26
27     inline void add(ll val) {
28         sum = (sum * 10 + val * len * 10 + val * width()) % MOD;
29         len = (len * 100) % MOD;
30         // 右懒惰
31         laz1 = (laz1 * 10 + val) % MOD;
32         // 左懒惰
33         laz2 = (laz2 + val * laz3) % MOD;
34         // 长度懒惰
35         laz3 = (laz3 * 10) % MOD;
36     }
37 };
38
39 struct SegTree {
40     int tot;
41     TreeNode node[N << 1];
42
43     inline void init() {
44         tot = 0;
45     }
46
47     inline void up(int k) {
48         TreeNode &nd = node[k];
49         nd.sum = (node[nd.lson].sum + node[nd.rson].sum) % MOD;
50         nd.len = (node[nd.lson].len + node[nd.rson].len) % MOD;
51     }
52
53     inline void push(int k) {
54         TreeNode &nd = node[k];
55         if (nd.laz3 == 1) return;
56         TreeNode &lson = node[nd.lson];
57         TreeNode &rson = node[nd.rson];
58
59         lson.sum = (nd.laz1 * lson.width() + lson.sum * nd.laz3 + nd.laz2 * lson.len %
MOD * nd.laz3) % MOD;
60         lson.len = (lson.len * nd.laz3 % MOD * nd.laz3) % MOD;
61         lson.laz1 = (lson.laz1 * nd.laz3 + nd.laz1) % MOD;
62         lson.laz2 = (nd.laz2 * lson.laz3 + lson.laz2) % MOD;
63         lson.laz3 = (lson.laz3 * nd.laz3) % MOD;
64

```



```

65     rson.sum = (nd.laz1 * rson.width() + rson.sum * nd.laz3 + nd.laz2 * rson.len %
MOD * nd.laz3) % MOD;
66     rson.len = (rson.len * nd.laz3 % MOD * nd.laz3) % MOD;
67     rson.laz1 = (rson.laz1 * nd.laz3 + nd.laz1) % MOD;
68     rson.laz2 = (nd.laz2 * rson.laz3 + rson.laz2) % MOD;
69     rson.laz3 = (rson.laz3 * nd.laz3) % MOD;
70
71     nd.laz1 = nd.laz2 = 0;
72     nd.laz3 = 1;
73 }
74
75 void build(int k, int l, int r) {
76     TreeNode &nd = node[k];
77     nd.init(l, r, tot + 1, tot + 2);
78     tot += 2;
79     if (l == r) {
80         return;
81     }
82     int mid = nd.mid();
83     build(nd.lson, nd.l, mid);
84     build(nd.rson, mid + 1, nd.r);
85     up(k);
86 }
87
88 void change(int k, int l, int r, ll val) {
89     TreeNode &nd = node[k];
90     if (nd.l == l && nd.r == r) {
91         nd.add(val);
92         return;
93     }
94     push(k);
95     int mid = nd.mid();
96     if (r <= mid) {
97         change(nd.lson, l, r, val);
98     } else if (l > mid) {
99         change(nd.rson, l, r, val);
100     } else {
101         change(nd.lson, l, mid, val);
102         change(nd.rson, mid + 1, r, val);
103     }
104     up(k);
105 }
106
107 ll query(int k, int l, int r) {
108     TreeNode &nd = node[k];
109     if (nd.l == l && nd.r == r) {
110         return nd.sum;
111     }
112     push(k);
113     int mid = nd.mid();
114     ll ans = 0;
115     if (r <= mid) {
116         ans += query(nd.lson, l, r);
117     } else if (l > mid) {
118         ans += query(nd.rson, l, r);
119     } else {
120         ans += query(nd.lson, l, mid);
121         ans += query(nd.rson, mid + 1, r);
122     }

```

```

123         return ans % MOD;
124     }
125 } tree;

```

3.6 二维线段树

```

1
2  const int N = 1005;
3
4  struct SegTree {
5
6      inline int son(int k, int x) {
7          return (k << 2) - 2 + x;
8      }
9
10     struct node {
11         int l, r;
12
13         node() = default;
14
15         node(int a, int b) : l(a), r(b) {}
16
17         inline int mid() {
18             return (l + r) >> 1;
19         }
20
21         inline node left() {
22             return node(l, mid());
23         }
24
25         inline node right() {
26             return node(mid() + 1, r);
27         }
28
29         inline bool in(int x) {
30             return x >= l && x <= r;
31         }
32
33         inline bool more() {
34             return l < r;
35         }
36
37         bool operator==(const node &t) {
38             return l == t.l && r == t.r;
39         }
40     };
41
42     ll c[N << 2][N << 2];
43     ll ans[N << 4];
44     ll laz[N << 4];
45
46     inline void up(int k, bool x, bool y) {
47         int s = (k << 2) - 2;
48         ll t = 0;
49         if (x) t += ans[s] + ans[s + 1] + laz[s] + laz[s + 1];
50         if (y) t += ans[s + 2] + ans[s + 3] + laz[s + 2] + laz[s + 3];
51         ans[k] = t;
52     }

```

```

53
54 inline void push(int k) {
55     int s = (k << 2) - 2;
56     laz[s] += laz[k];
57     laz[s + 1] += laz[k];
58     laz[s + 2] += laz[k];
59     laz[s + 3] += laz[k];
60     ans[k] += laz[k];
61     laz[k] = 0;
62 }
63
64 void build(node x, node y, int k) {
65     laz[k] = 0;
66     if (x.more() && y.more()) {
67         ans[k] = c[x.l][y.l];
68         return;
69     }
70     ans[k] = 0;
71     bool ax = false;
72     bool ay = false;
73     if (x.more()) {
74         build(x.left(), y, son(k, 0));
75         build(x.right(), y, son(k, 1));
76     }
77     if (y.more()) {
78         build(x, y.left(), son(k, 2));
79         build(x, y.right(), son(k, 3));
80     }
81     up(k, x.more(), y.more());
82 }
83
84 void change(node x, node y, int k, node l, node r, ll v) {
85     if (x == l && y == r) {
86         laz[k] += v;
87         return;
88     }
89     push(k);
90     if (x.more()) {
91         if (l.r <= x.mid()) {
92             change(x.left(), y, son(k, 0), l, r, v);
93         } else if (l.l > x.mid()) {
94             change(x.right(), y, son(k, 1), l, r, v);
95         } else {
96             change(x.left(), y, son(k, 0), node(l.l, x.mid()), r, v);
97             change(x.right(), y, son(k, 1), node(x.mid() + 1, l.r), r, v);
98         }
99     }
100     if (y.more()) {
101         if (r.l <= y.mid()) {
102             change(x, y.left(), son(k, 2), l, r, v);
103         } else if (r.r > y.mid()) {
104             change(x, y.right(), son(k, 3), l, r, v);
105         } else {
106             change(x, y.left(), son(k, 2), l, node(r.l, y.mid()), v);
107             change(x, y.right(), son(k, 3), l, node(y.mid() + 1, r.r), v);
108         }
109     }
110     up(k, x.more(), y.more());
111 }

```

```

112
113 ll query(node x, node y, int k, node l, node r) {
114     if (x == l && y == r) {
115         return ans[k] + laz[k];
116     }
117     push(k);
118     ll t = 0;
119     if (x.more()) {
120         if (l.r <= x.mid()) {
121             t += query(x.left(), y, son(k, 0), l, r);
122         } else if (l.l > x.mid()) {
123             t += query(x.right(), y, son(k, 1), l, r);
124         } else {
125             t += query(x.left(), y, son(k, 0), node(l.l, x.mid()), r);
126             t += query(x.right(), y, son(k, 1), node(x.mid() + 1, l.r), r);
127         }
128     }
129     if (y.more()) {
130         if (r.l <= y.mid()) {
131             t += query(x, y.left(), son(k, 2), l, r);
132         } else if (r.r > y.mid()) {
133             t += query(x, y.right(), son(k, 3), l, r);
134         } else {
135             t += query(x, y.left(), son(k, 2), l, node(r.l, y.mid()));
136             t += query(x, y.right(), son(k, 3), l, node(y.mid() + 1, r.r));
137         }
138     }
139     return t;
140 }
141 };

```

3.7 树状数组求逆序对

```

1 BITree t;
2 int n;
3 pii a[N];
4
5 void solve() {
6     t.init(n);
7     for (int i = 1; i <= n; i++) {
8         int x;
9         cin >> x;
10        a[i] = make_pair(x, i);
11    }
12    sort(a + 1, a + n + 1);
13    ll ans = 0;
14    for (int i = 1; i <= n; i++) {
15        t.change(a[i].second, 1);
16        ans += (i - t.query(a[i].second));
17    }
18    cout << ans << endl;
19 }

```

3.8 ST

```

1 // 只需要取值
2 struct ST {

```

```

3   int ck[N];
4   int dp[20][N];
5
6   void init(int n, int squ[]) {
7       ++n;
8       ck[0] = -1;
9       for (int i = 1; i <= n; i++) {
10          ck[i] = ck[i - 1] + ((i & (i - 1)) == 0 ? 1 : 0);
11      }
12      for (int i = 0; i < n; i++) {
13          dp[0][i] = squ[i];
14      }
15      for (int k = 1; k <= ck[n]; k++) {
16          int dk = k - 1;
17          for (int i = 0; i + (1 << k) - 1 < n; i++) {
18              dp[k][i] = max(dp[dk][i], dp[dk][i + (1 << dk)]);
19          }
20      }
21  }
22
23  int query(int l, int r) {
24      if (l > r) swap(l, r);
25      int k = ck[r - l + 1];
26      return max(dp[k][l], dp[k][r - (1 << k) + 1]);
27  }
28  };
29
30  // 可得到下标
31  struct ST {
32      int ck[N];
33      int rmq[N];
34      int dp[20][N];
35
36      void init(int n, int squ[]) {
37          ++n;
38          ck[0] = -1;
39          for (int i = 1; i <= n; i++) {
40              ck[i] = ck[i - 1] + ((i & (i - 1)) == 0 ? 1 : 0);
41          }
42          memcpy(rmq, squ, sizeof(int) * n);
43          for (int i = 0; i < n; i++) {
44              dp[0][i] = i;
45          }
46          for (int k = 1; k <= ck[n]; k++) {
47              int dk = k - 1;
48              for (int i = 0; i + (1 << k) - 1 < n; i++) {
49                  int a = dp[dk][i];
50                  int b = dp[dk][i + (1 << dk)];
51                  dp[k][i] = rmq[a] < rmq[b] ? a : b;
52              }
53          }
54      }
55
56      int query(int l, int r) {
57          if (l > r) swap(l, r);
58          int k = ck[r - l + 1];
59          int a = dp[k][l];
60          int b = dp[k][r - (1 << k) + 1];
61          return rmq[a] < rmq[b] ? a : b;

```

```

62     }
63 };

```

3.9 笛卡尔树

```

1  // 笛卡尔树, 静态建树, 区间最值跳转
2  struct CartesianTree {
3      int rt; // 根节点
4      pii ch[N]; // 左右儿子
5      int st[N]; // 单调栈
6
7      void build(int n, int p[]) {
8          rt = 0;
9          int t = 0;
10         for (int i = 1; i <= n; i++) {
11             ch[i] = {0, 0};
12             // 决定了大于还是小于
13             while (t && p[st[t]] > p[i]) --t;
14             if (t) {
15                 // 上一个点的右儿子作为自己的左儿子
16                 // 成为上一个点的右儿子
17                 ch[i].first = ch[st[t]].second;
18                 ch[st[t]].second = i;
19             } else { // 自己作为根节点
20                 ch[i].first = rt;
21                 rt = i;
22             }
23             st[++t] = i;
24         }
25     }
26 } dika;

```

3.10 DancingLinks

```

1  // Dancing Links
2  struct DLX {
3      int n, m, size;
4      int U[MaxNode], D[MaxNode], L[MaxNode], R[MaxNode], Row[MaxNode], Col[MaxNode];
5      int H[MaxN], S[MaxM];
6      int ansd, ans[MaxN];
7
8      void init(int _n, int _m) {
9          n = _n;
10         m = _m;
11         for (int i = 0; i <= m; i++) {
12             S[i] = 0;
13             U[i] = D[i] = i;
14             L[i] = i - 1;
15             R[i] = i + 1;
16         }
17         R[m] = 0;
18         L[0] = m;
19         size = m;
20         for (int i = 0; i <= n; i++) {
21             H[i] = -1;
22         }
23     }

```

```

24
25 void Link(int r, int c) {
26     ++S[Col[++size] = c];
27     Row[size] = r;
28     D[size] = D[c];
29     U[D[c]] = size;
30     U[size] = c;
31     D[c] = size;
32     if (H[r] < 0) {
33         H[r] = L[size] = R[size] = size;
34     } else {
35         R[size] = R[H[r]];
36         L[R[H[r]]] = size;
37         L[size] = H[r];
38         R[H[r]] = size;
39     }
40 }
41
42 void remove(int c) {
43     L[R[c]] = L[c];
44     R[L[c]] = R[c];
45     for (int i = D[c]; i != c; i = D[i]) {
46         for (int j = R[i]; j != i; j = R[j]) {
47             U[D[j]] = U[j];
48             D[U[j]] = D[j];
49             --S[Col[j]];
50         }
51     }
52 };
53
54 void resume(int c) {
55     for (int i = U[c]; i != c; i = U[i])
56         for (int j = L[i]; j != i; j = L[j])
57             ++S[Col[U[D[j]] = D[U[j]] = j]];
58     L[R[c]] = R[L[c]] = c;
59 }
60
61 bool Dance(int d) {
62     if (R[0] == 0) {
63         for (int i = 0; i < d; i++) {
64             printf("%d%c", ans[i], " \n"[i == d - 1]);
65         }
66         return true;
67     }
68     int c = R[0];
69     for (int i = R[0]; i != 0; i = R[i]) if (S[i] < S[c]) c = i;
70     remove(c);
71     for (int i = D[c]; i != c; i = D[i]) {
72         ans[d] = Row[i];
73         for (int j = R[i]; j != i; j = R[j]) remove(Col[j]);
74         if (Dance(d + 1)) return true;
75         for (int j = L[i]; j != i; j = L[j]) resume(Col[j]);
76     }
77     resume(c);
78     return false;
79 }
80 };

```

3.11 静态主席树

```

1 // m=update count,MAXN>=m*log(n)
2 const int N = int(2e5 + 10);
3 const int MAXN = int(1e7 + 10);
4
5 struct PSegTree {
6     const int *a;
7     pii ran; // Tree Range
8     int c[MAXN];
9     int tot = 0;
10    int lson[MAXN], rson[MAXN];
11
12    int build(int l, int r) {
13        int k = ++tot;
14        c[k] = 0;
15        if (l == r) {
16            return k;
17        }
18        int mid = (l + r) >> 1;
19        lson[k] = build(l, mid);
20        rson[k] = build(mid + 1, r);
21        return k;
22    }
23
24    int init(int l, int r, const int num[]) {
25        tot = 0;
26        a = num;
27        ran = {l, r};
28        return build(l, r);
29    }
30
31    int update(int rt, int p, int v) {
32        int k = ++tot, rst = k;
33        int l, r;
34        tie(l, r) = ran;
35        // calc
36        c[k] = c[rt] + v;
37        while (l < r) {
38            int mid = (l + r) >> 1;
39            // 下面的逗号表达式顺序不能换
40            if (p <= mid) {
41                // go left
42                rson[k] = rson[rt], rt = lson[rt], k = lson[k] = ++tot;
43                r = mid;
44            } else {
45                // go right
46                lson[k] = lson[rt], rt = rson[rt], k = rson[k] = ++tot;
47                l = mid + 1;
48            }
49            // calc
50            c[k] = c[rt] + v;
51        }
52        return rst;
53    }
54
55    // r1=right_root,r2=left_root,kth number
56    int query(int r1, int r2, int k) {
57        int l, r;

```



```

58     tie(l, r) = ran;
59     while (l < r) {
60         int mid = (l + r) >> 1;
61         int cnt = c[lson[r1]] - c[lson[r2]];
62         if (cnt >= k) {
63             r1 = lson[r1], r2 = lson[r2];
64             r = mid;
65         } else {
66             k -= cnt;
67             r1 = rson[r1], r2 = rson[r2];
68             l = mid + 1;
69         }
70     }
71     return l;
72 }
73
74 // r1=right_root,r2=left_root, sum of num<=k
75 int sum(int r1, int r2, int k) {
76     int l, r;
77     tie(l, r) = ran;
78     int ans = 0;
79     while (l < r) {
80         int mid = (l + r) >> 1;
81         int cnt = c[lson[r1]] - c[lson[r2]];
82         if (k <= mid) {
83             r1 = lson[r1], r2 = lson[r2];
84             r = mid;
85         } else {
86             ans += cnt;
87             r1 = rson[r1], r2 = rson[r2];
88             l = mid + 1;
89         }
90     }
91     ans += c[r1] - c[r2];
92     return ans;
93 }
94 } tree;

```

3.12 动态主席树

```

1 // m: update count, MAXN>=m*log(n)^2
2 const int N = int(2e5 + 10);
3 const int MAXN = int(2e7 + 10);
4 const int MAXM = int(2e7 + 10);
5 const int LN = 40;
6
7 struct PSegTree {
8     const int *a;
9     pii ran;
10    int n;
11    ll c[MAXN];
12    int tot = 0;
13    int lson[MAXN], rson[MAXN];
14    // t: static root, s: dynamic root
15    int s[N], t[N];
16
17    // SegTree Range and n points, num can be nullptr
18    void init(int l, int r, int _n, const int num[]) {

```

```

19     tot = 0;
20     a = num;
21     ran = {l, r};
22     n = _n;
23     for (int i = 0; i <= n; i++) s[i] = t[i] = 0;
24     // init node 0
25     lson[0] = rson[0] = 0;
26     c[0] = 0;
27 }
28
29 inline int get(int &k, bool flag) {
30     if (k == 0 || flag) {
31         k = ++tot;
32         lson[k] = rson[k] = 0;
33     }
34     return k;
35 }
36
37 // update the root in k
38 void update(int k[], int rt[], int cnt, int p, int v, bool flag = false) {
39     // calc
40     for (int i = 0; i < cnt; i++)
41         c[k[i]] = c[rt[i]] + v;
42     int l, r;
43     tie(l, r) = ran;
44     while (l < r) {
45         int mid = (l + r) >> 1;
46         // 下面的逗号表达式顺序不能换
47         if (p <= mid) {
48             // go left
49             for (int i = 0; i < cnt; i++) {
50                 rson[k[i]] = rson[rt[i]];
51                 rt[i] = lson[rt[i]], k[i] = get(lson[k[i]], flag);
52             }
53             r = mid;
54         } else {
55             // go right
56             for (int i = 0; i < cnt; i++) {
57                 lson[k[i]] = lson[rt[i]];
58                 rt[i] = rson[rt[i]], k[i] = get(rson[k[i]], flag);
59             }
60             l = mid + 1;
61         }
62         // calc
63         for (int i = 0; i < cnt; i++)
64             c[k[i]] = c[rt[i]] + v;
65     }
66 }
67
68 // build static tree
69 void change(int pos, int p, int v) {
70     // use int as the int[]
71     // must use variable because I use the pointer
72     int rt = t[pos - 1];
73     int k = t[pos] = ++tot;
74     update(&k, &rt, 1, p, v, true);
75 }
76
77 int use1[LN], use2[LN];

```

```

78
79 // edit dynamic tree
80 void add(int pos, int p, int v) {
81     // memory reuse
82     int *k = use1, *rt = use2;
83     int cnt = 0;
84     for (int i = pos; i <= n; i += (i & -i), cnt++) {
85         rt[cnt] = s[i], k[cnt] = get(s[i], false);
86     }
87     update(k, rt, cnt, p, v);
88 }
89
90 // calc lson value in use
91 inline ll sum(int use[], int cnt) {
92     ll ans = 0;
93     for (int i = 0; i < cnt; i++)
94         ans += c[lson[use[i]]];
95     return ans;
96 }
97
98 // calc value in use
99 inline ll calc(int use[], int cnt) {
100     ll ans = 0;
101     for (int i = 0; i < cnt; i++)
102         ans += c[use[i]];
103     return ans;
104 }
105
106 // ans=p1-p2
107 ll querySum(int p1, int p2, int k) {
108     int rt1 = t[p1], rt2 = t[p2];
109     ll cnt1 = 0, cnt2 = 0;
110     // calc root in need
111     for (int i = p1; i; i -= (i & -i)) use1[cnt1++] = s[i];
112     for (int i = p2; i; i -= (i & -i)) use2[cnt2++] = s[i];
113     int l, r;
114     tie(l, r) = ran;
115     ll ans = 0;
116     while (l < r) {
117         int mid = (l + r) >> 1;
118         if (k <= mid) {
119             // go left
120             rt1 = lson[rt1], rt2 = lson[rt2];
121             for (int i = 0; i < cnt1; i++) use1[i] = lson[use1[i]];
122             for (int i = 0; i < cnt2; i++) use2[i] = lson[use2[i]];
123             r = mid;
124         } else {
125             // go right
126             ll cnt = sum(use1, cnt1) - sum(use2, cnt2) + c[lson[rt1]] - c[lson[rt2]
127 ];
128             ans += cnt;
129             rt1 = rson[rt1], rt2 = rson[rt2];
130             for (int i = 0; i < cnt1; i++) use1[i] = rson[use1[i]];
131             for (int i = 0; i < cnt2; i++) use2[i] = rson[use2[i]];
132             l = mid + 1;
133         }
134     }
135     ll cnt = calc(use1, cnt1) - calc(use2, cnt2) + c[rt1] - c[rt2];
136     ans += cnt;

```

```

136     return ans;
137 }
138
139 // query k
140 int queryK(int p1, int p2, int k) {
141     int r1 = t[p1], r2 = t[p2];
142     int cnt1 = 0, cnt2 = 0;
143     // calc root in need
144     for (int i = p1; i; i -= (i & -i)) use1[cnt1++] = s[i];
145     for (int i = p2; i; i -= (i & -i)) use2[cnt2++] = s[i];
146     int l, r;
147     tie(l, r) = ran;
148     while (l < r) {
149         int mid = (l + r) >> 1;
150         int cnt = c[lson[r1]] - c[lson[r2]] + sum(use1, cnt1) - sum(use2, cnt2);
151         if (cnt >= k) {
152             // go left
153             r1 = lson[r1], r2 = lson[r2];
154             for (int i = 0; i < cnt1; i++) use1[i] = lson[use1[i]];
155             for (int i = 0; i < cnt2; i++) use2[i] = lson[use2[i]];
156             r = mid;
157         } else {
158             // go right
159             k -= cnt;
160             r1 = rson[r1], r2 = rson[r2];
161             for (int i = 0; i < cnt1; i++) use1[i] = rson[use1[i]];
162             for (int i = 0; i < cnt2; i++) use2[i] = rson[use2[i]];
163             l = mid + 1;
164         }
165     }
166     return l;
167 }
168 } tree;

```

3.13 伸展树 Splay

```

1  const int N = int(1e6 + 100);
2
3  struct Node;
4  Node *tail, *null;
5  // 回收栈
6  Node *st[N], **stop;
7
8  struct Node {
9      // 内存池
10     static Node pool[N];
11
12     Node *ch[2], *fa;
13     bool rev, edit;
14     int size, val;
15     ll sum;
16     ll dpl, dpr, dpm; // 左端开始最大, 右端开始最大, 实际最大
17
18     // 初始化内存池
19     static void init() {
20         null = tail = pool;
21         null->clear();
22         stop = st;

```

```

23     }
24
25     // 清空当前
26     inline void clear(int _val = 0, int _size = 0) {
27         edit = rev = false;
28         sum = val = _val;
29         size = _size;
30         fa = ch[0] = ch[1] = null;
31         dpl = dpr = dpm = _val;
32     }
33
34     inline void push_up() {
35         if (this == null) return;
36         size = ch[0]->size + ch[1]->size + 1;
37         sum = ch[0]->sum + ch[1]->sum + val;
38         Node *x = ch[0], *y = ch[1];
39         if (size == 1) {
40             dpl = dpr = dpm = val;
41         } else if (y == null) {
42             dpl = max(x->dpl, x->sum + val);
43             dpr = max(1ll * val, val + x->dpr);
44             dpm = max(x->dpm, val + max(x->dpr, 0ll));
45         } else if (x == null) {
46             dpl = max(1ll * val, val + y->dpl);
47             dpr = max(y->dpr, y->sum + val);
48             dpm = max(y->dpm, val + max(y->dpl, 0ll));
49         } else {
50             dpl = max(x->dpl, max(x->sum + val, x->sum + val + y->dpl));
51             dpr = max(y->dpr, max(y->sum + val, y->sum + val + x->dpr));
52             dpm = max(max(x->dpm, y->dpm), val + max(x->dpr, 0ll) + max(y->dpl, 0ll));
53         }
54     }
55
56     // 设置儿子
57     inline void setc(Node *p, int d) { ch[d] = p, p->fa = this; }
58
59     // 获取方向
60     inline bool d() { return fa->ch[1] == this; }
61
62     inline void update_rev() {
63         if (this == null) return;
64         swap(ch[0], ch[1]);
65         swap(dpl, dpr);
66         rev ^= 1;
67     }
68
69     inline void update_val(int v) {
70         if (this == null) return;
71         val = v;
72         sum = 1ll * size * v;
73         edit = 1;
74         dpl = dpr = dpm = max(1ll * val, sum);
75     }
76
77     inline void push_down() {
78         if (this == null) return;
79         if (rev) {
80             ch[0]->update_rev(), ch[1]->update_rev();
81             rev = 0;

```

```

82     }
83     if (edit) {
84         ch[0]->update_val(val), ch[1]->update_val(val);
85         edit = 0;
86     }
87 }
88
89 inline bool isroot() {
90     return fa == null || (this != fa->ch[0] && this != fa->ch[1]);
91 }
92 };
93
94 Node Node::pool[N];
95
96 // 获取第k个
97 Node *get_kth(Node *x, int k) {
98     while (x->ch[0]->size + 1 != k) {
99         x->push_down();
100         if (x->ch[0]->size >= k) {
101             x = x->ch[0];
102         } else {
103             k -= x->ch[0]->size + 1;
104             x = x->ch[1];
105         }
106     }
107     return x;
108 }
109
110 void rotate(Node *x) {
111     Node *f = x->fa, *ff = f->fa;
112     f->push_down();
113     x->push_down();
114     int c = x->d(), cc = f->d();
115     f->setc(x->ch[!c], c);
116     x->setc(f, !c);
117     if (ff->ch[cc] == f) ff->setc(x, cc);
118     else x->fa = ff;
119     f->push_up();
120 }
121
122 void splay(Node *&root, Node *x, Node *goal) {
123     for (Node *f; (f = x->fa) != goal; rotate(x)) {
124         if (f->fa == goal) continue;
125         f->fa->push_down();
126         f->push_down();
127         x->push_down();
128         rotate(x->d() == f->d() ? f : x);
129     }
130     x->push_up();
131     if (goal == null) root = x;
132 }
133
134 int a[N];
135
136 // 获取有效节点
137 inline Node *getNode() { return stop == st ? ++tail : *--stop; }
138
139 Node *build(int l, int r) {
140     int mid = (l + r) >> 1;

```

```

141     Node *root = getNode();
142     root->clear();
143     root->val = a[mid];
144     root->size = 1;
145     if (l < mid) root->setc(build(l, mid - 1), 0);
146     if (r > mid) root->setc(build(mid + 1, r), 1);
147     root->push_up();
148     return root;
149 }
150
151 // l->root, r->root.ch[1]
152 inline Node *make(Node *&root, int l, int r) {
153     Node *x = get_kth(root, l);
154     splay(root, x, null);
155     Node *y = get_kth(root, r);
156     splay(root, y, root);
157     return y;
158 }
159
160 // 插入p子树
161 inline void insert(Node *&root, int l, int r, Node *p) {
162     Node *x = make(root, l, r);
163     x->setc(p, 0);
164     x->push_up();
165     x->fa->push_up();
166 }
167
168 // 回收内存
169 inline void clear(Node *&x) {
170     if (x == null) return;
171     auto now = stop;
172     *stop++ = x;
173     while (now != stop) {
174         x = *now++;
175         if (x->ch[0] != null) *stop++ = x->ch[0];
176         if (x->ch[1] != null) *stop++ = x->ch[1];
177     }
178 }
179
180 // 释放子树
181 inline void del(Node *&root, int l, int r) {
182     Node *x = make(root, l, r);
183     clear(x->ch[0]);
184     x->ch[0] = null;
185     x->push_up();
186     x->fa->push_up();
187 }
188
189 // 转向
190 inline void reverse(Node *&root, int l, int r) {
191     Node *x = make(root, l, r);
192     x->ch[0]->update_rev();
193     x->push_up();
194     x->fa->push_up();
195 }
196
197 // set value
198 inline void make_same(Node *&root, int l, int r, int val) {
199     Node *x = make(root, l, r);

```

```

200     x->ch[0]->update_val(val);
201     x->push_up();
202     x->fa->push_up();
203 }
204
205 // 求和
206 inline ll sum(Node *&root, int l, int r) {
207     Node *x = make(root, l, r);
208     return x->ch[0]->sum;
209 }
210
211 // 求最大子串和
212 inline ll maxsum(Node *&root, int l, int r) {
213     Node *x = make(root, l, r);
214     return x->ch[0]->dpm;
215 }
216
217 void debug(Node *root) {
218     function<void(Node *)> dfs = [&dfs](Node *x) {
219         if (x == null) return;
220         x->push_down();
221         dfs(x->ch[0]);
222         cout << x->val << ' ';
223         dfs(x->ch[1]);
224     };
225     dfs(root);
226     cout << endl;
227 }

```

3.14 带权并查集

```

1  const int N = 100005;
2  int f[N], deep[N], d[N];
3
4  void init(int n) {
5      for (int i = 0; i <= n; i++) f[i] = i, d[i] = 0;
6  }
7
8  int fa(int x) {
9      if (f[x] == x) return x;
10     int fx = fa(f[x]);
11     (d[x] += d[f[x]]) %= 3;
12     return f[x] = fx;
13 }
14
15 bool un(int x, int y, int dis) {
16     int fx = fa(x), fy = fa(y);
17     if (fx == fy) {
18         return ((d[y] - d[x] + 3) % 3 != dis);
19     }
20     int w = (3 + (d[x] - d[y]) + dis) % 3;
21     // 按秩合并
22     if (deep[fx] < deep[fy]) {
23         swap(fx, fy);
24         w = (3 - w) % 3;
25     }
26     f[fy] = fx;
27     d[fy] = w;

```



```

28 // 按秩合并
29 deep[fx] += deep[fx] == deep[fy];
30 return true;
31 }

```

3.15 可持久化并查集

```

1  const int N = int(2e5 + 10);
2  const int MAXN = N * 150;
3
4  struct PArray {
5      int tot = 0;
6      struct node {
7          int val, deep;
8      } c[MAXN];
9      int lson[MAXN], rson[MAXN];
10     pii ran;
11
12     int build(int l, int r) {
13         int k = tot++;
14         if (l == r) {
15             c[k].val = l;
16             return k;
17         }
18         int mid = (l + r) >> 1;
19         lson[k] = build(l, mid);
20         rson[k] = build(mid + 1, r);
21         return k;
22     }
23
24     int init(int l, int r) {
25         ran = {l, r};
26         return build(l, r);
27     }
28
29     int update(int rt, int p, node w) {
30         int l = ran.first, r = ran.second;
31         int k = tot++, rst = k;
32         while (l < r) {
33             lson[k] = lson[rt], rson[k] = rson[rt];
34             int mid = (l + r) >> 1;
35             if (p <= mid) {
36                 rt = lson[rt];
37                 k = lson[k] = tot++;
38                 r = mid;
39             } else {
40                 rt = rson[rt];
41                 k = rson[k] = tot++;
42                 l = mid + 1;
43             }
44         }
45         c[k].val = w.val;
46         c[k].deep = c[rt].deep + w.deep;
47         return rst;
48     }
49
50     node query(int rt, int p) {
51         int l = ran.first, r = ran.second;

```

```

52     while (l < r) {
53         int mid = (l + r) >> 1;
54         if (p <= mid) {
55             rt = lson[rt];
56             r = mid;
57         } else {
58             rt = rson[rt];
59             l = mid + 1;
60         }
61     }
62     return c[rt];
63 }
64 };
65
66 struct PDSU {
67     PArray tree;
68     int root[N];
69
70     void init(int n) {
71         root[0] = tree.init(1, n);
72     }
73
74     PArray::node fa(int rt, int x) {
75         PArray::node u = tree.query(root[rt], x);
76         while (u.val != x) {
77             x = u.val;
78             u = tree.query(root[rt], x);
79         }
80         return u;
81     }
82
83     inline void change(int rt, int k) {
84         root[k] = root[rt];
85     }
86
87     inline void un(int rt, int x, int y) {
88         auto fx = fa(rt, x), fy = fa(rt, y);
89         if (fx.val == fy.val) return;
90         if (fx.deep > fy.deep) swap(fx, fy);
91         root[rt] = tree.update(root[rt], fx.val, {fy.val, fx.deep});
92         if (fx.deep == fy.deep) root[rt] = tree.update(root[rt], fy.val, {fy.val, fy.
            deep + 1});
93     }
94 } dsu;

```

4 图论

4.1 Graph

```

1  #define forg(i, h, eg) for(int i = (h); ~i; i = (eg[i]).nxt)
2
3  struct Edge {
4      int e, nxt;
5      ll v;
6      Edge() = default;
7      Edge(int a, ll b, int c = 0) : e(a), v(b), nxt(c) {}
8
9      bool operator<(const Edge &a) const {
10         return (a.v == v ? e < a.e : v < a.v);
11     }
12 };
13
14 const ll INF = ll(1e11);
15 const int N = int(1e5 + 10);
16 const int M = int(3e5 + 10);
17
18 struct Graph {
19     Edge eg[M];
20     int head[N];
21     int cnt;
22
23     void init(int n) {
24         memset(head, -1, sizeof(int) * ++n);
25         cnt = 0;
26     }
27
28     inline void addEdge(int x, int y, ll v = 0) {
29         eg[cnt] = Edge(y, v, head[x]);
30         head[x] = cnt++;
31     }
32 } gh;

```

4.2 Dijkstra

```

1  int dist[N];
2  int path[N];
3
4  void bfs(int s, int n) {
5      n++;
6      rep(i, 0, n) dist[i] = INF;
7      memset(path, -1, sizeof(int) * n);
8      dist[s] = 0;
9      path[s] = s;
10     // 注意优先队列默认less运算, 但选择最大的作为top, 注意cmp!!!
11     priority_queue<Edge, vector<Edge>, greater<Edge>> q;
12     q.push(Edge(s, dist[s]));
13     while (!q.empty()) {
14         Edge f = q.top();
15         q.pop();
16         for (int i = gh.head[f.e]; ~i; i = gh.eg[i].nxt) {
17             Edge &t = gh.eg[i];
18             if (dist[t.e] > f.v + t.v) {
19                 dist[t.e] = f.v + t.v;

```

```

20         path[t.e] = f.e;
21         q.push(Edge(t.e, dist[t.e]));
22     }
23 }
24 }
25 }
26
27 #include <ext/pb_ds/priority_queue.hpp>
28 #include <ext/pb_ds/assoc_container.hpp>
29 typedef __gnu_pbds::priority_queue<Edge, greater<Edge>> heap;
30 // 使用该模板, 需要注意因为使用了greater, 所以需要重载大于运算
31 // 默认pairing_heap_tag
32 // push O(1), pop O(logn) modify O(logn) erase O(logn) join O(1)
33 // 可选thin_heap_tag
34 // push O(1), pop O(logn) modify O(1) erase O(logn) join O(n)
35
36 heap::point_iterator its[N];
37 int cnt[N];
38
39 void bfs(int s, int n) {
40     n++;
41     rep(i, 0, n) dist[i] = INF;
42     memset(cnt, 0, sizeof(int) * n);
43     dist[s] = 0;
44     cnt[s] = 1;
45     heap q;
46     its[s] = q.push(Edge(s, dist[s]));
47     while (!q.empty()) {
48         Edge f = q.top();
49         q.pop();
50         for (int i = gh.head[f.e]; ~i; i = gh.eg[i].nxt) {
51             Edge &t = gh.eg[i];
52             its[t.e] = 0;
53             int v = f.v + t.v;
54             if (dist[t.e] > v) {
55                 dist[t.e] = v;
56                 if (its[t.e] != 0) {
57                     q.modify(its[t.e], Edge(t.e, dist[t.e]));
58                 } else {
59                     its[t.e] = q.push(Edge(t.e, dist[t.e]));
60                 }
61                 cnt[t.e] = cnt[f.e];
62             } else if (dist[t.e] == v) {
63                 (cnt[t.e] += cnt[f.e]) %= 100003;
64             }
65         }
66     }
67 }

```

4.3 spfa

```

1 vector<int> dist;
2 vector<vector<node>> eg;
3 vector<int> path;
4
5 bool spfa(int n, int start) {
6     dist.assign(n, INF);
7     dist[start] = 0;

```

```

8     deque<int> q;
9     q.push_back(start);
10    path.assign(n, -1);
11    vector<int> cnt(n, 0);
12    vector<bool> flag(n, false);
13    cnt[start] = flag[start] = true;
14    while (!q.empty()) {
15        const int now = q.front();
16        q.pop_front();
17        flag[now] = false;
18        for (auto i: eg[now]) {
19            if (dist[i.x] > dist[now] + i.d) {
20                dist[i.x] = dist[now] + i.d;
21                path[i.x] = now;
22                if (!flag[i.x]) {
23                    if (n == ++cnt[i.x]) return false;
24                    //队列非空且优于队首 (SLF)
25                    if (!q.empty() && dist[i.x] < dist[q.front()]) {
26                        q.push_front(i.x);
27                    } else {
28                        q.push_back(i.x);
29                    }
30                    flag[i.x] = true;
31                }
32            }
33        }
34    }
35    return true;
36 }

```

4.4 Dinic

```

1  struct Dinic {
2      Graph gh;
3      // 点的范围[0, n)
4      int n;
5      // 弧优化
6      int cur[N], dis[N];
7
8      Dinic(){};
9
10     // 设置N
11     void init(int _n) {
12         n = _n;
13         gh.init(n);
14     }
15
16     // 加流量
17     void addFlow(int x, int y, ll f) {
18         gh.addEdge(x, y, f);
19         gh.addEdge(y, x, 0);
20     }
21
22     bool bfs(int s, int e) {
23         memset(dis, -1, sizeof(int) * n);
24         int q[N];
25         int l, r;
26         l = r = 0;

```

```

27     dis[s] = 0;
28     q[r++] = s;
29     while (l < r) {
30         int f = q[l++];
31         for (int i = gh.head[f]; ~i; i = gh.eg[i].nxt) {
32             if (gh.eg[i].v > 0 && dis[gh.eg[i].e] == -1) {
33                 dis[gh.eg[i].e] = dis[f] + 1;
34                 q[r++] = gh.eg[i].e;
35             }
36         }
37     }
38     return dis[e] > 0;
39 }
40
41 ll dfs(int s, int e, ll mx) {
42     if (s == e || mx == 0) {
43         return mx;
44     }
45     ll flow = 0;
46     for (int &k = cur[s]; ~k; k = gh.eg[k].nxt) {
47         auto &eg = gh.eg[k];
48         ll a;
49         if (eg.v > 0 && dis[eg.e] == dis[s] + 1 && (a = dfs(eg.e, e, min(eg.v, mx)))
50     ) {
51         eg.v -= a;
52         gh.eg[k ^ 1].v += a;
53         flow += a;
54         mx -= a;
55         if (mx <= 0) break;
56     }
57     return flow;
58 }
59
60 ll max_flow(int s, int e) {
61     ll ans = 0;
62     while (bfs(s, e)) {
63         memcpy(cur, gh.head, sizeof(int) * n);
64         ans += dfs(s, e, INF);
65     }
66     return ans;
67 }
68 } dinic;

```

4.5 hungry

```

1  #define N 105
2  #define M 10005
3  int n, m, k;
4  pii eg[M * 2];
5  int result[N * 2];
6  int head[N * 2];
7  int cnt = 0;
8
9  void addEdge(int x, int y) {
10     eg[cnt].first = y;
11     eg[cnt].second = head[x];
12     head[x] = cnt++;

```

```

13 }
14
15 bool vis[M * 2] = {false};
16
17 int dfs(int x) {
18     for (int i = head[x]; ~i; i = eg[i].second) {
19         int y = eg[i].first;
20         if (!vis[y]) {
21             vis[y] = true;
22             if (result[y] == -1 || dfs(result[y])) {
23                 result[y] = x;
24                 return 1;
25             }
26         }
27     }
28     return 0;
29 }
30
31 int MaxMatch() {
32     int ans = 0;
33     memset(result, -1, sizeof(result));
34     rep(i, 1, n + 1) {
35         memset(vis, 0, sizeof(vis));
36         ans += dfs(i);
37     }
38     return ans;
39 }
40
41 void solve() {
42     scanf("%d%d", &m, &k);
43     memset(head, -1, sizeof(head));
44     cnt = 0;
45     rep(i, 0, k) {
46         int x, y;
47         scanf("%d%d", &x, &y);
48         addEdge(x, y);
49     }
50     int ans = MaxMatch();
51     printf("%d\n", ans);
52 }

```

4.6 MinSpanTree

```

1  /*
2  * Prim 求 MST
3  * 耗费矩阵 cost[][], 标号从 0 开始, 0~n-1
4  * 返回最小生成树的权值, 返回 -1 表示原图不连通
5  */
6  const int INF = 0x3f3f3f3f;
7  const int N = 110;
8  bool vis[N];
9  int lowc[N]; //点是 0 n-1
10 int prim(int cost[][N], int n) {
11     int ans = 0;
12     memset(vis, false, sizeof(vis));
13     vis[0] = true;
14     for (int i = 1; i < n; i++) lowc[i] = cost[0][i];
15     for (int i = 1; i < n; i++) {

```

```

16     int minc = INF;
17     int p = -1;
18
19     for (int j = 0; j < n; j++)
20         if (!vis[j] && minc > lowc[j]) {
21             minc = lowc[j];
22             p = j;
23         }
24     if (minc == INF) return -1; // 原图不连通
25     ans += minc;
26     vis[p] = true;
27     for (int j = 0; j < n; j++)
28         if (!vis[j] && lowc[j] > cost[p][j])
29             lowc[j] = cost[p][j];
30 }
31 return ans;
32 }

```

4.7 MinCostMaxFlow

```

1 struct Edge {
2     int e, nxt;
3     ll flow, cost;
4
5     Edge() {};
6
7     Edge(int a, ll b, ll c, int d = 0) : e(a), flow(b), cost(c), nxt(d) {}
8 };
9
10 const ll INF = 1000000;
11 const int N = int(1e5 + 10);
12 const int M = int(1e5 + 10);
13
14 // 前向星
15 struct Graph {
16     Edge eg[M];
17     int head[N];
18     int cnt;
19
20     void init(int n) {
21         memset(head, -1, sizeof(int) * ++n);
22         cnt = 0;
23     }
24
25     inline void addEdge(int x, int y, ll v, ll c) {
26         eg[cnt] = Edge(y, v, c, head[x]);
27         head[x] = cnt++;
28     }
29 };
30
31 struct MinCostMaxFlow {
32     Graph gh;
33     // 点的范围[0, n)
34     int n;
35
36     // 设置N
37     void init(int _n) {
38         n = _n + 1;

```



```

39     gh.init(n);
40 }
41
42 // 加流量, 反向是负的花费
43 void addFlow(int x, int y, ll f, ll c) {
44     // printf("%d->%d: %lld\t%lld\n", x, y, f, c); fflush(stdout);
45     gh.addEdge(x, y, f, c);
46     gh.addEdge(y, x, 0, -c);
47 }
48
49 // 该pre存的是边
50 int pre[N];
51 int dis[N];
52 bool vis[N];
53
54 bool spfa(int s, int e) {
55     queue<int> q;
56     for (int i = 0; i < n; i++) {
57         dis[i] = INF;
58         vis[i] = false;
59         pre[i] = -1;
60     }
61     dis[s] = 0;
62     vis[s] = true;
63     q.push(s);
64     while (!q.empty()) {
65         int u = q.front();
66         q.pop();
67         vis[u] = false;
68         for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
69             Edge &eg = gh.eg[i];
70             if (eg.flow > 0 && dis[eg.e] > dis[u] + eg.cost) {
71                 dis[eg.e] = dis[u] + eg.cost;
72                 pre[eg.e] = i;
73                 if (!vis[eg.e]) {
74                     vis[eg.e] = true;
75                     q.push(eg.e);
76                 }
77             }
78         }
79     }
80     return pre[e] != -1;
81 }
82
83 pll cal(int s, int e) {
84     ll flow = 0, cost = 0;
85     while (spfa(s, e)) {
86         ll f = INF;
87         for (int i = pre[e]; ~i; i = pre[gh.eg[i ^ 1].e]) {
88             f = min(f, gh.eg[i].flow);
89         }
90         for (int i = pre[e]; ~i; i = pre[gh.eg[i ^ 1].e]) {
91             gh.eg[i].flow -= f;
92             gh.eg[i ^ 1].flow += f;
93             cost += gh.eg[i].cost;
94         }
95         flow += f;
96     }
97     return make_pair(flow, cost);

```

```

98     }
99
100 } network;
101
102 // vector图存
103 struct MinCostMaxFlow {
104     vector<Edge> g[N];
105     // 点的范围[0, n)
106     int n = 0;
107
108     // 设置N
109     void init(int _n) {
110         rep(i, 0, n) {
111             g[i].clear();
112         }
113         n = _n + 1;
114     }
115
116     // 加流量, 反向是负的花费
117     void addFlow(int x, int y, int f, int c) {
118         g[x].push_back(Edge(y, f, c, g[y].size()));
119         g[y].push_back(Edge(x, 0, -c, g[x].size() - 1));
120     }
121
122     // 该pre存的是(点,边)
123     pii pre[N];
124     int dis[N];
125     bool vis[N];
126     int h[N];
127
128     int cnt = 0;
129
130     bool bfs(int s, int e) {
131         priority_queue<pii, vector<pii>, greater<pii>> q;
132         for (int i = 0; i < n; i++) {
133             dis[i] = INF;
134             vis[i] = false;
135             pre[i] = pii(-1, -1);
136         }
137         dis[s] = 0;
138         q.push(pii(0, s));
139         while (!q.empty()) {
140             pii f = q.top();
141             int u = f.second;
142             q.pop();
143             if (f.first != dis[u]) continue;
144             for (int i = 0; i < sz(g[u]); i++) {
145                 auto &eg = g[u][i];
146                 if (eg.flow == 0) continue;
147                 int v = eg.e;
148                 int cost = eg.cost + dis[u] + h[u] - h[v];
149                 if (dis[v] > cost) {
150                     cnt++;
151                     dis[v] = cost;
152                     pre[v] = pii(u, i);
153                     q.push(pii(dis[v], v));
154                 }
155             }
156         }

```

```

157     for (int i = 0; i < n; i++) {
158         h[i] += dis[i];
159     }
160     return pre[e].second != -1;
161 }
162
163 pii cal(int s, int e, int limit) {
164     int flow = 0, cost = 0;
165     memset(h, 0, sizeof(int) * n);
166     cnt = 0;
167     while (limit) {
168         if (!bfs(s, e)) break;
169         int f = INF;
170         for (int i = e; ~pre[i].second; i = pre[i].first) {
171             f = min(f, g[pre[i].first][pre[i].second].flow);
172         }
173         for (int i = e; ~pre[i].second; i = pre[i].first) {
174             g[pre[i].first][pre[i].second].flow -= f;
175             g[i][g[pre[i].first][pre[i].second].nxt].flow += f;
176         }
177         cost += f * h[e];
178         flow += f;
179         limit -= f;
180     }
181     return make_pair(flow, cost);
182 }
183
184 } network;

```

4.8 ISAP

```

1 struct ISAP {
2     Graph gh;
3     // 点的范围[0, n)
4     int n;
5     // 弧优化
6     int cur[N], dis[N];
7     ISAP() {}
8     // 设置N
9     void init(int _n) {
10         n = _n;
11         gh.init(n);
12     }
13
14     // 加流量
15     inline void addFlow(int x, int y, ll f) {
16         gh.addEdge(x, y, f);
17         gh.addEdge(y, x, 0);
18     }
19
20     int dep[N]; // 记录距离标号
21     int gap[N]; // gap常数优化
22     int q[N]; // 数组模拟队列
23
24     void bfs(int s, int e) {
25         memset(dep, -1, sizeof(int) * n);
26         memset(gap, 0, sizeof(int) * n);
27         gap[0] = 1;

```

```

28     dep[e] = 0;
29     int l = 0, r = 0;
30     q[r++] = e;
31     while (l < r) {
32         int u = q[l++];
33         for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
34             int v = gh.eg[i].e;
35             if (~dep[v]) continue;
36             q[r++] = v;
37             dep[v] = dep[u] + 1;
38             gap[dep[v]]++;
39         }
40     }
41 }
42
43 ll st[N]; // 栈优化
44
45 ll max_flow(int s, int e) {
46     bfs(s, e);
47     memcpy(cur, gh.head, sizeof(int) * n);
48     int top = 0;
49     int u = s;
50     ll ans = 0;
51     while (dep[s] < N) {
52         if (u == e) {
53             ll mf = INF;
54             int sel = 0;
55             for (int i = 0; i < top; i++) {
56                 if (mf > gh.eg[st[i]].v) {
57                     mf = gh.eg[st[i]].v;
58                     sel = i;
59                 }
60             }
61
62             for (int i = 0; i < top; i++) {
63                 gh.eg[st[i]].v -= mf;
64                 gh.eg[st[i] ^ 1].v += mf;
65             }
66             ans += mf;
67             top = sel;
68             u = gh.eg[st[top] ^ 1].e;
69             continue;
70         }
71         bool flag = false;
72         int v = 0;
73         for (int i = cur[u]; ~i; i = gh.eg[i].nxt) {
74             v = gh.eg[i].e;
75             if (gh.eg[i].v > 0 && dep[v] + 1 == dep[u]) {
76                 flag = true;
77                 cur[u] = i;
78                 break;
79             }
80         }
81         if (flag) {
82             st[top++] = cur[u];
83             u = v;
84             continue;
85         }
86         int mind = N;

```

```

87         for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
88             if (gh.eg[i].v > 0 && dep[gh.eg[i].e] < mind) {
89                 mind = dep[gh.eg[i].e];
90                 cur[u] = i;
91             }
92         }
93         gap[dep[u]]--; // 当前层无法连通, 降层
94         if (!gap[dep[u]]) return ans; // 断层结束运算
95         dep[u] = mind + 1; // 进入更高层
96         gap[dep[u]]++;
97         if (u != s) u = gh.eg[st[--top] ^ 1].e;
98     }
99     return ans;
100 }
101 } isap;

```

4.9 树链剖分

```

1 struct TreeChain {
2     int top[N]; // 链条顶端点ID
3     int fa[N]; // 父亲节点
4     int son[N]; // 重儿子
5     int deep[N]; // 深度
6     int num[N]; // 儿子节点数 (包括自己)
7
8
9     int p[N]; // 在线段树中的ID,
10    int fp[N]; // 线段树中ID对应的点
11    int tot;
12
13    void dfs(int u, int pre, int d) {
14        num[u] = 1;
15        deep[u] = d;
16        fa[u] = pre;
17        for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
18            int v = gh.eg[i].e;
19            if (v == pre) continue;
20            dfs(v, u, d + 1);
21            num[u] += num[v];
22            if (son[u] == -1 || num[v] > num[son[u]]) {
23                son[u] = v;
24            }
25        }
26    }
27
28    void getpos(int u, int sp) {
29        top[u] = sp;
30        p[u] = tot++;
31        fp[p[u]] = u;
32        if (son[u] == -1) return;
33        getpos(son[u], sp);
34        for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
35            int v = gh.eg[i].e;
36            if (v == son[u] || v == fa[u]) continue;
37            getpos(v, v);
38        }
39    }
40

```

```

41     void build(int start, int root, int n) {
42         memset(son, -1, sizeof(int) * ++n);
43         tot = start; // start是线段树中的ID起始数值
44         dfs(root, 0, 0);
45         getpos(root, root);
46     }
47 } treec;
48
49 // 树状数组, 如果无需在线查询可以使用差分树
50 BITree tree;
51
52 // 点权修改
53 void change1(int u, int v, ll val) {
54     int f1 = treec.top[u];
55     int f2 = treec.top[v];
56     while (f1 != f2) {
57         if (treec.deep[f1] < treec.deep[f2]) {
58             swap(f1, f2);
59             swap(u, v);
60         }
61         tree1.update(treec.p[f1], treec.p[u], val);
62         u = treec.fa[f1];
63         f1 = treec.top[u];
64     }
65     if (treec.deep[u] > treec.deep[v]) {
66         swap(u, v);
67     }
68     tree1.update(treec.p[u], treec.p[v], val);
69 }
70
71 // 边权修改
72 void change2(int u, int v, ll val) {
73     int f1 = treec.top[u];
74     int f2 = treec.top[v];
75     while (f1 != f2) {
76         if (treec.deep[f1] < treec.deep[f2]) {
77             swap(f1, f2);
78             swap(u, v);
79         }
80         tree2.update(treec.p[f1], treec.p[u], val);
81         u = treec.fa[f1];
82         f1 = treec.top[u];
83     }
84     if (treec.deep[u] > treec.deep[v]) {
85         swap(u, v);
86     }
87     tree2.update(treec.p[treec.son[u]], treec.p[v], val);
88 }

```

4.10 倍增 LCA

```

1  const int MAX_DEP = 20;
2
3  // 倍增 $2^k$ 的父亲
4  int fa[N][MAX_DEP];
5  int dep[N];
6
7  // 倍增LCA

```

```

8  int lca(int u, int v) {
9      if (dep[u] > dep[v]) {
10         swap(u, v);
11     }
12     int hu = dep[u], hv = dep[v];
13     int tu = u, tv = v;
14     for (int det = hv - hu, i = 0; det; det >>= 1, i++) {
15         if (det & 1)
16             tv = fa[tv][i];
17     }
18     if (tu == tv) {
19         return tu;
20     }
21     for (int i = MAX_DEP - 1; i >= 0; i--) {
22         if (fa[tu][i] == fa[tv][i]) {
23             continue;
24         }
25         tu = fa[tu][i];
26         tv = fa[tv][i];
27     }
28     return fa[tu][0];
29 }
30
31 // 动态更新节点的父亲属性
32 void lineFa(int u, int v) {
33     fa[u][0] = v;
34     for (int i = 1; i < MAX_DEP; i++) {
35         v = fa[u][i] = fa[v][i - 1];
36     }
37 }

```

4.11 Tarjan

```

1  int dfn[N], low[N], st[N], belong[N], num[N];
2  bool inst[N];
3  int idx, top, scc;
4
5  void tarjan(int u) {
6      dfn[u] = low[u] = ++idx;
7      st[top++] = u;
8      inst[u] = true;
9      for (int i = gh.head[u]; i != -1; i = gh.eg[i].nxt) {
10         int v = gh.eg[i].e;
11         if (!dfn[v]) {
12             tarjan(v);
13             low[u] = min(low[u], low[v]);
14         } else if (inst[v]) {
15             low[u] = min(low[u], dfn[v]);
16         }
17     }
18     int v;
19     if (dfn[u] == low[u]) {
20         scc++;
21         do {
22             v = st[--top];
23             inst[v] = false;
24             belong[v] = scc;
25             num[scc]++;

```

```

26         } while (u != v);
27     }
28 }
29
30 void work() {
31     fill_n(dfn, n + 1, 0);
32     fill_n(num, n + 1, 0);
33     fill_n(inst, n + 1, false);
34     idx = top = scc = 0;
35     for (int i = 1; i <= n; i++) {
36         if (!dfn[i])
37             tarjan(i);
38     }
39 }

```

4.12 支配树

```

1  const int MAX_DEP = 20;
2
3  // 注意0,1点的边界问题
4  struct DominatorTree {
5      int deg[N]; // 入度
6      int dep[N]; //
7      int dfn[N];
8      int st[N];
9      int tot;
10
11     // 拓扑序, 要保证root是入度为0
12     void bfs(Graph &gh, int root) {
13         queue<int> q;
14         q.push(root);
15         tot = 0;
16         while (!q.empty()) {
17             int u = q.front();
18             q.pop();
19             dfn[u] = ++tot;
20             st[tot] = u;
21             for (i = gh.head[u], gh.eg) {
22                 int v = gh.eg[i].e;
23                 if ((--deg[v]) == 0) {
24                     q.push(v);
25                 }
26             }
27         }
28     }
29
30     // 倍增2^k的父亲
31     int fa[N][MAX_DEP];
32
33     // 倍增LCA
34     int lca(int u, int v) {
35         if (dep[u] > dep[v]) {
36             swap(u, v);
37         }
38         int hu = dep[u], hv = dep[v];
39         int tu = u, tv = v;
40         for (int det = hv - hu, i = 0; det; det >>= 1, i++) {
41             if (det & 1)

```



```

42         tv = fa[tv][i];
43     }
44     if (tu == tv) {
45         return tu;
46     }
47     for (int i = MAX_DEP - 1; i >= 0; i--) {
48         if (fa[tu][i] == fa[tv][i]) {
49             continue;
50         }
51         tu = fa[tu][i];
52         tv = fa[tv][i];
53     }
54     return fa[tu][0];
55 }
56
57 // 动态更新节点的父亲属性
58 void lineFa(int u, int v) {
59     fa[u][0] = v;
60     for (int i = 1; i < MAX_DEP; i++) {
61         v = fa[u][i] = fa[v][i - 1];
62     }
63 }
64
65 // 建树, op是gh的反向图, 用来寻找其父亲
66 void build(Graph &gh, Graph &op, int n, int root) {
67     memcpy(deg, gh.deg, sizeof(int) * (n + 1));
68     bfs(gh, root);
69     for (int k = 1; k <= tot; k++) {
70         int u = st[k], fath = -1;
71         dep[u] = 0;
72         for (int i = op.head[u]; ~i; i = op.eg[i].nxt) {
73             int v = op.eg[i].e;
74             if (dfn[v] > dfn[u]) continue;
75             fath = (fath == -1 ? v : lca(fath, v));
76         }
77         if (fath == -1) fath = u;
78         lineFa(u, fath);
79         dep[u] = dep[fath] + 1;
80     }
81 }
82 } dtree;

```

4.13 Hopcroft-Karp

```

1  int dis;
2  // linkx: x链接的y, linky: y链接的x
3  int linkx[N], linky[N];
4  int dx[N], dy[N];
5  bool vis[N];
6
7  bool searchP(int n) {
8      queue<int> q;
9      dis = INF;
10     mst(dx, -1, n);
11     mst(dy, -1, n);
12     for (int i = 0; i < n; i++) {
13         if (linkx[i] == -1) {
14             q.push(i);

```

```

15         dx[i] = 0;
16     }
17 }
18 while (!q.empty()) {
19     int u = q.front();
20     q.pop();
21     if (dx[u] > dis) break;
22     for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
23         int v = gh.eg[i].e;
24         if (dy[v] == -1) {
25             dy[v] = dx[u] + 1;
26             if (linky[v] == -1) {
27                 dis = dy[v];
28             } else {
29                 dx[linky[v]] = dy[v] + 1;
30                 q.push(linky[v]);
31             }
32         }
33     }
34 }
35 return dis != INF;
36 }
37
38 bool dfs(int u) {
39     for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
40         int v = gh.eg[i].e;
41         if (!vis[v] && dy[v] == dx[u] + 1) {
42             vis[v] = true;
43             if (linky[v] != -1 && dy[v] == dis) continue;
44             if (linky[v] == -1 || dfs(linky[v])) {
45                 linky[v] = u;
46                 linkx[u] = v;
47                 return true;
48             }
49         }
50     }
51     return false;
52 }
53
54 int MaxMatch(int n) {
55     int rst = 0;
56     mst(linkx, -1, n);
57     mst(linky, -1, n);
58     while (searchP(n)) {
59         mst(vis, false, n);
60         for (int i = 0; i < n; i++) {
61             if (linkx[i] == -1 && dfs(i)) {
62                 rst++;
63             }
64         }
65     }
66     return rst;
67 }

```

5 博弈

5.1 GameProblem

```

1 // 巴什博弈, 是否先手必胜
2 inline bool bash_game(int n, int m) {
3     // 一堆东西, n个物品, 最多选m个
4     return n % (m + 1);
5 }
6
7 // 威佐夫博弈, 是否先手必胜
8 // 有两堆各若干的物品, 两人轮流从其中一堆取至少一件物品, 至多不限, 或从两堆中同时取相同件物品, 规定最后
   取完者胜利。
9 inline bool wythoff_game(int n, int m) {
10     if (n > m) {
11         swap(n, m);
12     }
13     int temp = floor((n2 - n1) * (1 + sqrt(5.0)) / 2.0);
14     return temp != n1;
15 }
16 // SG函数
17 #define N 1001
18 // f[]: 可以取走的石子个数
19 // sg[]: 0~n的SG函数值
20 int f[N], sg[N], mex[N];
21
22 void getSG(int n) {
23     int i, j;
24     memset(sg, 0, sizeof(sg));
25     for (i = 1; i <= n; i++) {
26         memset(mex, 0, sizeof(mex));
27         for (j = 1; f[j] <= i; j++)
28             mex[sg[i - f[j]]] = 1;
29         for (j = 0; j <= n; j++) { // 求mex{}中未出现的最小的非负整数
30             if (mex[j] == 0) {
31                 sg[i] = j;
32                 break;
33             }
34         }
35     }
36 }
37
38 // Auti-nim 反尼姆游戏
39 // 当先拿完所有石子时候输
40 // 当如下条件时, 先手必胜
41 // 0 : 所有堆的石子数均=1, 且有偶数堆。
42 // 1 : 至少有一个堆的石子数>1, 且石子堆的异或和≠0。

```

6 分治

6.1 IntegerFastPower

```

1 ll fpow(ll x, ll k) {
2     ll base = x, r = 1;
3     for (; k; k >>= 1) {
4         if (k & 1) r = r * base;
5         base = base * base;
6     }
7     return r;
8 }

```

6.2 MatrixFastPower

```

1 #define MAX_N 10
2 #define mod_num 9973
3
4 struct Mat {
5     long long mat[MAX_N][MAX_N];
6     long long n;
7     Mat() {
8         memset(mat, 0, sizeof(mat));
9         n = 0;
10    }
11    Mat(long long n) {
12        memset(mat, 0, sizeof(mat));
13        this->n = n;
14    }
15    void init() {
16        for (int i = 0; i < n; ++i) {
17            mat[i][i] = 1;
18        }
19    }
20    Mat(const long long ** list, long long n) {
21        this->n = n;
22        for (int i = 0; i < n; ++i) {
23            for (int j = 0; j < n; ++j) {
24                mat[i][j] = list[i][j];
25            }
26        }
27    }
28 };
29
30 Mat operator * (Mat a, Mat b) {
31     long long n = a.n;
32     Mat c(n);
33     memset(c.mat, 0, sizeof(c.mat));
34     for (int i = 0; i < n; ++i) {
35         for (int j = 0; j < n; ++j) {
36             for (int k = 0; k < n; ++k) {
37                 c.mat[i][j] += (a.mat[i][k] * b.mat[k][j]) % mod_num;
38                 c.mat[i][j] %= mod_num;
39             }
40         }
41     }
42     return c;
43 }

```

```

44
45 Mat operator ^ (Mat a, int k) {
46     long long n = a.n;
47     Mat c(n);
48     c.init();
49     for (; k; k >>= 1) {
50         if (k & 1) c = c * a;
51         a = a * a;
52     }
53     return c;
54 }

```

6.3 三维 CDQ

```

1 struct node {
2     // time: 时间 | id: 0,1 是否修改 | f: 正负 | x是下标 | y是权值
3     int time, id, f, x, y;
4 };
5
6 bool cmp(const node &a, const node &b) {
7     return a.x < b.x;
8 }
9
10 int ans[N];
11 node p[N << 2], et[N << 2];
12
13 void cdq(int l, int r) {
14     if (l + 1 == r) return;
15     int mid = (l + r) >> 1;
16     cdq(l, mid), cdq(mid, r);
17     int t = l;
18     for (int i = mid; i < r; i++) {
19         // if edit continue
20         if (p[i].id) continue;
21         for (; t < mid && p[t].x <= p[i].x; t++) {
22             if (p[t].id) tree.change(p[t].y, p[t].f);
23         }
24         int f = p[i].f;
25         int cnt = tree.query(p[i].y);
26         ans[p[i].time] += f * cnt;
27     }
28     // 逆操作p[t].y
29     while (--t >= l) {
30         if (p[t].id) tree.change(p[t].y, -p[t].f);
31     }
32     // 归并排序
33     int t1 = l, t2 = mid, k = 0;
34     while (t1 < mid && t2 < r) {
35         et[k++] = p[t1].x < p[t2].x ? p[t1++] : p[t2++];
36     }
37     copy(p + t1, p + mid, et + k);
38     copy(p + t2, p + r, et + k);
39     copy(et, et + (r - l), p + l);
40 }

```

6.4 树分治-点分治

```

1 // 题意: n个节点的树, 存在边权, 范围1e18
2 // 求任意两点之间点集的子集中两点之间路径异或和为0的个数
3 //  $u < v, u' < v', (u', v') \sqcap \text{path}(u, v)$ , 求 $\text{path}(u', v')$ 异或和==0
4
5 struct Edge {
6     int to, nxt;
7     ll w;
8 };
9 const int N = int(1e5 + 10);
10 const int M = N << 1;
11
12 struct Grahp {
13     int head[N];
14     Edge eg[M];
15     int tot;
16
17     void init(int n) {
18         memset(head, -1, sizeof(int) * ++n);
19     }
20
21     inline void addEdge(int u, int v, ll w) {
22         eg[tot] = {v, head[u], w};
23         head[u] = tot++;
24     }
25 } gh;
26
27 bool vis[N];
28 // q队列, fa祖先, sz是子树大小, smx是子树最大
29 int q[N], fa[N], sz[N], smx[N];
30
31 int froot(int s) {
32     int l, r, mn = N, rt = 0;
33     q[l = r = 1] = s;
34     while (l <= r) {
35         int u = q[l++];
36         sz[u] = 1;
37         smx[u] = 0;
38         for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
39             int v = gh.eg[i].to;
40             if (v == fa[u] || vis[v]) continue;
41             fa[v] = u;
42             q[++r] = v;
43         }
44     }
45     // 反向遍历所有点算size
46     while (--l) {
47         int u = q[l];
48         int mx = max(smx[u], r - sz[u]);
49         if (mx < mn) mn = mx, rt = u;
50         if (l == 1) break; // 根节点没有fa
51         sz[fa[u]] += sz[u];
52         smx[fa[u]] = max(smx[fa[u]], sz[u]);
53     }
54     return rt;
55 }
56
57 // sons子树方向节点个数, val根到该节点异或和, gc边后继方向的节点个数
58 int sons[N], gc[M];
59 ll val[N];

```

```

60 ll ans = 0;
61 int n;
62
63 const int MOD = int(1e9 + 7);
64
65 ll nums[N];
66 int cnt[N];
67
68 void go(int s, int rt) {
69     fa[s] = rt;
70     val[s] = 0;
71     int l, r;
72     // 不计算s
73     q[l = r = 0] = s;
74     int m = 0;
75     while (l <= r) {
76         int u = q[l++];
77         nums[m++] = val[u];
78         for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
79             int v = gh.eg[i].to;
80             if (v == fa[u] || vis[v]) continue;
81             fa[v] = u;
82             q[++r] = v;
83             val[v] = val[u] ^ gh.eg[i].w;
84             // 这个点方向后面有多少点
85             sons[v] = gc[i];
86         }
87     }
88     sort(nums, nums + m);
89     m = unique(nums, nums + m) - nums;
90     mst(cnt, 0, m);
91     // 遍历分支
92     for (int j = gh.head[s]; ~j; j = gh.eg[j].nxt) {
93         // 分支的根
94         int du = gh.eg[j].to;
95         if (vis[du]) continue;
96         q[l = r = 1] = du;
97         while (l <= r) {
98             int u = q[l++];
99             int k = lower_bound(nums, nums + m, val[u]) - nums;
100             (ans += 1ll * sons[u] * cnt[k] % MOD) %= MOD;
101             if (val[u] == 0) {
102                 (ans += 1ll * sons[u] * (n - gc[j]) % MOD) %= MOD;
103             }
104             for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
105                 int v = gh.eg[i].to;
106                 if (v == fa[u] || vis[v]) continue;
107                 q[++r] = v;
108             }
109         }
110         // 增加这个方向的值
111         while (--l) {
112             int u = q[l];
113             int k = lower_bound(nums, nums + m, val[u]) - nums;
114             (cnt[k] += sons[u]) %= MOD;
115         }
116     }
117 }
118

```

```

119 void work(int u) {
120     // 换根
121     u = froot(u);
122     vis[u] = true;
123     go(u, 0);
124     for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
125         int v = gh.eg[i].to;
126         if (vis[v]) continue;
127         work(v);
128     }
129 }
130
131 // 预处理边后继节点个数
132 int pdfs(int u, int f) {
133     int fg_id = -1;
134     int s = 1;
135     for (int i = gh.head[u]; ~i; i = gh.eg[i].nxt) {
136         int v = gh.eg[i].to;
137         if (v == f) { // 记录父边ID
138             fg_id = i;
139             continue;
140         }
141         int c = pdfs(v, u);
142         gc[i] = c;
143         s += c;
144     }
145     // 存在父边
146     if (~fg_id) gc[fg_id] = n - s;
147     return s;
148 }
149
150 void solve() {
151     while (cin >> n) {
152         gh.init(n);
153         for (int i = 2; i <= n; i++) {
154             int u, v;
155             ll w;
156             u = i;
157             cin >> v >> w;
158             gh.addEdge(u, v, w);
159             gh.addEdge(v, u, w);
160         }
161         mst(vis, false, n + 1);
162         pdfs(1, 0);
163         ans = 0;
164         work(1);
165         cout << ans << endl;
166     }
167 }

```

6.5 DsuOnTree1

```

1  /*
2  DSU On Tree 树上启发式合并
3  进行轻重链剖分，每次先递归轻链，然后消除轻儿子影响，然后计算重儿子，并且保留重儿子结果
4  然后以常数级别复杂度将重儿子状态修改成当前节点状态!!! (<-----重点)
5  然后递归计算当前子树结果
6  复杂度O(nlogn)*O(计算/更新)

```



```

7
8 [CF741D]一棵有根树，边上有字母a~v，求每个子树中最长的边，满足这个边上的所有字母重排后可以构成回文。
9 很容易想到点分治，但是由于是有根树，所以点分治是做不了的。
10 先对没给点记录xn[x]表示x到根的路径的各个字母出现奇偶性，然后b[S]记录满足xn[x]=S的所有点x的最大深度。
11 类似点分治，一棵子树一棵子树地处理，每次先对子树内每个点查找之前子树中是否有能与它拼成回文串的点与它的最大深度，再更新b[]。
12 注意查找和更新不能同时进行，要整棵子树都查询完毕之后再进行更新操作。注意查找与更新当前子树的根。
13 我试图去写了一个一次进出完整查询和更新的代码，逻辑是先查询后进入最后更新，但没有合适的写法，难度太大
14 */
15
16 const int N = 500005;
17 const int M = N << 1;
18 struct Edge {
19     int to, next;
20 };
21
22 struct Graph {
23     int head[N];
24     Edge eg[M];
25     int tot;
26
27     void init(int n) {
28         tot = 0;
29         memset(head, -1, sizeof(int) * ++n);
30     }
31
32     inline void addEdge(int u, int v) {
33         eg[tot] = {v, head[u]};
34         head[u] = tot++;
35     }
36 } gh;
37
38 int tsz[N], son[N], cson;
39 int dep[N] = {0};
40
41 void pdfs(int u, int f) {
42     dep[u] = dep[f] + 1;
43     tsz[u] = 1;
44     son[u] = -1;
45     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
46         int v = gh.eg[i].to;
47         if (v == f) continue;
48         pdfs(v, u);
49         tsz[u] += tsz[v];
50         if (son[u] == -1 || tsz[v] > tsz[son[u]]) son[u] = v;
51     }
52 }
53
54 bool ans[N];
55 char s[N];
56 int p[N];
57
58 void calc(int u, int f, int d) {
59     p[dep[u]] ^= (1 << (s[u] - 'a'));
60     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
61         int v = gh.eg[i].to;
62         if (v == f || v == cson) continue;
63         calc(v, u, d);
64     }

```

```

65 }
66
67 void dfs(int u, int f, int d) {
68     // 遍历轻儿子, 结果删除
69     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
70         int v = gh.eg[i].to;
71         if (v == f || v == son[u]) continue;
72         dfs(v, u, 0);
73     }
74     if (~son[u]) { // 计算重儿子, 结果保留
75         dfs(son[u], u, 1);
76         cson = son[u];
77     }
78     calc(u, f, 1);
79     cson = -1;
80     for (int i = qry.head[u]; ~i; i = qry.eg[i].next) {
81         int h = qry.eg[i].to;
82         ans[i] = __builtin_popcount(p[h]) <= 1;
83     }
84     if (d == 0) { // 删除当前子树结果
85         calc(u, f, -1);
86     }
87 }
88
89 void solve() {
90     int n, m;
91     while (cin >> n >> m) {
92         gh.init(n);
93         qry.init(n);
94         for (int i = 2; i <= n; i++) {
95             int u;
96             cin >> u;
97             gh.addEdge(u, i);
98         }
99         s[0] = ' ';
100         cin >> (s + 1);
101         rep(i, 0, m) {
102             int v, h;
103             cin >> v >> h;
104             qry.addEdge(v, h);
105         }
106         pdfs(1, 0);
107         dfs(1, 0, 0);
108         rep(i, 0, m) {
109             cout << (ans[i] ? "Yes" : "No") << endl;
110         }
111     }
112 }
113
114 const int N = 500005;
115 const int M = N << 1;
116 struct Edge {
117     int to, next;
118 };
119
120 struct Gragh {
121     int head[N];
122     Edge eg[M];
123     int tot;

```

```

124
125 void init(int n) {
126     tot = 0;
127     memset(head, -1, sizeof(int) * ++n);
128 }
129
130 inline void addEdge(int u, int v) {
131     eg[tot] = {v, head[u]};
132     head[u] = tot++;
133 }
134 } gh, qry;
135
136 int tsz[N], son[N], dep[N] = {0}, fa[N], cson;
137 int xn[N];
138 int a[N];
139
140 void pdfs(int u, int f) {
141     fa[u] = f;
142     dep[u] = dep[f] + 1;
143     tsz[u] = 1;
144     son[u] = -1;
145
146     xn[u] = xn[f] ^ a[u];
147     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
148         int v = gh.eg[i].to;
149         if (v == f) continue;
150         pdfs(v, u);
151         tsz[u] += tsz[v];
152         if (son[u] == -1 || tsz[v] > tsz[son[u]]) son[u] = v;
153     }
154 }
155
156
157 int b[1 << 22];
158 int rst, ans[N], mx, root;
159 int num[N], tot = 0;
160
161 void check(int u) {
162     int bs = xn[u];
163     if (b[bs]) {
164         rst = max(rst, dep[u] + b[bs] - dep[root] * 2);
165     }
166     for (int i = 0; i < 22; i++) {
167         int bt = bs ^ (1 << i);
168         if (b[bt]) {
169             rst = max(rst, dep[u] + b[bt] - dep[root] * 2);
170         }
171     }
172     bs ^= xn[root];
173     if (bs == (bs & (-bs))) {
174         rst = max(rst, dep[u] - dep[root]);
175     }
176 }
177
178 void calc(int u) {
179     check(u);
180     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
181         int v = gh.eg[i].to;
182         if (v == fa[u]) continue;

```

```

183     calc(v);
184 }
185 }
186
187 void add(int u) {
188     if (b[xn[u]]) {
189         b[xn[u]] = max(b[xn[u]], dep[u]);
190     } else {
191         b[xn[u]] = dep[u];
192         num[tot++] = xn[u];
193     }
194     if (u == cson) return;
195     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
196         int v = gh.eg[i].to;
197         if (v == fa[u]) continue;
198         add(v);
199     }
200 }
201
202 void go(int u) {
203     rst = 0;
204     if (~son[u]) {
205         rst = 1;
206         root = son[u];
207         check(son[u]);
208         add(son[u]);
209     }
210     root = u;
211     check(u);
212     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
213         int v = gh.eg[i].to;
214         if (v == fa[u] || v == cson) continue;
215         calc(v);
216         add(v);
217     }
218 }
219
220 void del() {
221     for (int i = 0; i < tot; b[num[i++]] = 0);
222     tot = 0;
223 }
224
225 void dfs(int u, int d) {
226     // 遍历轻儿子, 结果删除
227     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
228         int v = gh.eg[i].to;
229         if (v == fa[u] || v == son[u]) continue;
230         dfs(v, 0);
231     }
232     if (~son[u]) { // 计算重儿子, 结果保留
233         dfs(son[u], 1);
234         cson = son[u];
235     }
236     go(u); // 计算当前
237     cson = -1;
238     ans[u] = rst;
239     if (d == 0) {
240         del();
241     }

```

```

242 }
243
244 void dfs2(int u) {
245     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
246         int v = gh.eg[i].to;
247         dfs2(v);
248         ans[u] = max(ans[u], ans[v]);
249     }
250 }
251
252 void input(int n) {
253     a[1] = 0;
254     for (int i = 2; i <= n; i++) {
255         int f;
256         char c;
257         cin >> f >> c;
258         gh.addEdge(f, i);
259         a[i] = 1 << (c - 'a');
260     }
261 }
262
263 void solve() {
264     int n;
265     while (cin >> n) {
266         gh.init(n);
267         input(n);
268         memset(b, 0, sizeof(b));
269         pdfs(1, 0);
270         dfs(1, 0);
271         dfs2(1);
272         for (int i = 1; i <= n; i++) {
273             printf("%d%c", ans[i], " \n"[i == n]);
274         }
275     }
276 }

```

6.6 DsuOnTree2

```

1  /*
2  [CF570D] 一棵树，询问某棵子树指定深度(对于树根的深度)的点能否构成回文。
3  用二进制记录每个深度的每个字母出现次数的奇偶性即可。
4  */
5
6  const int N = 500005;
7  const int M = N << 1;
8  struct Edge {
9      int to, next;
10 };
11
12 struct Graph {
13     int head[N];
14     Edge eg[M];
15     int tot;
16
17     void init(int n) {
18         tot = 0;
19         memset(head, -1, sizeof(int) * ++n);
20     }

```

```

21
22     inline void addEdge(int u, int v) {
23         eg[tot] = {v, head[u]};
24         head[u] = tot++;
25     }
26 } gh, qry;
27
28 int tsz[N], son[N], cson;
29 int dep[N] = {0};
30
31 void pdfs(int u, int f) {
32     dep[u] = dep[f] + 1;
33     tsz[u] = 1;
34     son[u] = -1;
35     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
36         int v = gh.eg[i].to;
37         if (v == f) continue;
38         pdfs(v, u);
39         tsz[u] += tsz[v];
40         if (son[u] == -1 || tsz[v] > tsz[son[u]]) son[u] = v;
41     }
42 }
43
44 bool ans[N];
45 char s[N];
46 int p[N];
47
48 void calc(int u, int f, int d) {
49     p[dep[u]] ^= (1 << (s[u] - 'a'));
50     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
51         int v = gh.eg[i].to;
52         if (v == f || v == cson) continue;
53         calc(v, u, d);
54     }
55 }
56
57 void dfs(int u, int f, int d) {
58     // 遍历轻儿子, 结果删除
59     for (int i = gh.head[u]; ~i; i = gh.eg[i].next) {
60         int v = gh.eg[i].to;
61         if (v == f || v == son[u]) continue;
62         dfs(v, u, 0);
63     }
64     if (~son[u]) { // 计算重儿子, 结果保留
65         dfs(son[u], u, 1);
66         cson = son[u];
67     }
68     calc(u, f, 1);
69     cson = -1;
70     for (int i = qry.head[u]; ~i; i = qry.eg[i].next) {
71         int h = qry.eg[i].to;
72         ans[i] = __builtin_popcount(p[h]) <= 1;
73     }
74     if (d == 0) { // 删除当前子树结果
75         calc(u, f, -1);
76     }
77 }
78
79 void solve() {

```

```
80     int n, m;
81     while (cin >> n >> m) {
82         gh.init(n);
83         qry.init(n);
84         for (int i = 2; i <= n; i++) {
85             int u;
86             cin >> u;
87             gh.addEdge(u, i);
88         }
89         s[0] = ' ';
90         cin >> (s + 1);
91         rep(i, 0, m) {
92             int v, h;
93             cin >> v >> h;
94             qry.addEdge(v, h);
95         }
96         pdfs(1, 0);
97         dfs(1, 0, 0);
98         rep(i, 0, m) {
99             cout << (ans[i] ? "Yes" : "No") << endl;
100         }
101     }
102 }
```

7 数论

7.1 线性基

```

1  #define rep(i, l, r) for(int i=(l);i<(r);++i)
2  #define per(i, l, r) for(int i=(r)-1;i>=(l);--i)
3  #define pw(x) (1ll << (x))
4  #define bt(x, i) ((x >> i) & 1)
5  const int LN = 61;
6  struct LB {
7      ll d[LN] = {0}, p[LN] = {0};
8      int g[LN] = {0};
9      int cnt = 0;
10
11      LB() = default;
12
13      ll &operator[](int pos) {
14          return d[pos];
15      }
16
17      const ll &operator[](int pos) const {
18          return d[pos];
19      }
20
21      void insert(ll val, int pos) {
22          per(i, 0, LN) {
23              if (val & pw(i)) {
24                  if (!d[i]) {
25                      d[i] = val;
26                      g[i] = pos;
27                      return;
28                  }
29                  // 贪心保留最右
30                  if (pos > g[i]) {
31                      swap(pos, g[i]);
32                      swap(val, d[i]);
33                  }
34                  val ^= d[i];
35              }
36          }
37      }
38
39      ll query_max(int l) {
40          ll ret = 0;
41          per(i, 0, LN) {
42              if (g[i] >= l)
43                  ret = max(ret, ret ^ d[i]);
44          }
45          return ret;
46      }
47
48      ll query_max() {
49          ll ret = 0;
50          per(i, 0, LN) {
51              ret = max(ret, ret ^ d[i]);
52          }
53          return ret;
54      }
55

```



```

56     ll query_min() {
57         rep(i, 0, LN) {
58             if (d[i]) return d[i];
59         }
60         return 0;
61     }
62
63     bool test(ll x) const {
64         per(i, 0, LN) {
65             if (bt(x, i)) {
66                 if (!d[i]) return false;
67                 x ^= d[i];
68             }
69         }
70         return true;
71     }
72
73     void rebuild() {
74         per(i, 0, LN) {
75             per(j, 0, i) {
76                 if (d[i] & (1LL << j)) d[i] ^= d[j];
77             }
78         }
79         rep(i, 0, LN) {
80             if (d[i]) p[cnt++] = d[i];
81         }
82     }
83
84     ll kth_query(ll k) {
85         int ret = 0;
86         if (k >= pw(cnt)) return -1;
87         per(i, 0, LN) {
88             if (bt(k, 1)) ret ^= p[i];
89         }
90         return ret;
91     }
92 };
93 // 求并集
94 LB operator+(const LB &n1, const LB &n2) {
95     LB ret = n1;
96     per(i, 0, LN)
97         if (n2.d[i])
98             ret.insert(n1.d[i], n1.g[i]);
99     return ret;
100 }
101 // 求交集
102 LB operator^(const LB &n1, const LB &n2) {
103     LB ans = {}, c = n2, d = n2;
104     rep(i, 0, LN) {
105         ll x = n1[i];
106         if (!x) continue;
107         int p = i;
108         ll T = 0;
109         per(j, 0, p + 1) {
110             if (bt(x, j)) {
111                 if (c[j]) {
112                     x ^= c[j];
113                     T ^= d[j];
114                 } else {

```

```

115         p = j;
116         break;
117     }
118 }
119 }
120 if (!x) {
121     ans[i] = T;
122 } else {
123     c[p] = x;
124     d[p] = T;
125 }
126 }
127 return ans;
128 }

```

7.2 FWT

```

1 void FWT(int p[], int n) { // 如果要取模运算记得-x+MOD,*inv
2     for (int i = 1; i < n; i <= 1) {
3         for (int j = 0; j < n; j += (i << 1)) {
4             for (int k = 0; k < i; k++) {
5                 // or{
6                 p[i + j + k] += p[j + k];
7                 // and
8                 p[j + k] += p[i + j + k];
9                 // xor
10                tie(p[j + k], p[i + j + k]) = make_pair(p[j + k] + p[i + j + k], p[j +
11                k] - p[i + j + k]);
12            }
13        }
14    }
15
16 void IFWT(int p[], int n) { // 如果要取模运算记得-x+MOD,*inv
17     for (int i = 1; i < n; i <= 1) {
18         for (int j = 0; j < n; j += (i << 1)) {
19             for (int k = 0; k < i; k++) {
20                 // or
21                 p[i + j + k] -= p[j + k];
22                 // and
23                 p[j + k] -= p[i + j + k];
24                 // xor
25                tie(p[j + k], p[i + j + k]) = make_pair(p[j + k] + p[i + j + k], p[j +
26                k] - p[i + j + k]);
27                p[j + k] = p[j + k] / 2, p[i + j + k] = p[i + j + k] / 2;
28            }
29        }
30    }

```

7.3 FFT

```

1 inline int lowbit(int x) { return x & -x; }
2
3 int calc(int n) {
4     int k = 0;
5     while ((1 << k) < n) k++;

```

```

6     return k;
7 }
8
9 // FFT
10 const double pi = acos(-1.0);
11
12 const int N = (1 << 20);
13 using Complex = complex<double>;
14
15 void change(Complex p[], int n) {
16     int k = calc(n);
17     n = 1 << k;
18     vector<int> r(n, 0);
19     for (int i = 0; i < n; i++) r[i] = (r[i >> 1] >> 1) | ((i & 1) << (k - 1));
20     for (int i = 0; i < n; i++) if (i < r[i]) swap(p[i], p[r[i]]);
21 }
22
23 void FFT(Complex p[], int n, int type) {
24     change(p, n);
25     for (int mid = 1; mid < n; mid <= 1) { //待合并区间的长度的一半
26         Complex wn(cos(pi / mid), type * sin(pi / mid)); //单位根
27         for (int R = mid << 1, j = 0; j < n; j += R) { //R是区间的长度, j表示前已经到哪个位置
28             Complex w(1, 0); //幂
29             for (int k = 0; k < mid; k++, w = w * wn) { //枚举左半部分
30                 Complex x = p[j + k], y = w * p[j + mid + k]; //蝴蝶效应
31                 p[j + k] = x + y;
32                 p[j + mid + k] = x - y;
33             }
34         }
35     }
36 }

```

7.4 圆上整点

```

1 //  $x^2+y^2=r^2 \rightarrow y^2=(r-x)*(r+x)$ 
2 //  $d = \gcd(r-x, r+x)$ ,  $n=(r-x)/d$ ,  $m=(r+x)/d$ ,  $y^2=d^2*m*n$ 
3 // 因为 $y^2$ 和 $d^2$ 为完全平方数, 所以  $n*m$  为完全平方数
4 // 又因为 $n, m$ 互质, 所以  $n=u^2$ ,  $m=v^2$ 
5 // 所以  $r-y=d*u^2$ ,  $r+y=d*v^2$ 
6 // 可得  $x=d*(v^2-u^2)$ ,  $y=d*u*v$ 
7
8 ll gcd(ll a, ll b) { return !b ? a : gcd(b, a % b); }
9
10 inline int work(vector<pll> &p, ll d, ll t) { //  $d * t == 2 * r$ 
11     int sum = 0;
12     for (ll u = 1; 2 * u * u < t; u++) {
13         ll v = ll(sqrt(t - u * u));
14         if (v == u || v * v + u * u != t || gcd(u, v) != 1) continue;
15         ll x = d * (v * v - u * u) / 2;
16         ll y = d * u * v;
17         p.push_back({x, y});
18         sum++;
19     }
20     return sum;
21 }
22
23 int calc(vector<pll> &p, ll r) {

```

```

24     int sum = 0;
25     r <= 1;
26     for (ll i = 1; i * i <= r; i++) { // sqrt 枚举因子
27         if (r % i) continue;
28         sum += work(p, i, r / i);
29         if (i * i < r) sum += work(p, r / i, i);
30     }
31     for (int i = 0, cnt = p.size(); i < cnt; i++) {
32         int x = p[i].fi, y = p[i].se;
33         p.push_back({x, -y}), p.push_back({-x, y}), p.push_back({-x, -y});
34     }
35     sum <= 2;
36     r >= 1;
37     sum += 4;
38     p.push_back({r, 0}), p.push_back({-r, 0}), p.push_back({0, r}), p.push_back({0, -r});
39     sort(p.begin(), p.end());
40     return sum;
41 }

```

7.5 线性逆元

```

1 // 逆元, 阶乘, 阶乘逆元
2 ll inv[N] = {1, 1}, fac[N] = {1, 1}, ifac[N] = {1, 1};
3 // 线性求逆元
4 void init() {
5     for (int i = 2; i < N; i++) {
6         inv[i] = (MOD - (MOD / i)) * inv[MOD % i] % MOD;
7         fac[i] = fac[i - 1] * i % MOD;
8         ifac[i] = ifac[i - 1] * inv[i] % MOD;
9     }
10 }

```

8 其他

8.1 BigInteger

```

1 // base and base_digits must be consistent
2 constexpr int base = 1000000000;
3 constexpr int base_digits = 9;
4
5 struct bigint {
6     // value == 0 is represented by empty z
7     vector<int> z; // digits
8
9     // sign == 1 <==> value >= 0
10    // sign == -1 <==> value < 0
11    int sign;
12
13    bigint() : sign(1) {}
14
15    bigint(ll v) { *this = v; }
16
17    bigint &operator=(ll v) {
18        sign = v < 0 ? -1 : 1;
19        v *= sign;
20        z.clear();
21        for (; v > 0; v = v / base) z.push_back((int) (v % base));
22        return *this;
23    }
24
25    bigint(const string &s) { read(s); }
26
27    bigint &operator+=(const bigint &other) {
28        if (sign == other.sign) {
29            for (int i = 0, carry = 0; i < other.z.size() || carry; ++i) {
30                if (i == z.size())
31                    z.push_back(0);
32                z[i] += carry + (i < other.z.size() ? other.z[i] : 0);
33                carry = z[i] >= base;
34                if (carry)
35                    z[i] -= base;
36            }
37        } else if (other != 0 /* prevent infinite loop */) {
38            *this -= -other;
39        }
40        return *this;
41    }
42
43    friend bigint operator+(bigint a, const bigint &b) { return a += b; }
44
45    bigint &operator-=(const bigint &other) {
46        if (sign == other.sign) {
47            if (sign == 1 && *this >= other || sign == -1 && *this <= other) {
48                for (int i = 0, carry = 0; i < other.z.size() || carry; ++i) {
49                    z[i] -= carry + (i < other.z.size() ? other.z[i] : 0);
50                    carry = z[i] < 0;
51                    if (carry)
52                        z[i] += base;
53                }
54                trim();
55            } else {

```

```

56         *this = other - *this;
57         this->sign = -this->sign;
58     }
59     } else {
60         *this += -other;
61     }
62     return *this;
63 }
64
65 friend bigint operator-(bigint a, const bigint &b) {
66     return a -= b;
67 }
68
69 bigint &operator*=(int v) {
70     if (v < 0) sign = -sign, v = -v;
71     for (int i = 0, carry = 0; i < z.size() || carry; ++i) {
72         if (i == z.size()) z.push_back(0);
73         ll cur = (ll) z[i] * v + carry;
74         carry = (int) (cur / base);
75         z[i] = (int) (cur % base);
76     }
77     trim();
78     return *this;
79 }
80
81 bigint operator*(int v) const { return bigint(*this) *= v; }
82
83 friend pair<bigint, bigint> divmod(const bigint &a1, const bigint &b1) {
84     int norm = base / (b1.z.back() + 1);
85     bigint a = a1.abs() * norm;
86     bigint b = b1.abs() * norm;
87     bigint q, r;
88     q.z.resize(a.z.size());
89
90     for (int i = (int) a.z.size() - 1; i >= 0; i--) {
91         r *= base;
92         r += a.z[i];
93         int s1 = b.z.size() < r.z.size() ? r.z[b.z.size()] : 0;
94         int s2 = b.z.size() - 1 < r.z.size() ? r.z[b.z.size() - 1] : 0;
95         int d = (int) (((ll) s1 * base + s2) / b.z.back());
96         r -= b * d;
97         while (r < 0) r += b, --d;
98         q.z[i] = d;
99     }
100
101     q.sign = a1.sign * b1.sign;
102     r.sign = a1.sign;
103     q.trim();
104     r.trim();
105     return {q, r / norm};
106 }
107
108 friend bigint sqrt(const bigint &a1) {
109     bigint a = a1;
110     while (a.z.empty() || a.z.size() % 2 == 1) a.z.push_back(0);
111
112     int n = a.z.size();
113
114     int firstDigit = (int) ::sqrt((double) a.z[n - 1] * base + a.z[n - 2]);

```

```

115     int norm = base / (firstDigit + 1);
116     a *= norm;
117     a *= norm;
118     while (a.z.empty() || a.z.size() % 2 == 1) a.z.push_back(0);
119
120     bigint r = (ll) a.z[n - 1] * base + a.z[n - 2];
121     firstDigit = (int) ::sqrt((double) a.z[n - 1] * base + a.z[n - 2]);
122     int q = firstDigit;
123     bigint res;
124
125     for (int j = n / 2 - 1; j >= 0; j--) {
126         for (; --q) {
127             bigint r1 = (r - (res * 2 * base + q) * q) * base * base +
128                 (j > 0 ? (ll) a.z[2 * j - 1] * base + a.z[2 * j - 2] : 0);
129             if (r1 >= 0) {
130                 r = r1;
131                 break;
132             }
133         }
134         (res *= base) += q;
135
136         if (j > 0) {
137             int d1 = res.z.size() + 2 < r.z.size() ? r.z[res.z.size() + 2] : 0;
138             int d2 = res.z.size() + 1 < r.z.size() ? r.z[res.z.size() + 1] : 0;
139             int d3 = res.z.size() < r.z.size() ? r.z[res.z.size()] : 0;
140             q = (int) (((ll) d1 * base * base + (ll) d2 * base + d3) / (firstDigit
141 * 2));
142         }
143     }
144     res.trim();
145     return res / norm;
146 }
147
148 bigint operator/(const bigint &v) const {
149     return divmod(*this, v).first;
150 }
151
152 bigint operator%(const bigint &v) const {
153     return divmod(*this, v).second;
154 }
155
156 bigint &operator/=(int v) {
157     if (v < 0) sign = -sign, v = -v;
158     for (int i = (int) z.size() - 1, rem = 0; i >= 0; --i) {
159         ll cur = z[i] + rem * (ll) base;
160         z[i] = (int) (cur / v);
161         rem = (int) (cur % v);
162     }
163     trim();
164     return *this;
165 }
166
167 bigint operator/(int v) const {
168     return bigint(*this) /= v;
169 }
170
171 int operator%(int v) const {
172     if (v < 0) v = -v;

```

```

173     int m = 0;
174     for (int i = (int) z.size() - 1; i >= 0; --i)
175         m = (int) ((z[i] + m * (ll) base) % v);
176     return m * sign;
177 }
178
179 bigint &operator*=(const bigint &v) {
180     return *this = *this * v;;
181 }
182
183 bigint &operator/=(const bigint &v) {
184     return *this = *this / v;
185 }
186
187 bool operator<(const bigint &v) const {
188     if (sign != v.sign)
189         return sign < v.sign;
190     if (z.size() != v.z.size())
191         return z.size() * sign < v.z.size() * v.sign;
192     for (int i = (int) z.size() - 1; i >= 0; i--)
193         if (z[i] != v.z[i])
194             return z[i] * sign < v.z[i] * sign;
195     return false;
196 }
197
198 bool operator>(const bigint &v) const { return v < *this; }
199
200 bool operator<=(const bigint &v) const { return !(v < *this); }
201
202 bool operator>=(const bigint &v) const { return !(*this < v); }
203
204 bool operator==(const bigint &v) const { return !(*this < v) && !(v < *this); }
205
206 bool operator!=(const bigint &v) const { return *this < v || v < *this; }
207
208 void trim() {
209     while (!z.empty() && z.back() == 0) z.pop_back();
210     if (z.empty()) sign = 1;
211 }
212
213 bool isZero() const {
214     return z.empty();
215 }
216
217 friend bigint operator-(bigint v) {
218     if (!v.z.empty()) v.sign = -v.sign;
219     return v;
220 }
221
222 bigint abs() const {
223     return sign == 1 ? *this : -*this;
224 }
225
226 ll longValue() const {
227     ll res = 0;
228     for (int i = (int) z.size() - 1; i >= 0; i--)
229         res = res * base + z[i];
230     return res * sign;
231 }

```



```

232
233     friend bigint gcd(const bigint &a, const bigint &b) {
234         return b.isZero() ? a : gcd(b, a % b);
235     }
236
237     friend bigint lcm(const bigint &a, const bigint &b) {
238         return a / gcd(a, b) * b;
239     }
240
241     void read(const string &s) {
242         sign = 1;
243         z.clear();
244         int pos = 0;
245         while (pos < s.size() && (s[pos] == '-' || s[pos] == '+')) {
246             if (s[pos] == '-') sign = -sign;
247             ++pos;
248         }
249         for (int i = (int) s.size() - 1; i >= pos; i -= base_digits) {
250             int x = 0;
251             for (int j = max(pos, i - base_digits + 1); j <= i; j++)
252                 x = x * 10 + s[j] - '0';
253             z.push_back(x);
254         }
255         trim();
256     }
257
258     friend istream &operator>>(istream &stream, bigint &v) {
259         string s;
260         stream >> s;
261         v.read(s);
262         return stream;
263     }
264
265     friend ostream &operator<<(ostream &stream, const bigint &v) {
266         if (v.sign == -1)
267             stream << '-';
268         stream << (v.z.empty() ? 0 : v.z.back());
269         for (int i = (int) v.z.size() - 2; i >= 0; --i)
270             stream << setw(base_digits) << setfill('0') << v.z[i];
271         return stream;
272     }
273
274     static vector<int> convert_base(const vector<int> &a, int old_digits, int
new_digits) {
275         vector<ll> p(max(old_digits, new_digits) + 1);
276         p[0] = 1;
277         for (int i = 1; i < p.size(); i++)
278             p[i] = p[i - 1] * 10;
279         vector<int> res;
280         ll cur = 0;
281         int cur_digits = 0;
282         for (int v : a) {
283             cur += v * p[cur_digits];
284             cur_digits += old_digits;
285             while (cur_digits >= new_digits) {
286                 res.push_back(int(cur % p[new_digits]));
287                 cur /= p[new_digits];
288                 cur_digits -= new_digits;
289             }

```

```

290     }
291     res.push_back((int) cur);
292     while (!res.empty() && res.back() == 0) res.pop_back();
293     return res;
294 }
295
296 typedef vector<ll> vll;
297
298 static vll karatsubaMultiply(const vll &a, const vll &b) {
299     int n = a.size();
300     vll res(n + n);
301     if (n <= 32) {
302         for (int i = 0; i < n; i++)
303             for (int j = 0; j < n; j++)
304                 res[i + j] += a[i] * b[j];
305         return res;
306     }
307
308     int k = n >> 1;
309     vll a1(a.begin(), a.begin() + k);
310     vll a2(a.begin() + k, a.end());
311     vll b1(b.begin(), b.begin() + k);
312     vll b2(b.begin() + k, b.end());
313
314     vll a1b1 = karatsubaMultiply(a1, b1);
315     vll a2b2 = karatsubaMultiply(a2, b2);
316
317     for (int i = 0; i < k; i++) a2[i] += a1[i];
318     for (int i = 0; i < k; i++) b2[i] += b1[i];
319
320     vll r = karatsubaMultiply(a2, b2);
321     for (int i = 0; i < a1b1.size(); i++) r[i] -= a1b1[i];
322     for (int i = 0; i < a2b2.size(); i++) r[i] -= a2b2[i];
323
324     for (int i = 0; i < r.size(); i++) res[i + k] += r[i];
325     for (int i = 0; i < a1b1.size(); i++) res[i] += a1b1[i];
326     for (int i = 0; i < a2b2.size(); i++) res[i + n] += a2b2[i];
327     return res;
328 }
329
330 bigint operator*(const bigint &v) const {
331     vector<int> a6 = convert_base(this->z, base_digits, 6);
332     vector<int> b6 = convert_base(v.z, base_digits, 6);
333     vll a(a6.begin(), a6.end());
334     vll b(b6.begin(), b6.end());
335     while (a.size() < b.size()) a.push_back(0);
336     while (b.size() < a.size()) b.push_back(0);
337     while (a.size() & (a.size() - 1)) a.push_back(0), b.push_back(0);
338     vll c = karatsubaMultiply(a, b);
339     bigint res;
340     res.sign = sign * v.sign;
341     for (int i = 0, carry = 0; i < c.size(); i++) {
342         ll cur = c[i] + carry;
343         res.z.push_back((int) (cur % 1000000));
344         carry = (int) (cur / 1000000);
345     }
346     res.z = convert_base(res.z, 6, base_digits);
347     res.trim();
348     return res;

```

```

349     }
350 };

```

8.2 FastIO

```

1  /*
2  * FastIO
3  * 代码模板 !
4  * 如有雷同 !
5  * 纯属巧合 !
6  */
7  namespace FastIO {
8  #define BUF_SIZE 10000000
9  #define OUT_SIZE 10000000
10 #define ll long long
11     //fread->read
12     bool IOerror = 0;
13
14     inline char nc() {
15         static char buf[BUF_SIZE], *p1 = buf + BUF_SIZE, *pend = buf + BUF_SIZE;
16         if (p1 == pend) {
17             p1 = buf;
18             pend = buf + fread(buf, 1, BUF_SIZE, stdin);
19             if (pend == p1) {
20                 IOerror = 1;
21                 return -1;
22             }
23             // {printf("IO error!\n");system("pause");for (;;);exit(0);}
24         }
25         return *p1++;
26     }
27
28     inline bool blank(char ch) { return ch == ' ' || ch == '\n' || ch == '\r' || ch ==
29 '\t'; }
30
31     inline void read(int &x) {
32         bool sign = 0;
33         char ch = nc();
34         x = 0;
35         for (; blank(ch); ch = nc());
36         if (IOerror) return;
37         if (ch == '-') sign = 1, ch = nc();
38         for (; ch >= '0' && ch <= '9'; ch = nc()) x = x * 10 + ch - '0';
39         if (sign) x = -x;
40     }
41
42     inline void read(ll &x) {
43         bool sign = 0;
44         char ch = nc();
45         x = 0;
46         for (; blank(ch); ch = nc());
47         if (IOerror) return;
48         if (ch == '-') sign = 1, ch = nc();
49         for (; ch >= '0' && ch <= '9'; ch = nc()) x = x * 10 + ch - '0';
50         if (sign) x = -x;
51     }
52
53     inline void read(double &x) {

```

```

53     bool sign = 0;
54     char ch = nc();
55     x = 0;
56     for (; blank(ch); ch = nc());
57     if (I0error) return;
58     if (ch == '-') sign = 1, ch = nc();
59     for (; ch >= '0' && ch <= '9'; ch = nc()) x = x * 10 + ch - '0';
60     if (ch == '.') {
61         double tmp = 1;
62         ch = nc();
63         for (; ch >= '0' && ch <= '9'; ch = nc()) tmp /= 10.0, x += tmp * (ch - '0')
;
64     }
65     if (sign) x = -x;
66 }
67
68 inline void read(char *s) {
69     char ch = nc();
70     for (; blank(ch); ch = nc());
71     if (I0error) return;
72     for (; !blank(ch) && !I0error; ch = nc()) *s++ = ch;
73     *s = 0;
74 }
75
76 inline void read(char &c) {
77     for (c = nc(); blank(c); c = nc());
78     if (I0error) {
79         c = -1;
80         return;
81     }
82 }
83
84 //fwrite->write
85 struct Ostream_fwrite {
86     char *buf, *p1, *pend;
87     Ostream_fwrite() {
88         buf = new char[OUT_SIZE];
89         p1 = buf;
90         pend = buf + OUT_SIZE;
91     }
92     void out(char ch) {
93         if (p1 == pend) {
94             fwrite(buf, 1, OUT_SIZE, stdout);
95             p1 = buf;
96         }
97         *p1++ = ch;
98     }
99     void print(int x) {
100         static char s[15], *s1;
101         s1 = s;
102         if (!x) *s1++ = '0';
103         if (x < 0) out('-'), x = -x;
104         while (x) *s1++ = x % 10 + '0', x /= 10;
105         while (s1-- != s) out(*s1);
106     }
107     void println(int x) {
108         static char s[15], *s1;
109         s1 = s;
110         if (!x) *s1++ = '0';

```

```

111         if (x < 0)out('-'), x = -x;
112         while (x)*s1++ = x % 10 + '0', x /= 10;
113         while (s1-- != s)out(*s1);
114         out('\n');
115     }
116     void print(ll x) {
117         static char s[25], *s1;
118         s1 = s;
119         if (!x)*s1++ = '0';
120         if (x < 0)out('-'), x = -x;
121         while (x)*s1++ = x % 10 + '0', x /= 10;
122         while (s1-- != s)out(*s1);
123     }
124     void println(ll x) {
125         static char s[25], *s1;
126         s1 = s;
127         if (!x)*s1++ = '0';
128         if (x < 0)out('-'), x = -x;
129         while (x)*s1++ = x % 10 + '0', x /= 10;
130         while (s1-- != s)out(*s1);
131         out('\n');
132     }
133     void print(double x, int y) {
134         static ll mul[] = {1, 10, 100, 1000, 10000, 100000, 1000000, 10000000,
100000000,
135                                1000000000, 10000000000LL, 100000000000LL, 1000000000000LL,
136                                10000000000000LL, 100000000000000LL, 1000000000000000LL, 10000000000000000LL};
137         if (x < -1e-12)out('-'), x = -x;
138         x *= mul[y];
139         ll x1 = (ll) floor(x);
140         if (x - floor(x) >= 0.5)++x1;
141         ll x2 = x1 / mul[y], x3 = x1 - x2 * mul[y];
142         print(x2);
143         if (y > 0) {
144             out('.');
145             for (size_t i = 1; i < y && x3 * mul[i] < mul[y]; out('0'), ++i);
146             print(x3);
147         }
148     }
149     void println(double x, int y) {
150         print(x, y);
151         out('\n');
152     }
153     void print(char *s) { while (*s)out(*s++); }
154     void println(char *s) {
155         while (*s)out(*s++);
156         out('\n');
157     }
158     void flush() {
159         if (p1 != buf) {
160             fwrite(buf, 1, p1 - buf, stdout);
161             p1 = buf;
162         }
163     }
164     ~Ostream_fwrite() { flush(); }
165 } Ostream;
166 inline void print(int x) { Ostream.print(x); }

```

```

167     inline void println(int x) { Ostream.println(x); }
168     inline void print(char x) { Ostream.out(x); }
169     inline void println(char x) {
170         Ostream.out(x);
171         Ostream.out('\n');
172     }
173     inline void print(ll x) { Ostream.print(x); }
174     inline void println(ll x) { Ostream.println(x); }
175     inline void print(double x, int y) { Ostream.print(x, y); }
176     inline void println(double x, int y) { Ostream.println(x, y); }
177     inline void print(char *s) { Ostream.print(s); }
178     inline void println(char *s) { Ostream.println(s); }
179     inline void println() { Ostream.out('\n'); }
180     inline void flush() { Ostream.flush(); }
181 };
182 using namespace FastIO;

```

8.3 InputOutputSpeedUp

```

1
2
3 template <class T>
4 inline bool read(T &x) {
5     x = 0;
6     char c = getchar();
7     if(c == EOF) return false;
8     bool f = false;
9     for (; !isdigit(c); c = getchar()) f ^= (c == '-');
10    for (; isdigit(c); c = getchar()) x = x * 10 + (c - '0');
11    x = f ? -x : x;
12    return true;
13 }
14
15 template <class T>
16 inline void write(T x) {
17     if (x < 0) {
18         putchar('-');
19         x = -x;
20     }
21     T y = 1;
22     int len = 1;
23     for (; y <= x / 10; y *= 10) ++len;
24     for (; len; --len, x %= y, y /= 10) putchar(x / y + '0');
25 }

```

8.4 gcd

```

1 ll gcd(ll x, ll y) { // 循环版
2     ll t;
3     while (y){
4         t = x % y;
5         x = y;
6         y = t;
7     }
8     return x;
9 }
10

```

```

11 ll gcd(ll a, ll b) { // 递归版
12     return b == 0 ? a : gcd(b, a % b);
13 }
14
15 // 扩展欧几里得
16 ll exgcd(ll a, ll b, ll &x, ll &y) {
17     if (b == 0) {
18         x = 1, y = 0;
19         return a;
20     }
21     ll q = exgcd(b, a % b, y, x);
22     y -= a / b * x;
23     return q;
24 }

```

8.5 myItoa

```

1 char * myItoa(int value, char* result, int base = 10);
2
3 char * myItoa(int value, char* result, int base) {
4     // check that the base is valid
5
6     if (base < 2 || base > 16) { *result = 0; return result; }
7     char* out = result;
8     int quotient = abs(value);
9     do {
10         const int tmp = quotient / base;
11         *out = "0123456789abcdef"[quotient - (tmp*base)];
12         ++out;
13         quotient = tmp;
14     } while (quotient);
15     // Apply negative sign
16     if (value < 0) *out++ = '-';
17     std::reverse(result, out);
18     *out = 0;
19     return result;
20 }

```

8.6 Permutation

```

1 // 错排问题
2 //  $D(n) = n! [(-1)^2/2! + \dots + (-1)^{(n-1)}/(n-1)! + (-1)^n/n!]$ .
3 long long table[1000] = {0, 0, 1};
4 void init() {
5     for (int i = 3; i <= 20; i++) {
6         table[i] = (i - 1) * (table[i - 1] + table[i - 2]);
7     }
8 }

```

8.7 prime

```

1 // 普通素数筛
2 const int PMAX = 1000000;
3
4 int prime_count = 0;
5 bool prime_list[PMAX] = { false }; // 元素值为0代表是素数

```

```

6  int prime_table[PMAX] = { 0 };
7
8  void initPrime() {
9      for (int i = 2; i < PMAX; i++) {
10         if (!prime_list[i])
11             prime_table[prime_count++] = i;
12         for (int j = 0, e = (PMAX - 1) / i;
13             j < prime_count && prime_table[j] <= e; j++) {
14             prime_list[i * prime_table[j]] = true;
15             if (i % prime_table[j] == 0) break;
16         }
17     }
18 }
19
20
21 // 可以得到其中一个质因子的素数筛
22 const int PMAX = 1000005;
23
24 int prime_count = 0;
25 int prime_list[PMAX] = {0}; //元素值为0代表是素数
26 int prime_table[PMAX] = {0};
27
28 void initPrime() {
29     for (int i = 2; i < PMAX; i++) {
30         if (!prime_list[i])
31             prime_list[i] = prime_table[prime_count++] = i;
32         for (int j = 0, e = (PMAX - 1) / i, now;
33             j < prime_count && prime_table[j] <= e; j++) {
34             prime_list[i * now] = now;
35             if (i % now == 0) break;
36         }
37     }
38 }

```

8.8 Hash

```

1  struct Hash {
2      int num[N];
3      int tot;
4
5      void init() { tot = 0; }
6
7      void insert(int x) { num[tot++] = x; }
8
9      void build() {
10         sort(num, num + tot);
11         tot = unique(num, num + tot) - num;
12     }
13
14     inline int operator[](int x) { return lower_bound(num, num + tot, x) - num; }
15 } hs;

```