

ACM/ICPC Template Manaual

ZheJiang GongShang University

Happy Otaku

April 26, 2019

ACM/ICPC Template Manaual, Happy Otaku

Contents

0	头文件 0.1 stdc++	. 1 . 1
1	字串符 1.1 KMP	3
2	动态规划 2.1 01Bag	5 . 5
	2.2 BagProblem	
	2.3 FullBag	
	2.4 MultiBag	
3	数据结构	8
	3.1 BTree	
	3.2 pbds-bbtree	
	3.3 树状数组	
	3.4 二维树状数组	
	3.5 线段树	
	3.6 二维线段树	
	3.7 树状数组求逆序对	. 15
4	图论	16
	4.1 Dijkstra	
	4.2 spfa	
	4.3 Dinic	
	4.4 hungry	
	4.5 MinSpanTree	. 20
5	博弈	22
	5.1 GameProblem	. 22
6	分治	23
	6.1 IntegerFastPower	
	6.2 MatrixFastPower	. 23
7	其他	2 5
	7.1 BigInteger	
	7.2 FastIO	
	7.3 InputOutputSpeedUp	
	7.4 gcd	
	7.5 myItoa	
	7.6 Permutation	
	7.7 prime	. 35

0 头文件

```
// 巨菜的ACMer-Happy233
 3
   #include <bits/stdc++.h>
 4
   using namespace std;
 5
 6
7
   //----
 8 typedef long long ll;
9 typedef vector<int> vi;
10 typedef pair<int, int> pii;
11 #define pw(x) (111 << (x))
12 #define sz(x) ((int)(x).size())
13 #define all(x) (x).begin(),(x).end()
14 #define rep(i, l, r) for(int i=(l);i<(r);++i)</pre>
   #define per(i, l, r) for(int i=(r)-1; i>=(l); --i)
   #define sf(x) scanf("%d", &(x))
16
17
18 using namespace std;
19
20 const double pi = acos(-1);
   0.1 \text{ stdc}++
1 // C
 2 #ifndef _GLIBCXX_NO_ASSERT
3 #include <cassert>
 4 #endif
5 #include <cctype>
6 #include <cerrno>
 7 #include <cfloat>
 8 #include <ciso646>
9 #include <climits>
10 #include <clocale>
11 #include <cmath>
12 #include <csetjmp>
13 #include <csiqnal>
14 #include <cstdara>
15 #include <cstddef>
16 #include <cstdio>
17 #include <cstdlib>
18 #include <cstring>
19 #include <ctime>
20
21 #if __cplusplus >= 201103L
22 #include <ccomplex>
23 #include <cfenv>
24 #include <cinttypes>
25 #include <cstdalign>
26 #include <cstdbool>
27 #include <cstdint>
28 #include <ctamath>
29 #include <cuchar>
30 #include <cwchar>
31 #include <cwctype>
32 #endif
33
```

```
34 // C++
35 #include <algorithm>
36 #include <bitset>
37 #include <complex>
38 #include <deque>
39 #include <exception>
40 #include <fstream>
41 #include <functional>
42 #include <iomanip>
43 #include <ios>
44 #include <iosfwd>
45 #include <iostream>
46 #include <istream>
47 #include <iterator>
48 #include <limits>
49 #include <list>
50 #include <locale>
51 #include <map>
52 #include <memory>
53 #include <new>
54 #include <numeric>
55 #include <ostream>
56 #include <queue>
57 #include <set>
58 #include <sstream>
59 #include <stack>
60 #include <stdexcept>
61 #include <streambuf>
62 #include <string>
63 #include <typeinfo>
64 #include <utility>
65 #include <valarray>
66 #include <vector>
67
68 #if __cplusplus >= 201103L
69 #include <array>
70 #include <atomic>
71 #include <chrono>
72 #include <codecvt>
73 #include <condition_variable>
74 #include <forward_list>
75 #include <future>
76 #include <initializer_list>
77 #include <mutex>
78 #include <random>
79 #include <ratio>
80 #include <regex>
81 #include <scoped_allocator>
82 #include <system_error>
83 #include <thread>
84 #include <tuple>
85 #include <typeindex>
86 #include <type_traits>
87 #include <unordered_map>
88 #include <unordered_set>
89 #endif
90 #if __cplusplus >= 201402L
91 #include <shared_mutex>
92 #endif
```

1 字串符

1.1 KMP

```
template<class elemType>
   inline void kmp_nxt(elemType &T, vector<int> &nxt) {
3
        nxt[0] = -1;
        for (int i = 1; i < T.size(); i++) {</pre>
4
            int j = nxt[i - 1];
5
            while (j \ge 0 \& T[i - 1] != T[j]) j = nxt[j];
6
            if (j \ge 0 \&\& T[i - 1] == T[j]) nxt[i] = j + 1;
7
8
            else nxt[i] = 0;
9
        }
10
   }
11
   template<class elemType>
12
   inline int kmp_count(elemType &S, elemType &T) {
        vector<int> nxt(T.size());
14
        kmp_nxt(T, nxt);
15
        int index, count = 0;
16
        for (index = 0; index < S.size(); ++index) {</pre>
17
            int pos = 0;
18
            int iter = index;
19
            while (pos < T.size() && iter < S.size()) {</pre>
20
                if (S[iter] == T[pos]) {
21
22
                     ++iter;
23
                     ++pos;
24
                } else {
25
                     if (pos == 0) ++iter;
26
                     else pos = nxt[pos - 1] + 1;
                }
27
28
29
            if (pos == T.size() && (iter - index) == T.size()) ++count;
30
31
        return count;
32
   }
33
   template<class elemType>
   inline void kmp_next(elemType T[], int count, vector<int> &nxt) {
36
        nxt[0] = -1;
37
        for (int i = 1; i < count; i++) {</pre>
            int j = nxt[i - 1];
38
            while (j \ge 0 \&\& T[i - 1] != T[j]) j = nxt[j];
39
            if (j \ge 0 \& T[i - 1] == T[j]) nxt[i] = j + 1;
40
            else nxt[i] = 0;
41
42
        }
   }
43
44
   template<class elemType>
45
   inline int kmp_count(elemType S[], int c1, elemType T[], int c2) {
        vector<int> nxt(c2);
47
48
        kmp_nxt(T, c2, nxt);
        int index, count = 0;
49
        for (index = 0; index < c1; ++index) {
50
            int pos = 0;
51
            int iter = index;
52
            while (pos < c2 && iter < c1) {</pre>
53
                if (S[iter] == T[pos]) {
54
                     ++iter;
55
```

```
56
                         ++pos;
                   }
else {
   if (pos == 0) ++iter;
   else pos = nxt[pos - 1] + 1;
57
58
59
60
61
               }
if (pos == c2 && (iter - index) == c2) ++count;
62
63
64
          }
65
          return count;
66 }
```

2 动态规划

2.1 01Bag

```
void dp(int n, int m) {
1
2
       // n=物品个数
       for (int i = 0; i < n; i++) {
3
           // m=背包最大容量
4
           for (int j = m; j >= wei[i]; j--)
5
              // wei=大小 val=价值
6
7
              f[j] = max(f[j], f[j - wei[i]] + val[i]);
8
       }
9
   }
   2.2 BagProblem
1 #define N 1000
  // val=价值 wei=重量 num=数量
  int val[N], wei[N], num[N], f[N];
  // n=种类个数 m=背包最大值
5
  // 01背包
6
   void dp1(int n, int m) {
7
8
       for (int i = 0; i < n; i++) {
9
           for (int j = m; j >= wei[i]; j--)
10
              f[j] = max(f[j], f[j - wei[i]] + val[i]);
11
       }
   }
12
13
  // 完全背包
14
   void dp2(int n, int m) {
15
16
       //初始化看要求
       for (int i = 0; i <= m; i++) {
17
           f[i] = INF;
18
19
       f[0] = 0;
20
       //若要求恰好装满背包,那在初始化时除了f[0]=0其它f[1..V]均=-∞
21
22
       //若没要求背包装满,只希望价格大,初始化时应将f[0..V]=0)
23
       for (int i = 0; i < n; i++)
24
           for (int j = wei[i]; j <= m; j++)</pre>
              f[j] = max(f[j], f[j - wei[i]] + val[i]);
25
26 }
27
  // 多重背包
28
   void dp3(int n, int m) {
       for (int i = 0; i < n; i++)
30
           for (int k = 0; k < num[i]; k++)</pre>
31
32
              for (int j = m; j >= wei[i]; j--)
                  f[j] = max(f[j], f[j - wei[i]] + val[i]);
33
34 }
       FullBag
   2.3
1 /*
  完全背包问题的特点是,每种物品可以无限制的重复使用,可以选择放或不放。
  完全背包问题描述:
4 有N物品和一个容量为V的背包。第i件物品的重量是wei[i],价值是val[i]。
```

```
*/
5
6
   #include <cstdio>
7
   #define INF 0x3fffffff
8
   #define N 10047
9
  int f[N], val[N], wei[N];
10
  int min(int a,int b)
11
12
   {
       return x<y?x:y;</pre>
13
   }
14
  int main()
15
16
   {
       int t,i,j,k,E,F,m,n;
17
       scanf("%d",&t);
18
       while(t--)
19
20
          scanf("%d%d",&E,&F);
21
          int c = F-E;
22
          for(i = 0 ; i \le c ; i++)
23
              f[i]=INF;
24
          scanf("%d",&n);
25
          for(i = 0 ; i < n ; i++)
26
          {
27
28
              scanf("%d%d",&val[i],&wei[i]);//val[i]为面额,wei[i]为重量
29
30
          f[0]=0;//因为此处假设的是小猪储钱罐 恰好装满 的情况
          //注意初始化(要求恰好装满背包,那么在初始化时除了f[0]为0其它f[1..V]均设为-∞,
31
          //这样就可以保证最终得到的f[N]是一种恰好装满背包的最优解。
32
          //如果并没有要求必须把背包装满,而是只希望价格尽量大,初始化时应该将f[0..V]全部设为0)
33
34
          for(i =0; i < n; i++)
35
          {
              for(j = wei[i] ; j <= c ; j++)</pre>
36
37
                  f[j] = min(f[j], f[j-wei[i]]+val[i]); //此处求的是最坏的情况所以用min,确定最少
38
       的钱,当然最后就用max了, HEHE
39
40
          }
41
          if(f[c] == INF)
              printf("This is impossible.\n");
42
43
              printf("The minimum amount of money in the piggy-bank is %d.\n",f[c]);
44
45
46
       return 0;
47
   //此代码为HDU1114;
   2.4 MultiBag
1 //多重背包(MultiplePack): 有N种物品和一个容量为V的背包。
2 //第i种物品最多有n[i]件可用,每件费用是c[i],价值是w[i]。
3 //求解将哪些物品装入背包可使这些物品的费用总和不超过背包容量,
4 //且价值总和最大。
  //HDU 2191
5
6
  #include <cstdio>
7
8
  #include <cstring>
  #define N 247
10 int max(int x,int y){
```

```
11
       return x>y?x:y;
   int main() {
12
13
       int t,n,m,i,j,k;
14
       int w[N],pri[N],num[N],f[N];
15
       while(~scanf("%d",&t)){
16
           while(t--){
17
                memset(f,0,sizeof(f));
18
                scanf("%d%d",&n,&m);//n为总金额, m为大米种类
19
               for(i = 0; i < m; i++){
20
                    scanf("%d%d%d",&pri[i],&w[i],&num[i]);//num[i]为每种大米的袋数
21
                }
22
                for(i = 0 ; i < m ; i++){
23
                    for(k = 0 ; k < num[i] ; k++){
24
                        for(j = n ; j >= pri[i]; j--){
25
                            f[j] = max(f[j],f[j-pri[i]]+w[i]);
26
                        }
27
                    }
28
29
30
                printf("%d\n",f[n]);
31
           }
32
       }
33
       return 0;
34 }
```

3 数据结构

3.1 BTree

```
template<class T>
1
2
3
   struct TreeNode {
        T value;
4
        TreeNode *left;
5
        TreeNode *right;
6
   };
7
8
   template<class T>
9
10
   TreeNode<T> *createTree(const T *pre, const T *in, const int len) {
        TreeNode<T> *t = NULL;
11
        if (len > 0) {
12
            t = new TreeNode<T>;
13
            t->value = pre[0];
14
            int index;
15
            for (index = 0; index < len; index++) {</pre>
16
                if (in[index] == pre[0]) {
17
                     break;
18
                }
19
20
            if (index == len) {
21
22
                index = -1;
23
            }
24
            t->left = createTree(pre + 1, in, index);
25
            t->right = createTree(pre + index + 1, in + index + 1, len - index - 1);
26
27
        return t;
28
   }
29
30
   template<class T>
   int preOrder(TreeNode<T> *root, queue<T> &out) {
31
32
        if (root) {
            int count = 1;
33
34
            out.push(root->value);
35
            count += pre0rder(root->left, out);
36
            count += pre0rder(root->right, out);
37
            return count;
        } else {
38
39
            return 0;
40
        }
   }
41
42
   template<class T>
43
   int inOrder(TreeNode<T> *root, queue<T> &out) {
44
        if (root) {
45
            int count = 1;
46
            count += inOrder(root->left, out);
47
48
            out.push(root->value);
            count += inOrder(root->right, out);
49
50
            return count;
51
        } else {
52
            return 0;
53
        }
54
   }
55
```

```
template<class T>
    void postOrder(TreeNode<T> *root, queue<T> &out) {
57
         if (root) {
58
             postOrder(root->left, out);
59
60
             postOrder(root->right, out);
             out.push(root->value);
61
         } else {
62
             return;
63
         }
64
    }
65
66
67
    template<class T>
    T *convertQueueToArray(queue<T> &out, int len) {
68
         T *list = new T[len];
69
         int now = 0;
70
         while (!out.empty() && now < len) {</pre>
71
             list[now] = out.front();
72
73
             out.pop();
74
             now++;
75
         return list;
76
    }
77
78
79
    template<class T>
    void destroyTree(TreeNode<T> *root) {
81
         if (root) {
             destroyTree(root->left);
82
             destroyTree(root->right);
83
             delete root;
84
85
         } else return;
    }
86
87
    template<class T>
88
    void insertIntoBSTree(TreeNode<T> *root, const T &value) {
89
         if (!root) {
90
             return;
91
92
93
         if (value < root->value) {
             if (root->left) {
94
                 insertIntoTree(root->left, value);
95
             } else {
96
                 root->left = new TreeNode<T>;
97
                 root->left->value = value;
98
99
                 root->left->left = NULL;
                 root->left->right = NULL;
100
             }
101
         } else if (value > root->value) {
102
             if (root->right) {
103
                 insertIntoTree(root->right, value);
104
105
106
                 root->right = new TreeNode<T>;
107
                 root->right->value = value;
                 root->right->left = NULL;
108
109
                 root->right->right = NULL;
             }
110
111
         }
112
113
114 template<class T>
```

```
TreeNode<T> *createBSTree(T *list, int len) {
        if (len < 1) {
116
            return NULL;
117
118
        TreeNode<T> *root = new TreeNode<char>;
119
        root->value = list[0];
120
        root->left = NULL;
121
        root->right = NULL;
122
        for (int i = 1; i < len; i++) {
123
            insertIntoBSTree(root, list[i]);
124
125
126
        return root;
127 }
    3.2 pbds-bbtree
 1 #include <ext/pb_ds/tree_policy.hpp>
 2 #include <ext/pb_ds/assoc_container.hpp>
 3 // 红黑树
   __gnu_pbds::tree<int, null_type, less<int>, rb_tree_tag,
        tree_order_statistics_node_update> t;
 5 // null_type无映射(低版本g++为null_mapped_type)
   // 类似multiset
    __gnu_pbds::tree<int, null_type, less_equal<int>, rb_tree_tag,
        tree_order_statistics_node_update> t;
 8 find_by_order(size_t order);
 9 // 结点更新
10 tree_order_statistics_node_update
11 insert(p);
12 erase(it);
13 // 求k在树中是第几大:
14 order_of_key(p);
15 // 找到第order小的迭代器
16 find_by_order(order);
17 // 前驱
18 lower_bound(p);
19 // 后驱
20 upper_bound(p);
21 // 合并
22 a.join(b);
23 // 分割 key小于等于v的元素属于a, 其余的属于b
24 a.split(v, b);
    3.3
        树状数组
    const int N = 1000005;
 1
    struct BITree {
 2
 3
        int n;
        ll c[N];
 4
 5
        void init(int n) {
 6
 7
            memset(c, 0, sizeof(ll) * ++n);
 8
            this->n = n;
        }
 9
10
        int change(int pos, ll v) {
11
            for (int i = pos; i < n; i += i & (-i))
12
```

```
13
                c[i] += v;
14
            return 0;
        }
15
16
        ll query(int x) {
17
            ll ans = 0;
18
            for (int i = x; i > 0; i -= i & (-i))
19
                ans += c[i];
20
21
            return ans;
22
        }
23 };
   3.4 二维树状数组
   const int N = 2005;
2
   struct TdBITree {
3
        int n, m;
4
5
        11 c[N][N];
6
        void init(int n, int m) {
7
            this->n = n;
8
9
            this->m = m;
            memset(c, 0, sizeof(c))
10
11
        }
12
13
        inline int lowbit(const int &x) {
14
            return x & -x;
        }
15
16
17
        void init(int n, int m, ll v) {
18
            this->n = n;
19
            this->m = m;
20
            rep(x, 1, N) {
                rep(y, 1, N) {
21
                     c[x][y] = (x * y + (x - lowbit(x)) * (y - lowbit(y)) - x * (y - lowbit(x))
22
       y)) - (x - lowbit(x)) * y) * v;
23
                }
24
            }
        }
25
26
        int change(int x, int y, ll v) {
27
            for (int i = x; i <= n; i += lowbit(i))</pre>
28
29
                 for (int j = y; j <= m; j += lowbit(j))</pre>
                     c[i][j] += v;
30
            return 0;
31
32
        }
33
        11 query(int x, int y) {
34
35
            11 \text{ ans} = 0;
            for (int i = x; i >= 1; i -= lowbit(i))
36
37
                 for (int j = y; j >= 1; j -= lowbit(j))
38
                     ans += c[i][j];
39
            return ans;
        }
40
41
        11 solve(int x1, int y1, int x2, int y2) {
42
```

```
return query(x2, y2) - query(x1 - 1, y2) - query(x2, y1 - 1) + query(x1 - 1, y1
43
         - 1);
44
45 };
   3.5 线段树
   const int N = 50005;
1
2
   struct SegTree {
3
4
        ll c[N];
        ll\ ans[N << 2];
5
6
        ll laz[N << 2];
7
        void init(int n) {
8
            memset(c, 0, sizeof(ll) * (n + 1));
9
10
11
12
        inline void up(int k) {
13
            ans[k] = ans[k << 1] + laz[k << 1] + ans[k << 1 | 1] + laz[k << 1 | 1];
14
15
        inline void push(int k) {
16
            laz[k \ll 1] += laz[k];
17
            laz[k << 1 | 1] += laz[k];
18
19
            ans[k] += laz[k];
20
            laz[k] = 0;
21
        }
22
        void build(int x, int y, int k) {
23
24
            laz[k] = 0;
25
            if (x == y) {
26
                ans[k] = c[x];
27
                return;
28
29
            int m = (x + y) >> 1;
30
            build(x, m, k \ll 1);
31
            build(m + 1, y, k << 1 | 1);
32
            up(k);
33
34
        void change(int x, int y, int k, int l, int r, ll v) {
35
36
            if (x == 1 \&\& y == r) {
                laz[k] += v;
37
38
                return;
            }
39
            push(k);
40
            int m = (x + y) >> 1;
41
            if (r \ll m) change(x, m, k \ll 1, l, r, v);
42
            else if (l > m)change(m + 1, y, k << 1 | 1, l, r, v);
43
            else change(x, m, k << 1, l, m, v), change(m + 1, y, k << 1 \mid 1, m + 1, r, v);
44
            up(k);
45
        }
46
47
        11 query(int x, int y, int k, int l, int r) {
48
            if (x == 1 &  y == r) 
49
                return ans[k] + laz[k];
50
            }
51
```

```
int m = (x + y) >> 1;
52
            push(k);
53
            if (r <= m) return query(x, m, k << 1, 1, r);</pre>
54
            else if (l > m) return query(m + 1, y, k \ll 1 \mid 1, l, r);
55
            else return query(x, m, k << 1, l, m) + query(m + 1, y, k << 1 | 1, m + 1, r);
56
57
        }
58 };
         二维线段树
   3.6
2
   const int N = 1005;
3
4
   struct SegTree {
5
        inline int son(int k, int x) {
6
7
            return (k << 2) - 2 + x;
        }
8
9
10
        struct node {
            int l, r;
11
12
            node() = default;
13
14
            node(int a, int b) : l(a), r(b) {}
15
16
17
            inline int mid() {
                return (l + r) \gg 1;
18
            }
19
20
21
            inline node left() {
22
                return node(l, mid());
23
            }
24
            inline node right() {
25
                return node(mid() + 1, r);
26
            }
27
28
29
            inline bool in(int x) {
30
                 return x >= 1 && x <= r;
            }
31
32
            inline bool more() {
33
                return l < r;</pre>
34
            }
35
36
            bool operator==(const node &t) {
37
                return l == t.l && r == t.r;
38
            }
39
        };
40
41
        11 c[N << 2][N << 2];
42
43
        ll\ ans[N << 4];
        ll laz[N << 4];
44
45
        inline void up(int k, bool x, bool y) {
46
            int s = (k << 2) - 2;
47
            11 t = 0;
48
```

```
if(x) t += ans[s] + ans[s + 1] + laz[s] + laz[s + 1];
49
             if (y) t += ans[s + 2] + ans[s + 3] + laz[s + 2] + laz[s + 3];
50
             ans[k] = t;
51
52
53
        inline void push(int k) {
54
             int s = (k << 2) - 2;
55
             laz[s] += laz[k];
56
             laz[s + 1] += laz[k];
57
             laz[s + 2] += laz[k];
58
             laz[s + 3] += laz[k];
59
60
             ans[k] += laz[k];
             laz[k] = 0;
61
        }
62
63
        void build(node x, node y, int k) {
64
             laz[k] = 0;
65
             if (x.more() && y.more()) {
66
67
                 ans[k] = c[x.1][y.1];
68
                 return;
             }
69
             ans[k] = 0;
70
             bool ax = false;
71
72
             bool ay = false;
73
             if (x.more()) {
                 build(x.left(), y, son(k, 0));
74
                 build(x.right(), y, son(k, 1));
75
76
             if (y.more()) {
77
                 build(x, y.left(), son(k, 2));
78
79
                 build(x, y.right(), son(k, 3));
80
             up(k, x.more(), y.more());
81
        }
82
83
        void change(node x, node y, int k, node l, node r, ll v) {
84
             if (x == 1 \&\& y == r) {
85
86
                 laz[k] += v;
87
                 return;
             }
88
             push(k);
89
             if (x.more()) {
90
91
                 if (l.r <= x.mid()) {
                      change(x.left(), y, son(k, \emptyset), l, r, v);
92
                 } else if (l.l > x.mid()) {
93
                      change(x.right(), y, son(k, 1), l, r, v);
94
                 } else {
95
                      change(x.left(), y, son(k, 0), node(l.l, x.mid()), r, v);
96
                      change(x.right(), y, son(k, 1), node(x.mid() + 1, l.r), r, v);
97
                 }
98
99
             if (y.more()) {
100
101
                 if (r.l <= y.mid()) {</pre>
                      change(x, y.left(), son(k, 2), l, r, v);
102
                 } else if (r.r > y.mid()) {
103
104
                      change(x, y.right(), son(k, 3), 1, r, v);
105
                 } else {
106
                      change(x, y.left(), son(k, 2), l, node(r.l, y.mid()), v);
                      change(x, y.right(), son(k, 3), l, node(y.mid() + 1, r.r), v);
107
```

```
}
108
109
             up(k, x.more(), y.more());
110
         }
111
112
         11 query(node x, node y, int k, node l, node r) {
113
             if (x == 1 \&\& y == r) {
114
                 return ans[k] + laz[k];
115
             }
116
             push(k);
117
             11 t = 0;
118
             if (x.more()) {
119
120
                 if (l.r <= x.mid()) {</pre>
                      t += query(x.left(), y, son(k, 0), l, r);
121
                 } else if (l.l > x.mid()) {
122
                      t += query(x.right(), y, son(k, 1), l, r);
123
124
                 } else {
                      t \leftarrow query(x.left(), y, son(k, 0), node(l.l, x.mid()), r);
125
                      t \leftarrow query(x.right(), y, son(k, 1), node(x.mid() + 1, l.r), r);
126
                 }
127
128
             if (y.more()) {
129
                 if (r.l <= y.mid()) {</pre>
130
131
                      t \leftarrow query(x, y.left(), son(k, 2), l, r);
                  } else if (r.r > y.mid()) {
132
                      t += query(x, y.right(), son(k, 3), l, r);
133
                 } else {
134
                      t += query(x, y.left(), son(k, 2), l, node(r.l, y.mid()));
135
                      t \leftarrow query(x, y.right(), son(k, 3), l, node(y.mid() + 1, r.r));
136
137
138
             }
139
             return t;
140
         }
141 };
    3.7 树状数组求逆序对
    BITree t;
 1
 2
    int n;
    pii a[N];
 3
    void solve() {
 5
         t.init(n);
 6
 7
         for (int i = 1; i <= n; i++) {
             int x;
 8
 9
             cin >> x;
             a[i] = make_pair(x, i);
10
11
         sort(a + 1, a + n + 1);
12
13
         11 ans = 0;
         for (int i = 1; i <= n; i++) {
14
15
             t.change(a[i].second, 1);
             ans += (i - t.query(a[i].second));
16
17
18
         cout << ans << endl;</pre>
19 }
```

4 图论

4.1 Dijkstra

```
struct node {
1
2
        int e, v, nxt;
3
        node() = default;
        node(int a, int b, int c = 0) : e(a), v(b), nxt(c) {}
4
5
        bool operator<(const node &a) const {</pre>
6
7
            return (a.v == v ? e < a.e : v < a.v);
8
        }
9
   };
10
   const ll INF = 10000000;
11
  const int N = 100000;
12
13 const int M = 100000;
14
   struct Graph {
15
16
        node eg[M];
17
        int head[N];
        int cnt;
18
19
20
        void init(int n) {
            memset(head, -1, sizeof(int) * ++n);
21
22
            cnt = 0;
23
24
        inline void addEdge(int x, int y, int v) {
25
            eg[cnt] = node(y, v, head[x]);
26
            head[x] = cnt++;
27
28
   } gh;
29
30 int dist[N];
31 int path[N];
32
33
   void bfs(int s, int n) {
34
        n++;
35
        rep(i, 0, n) dist[i] = INF;
36
        memset(path, -1, sizeof(int) * n);
37
        dist[s] = 0;
        path[s] = s;
38
39
        priority_queue<node> q;
        q.push(node(s, dist[s]));
40
        while (!q.empty()) {
41
42
            node f = q.top();
43
            q.pop();
            for (int i = gh.head[f.e]; \sim i; i = gh.eg[i].nxt) {
44
                node &t = gh.eg[i];
45
                if (dist[t.e] > f.v + t.v) {
46
                     dist[t.e] = f.v + t.v;
47
48
                     path[t.e] = f.e;
                     q.push(node(t.e, dist[t.e]));
49
50
                }
            }
51
        }
52
53
  #include <ext/pb_ds/priority_queue.hpp>
```

```
#include <ext/pb_ds/assoc_container.hpp>
   typedef __gnu_pbds::priority_queue<node, greater<node>> heap;
57
58
   heap::point_iterator its[N];
59
60
   int cnt[N];
61
   void dfs(int s, int n) {
62
63
        n++;
        rep(i, 0, n) dist[i] = INF;
64
        memset(cnt, 0, sizeof(int) * n);
65
66
        dist[s] = 0;
67
        cnt[s] = 1;
68
        heap q;
        its[s] = q.push(node(s, dist[s]));
69
        while (!q.empty()) {
70
            node f = q.top();
71
            q.pop();
72
            for (int i = gh.head[f.e]; \sim i; i = gh.eg[i].nxt) {
73
                node &t = gh.eg[i];
74
                its[t.e] = 0;
75
                int v = f.v + t.v;
76
                if (dist[t.e] > v) {
77
                    dist[t.e] = v;
78
79
                    if (its[t.e] != 0) {
80
                         q.modify(its[t.e], node(t.e, dist[t.e]));
81
                    } else {
                         its[t.e] = q.push(node(t.e, dist[t.e]));
82
83
                    cnt[t.e] = cnt[f.e];
84
                } else if (dist[t.e] == v) {
85
                    (cnt[t.e] += cnt[f.e]) \% = 100003;
86
87
88
            }
        }
89
  }
90
   4.2 spfa
   vector<int> dist;
2
   vector<vector<node>> eq;
3
   vector<int> path;
4
   bool spfa(int n, int start) {
5
        dist.assign(n, INF);
6
7
        dist[start] = 0;
        deque<int> q;
8
        q.push_back(start);
9
        path.assign(n, -1);
10
        vector<int> cnt(n, 0);
11
        vector<bool> flag(n, false);
12
        cnt[start] = flag[start] = true;
13
        while (!q.empty()) {
14
            const int now = q.front();
15
16
            q.pop_front();
            flag[now] = false;
17
            for (auto i: eg[now]) {
18
                if (dist[i.x] > dist[now] + i.d) {
19
20
                    dist[i.x] = dist[now] + i.d;
```

```
21
                     path[i.x] = now;
                     if (!flag[i.x]) {
22
                         if (n == ++cnt[i.x]) return false;
23
                         //队列非空且优于队首 (SLF)
24
                         if (!q.empty() && dist[i.x] < dist[q.front()]) {</pre>
25
                             q.push_front(i.x);
26
27
                         } else {
28
                             q.push_back(i.x);
29
                         flag[i.x] = true;
30
31
                     }
32
                }
            }
33
        }
34
35
        return true;
36
   4.3 Dinic
   #define N 2005
1
2
   #define INF 0x7fffffff
3
   struct dinic {
4
5
6
        struct node {
7
            int e;
8
            11 f;
9
10
            node() = default;
11
            node(int a, ll b) : e(a), f(b) {}
12
13
        };
14
        // 点的范围[0, n)
15
16
        int n;
        vector<node> eg;
17
        vector<int> head[N];
18
        // 弧优化
19
20
        int cur[N], dis[N];
21
        dinic() = default;
22
23
        // 设置N
24
        void setN(int n) {
25
26
            this -> n = n;
27
28
        inline void addEdge(int x, int y, ll f) {
29
            //printf("%d->%d: %lld\n", x, y, f);
30
            head[x].push_back(static_cast<int &&>(eg.size()));
31
            eg.push_back({y, f});
32
33
        }
34
        // 加流量
35
        void addFlow(int x, int y, ll f) {
36
            addEdge(x, y, f);
37
            addEdge(y, x, 0);
38
        }
39
```

```
40
        bool bfs(int s, int e) {
41
            fill_n(dis, n, -1);
42
            int q[N];
43
            int l, r;
44
            1 = r = 0;
45
            dis[s] = 0;
46
            q[r++] = s;
47
            while (l < r) {
48
                 int f = q[l++];
49
                 for (const auto &i: head[f]) {
50
51
                     if (eg[i].f > 0 && dis[eg[i].e] == -1) {
                         dis[eg[i].e] = dis[f] + 1;
52
                         q[r++] = eg[i].e;
53
                     }
54
                 }
55
56
            return dis[e] > 0;
57
        }
58
59
        ll dfs(int s, int e, ll mx) {
60
            if (s == e \mid \mid mx == 0) {
61
                 return mx;
62
63
64
            int flow = 0;
            for (int &k = cur[s]; k < head[s].size(); k++) {</pre>
65
                 int &i = head[s][k];
66
                 auto &te = eg[i];
67
                 11 a;
68
                 if (te.f > 0 \& dis[te.e] == dis[s] + 1 \& (a = dfs(te.e, e, min(te.f, mx)))
69
        )) {
70
                     te.f -= a;
                     eg[i ^ 1].f += a;
71
72
                     flow += a;
73
                     mx -= a;
74
                     if (mx <= 0) break;
75
                 }
76
            }
            return flow;
77
78
        }
79
        ll max_flow(int s, int e) {
80
            ll ans = 0;
81
            while (bfs(s, e)) {
82
83
                 fill_n(cur, n, 0);
84
                 ans += dfs(s, e, INF);
85
            }
            return ans;
86
        }
87
88
89
        // 清空数据
90
        void clear() {
            rep(i, 0, n) head[i].clear();
91
92
            eg.clear();
93
        }
94 };
```

4.4 hungry

```
1 #define N 105
2 #define M 10005
3 int n, m, k;
4 pii eg[M * 2];
5 int result[N * 2];
6 int head[N * 2];
   int cnt = 0;
7
8
   void addEdge(int x, int y) {
9
        eg[cnt].first = y;
10
        eg[cnt].second = head[x];
11
12
        head[x] = cnt++;
   }
13
14
   bool vis[M * 2] = {false};
15
16
17
   int dfs(int x) {
        for (int i = head[x]; \sim i; i = eg[i].second) {
18
19
            int y = eg[i].first;
            if (!vis[y]) {
20
                vis[y] = true;
21
                if (result[y] == -1 || dfs(result[y])) {
22
                     result[y] = x;
23
                     return 1;
24
25
                }
26
            }
27
28
        return 0;
   }
29
30
   int MaxMatch() {
31
32
        int ans = 0;
33
        memset(result, -1, sizeof(result));
        rep(i, 1, n + 1) {
34
            memset(vis, 0, sizeof(vis));
35
            ans += dfs(i);
36
37
38
        return ans;
39
   }
40
41
   void solve() {
        scanf("%d%d", &m, &k);
42
        memset(head, -1, sizeof(head));
43
44
        cnt = 0;
45
        rep(i, 0, k) {
            int x, y;
scanf("%d%d", &x, &y);
46
47
            addEdge(x, y);
48
49
        int ans = MaxMatch();
50
        printf("%d\n", ans);
51
52 }
```

4.5 MinSpanTree

1 /*

```
2 * Prim 求 MST
   * 耗费矩阵 cost□□, 标号从 0 开始, 00n-1
3
   * 返回最小生成树的权值,返回 -1 表示原图不连通
6 const int INF = 0x3f3f3f3f;
7
   const int N = 110;
   bool vis[N];
9 int lowc[N]; //点是 0 n-1
  int prim(int cost[][N], int n) {
10
       int ans = 0;
memset(vis, false, sizeof(vis));
11
12
13
       vis[0] = true;
       for (int i = 1; i < n; i++)lowc[i] = cost[0][i];</pre>
14
       for (int i = 1; i < n; i++) {
15
            int minc = INF;
16
            int p = -1;
17
            19
18
            for (int j = 0; j < n; j++)
19
                if (!vis[j] && minc > lowc[j]) {
20
                   minc = lowc[j];
21
22
                    p = j;
23
24
            if (minc == INF)return -1;//原图不连通
25
           ans += minc;
           vis[p] = true;
26
27
            for (int j = 0; j < n; j++)
                if (!vis[j] && lowc[j] > cost[p][j])
28
29
                    lowc[j] = cost[p][j];
30
31
       return ans;
32 }
```

5 博弈

5.1 GameProblem

```
// 巴什博奕, 是否先手必胜
   inline bool bash_game(int n, int m) {
3
       //一堆东西, n个物品,最多选m个
       return n % (m + 1);
4
   }
5
6
   // 威佐夫博弈, 是否先手必胜
7
   // 有两堆各若干的物品,两人轮流从其中一堆取至少一件物品,至多不限,或从两堆中同时取相同件物品,规定最后
       取完者胜利。
   inline bool wythoff_game(int n, int m) {
9
       if (n > m) {
10
           swap(n, m);
11
12
       int temp = floor((n2 - n1) * (1 + sqrt(5.0)) / 2.0);
13
       return temp != n1;
14
15 }
16 // SG函数
17 #define N 1001
18 //f[]: 可以取走的石子个数
   //sg[]:0~n的SG函数值
20 int f[N], sg[N], mex[N];
21
   void getSG(int n) {
22
23
       int i, j;
       memset(sg, 0, sizeof(sg));
24
25
       for (i = 1; i <= n; i++) {
          memset(mex, 0, sizeof(mex));
26
           for (j = 1; f[j] \le i; j++)
27
28
              mex[sg[i - f[j]]] = 1;
           for (j = 0; j <= n; j++) { //求mes{}}中未出现的最小的非负整数
29
              if (mex[j] == 0) {
30
                  sg[ij] = j;
31
                  break;
32
33
              }
34
          }
35
       }
36 }
```

6 分治

6.1 IntegerFastPower

```
1 ll fpow(ll x, ll k) {
2          ll base = x, r = 1;
3          for (; k; k >>= 1) {
4              if (k & 1) r = r * base;
5             base = base * base;
6          }
7          return r;
8 }
```

6.2 MatrixFastPower

```
#define MAX_N 10
2
   #define mod_num 9973
3
   struct Mat {
4
5
        long long mat[MAX_N][MAX_N];
        long long n;
6
7
        Mat() {
8
            memset(mat, 0, sizeof(mat));
            n = 0;
9
10
        Mat(long long n) {
11
12
            memset(mat, 0, sizeof(mat));
13
            this->n = n;
14
        void init() {
15
            for (int i = 0; i < n; ++i) {</pre>
16
17
                mat[i][i] = 1;
18
19
        Mat(const long long ** list, long long n) {
20
21
            this->n = n;
            for (int i = 0; i < n; ++i) {
22
23
                for (int j = 0; j < n; ++j) {
24
                     mat[i][j] = list[i][j];
25
26
            }
        }
27
28
   };
29
   Mat operator * (Mat a, Mat b) {
30
        long long n = a.n;
31
        Mat c(n);
32
        memset(c.mat, 0, sizeof(c.mat));
33
        for (int i = 0; i < n; ++i) {
34
            for (int j = 0; j < n; ++j) {
35
                for (int k = 0; k < n; ++k) {
36
                     c.mat[i][j] += (a.mat[i][k] * b.mat[k][j]) % mod_num;
37
38
                     c.mat[i][j] %= mod_num;
39
                }
            }
40
41
42
        return c;
43
   }
```

```
44
45 Mat operator ^ (Mat a, int k) {
46     long long n = a.n;
47     Mat c(n);
48     c.init();
49     for (; k; k >>= 1) {
50         if (k & 1) c = c * a;
51         a = a * a;
52     }
53     return c;
54 }
```

7 其他

7.1 BigInteger

```
// base and base_digits must be consistent
   constexpr int base = 1000000000;
   constexpr int base_digits = 9;
3
4
   struct bigint {
5
       // value == 0 is represented by empty z
6
7
       vector<int> z; // digits
8
       // sign == 1 <==> value >= 0
9
10
       // sign == -1 <==> value < 0
11
       int sign;
12
       bigint() : sign(1) {}
13
14
       bigint(ll v) { *this = v; }
15
16
       bigint &operator=(ll v) {
17
            sign = v < 0 ? -1 : 1;
18
            v *= sign;
19
            z.clear();
20
            for (; v > 0; v = v / base) z.push_back((int) (v \% base));
21
            return *this;
22
23
       }
24
25
       bigint(const string &s) { read(s); }
26
       bigint &operator+=(const bigint &other) {
27
            if (sign == other.sign) {
28
29
                for (int i = 0, carry = 0; i < other.z.size() | | carry; ++i) {
30
                    if (i == z.size())
                        z.push_back(0);
31
                    z[i] += carry + (i < other.z.size() ? other.z[i] : 0);
32
                    carry = z[i] >= base;
33
34
                    if (carry)
35
                        z[i] -= base;
36
            } else if (other != 0 /* prevent infinite loop */) {
37
38
                *this -= -other;
39
40
            return *this;
41
42
       friend bigint operator+(bigint a, const bigint &b) { return a += b; }
43
44
       bigint &operator-=(const bigint &other) {
45
            if (sign == other.sign) {
46
                if (sign == 1 && *this >= other || sign == -1 && *this <= other) {
47
                    for (int i = 0, carry = 0; i < other.z.size() | | carry; ++i) {
48
                        z[i] = carry + (i < other.z.size() ? other.z[i] : 0);
49
                        carry = z[i] < 0;
50
51
                        if (carry)
                             z[i] += base;
52
53
54
                    trim();
                } else {
55
```

```
*this = other - *this;
56
                      this->sign = -this->sign;
57
58
59
             } else {
                 *this += -other;
60
61
             return *this;
62
         }
63
64
         friend bigint operator-(bigint a, const bigint &b) {
65
             return a -= b;
66
67
         }
68
         bigint &operator*=(int v) {
69
             if (v < 0) sign = -sign, v = -v;
70
             for (int i = 0, carry = 0; i < z.size() || carry; ++i) {
71
                 if (i == z.size()) z.push_back(0);
 72
                 ll cur = (ll) z[i] * v + carry;
73
                 carry = (int) (cur / base);
74
                 z[i] = (int) (cur % base);
75
             }
76
             trim();
77
             return *this;
78
79
         }
80
         bigint operator*(int v) const { return bigint(*this) *= v; }
81
82
         friend pair<bigint, bigint> divmod(const bigint &a1, const bigint &b1) {
83
             int norm = base / (b1.z.back() + 1);
84
             bigint a = a1.abs() * norm;
85
             bigint b = b1.abs() * norm;
86
87
             bigint q, r;
             q.z.resize(a.z.size());
88
89
             for (int i = (int) \ a.z.size() - 1; \ i >= 0; \ i--) {
90
                 r *= base;
91
                 r += a.z[i];
92
93
                 int s1 = b.z.size() < r.z.size() ? r.z[b.z.size()] : 0;</pre>
                 int s2 = b.z.size() - 1 < r.z.size() ? r.z[b.z.size() - 1] : 0;</pre>
94
                 int d = (int) (((ll) s1 * base + s2) / b.z.back());
95
                 r -= b * d;
96
                 while (r < 0) r += b, --d;
97
98
                 q.z[i] = d;
             }
99
100
             q.sign = a1.sign * b1.sign;
101
             r.sign = a1.sign;
102
             q.trim();
103
104
             r.trim();
             return {q, r / norm};
105
106
107
108
         friend bigint sqrt(const bigint &a1) {
             bigint a = a1;
109
             while (a.z.empty() \mid | a.z.size() \% 2 == 1) a.z.push_back(0);
110
111
112
             int n = a.z.size();
113
             int firstDigit = (int) ::sqrt((double) a.z[n - 1] * base + a.z[n - 2]);
114
```

```
int norm = base / (firstDigit + 1);
115
             a *= norm;
116
             a *= norm;
117
             while (a.z.empty() \mid | a.z.size() \% 2 == 1) a.z.push_back(0);
118
119
             bigint r = (ll) a.z[n - 1] * base + a.z[n - 2];
120
             firstDigit = (int) ::sqrt((double) a.z[n - 1] * base + a.z[n - 2]);
121
             int q = firstDigit;
122
             bigint res;
123
124
125
             for (int j = n / 2 - 1; j >= 0; j--) {
126
                 for (;; --q) {
                      bigint r1 = (r - (res * 2 * base + q) * q) * base * base +
127
                                  (j > 0? (ll) a.z[2 * j - 1] * base + a.z[2 * j - 2] : 0);
128
                      if (r1 >= 0) {
129
                          r = r1;
130
131
                          break;
                     }
132
133
                 (res *= base) += q;
134
135
                 if (j > 0) {
136
                      int d1 = res.z.size() + 2 < r.z.size() ? r.z[res.z.size() + 2] : 0;</pre>
137
                      int d2 = res.z.size() + 1 < r.z.size() ? r.z[res.z.size() + 1] : 0;
138
139
                      int d3 = res.z.size() < r.z.size() ? r.z[res.z.size()] : 0;</pre>
                      q = (int) (((ll) d1 * base * base + (ll) d2 * base + d3) / (firstDigit
140
        * 2));
141
             }
142
143
144
             res.trim();
             return res / norm;
145
146
        }
147
        bigint operator/(const bigint &v) const {
148
             return divmod(*this, v).first;
149
150
        }
151
        bigint operator%(const bigint &v) const {
152
             return divmod(*this, v).second;
153
154
155
        bigint &operator/=(int v) {
156
             if (v < 0) sign = -sign, v = -v;
157
             for (int i = (int) z.size() - 1, rem = 0; i >= 0; --i) {
158
                 ll cur = z[i] + rem * (ll) base;
159
                 z[i] = (int) (cur / v);
160
                 rem = (int) (cur % v);
161
162
             trim();
163
164
             return *this;
165
        }
166
167
        bigint operator/(int v) const {
             return bigint(*this) /= v;
168
        }
169
170
171
        int operator%(int v) const {
             if (v < 0) v = -v;
172
```

```
173
             int m = 0;
             for (int i = (int) z.size() - 1; i >= 0; --i)
174
                 m = (int) ((z[i] + m * (ll) base) % v);
175
176
             return m * sign;
         }
177
178
179
         bigint &operator*=(const bigint &v) {
             return *this = *this * v;;
180
181
182
183
         bigint &operator/=(const bigint &v) {
184
             return *this = *this / v;
185
186
         bool operator<(const bigint &v) const {</pre>
187
             if (sign != v.sign)
188
                  return sign < v.sign;</pre>
189
190
             if (z.size() != v.z.size())
                 return z.size() * sign < v.z.size() * v.sign;</pre>
191
             for (int i = (int) z.size() - 1; i >= 0; i--)
192
                  if (z[i] != v.z[i])
193
                      return z[i] * sign < v.z[i] * sign;</pre>
194
             return false;
195
196
         }
197
         bool operator>(const bigint &v) const { return v < *this; }</pre>
198
199
         bool operator<=(const bigint &v) const { return !(v < *this); }</pre>
200
201
         bool operator>=(const bigint &v) const { return !(*this < v); }</pre>
202
203
204
         bool operator==(const bigint &v) const { return !(*this < v) && !(v < *this); }</pre>
205
206
         bool operator!=(const bigint &v) const { return *this < v | | v < *this; }</pre>
207
208
         void trim() {
209
             while (!z.empty() && z.back() == 0) z.pop_back();
210
             if (z.empty()) sign = 1;
         }
211
212
213
         bool isZero() const {
             return z.empty();
214
         }
215
216
217
         friend bigint operator-(bigint v) {
218
             if (!v.z.empty()) v.sign = -v.sign;
219
             return v;
220
         }
221
222
         bigint abs() const {
223
             return sign == 1 ? *this : -*this;
224
         }
225
         ll longValue() const {
226
             11 \text{ res} = 0;
227
             for (int i = (int) z.size() - 1; i >= 0; i--)
228
229
                  res = res * base + z[i];
             return res * sign;
230
         }
231
```

```
232
233
         friend bigint gcd(const bigint &a, const bigint &b) {
234
             return b.isZero() ? a : gcd(b, a % b);
235
236
         friend bigint lcm(const bigint &a, const bigint &b) {
237
238
             return a / gcd(a, b) * b;
         }
239
240
         void read(const string &s) {
241
242
             sign = 1;
243
             z.clear();
244
             int pos = 0;
             while (pos < s.size() && (s[pos] == '-' || s[pos] == '+')) {</pre>
245
                 if (s[pos] == '-') sign = -sign;
246
247
                 ++pos;
248
             for (int i = (int) s.size() - 1; i >= pos; i -= base_digits) {
249
                 int x = 0;
250
                 for (int j = max(pos, i - base_digits + 1); j <= i; j++)
251
                      x = x * 10 + s[j] - '0';
252
                 z.push_back(x);
253
254
255
             trim();
256
         }
257
258
         friend istream &operator>>(istream &stream, bigint &v) {
259
             string s;
             stream >> s;
260
             v.read(s);
261
262
             return stream;
263
         }
264
         friend ostream &operator<<(ostream &stream, const bigint &v) {</pre>
265
266
             if (v.sign == -1)
                 stream << '-';
267
268
             stream << (v.z.empty() ? 0 : v.z.back());</pre>
269
             for (int i = (int) v.z.size() - 2; i >= 0; --i)
                 stream << setw(base_digits) << setfill('0') << v.z[i];</pre>
270
271
             return stream;
272
         }
273
         static vector<int> convert_base(const vector<int> &a, int old_digits, int
274
        new_digits) {
             vector<ll> p(max(old_digits, new_digits) + 1);
275
276
             p[0] = 1;
277
             for (int i = 1; i < p.size(); i++)</pre>
                 p[i] = p[i - 1] * 10;
278
             vector<int> res;
279
280
             11 \text{ cur} = 0;
281
             int cur_digits = 0;
282
             for (int v : a) {
                 cur += v * p[cur_digits];
283
                 cur_digits += old_digits;
284
                 while (cur_digits >= new_digits) {
285
                      res.push_back(int(cur % p[new_digits]));
286
287
                      cur /= p[new_digits];
288
                      cur_digits -= new_digits;
                 }
289
```

```
}
290
             res.push_back((int) cur);
291
             while (!res.empty() && res.back() == 0) res.pop_back();
292
293
             return res;
294
        }
295
296
        typedef vector<ll> vll;
297
        static vll karatsubaMultiply(const vll &a, const vll &b) {
298
299
             int n = a.size();
300
             vll res(n + n);
301
             if (n <= 32) {
                 for (int i = 0; i < n; i++)
302
303
                     for (int j = 0; j < n; j++)
                         res[i + j] += a[i] * b[j];
304
305
                 return res;
             }
306
307
308
             int k = n \gg 1;
             vll a1(a.begin(), a.begin() + k);
309
             vll a2(a.begin() + k, a.end());
310
             vll b1(b.begin(), b.begin() + k);
311
             vll b2(b.begin() + k, b.end());
312
313
             vll a1b1 = karatsubaMultiply(a1, b1);
314
             vll a2b2 = karatsubaMultiply(a2, b2);
315
316
             for (int i = 0; i < k; i++) a2[i] += a1[i];
317
             for (int i = 0; i < k; i++) b2[i] += b1[i];
318
319
             vll r = karatsubaMultiply(a2, b2);
320
             for (int i = 0; i < a1b1.size(); i++) r[i] -= a1b1[i];
321
322
             for (int i = 0; i < a2b2.size(); i++) r[i] -= a2b2[i];
323
             for (int i = 0; i < r.size(); i++) res[i + k] += r[i];
324
             for (int i = 0; i < a1b1.size(); i++) res[i] += a1b1[i];
325
326
             for (int i = 0; i < a2b2.size(); i++) res[i + n] += a2b2[i];
327
             return res;
        }
328
329
330
        bigint operator*(const bigint &v) const {
             vector<int> a6 = convert_base(this->z, base_digits, 6);
331
             vector<int> b6 = convert_base(v.z, base_digits, 6);
332
333
             vll a(a6.begin(), a6.end());
             vll b(b6.begin(), b6.end());
334
             while (a.size() < b.size()) a.push_back(0);</pre>
335
             while (b.size() < a.size()) b.push_back(0);</pre>
336
             while (a.size() & (a.size() - 1)) a.push_back(0), b.push_back(0);
337
             vll c = karatsubaMultiply(a, b);
338
             bigint res;
339
340
             res.sign = sign * v.sign;
341
             for (int i = 0, carry = 0; i < c.size(); i++) {
                 ll cur = c[i] + carry;
342
                 res.z.push_back((int) (cur % 1000000));
343
                 carry = (int) (cur / 1000000);
344
345
346
             res.z = convert_base(res.z, 6, base_digits);
347
             res.trim();
348
             return res;
```

```
349
        }
350 };
    7.2 FastIO
 1
     * FastIO
 2
 3
     * 代码模板!
     * 如有雷同!
 4
     * 纯属巧合!
 5
     */
 6
 7 namespace FastIO {
    #define BUF_SIZE 10000000
 9
   #define OUT_SIZE 10000000
    #define ll long long
10
11
        //fread->read
        bool IOerror = 0;
12
13
        inline char nc() {
14
             static char buf[BUF_SIZE], *p1 = buf + BUF_SIZE, *pend = buf + BUF_SIZE;
15
             if (p1 == pend) {
16
                 p1 = buf;
17
                 pend = buf + fread(buf, 1, BUF_SIZE, stdin);
18
19
                 if (pend == p1) {
                     I0error = 1;
20
21
                     return -1;
22
                 //{printf("IO error!\n");system("pause");for (;;);exit(0);}
23
24
25
             return *p1++;
26
        }
27
28
        inline bool blank(char ch) { return ch == ' ' | | ch == '\n' | | ch == '\r' | | ch ==
        '\t'; }
29
        inline void read(int &x) {
30
31
            bool sign = 0;
32
             char ch = nc();
33
            x = 0;
34
             for (; blank(ch); ch = nc());
35
             if (I0error)return;
             if (ch == '-')sign = 1, ch = nc();
36
             for (; ch \ge 0' \& ch \le 9'; ch = nc()x = x * 10 + ch - 0';
37
             if (sign)x = -x;
38
        }
39
40
        inline void read(ll &x) {
41
            bool sign = 0;
42
             char ch = nc();
43
             x = 0;
44
             for (; blank(ch); ch = nc());
45
             if (I0error)return;
46
             if (ch == '-')sign = 1, ch = nc();
47
             for (; ch \ge '0' \&\& ch \le '9'; ch = nc())x = x * 10 + ch - '0';
48
49
             if (sign)x = -x;
        }
50
51
        inline void read(double &x) {
52
```

```
bool sign = 0;
53
             char ch = nc();
54
             x = 0;
55
             for (; blank(ch); ch = nc());
56
             if (I0error)return;
57
             if (ch == '-')sign = 1, ch = nc();
58
             for (; ch \ge 0' \& ch \le 9'; ch = nc()x = x * 10 + ch - 0';
59
             if (ch == '.') {
60
                 double tmp = 1;
61
62
                 ch = nc();
                 for (; ch >= '0' && ch <= '9'; ch = nc())tmp /= 10.0, x += tmp * (ch - '0')
63
64
             if (sign)x = -x;
65
66
67
        inline void read(char *s) {
68
             char ch = nc();
69
             for (; blank(ch); ch = nc());
70
             if (I0error)return;
71
             for (; !blank(ch) && !I0error; ch = nc()*s++ = ch;
72
             *s = 0;
73
        }
74
75
76
        inline void read(char &c) {
             for (c = nc(); blank(c); c = nc());
77
             if (I0error) {
78
                 c = -1;
79
                 return;
80
81
             }
        }
82
83
        //fwrite->write
84
        struct Ostream_fwrite {
85
             char *buf, *p1, *pend;
86
             Ostream_fwrite() {
87
88
                 buf = new char[OUT_SIZE];
89
                 p1 = buf;
                 pend = buf + OUT_SIZE;
90
91
             void out(char ch) {
92
                 if (p1 == pend) {
93
                     fwrite(buf, 1, OUT_SIZE, stdout);
94
95
                     p1 = buf;
96
                 *p1++ = ch;
97
98
             void print(int x) {
99
                 static char s[15], *s1;
100
101
                 s1 = s;
102
                 if (!x)*s1++ = '0';
                 if (x < 0)out('-'), x = -x;
103
                 while (x)*s1++ = x % 10 + '0', x /= 10;
104
                 while (s1-- != s)out(*s1);
105
106
107
             void println(int x) {
108
                 static char s[15], *s1;
                 s1 = s;
109
                 if (!x)*s1++ = '0';
110
```

```
if (x < 0)out('-'), x = -x;
111
                while (x)*s1++ = x \% 10 + '0', x /= 10;
112
                while (s1-- != s)out(*s1);
113
                out('\n');
114
115
            void print(ll x) {
116
                static char s[25], *s1;
117
                s1 = s;
118
                if (!x)*s1++ = '0';
119
                if (x < 0)out('-'), x = -x;
120
                while (x)*s1++ = x % 10 + '0', x /= 10;
121
122
                while (s1-- != s)out(*s1);
123
            }
            void println(ll x) {
124
125
                static char s[25], *s1;
                s1 = s;
126
                if (!x)*s1++ = '0';
127
                if (x < 0)out('-'), x = -x;
128
                while (x)*s1++ = x % 10 + '0', x /= 10;
129
                while (s1-- != s)out(*s1);
130
                out('\n');
131
132
            void print(double x, int y) {
133
                static ll mul[] = {1, 10, 100, 1000, 10000, 100000, 1000000, 10000000,
134
        100000000,
                                   135
        LL, 10000000000000LL,
                                   136
        LL, 1000000000000000000LL};
                if (x < -1e-12)out('-'), x = -x;
137
                x *= mul[y];
138
                ll x1 = (ll) floor(x);
139
                if (x - floor(x) >= 0.5) ++ x1;
140
                ll x2 = x1 / mul[y], x3 = x1 - x2 * mul[y];
141
                print(x2);
142
                if (y > 0) {
143
                    out('.');
144
145
                    for (size_t i = 1; i < y && x3 * mul[i] < mul[y]; out('0'), ++i);</pre>
146
                    print(x3);
                }
147
            }
148
            void println(double x, int y) {
149
                print(x, y);
150
                out('\n');
151
152
            void print(char *s) { while (*s)out(*s++); }
153
            void println(char *s) {
154
                while (*s)out(*s++);
155
                out('\n');
156
            }
157
158
            void flush() {
159
                if (p1 != buf) {
160
                    fwrite(buf, 1, p1 - buf, stdout);
                    p1 = buf;
161
162
163
164
            ~Ostream_fwrite() { flush(); }
165
        } Ostream;
        inline void print(int x) { Ostream.print(x); }
166
```

```
inline void println(int x) { Ostream.println(x); }
167
        inline void print(char x) { Ostream.out(x); }
168
        inline void println(char x) {
169
170
            Ostream.out(x);
171
            Ostream.out('\n');
172
        inline void print(ll x) { Ostream.print(x); }
173
        inline void println(ll x) { Ostream.println(x); }
174
        inline void print(double x, int y) { Ostream.print(x, y); }
175
        inline void println(double x, int y) { Ostream.println(x, y); }
176
        inline void print(char *s) { Ostream.print(s); }
177
178
        inline void println(char *s) { Ostream.println(s); }
        inline void println() { Ostream.out('\n'); }
179
        inline void flush() { Ostream.flush(); }
180
181
    };
    using namespace FastIO;
182
    7.3 InputOutputSpeedUp
 1 //适用于正负整数
   template <class T>
 2
    inline bool scan_d (T &ret) {
 3
        char c; int sqn;
 4
        if(c = getchar(), c == EOF)
 5
                                       return 0; //EOF
        while (c != '-' && (c < '0' || c > '9')) c = getchar();
 6
        sgn = (c == '-') ? -1 : 1;
 7
        ret = (c == '-') ? 0 : (c - '0');
 8
        while (c = getchar(), c >= '0' \&\& c <= '9') ret = ret * 10 + (c - '0');
 9
        ret *= sgn;
10
        return 1;
11
12 }
   //适用于正负整数
13
   template <class T>
   inline void outU (T x) {
15
        if (x < 0) putchar('-'), x = -x;
16
        if (x > 9) out (x / 10);
17
        putchar (x \% 10 + '0');
18
19
    }
    7.4 gcd
    ll gcd(ll x, ll y) { // 循环版
 2
        ll t;
 3
        while (y){
 4
            t = x \% y;
 5
            x = y;
 6
            y = t;
 7
 8
        return x;
    }
 9
10
    ll gcd(ll a, ll b) { // 递归版
11
12
        return b == 0? a : gcd(b, a % b);
13
14
15 // 扩展欧几里得
   ll exgcd(ll a, ll b, ll &x, ll &y) {
```

```
if (b == 0) {
17
           x = 1, y = 0;
18
19
           return a;
20
       ll q = exgcd(b, a \% b, y, x);
21
       y -= a / b * x;
22
23
       return q;
24 }
   7.5 myItoa
   char * myItoa(int value, char* result, int base = 10);
2
   char * myItoa(int value, char* result, int base) {
3
       // check that the base if valid
4
5
       if (base < 2 || base > 16) { *result = 0; return result; }
6
7
       char* out = result;
       int quotient = abs(value);
8
       do {
9
           const int tmp = quotient / base;
10
            *out = "0123456789abcdef"[quotient - (tmp*base)];
11
           ++out;
12
           quotient = tmp;
13
       } while (quotient);
14
15
       // Apply negative sign
       if (value < 0) *out++ = '-';
16
17
       std::reverse(result, out);
18
       *out = 0;
       return result;
19
20 }
   7.6 Permutation
1 // 错排问题
  // D(n) = n! [(-1)^2/2! + \cdots + (-1)^(n-1)/(n-1)! + (-1)^n/n!].
  long long table[1000] = \{0, 0, 1\};
4 void init() {
       for (int i = 3; i \le 20; i++) {
5
           table[i] = (i - 1) * (table[i - 1] + table[i - 2]);
6
7
8
   }
   7.7 prime
1 #define prime_max 1000000
3 int prime_count = 0;
4 bool prime_list[prime_max] = { false };//元素值为0代表是素数
5 int prime_table[prime_max] = { 0 };
6
   void initPrime() {
7
       for (int i = 2; i < prime_max; i++) {</pre>
8
           if (!prime_list[i])
9
               prime_table[prime_count++] = i;
10
           for (int j = 0, e = prime_max / i;
11
```

```
j < prime_count && prime_table[j] <= e; j++) {
prime_list[i * prime_table[j]] = 1;
if (i % prime_table[j] == 0) break;
}
for a prime_table[j] == 0 break;
}
for a prime_table[j] == 0 break;
for
```