

Goal: to explore tree manipulation in Standard ML.

Setting: Consider the polymorphic datatype

```
datatype 'a BinTree =  
  Leaf of 'a  
| Node of 'a BinTree * 'a BinTree
```

Example: An integer tree and its representation:



```
val Tree1 = Node(
  Node (Node(Leaf(4), Leaf(7)),
        Leaf(8)),
  Node (Leaf(5),
        Node(Leaf(3), Leaf(11))))
```

Functions You Must Write (submit sml file)

`print_tree` that given a function that converts tree values into strings, and a binary tree, returns the values in that tree, with `and` between them.

```
- print_tree;  
val it = fn : ('a -> string) -> 'a BinTree -> string  
- print_tree Int.toString Tree1;  
val it = "4_and_7_and_8_and_5_and_3_and_11" : string
```

`deepest` that returns the `height` (the maximal distance from the root to a leaf) of a binary tree, together with a list of the “deepest” nodes.

```
val it = fn : 'a BinTree -> int * 'a list  
- deepest Tree1;  
val it = (3,[4,7,3,11]) : int * int list
```

`foldt` that folds a binary tree, given a function combining two results, and a function converting a leaf into a result.

```
.. ('a * 'a -> 'a) -> ('b -> 'a) -> 'b BinTree -> 'a  
- foldt op+ (fn x => x+1) Tree1;  
val it = 44 : int
```

`print_tree'` with type and functionality as `print_tree` but defined using `foldt` and `not` by pattern matching.