

Parameter	Statistic	Standard Error	Distribution	Tech. Conditions
p	\hat{p}	$\sqrt{p_0(1-p_0)/n}$ (HT) $\sqrt{\hat{p}(1-\hat{p})/n}$ (CI)	Z Z	successes & failures ≥ 10 p_0 is the number in H_0
$p_1 - p_2$	$\hat{p}_1 - \hat{p}_2$ (2 independent samples)	$\sqrt{\hat{p}(1-\hat{p})(1/n_1 + 1/n_2)}$ (HT) $\sqrt{\frac{\hat{p}_1(1-\hat{p}_1)}{n_1} + \frac{\hat{p}_2(1-\hat{p}_2)}{n_2}}$ (CI)	Z Z	successes & failures ≥ 10 in each group
$\ln(RR) = \ln(p_1/p_2)$ take inverse $\ln(e)$ for CI	$\ln(\hat{p}_1/\hat{p}_2)$	$\sqrt{\frac{1}{a} - \frac{1}{a+c} + \frac{1}{b} - \frac{1}{b+d}}$	Z	large samples
$\ln(OR)$ take inverse $\ln(e)$ for CI	$\ln(\hat{OR})$	$\sqrt{\frac{1}{a} + \frac{1}{b} + \frac{1}{c} + \frac{1}{d}}$	Z	large samples
μ	\bar{x}	σ/\sqrt{n} (σ known) s/\sqrt{n} (σ unknown)	Z $t, df = n - 1$	$n \geq 30$ or normal
$\mu_1 - \mu_2$	$\bar{x}_1 - \bar{x}_2$ (2 independent samples)	$\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}$	$t, df \approx \min\{n_1, n_2\} - 1$	$n_1, n_2 \geq 30$ or normal
μ_d	\bar{x}_d (matched pairs)	s_d/\sqrt{n} ($n = \#$ pairs)	$t, df = n - 1$	$n \geq 30$ or normal
X_{n+1}	\bar{x}	$\sqrt{s^2 + \frac{s^2}{n}}$	$t, df = n - 1$	normal

To find the p -value of a HT, look up the score $\frac{\text{statistic} - \text{hypothesized value}}{\text{SE}}$ on the specified distribution in the direction of H_A .

A $(100 - \alpha)\%$ CI is of the form $\text{statistic} \pm \text{multiplier} \times \text{SE}$. The multiplier is the $(100 - \alpha/2)\%$ point from the specified distribution.

All hypothesis tests and confidence intervals are appropriate when applied to random samples from a population. If random samples are not taken, care must be used to assess whether or not the inferential conclusions are valid for the data at hand. In particular, it is important that the observations themselves are independent.

Inference for two variables (explanatory variable not necessarily binary)

Two categorical variables (χ^2 test). χ^2 -statistic = $\sum_{i=1}^r \sum_{j=1}^c \frac{(\text{observed}_{ij} - \text{expected}_{ij})^2}{\text{expected}_{ij}}$, where $\text{expected}_{ij} = \frac{(\text{total of row } i) \times (\text{total of column } j)}{\text{grand total}}$.

When the null hypothesis is true, the statistic follows a χ^2 distribution with $(r-1)(c-1)$ degrees of freedom. TECHNICAL CONDITIONS: the χ^2 test can be used if there are at least five expected counts in each cell.

Categorical explanatory, quantitative response variables (ANOVA). F -statistic = $\frac{\text{MSG}}{\text{MSE}}$, where $\text{MSG} = \frac{n_1(\bar{x}_1 - \bar{x})^2 + \cdots + n_I(\bar{x}_I - \bar{x})^2}{I-1}$

and $\text{MSE} = \frac{(n_1-1)s_1^2 + \cdots + (n_I-1)s_I^2}{N-I}$. When the null hypothesis is true, the statistic follows an F distribution with $(I-1, N-I)$ degrees of freedom. TECHNICAL CONDITIONS: an ANOVA test can be used if the data are approximately normal and the variance within each group is approximately equal.

Two quantitative variables (Simple Linear Regression).

$$r = \frac{1}{n-1} \sum_{i=1}^n \frac{(x_i - \bar{x})(y_i - \bar{y})}{s_x s_y}, \quad b_1 = r \frac{s_y}{s_x}, \quad b_0 = \bar{y} - b_1 \bar{x}, \quad \hat{y} = b_0 + b_1 x, \quad SE(b_1) = \frac{s}{s_x} \frac{1}{\sqrt{n-2}}.$$

Under the null hypothesis $H_0 : \beta_1 = 0$, the standardized slope statistic $\frac{b_1 - 0}{SE(b_1)}$ follows a t distribution with $n-2$ degrees of freedom.

TECHNICAL CONDITIONS: the SLR model is appropriate if the data are L(inear), I(ndependent observations), (nearly) N(ormal residuals / response variable around the line), and E(qual variability around the line).