

WU #21

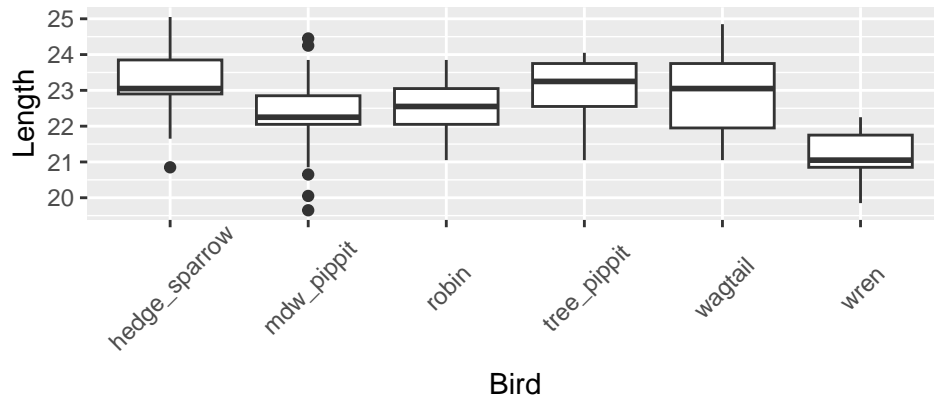
Math 58B, Spring 2023

Thursday, April 13, 2023

Your Name: _____

Names of people you worked with: _____

1. With your friends, would you rather play board games / cards or play video games?
2. Which models the size of the boxplot: MSG or MSE? How?
3. Using the model below, predict the average length of Cuckoo bird eggs for each of the 6 host birds.



Converting the Bird variable:

$$X_{mdw_pippit} = \begin{cases} 1 & \text{if mdw_pippit} \\ 0 & \text{otherwise} \end{cases} \quad X_{robin} = \begin{cases} 1 & \text{if robin} \\ 0 & \text{otherwise} \end{cases}$$

$$X_{tree_pippit} = \begin{cases} 1 & \text{if tree_pippit} \\ 0 & \text{otherwise} \end{cases} \quad X_{wagtail} = \begin{cases} 1 & \text{if wagtail} \\ 0 & \text{otherwise} \end{cases}$$

$$X_{wren} = \begin{cases} 1 & \text{if wren} \\ 0 & \text{otherwise} \end{cases}$$

So the model which describes the average egg length (denoted with the \hat{Y} notation) can be written as the following:

$$\hat{Y} = 23.12 - 0.82 \cdot X_{mdw_pippit} - 0.54 \cdot X_{robin} - 0.03 \cdot X_{tree_pippit} - 0.21 \cdot X_{wagtail} - 1.99 \cdot X_{wren}$$

```
Cuckoo %>%
  lm(Length ~ Bird, data = .) %>%
  tidy()
```

```
## # A tibble: 6 x 5
##   term                estimate std.error statistic    p.value
##   <chr>                <dbl>    <dbl>    <dbl>    <dbl>
## 1 (Intercept)          23.1      0.243     95.1 1.87e-110
## 2 Birdmdw_pippit     -0.823    0.278    -2.96 3.79e- 3
## 3 Birdrobin         -0.546    0.333    -1.64 1.03e- 1
## 4 Birdtree_pippit   -0.0314   0.338   -0.0930 9.26e- 1
## 5 Birdwagtail       -0.218    0.338   -0.645 5.20e- 1
## 6 Birdwren          -1.99     0.338   -5.89 3.91e- 8
```

Solution:

2. The size of the boxplot represents the variability of the data within each group. The variability is quantified by the value s_i which is used in the mean squared error.

$$MSE = \frac{\sum_{i=1}^I s_i^2 (n_i - 1)}{N - I}$$

3. For each host bird, calculate the average predicted egg length by adding the relevant coefficient to the intercept. For the `hedge_sparrow`, use the intercept.

$$\begin{aligned}\hat{Y}_{\text{hedge_sparrow}} &= 23.12 - 0.82 \cdot 0 - 0.54 \cdot 0 - 0.03 \cdot 0 - 0.21 \cdot 0 - 1.99 \cdot 0 = 23.12 \\ \hat{Y}_{\text{mdw_pippit}} &= 23.12 - 0.82 \cdot 1 - 0.54 \cdot 0 - 0.03 \cdot 0 - 0.21 \cdot 0 - 1.99 \cdot 0 = 22.30 \\ \hat{Y}_{\text{robin}} &= 23.12 - 0.82 \cdot 0 - 0.54 \cdot 1 - 0.03 \cdot 0 - 0.21 \cdot 0 - 1.99 \cdot 0 = 22.58 \\ \hat{Y}_{\text{tree_pippit}} &= 23.12 - 0.82 \cdot 0 - 0.54 \cdot 0 - 0.03 \cdot 1 - 0.21 \cdot 0 - 1.99 \cdot 0 = 23.09 \\ \hat{Y}_{\text{wagtail}} &= 23.12 - 0.82 \cdot 0 - 0.54 \cdot 0 - 0.03 \cdot 0 - 0.21 \cdot 1 - 1.99 \cdot 0 = 22.91 \\ \hat{Y}_{\text{wren}} &= 23.12 - 0.82 \cdot 0 - 0.54 \cdot 0 - 0.03 \cdot 0 - 0.21 \cdot 0 - 1.99 \cdot 1 = 21.13\end{aligned}$$

```
Cuckoo %>%
  group_by(Bird) %>%
  summarize(mean_length = mean(Length))
```

```
## # A tibble: 6 x 2
##   Bird          mean_length
##   <fct>          <dbl>
## 1 hedge_sparrow    23.1
## 2 mdw_pippit      22.3
## 3 robin           22.6
## 4 tree_pippit     23.1
## 5 wagtail         22.9
## 6 wren            21.1
```