# CPSC 213

# Introduction to Computer Systems

Winter Session 2016, Term 2

Unit 1a — Jan 6, 8 and 11

Memory and Numbers

#### Unit 1a Overview

#### Reading

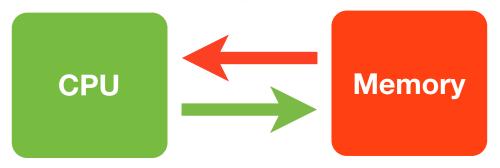
• Companion: 2.2.2

• Textbook: 2.1 - 2.3

#### Learning Objectives

- know the number of bits in a byte and the number of bytes in a short, long and quad
- determine whether an address is aligned to a given size
- translate between integers and values stored in memory for both big- and littleendian machines
- evaluate and write Java expressions using bitwise operators (&, |, <<, >>, and >>>)
- determine when sign extension is unwanted and eliminate it in Java
- evaluate and write C expressions that include type casting and the addressing operators (& and \*)
- translate integer values by hand (no calculator) between binary and hexadecimal, subtract hexadecimal numbers and convert small numbers between binary and decimal

## A Simple Computing Machine



#### Memory

- stores data encoded as bits
- program instructions and state (variables, objects, etc.)

#### **CPU**

- reads instruction and data from memory
- performs specified computation and writes result back to memory

#### Example

- C = A + B
- memory stores: add instruction, and variables A, B and C
- CPU reads instruction and values of A and B, adds values and writes result to C

Memory is a big bag of **BYTE**s

CPU

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a BYTE (8 bits)

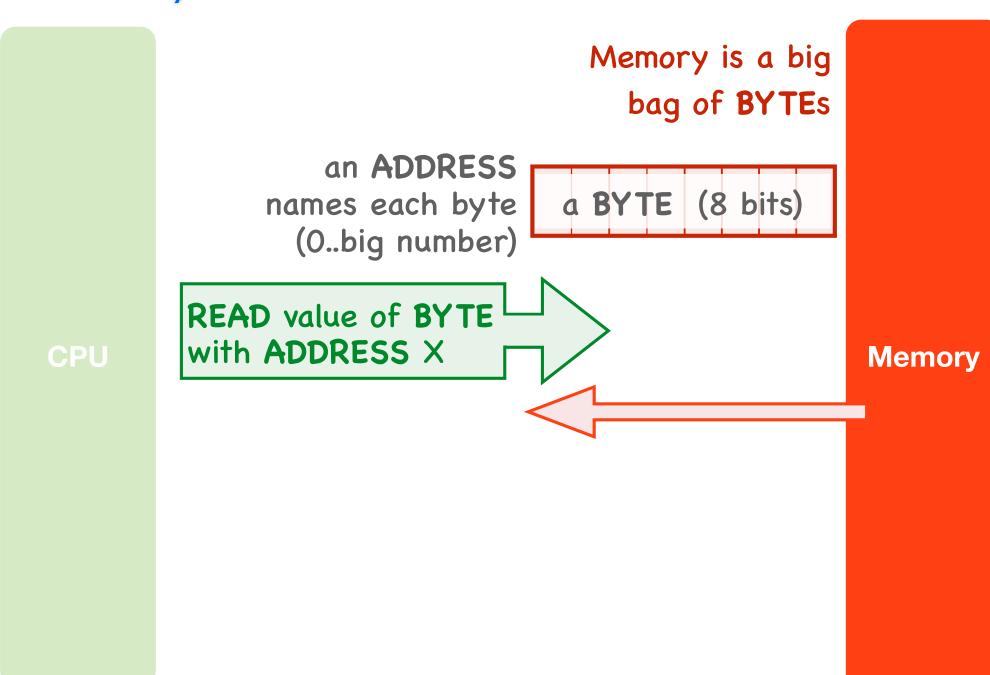
CPU

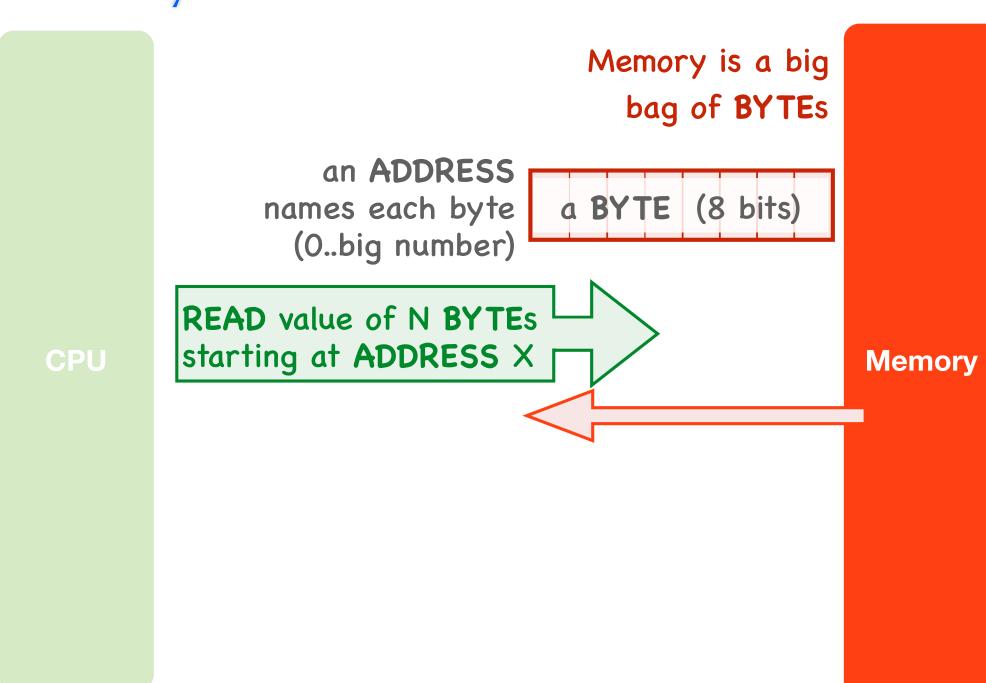
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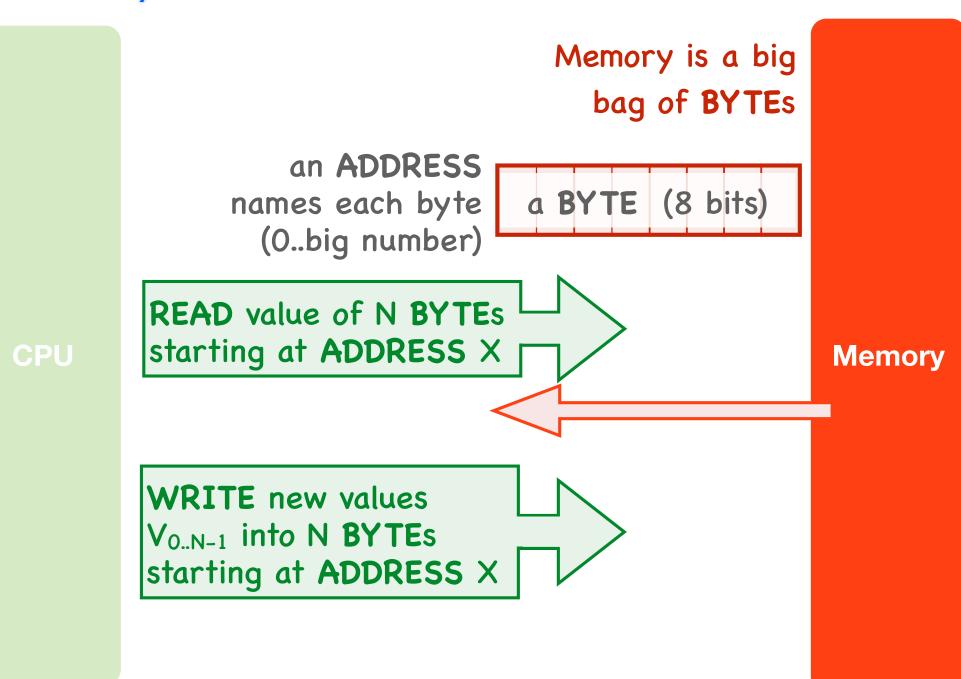
an ADDRESS names each byte (0..big number)

a BYTE (8 bits)

CPU







### Memory Summary

#### Memory

#### Naming

- unit of addressing is a byte (8 bits)
- every byte of memory has a unique address
- some machines have 32-bit memory addresses, some have 64
  - our machine will have 32

#### Access

- lots of things are too big to fit in a single byte
  - unsigned numbers > 255, signed numbers < -128 or > 127, most instructions, etc.
- CPU accesses memory in contiguous, power-of-two-size chunks of bytes
   Integer Data Types by Size

# bytes	# bits	С	Java		Asm
1	8	char	byte	b	byte
2	16	short	short	w	word
4	32	int	int	I	long
8	64	long	long	q	quad

address of a chunk is address of first byte

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8	64	lona	lona	<b>a</b> quad

We will use only 32-bit integers

address of a chunk is address of first byte







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  - base 10 is natural for this





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  - memory addresses are big numbers that name power-of-two size things
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- ▶ We might use base-2, binary
  - a small 256-byte memory has addresses 0<sub>2</sub> to 111111111<sub>2</sub>
  - if you don't have subscripts, 111111112 is written as 0b111111111
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- Once we used base-8, octal
  - 64-KB memory addresses go up to 111111111111111111 = 1777778
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  - if you don't have subscripts, 1777778 is written as 0177777
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- Now we use base-16, hexadecimal
  - 4-GB memory addresses go up to 37777777778 = fffffffff<sub>16</sub>
  - if you don't have subscripts, fffffffff16 is written as 0xfffffffff

01101010010101010000111010100011

How many bits in a hex "digit", a hexit?

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0110 1010 0101 0101 0000 1110 1010 0011

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Consider ONE hexit at a time:  $8 \times i_4 + 4 \times i_3 + 2 \times i_2 + 1 \times i_1$ 

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6 a 5 5 0 e a 3

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Its easy to see the value of each byte (i.e., two hexits)

0x6a 0x55 0x0e 0xa3

#### Question 1a.1: Hexadecimal Notation

#### Which of these statements is true

- A. The Java constants 16 and 0x10 are exactly the same integer
- B. 16 and 0x10 are different integers
- C. Neither
- D. I don't know

#### We use Hex for addresses

- while we don't really care what their base-10 value is
- we sometimes compute the size of things by subtracting two addresses
  - and that will then be in decimal

#### Subtracting in Hex

$$0 \times 2000 - 0 \times 1 \text{ff0} = ?$$

- you could convert both numbers to decimal, but that might be too hard
- you can subtract in hex
  - carry is 0x10 == 16
  - to subtract a..f digits convert to their decimal value
- or you can use two's compliment addition
  - negate a number of complimenting and incrementing it
    - -x == !x + 1
  - complimenting in hex is easy
    - swap 1's and 0's
    - · need a quick switch to/from binary

- not too bad for small numbers ... tedious for large ones
- $\bullet 0xijkl = i*16^3 + j*16^2 + k*16^1 + l*16^0$

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0x2000 -0x1ff0	0x1f00 -0x1ff0	0x1f00 -0x1ff0
0	0	0010

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		1		1
0×2000	Fig.	0x1f00	Side:	0x1f00
-0x1ff0		-0x1ff0		-0x1ff0
0		0		0010

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$$0 \times 2000 - 0 \times 1 \text{ff0} == 0 \times 2000 + 0 \times 1 \text{fffe010}$$
  
==  $0 \times 10$ 

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- $0 \times ijkl = i*16^3 + j*16^2 + k*16^1 + l*16^0 0 \times 10 == 1*16 + 0$

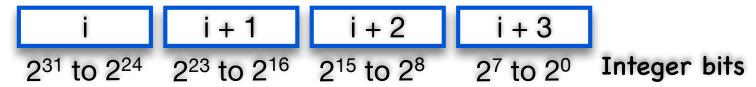
### Question 1a.2: Subtracting in Hex

- Object A is at address 0x10d4 and object B at 0x1110. They are stored contiguously in memory (i.e., they are adjacent to each other). How big is A?
  - A. 16 bytes
  - B. 48 bytes
  - C. 60 bytes
  - D. 80 bytes
  - E. You can't tell for sure from the information given
  - F. I need a calculator
  - G. I don't know

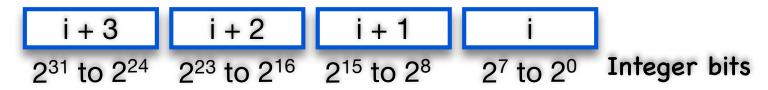
- Our first architectural decision
  - assembling memory bytes into integers
- Consider 4-byte memory word and 32-bit integer
  - it has memory addresses i, i+1, i+2, and i+3
  - we'll just say its "at address i and is 4 bytes long"
  - e.g., the word at address 4 is in bytes 4, 5, 6 and 7.

#### Big or Little Endian

we could start addressing at the BIG END of the number



or we could start at the LITTLE END (Intel)



Memory





i + 2

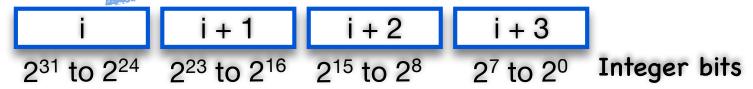
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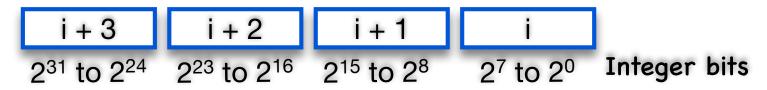
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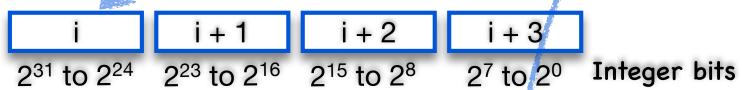
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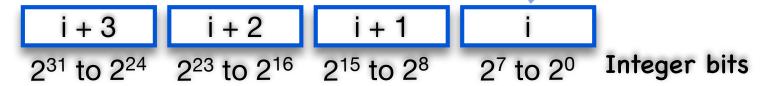
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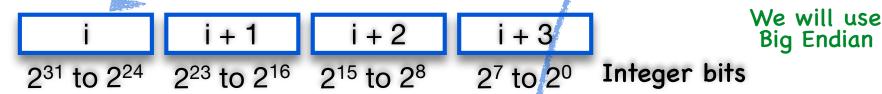


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- i + 1
- i + 2
- i + 3

- Big or Little Endian
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#### Question 1a.3: Endianness

▶ What is the Little-Endian integer value at address 4 below?

- A. 0x1c04b673
- B. 0xc1406b37
- C. 0x73b6041c
- D. 0x376b40c1
- E. none of these
- F. I don't know

#### Memory

Addr Value

0x0: 0xfe

0x1: 0x32

 $0 \times 2$ :  $0 \times 87$ 

0x3: 0x9a

0x4: 0x73

0x5: 0xb6

 $0 \times 6$ :  $0 \times 04$ 

 $0 \times 7 : 0 \times 1c$ 

### In Lab: Endianness.java

```
public static void main (String[] args) {
   Byte mem[] = new Byte[4];
   try {
     for (int i=0; i<4; i++)
        mem [i] = Integer.valueOf (args[i], 16) .byteValue();
   } catch (Exception e) {
   }
   int bi = bigEndianValue (mem);
   int li = littleEndianValue (mem);
   ...</pre>
```

#### Complete this program

- implement bigEndianValue and littleEndianValue
- Run in for various byte sequences
  - four command-line arguments are for consecutive byte values, in hex
  - for example typing the following at UNIX shell command line

```
    java Endianness 0 0 0 1 should print big-endian value of 1
    java Endianness 1 0 0 0 should print little-endian value of 1
    java Endianness ff ff ff should print value of -1 for both
```

### In Lab: Endianness.java

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public static void main (String[] args) {
   Byte mem[] = new Byte[4];
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      for (int i=0; i<4; i++)
        mem [i] = Integer.valueOf (args[i], 16) .byteValue();
   } catch (Exception e) {
   }
   int bi = bigEndianValue (mem);
   int li = littleEndianValue (mem);
   ...</pre>
Load 4 byte values provided on memory in sequence.
```

### Complete this program

address 3

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### Some addresses are better than others

### Address Alignment

we could allow any number to address a 4-byte integer, e.g.



- but, better for hardware is to require addresses be aligned
  - an address is aligned to size x if the address mod x is zero



### Alignment to power-of-two size

- smaller things always fit completely inside of bigger things



e.g., a word contains exactly two complete shorts

- address computations are achieved by shifting bits; e.g., array-element address from index &a[i] == &a[0] + i\*(s==2^j) == &a[0]\_ $\frac{1}{2}$  i << j

### Some addresses are better than others

### Address Alignment

we could allow any number to address a 4-byte integer, e.g.





- \* disallowed on many architectures
- \* allowed on Intel, but usually slower example ....
- but, better for hardware is to require addresses be aligned
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### Alignment to power-of-two size

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- address computations are achieved by shifting bits; e.g., array-element address from index &a[i] == &a[0] + i\*(s==2^j) == &a[0]\_ $\frac{1}{4}$  i << j

## Advantages of Power-of-Two Alignment

#### Memory Implementation Detail (simplified)

- memory is actually organized internally into larger chucks called blocks
- lets say a block is 16 bytes
- every memory access, internally requires accessing one of these blocks
- you'll see in 313 that this relates to memory caches

#### Anyway ...

- a CPU memory access looks like this
  - Read/Write N bytes starting at address A
- the memory converts this to
  - R/W **N bytes** starting at **O**<sup>th</sup> byte of **block B** (**O** is the *block offset* and **B** is the *block number*)
  - blocks are numbered, such that block 0 contains addresses 0 .. 15
- do the calculation
  - (B, O) = f(A)
- how is this simplified IF
  - N is a power of 2 and
  - A is aligned (i.e., A mod N == 0)?

## Question 1a.4: Alignment

- Which of the following statement (s) is (are) true?
  - A. the address 6 (110<sub>2</sub>) is aligned for addressing a *short*
  - B. the address 6 (110<sub>2</sub>) is aligned for addressing an *int* (i.e., 4-bytes)
  - C. the address 20 (10100<sub>2</sub>) is aligned for addressing an int
  - D. the address 20 (10100<sub>2</sub>) is aligned for addressing a *long* (i.e., 8-bytes)

- Shifting multiplies or divides by power of 2
  - shifting left b bits is the same multiplying by 2<sup>b</sup>
  - shifting right is the same as dividing by 2<sup>b</sup>

$$0x6 >> 1 == 110_2 >> 1$$
  
== 11<sub>2</sub>  
== 0x3

### Shifting multiplies or divides by power of 2

• shifting left b bits is the same multiplying by  $2^b$   $0x6 >> 1 == 110_2 >> 1$   $== 11_2$ 

shifting right is the same as dividing by 2<sup>b</sup>

### But, what about negative numbers

recall that negative numbers are represented in two's compliment form

== 0x3

- -6 ==  $0xfa == 111111010_2$  (i.e.,  $111111010_2 + 00000110_2 == 0$ )
- -6 / 2 == -3, but  $11111010_2$  shifted right is  $011111101_2$  == 125, not -3

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== 11<sub>2</sub>  
== 0 \times 3

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### There are two kinds of right shifts

- SIGNED ">>" shifts, but keeps high-order bit (the sign bit) the same
  - $-6- >> 1 == 111111101_2 == -3$  (i.e.,  $111111101_2 + 00000011_2 == 0$ )
- UNSIGNED ">>>", shifts and sets high-order bit to 0
  - $-6 >>> 1 == 011111101_2$  ... 0xfa >>> 1 == 0x7d
- In Java you choose. In C the compiler chooses.
  - C as both signed and unsigned integer data types and no ">>>". Java has only signed.

#### Extending is

when you increase the number of bytes used to store an integer

```
byte b = -6;
int i = b;
out.printf ("b: 0x%x %d, i: 0x%x %d\n", b, b, i, i);
```

what prints?

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• what prints? b: 0xfa -6, i: 0xfffffffa -6

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- copies sign bit into upper, empty bits of the extended number

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### Signed Extension

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#### Zero Extension

- used with unsigned numbers (e.g., in C)
- sets upper, empty bits to 0
- you can force zero-extension using logical, bit-wise AND (e.g., in Java):

```
int u = b & 0xff;
out.printf ("u: 0x%x %d\n", u, u);
```

u: 0xfa 250

## Truncating an Integer

### Truncating an Integer

- You can also go the other way
  - more bits to fewer bits

```
int i = -6;
byte b = i;
out.printf ("b: 0x%x %d, i: 0x%x %d\n", b, b, i, i);
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- what could go wrong?
  - If i is 256, what is b? What if i is 128?

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```

- what could go wrong?
  - If i is 256, what is b? What if i is 128?

### Java warns you

- if you truncate an integer without an explicit cast as above
  - "Possible Loss of Precision"
- you get rid of the warning by explicitly casting
  - the cast has no effect on the value of b
  - it just tells the compiler that you know what your doing ... obviously, be sure you do

```
int i = -6;
byte b = (byte) i;
out.printf ("b: 0x%x %d, i: 0x%x %d\n", b, b, i, i);
```

### Questions 1a.5 and 1a.6: Shift and Mask

1. What is the value of i after this Java statement executes?

```
int i = ((byte) 0x8b) << 16;</pre>
```

- A. 0x8b
- B. 0x0000008b
- C. 0x008b0000
- D. 0xff8b0000
- E. None of these
- F. I don't know

2. What is the value of i after this Java statement executes?

```
i = 0xff8b0000 & 0x00ff0000;
```

- A. 0xffff0000
- B. 0xff8b0000
- C. 0x008b0000
- D. None of these
- E. I don't know